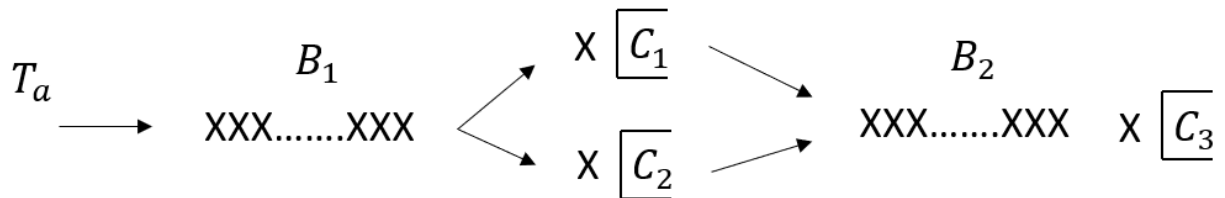


# IE 413 - Homework 1

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## Problem 1 - Coffee Shop

We assumed the area to pick up the order is modeled as a buffer and another cashier/barista.



### Entities

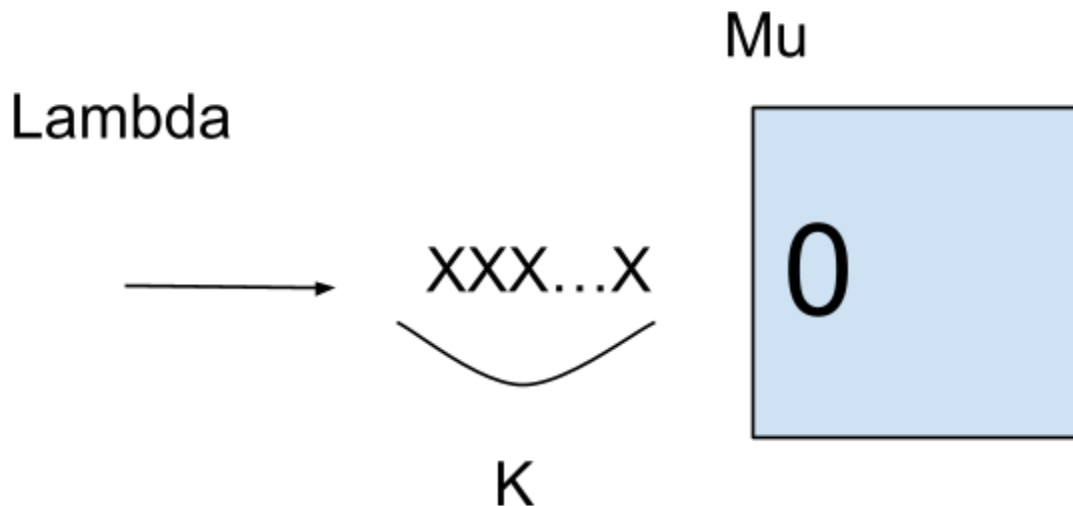
- Cashier/Barista  $C_i$  - Assists customers with order
  - $S_i \in \{-2, -1, 0, 1\}$  Status of cashier. 1 meaning they are ready for another customer, 0 meaning they are currently assisting a customer, -1 means the next buffer is full and can't take another customer. -2 means the register is currently closed.
  - $\mu_i \in [10, 300]$  Time to process order for cashier i in seconds. Range is an example and is subject to change. Consider modeling  $\mu_i \sim \text{Exp}(M_i)$  and assume  $M_1 = M_2$
- Buffer  $B_i$  - Waiting line to order/pick up food. First come first serve.
  - $n_i \in \{0, 1, 2, \dots, N_i\}$  Current number of customers in buffer i
  - $N_i \in \{20, 21, 22, \dots, 100\}$  Max number of customers that can be in buffer i. Range is an example and is subject to change.
- Customers - people looking to buy coffee.
  - Arrival time  $T_A \in [0, 25000]$  - Time between for customers arriving at the coffee shop in seconds. Consider modeling  $T_A \sim \text{Exp}(\lambda_A)$  dependent on the time of day

### Policies

- We have 2 Cashiers/Baristas and they work in a first come first serve manner.
- Cashiers can only process 1 customer at a time and can not process someone if the pick up line is full.
- Customers are indistinguishable

## Problem 2 - Call Center

The system is represented as a M/M/1/K queue.



### Entities

- Cell phone service operator - handles customer calls.
  - $S \in \{0, 1\}$  Status of operator. 0 is busy, 1 is idle.
  - $\mu \sim \text{Exp}(1/T_s)$  Service time is exponentially distributed with mean  $T_s$ .
  - $T_s = 5$  minutes.
- Queue - A caller is in the queue while they are on hold.
  - $Q \in \{0, 1, \dots, K\}$  Number of callers in queue—"on hold."
  - $K = 10$ , the maximum number of callers that can be on hold. If  $Q = K$ , no one else can be put on hold.
- Callers - Those calling in and receiving service.
  - $\lambda \sim \text{Exp}(1/T_a)$  Interarrival times are exponentially distributed with mean  $T_a$ .
  - $T_a = 7$  minutes.

### States & Changes

- $S$  = operator status (0 busy, 1 idle).  $Q$  = number of people on hold (does not include person receiving service)
- $Q$  can increment or decrement by one, depending on caller arrival or completion of service, respectively. If  $Q = K$ , then cannot increment to  $K+1$ .
- $S$  remains at zero while callers are in system, and will equal one when the final caller is completed with zero on hold. Will return to zero when a new caller arrives.

### Laws

- No notable laws

### Policies

- Operator can only handle one caller at a time.
- Callers are served first come first serve and are indistinguishable.
- No new callers can be put on hold once capacity  $K$  is reached.