

# CS443: Compiler Construction

Lecture 17: Optimizations

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Based on material by Stephen Chong

# Constant Propagation: If a var is known to be constant, replace var w/ constant

```
int N = 10000;
int a[] = malloc(N * sizeof(int));
for (int i = 0; i < N; i++) {
    a[i] = f(i, N);
}
```

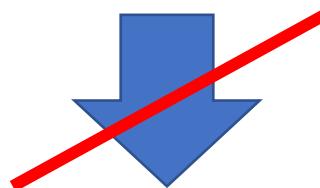
Now unnecessary!  
(Dead code—later)

```
int N = 10000;
int a[] = malloc(10000 * sizeof(int));
for (int i = 0; i < 10000; i++) {
    a[i] = f(i, 10000);
}
```

# Constant Propagation: Safety

- Need to make sure N isn't redefined

```
int N = 10000;
int a[] = malloc(10000 * sizeof(int));
for (int i = 0; i < N; i++) {
    a[i] = f(i, N);
    N = g(i);
}
```



# Constant Propagation: In SSA, don't have to worry about other definitions

```
int N1 = 10000;
int a[] = malloc(N1 * sizeof(int));
N2 = Φ(N1, N3) for (int i = 0; i < N2; i++) {
    a[i] = f(i, N2);
    N3 = g(i);
}
```



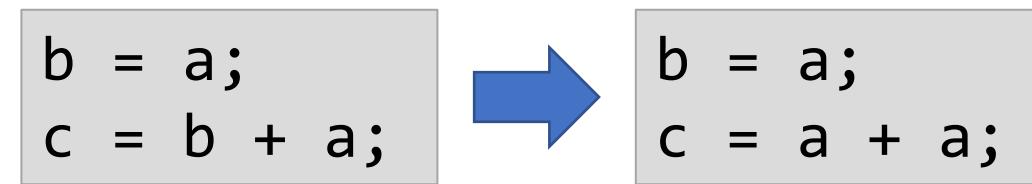
# Constant Propagation: Also have to worry about multiple branches

```
int a = 0;  
if (p) {  
    a = 1;  
} else {  
    a = 2;  
}
```

- Normally: use reaching definitions analysis
- SSA: Fine

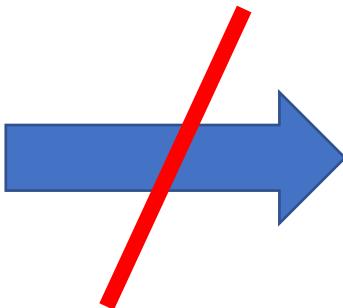


# Generalize: Copy Propagation

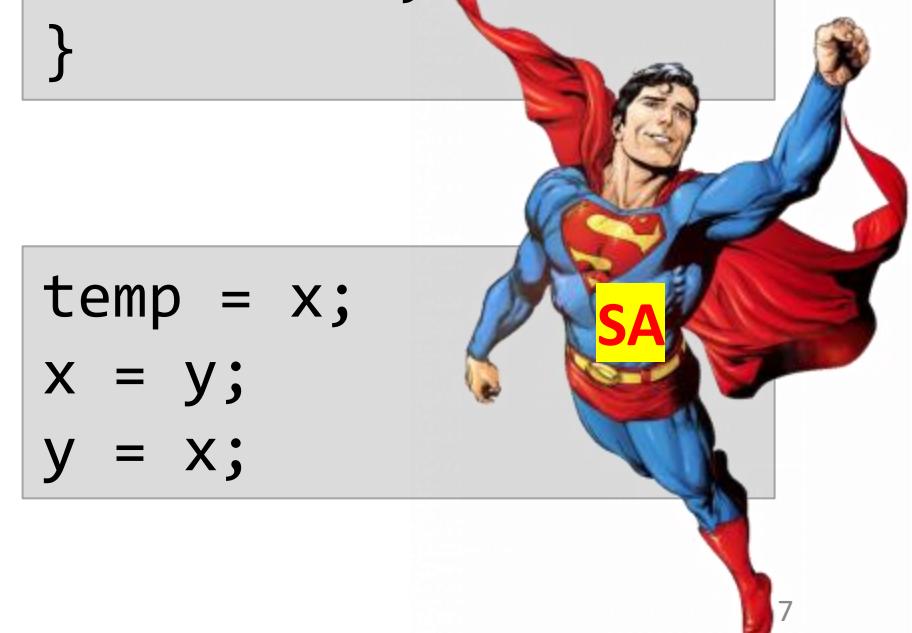


# Copy Propagation: Need to make sure neither var is redefined

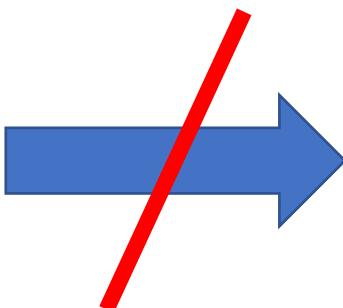
```
int sqrt(int n) {  
    int i = n;  
    while (i * i > n)  
        i--;  
    return i;  
}
```



```
int sqrt(int n) {  
    int i = n;  
    while (n * n > n)  
        i = n - 1;  
    return n;  
}
```



```
temp = x;  
x = y;  
y = temp;
```



```
temp = x;  
x = y;  
y = x;
```

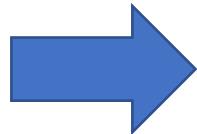
But we don't even have a move/set instruction! Why would you need this?

Other optimizations may generate move instructions (which you then need to get rid of to have valid LLVM!)



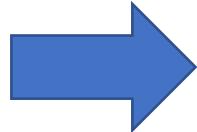
# Constant Prop. Example #1

```
int n = 5;
int a = n * 2;
if (n < 6) n++
int b = n + 1;
```



# Constant Prop. Example #1

```
int n = 5;  
int a = n * 2;  
if (n < 6) n++  
int b = n + 1;
```



```
int n = 5;  
int a = 5 * 2;  
if (5 < 6) n = 5 + 1  
int b = n + 1;
```

# Constant Prop. Example #2

```
%n1 = bitcast i32 %x to i32
%x1 = add i32 %n1, 2
%n2 = mul i32 %n1, 2
%x2 = add i32 %n2, 5
```



# Constant Prop. Example #2

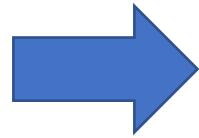
```
%n1 = bitcast i32 %x to i32
%  
x1 = add i32 %n1, 2
%n2 = mul i32 %n1, 2
%  
x2 = add i32 %n2, 5
```



```
%n1 = bitcast i32 %x to i32
%  
x1 = add i32 %x, 2
%n2 = mul i32 %x, 2
%  
x2 = add i32 %n2, 5
```

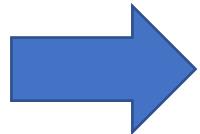
# Constant Prop. Example #3

```
int n = 5;  
int a = f(&n);  
int b = n + 1;
```



# Constant Prop. Example #3

```
int n = 5;  
int a = f(&n);  
int b = n + 1;
```



```
int n = 5;  
int a = f(&n);  
int b = n + 1;
```

Might change n

# Constant/Copy Propagation: Summary

- What does it optimize?
  - Time
  - Space (registers + maybe stack)
- When is it safe?
  - Non-SSA: if variable(s) haven't been redefined
  - SSA: always
- When is it an optimization?
  - Always (at least, shouldn't make things worse)

# Implementing Constant/Copy Propagation on SSA code

- For each instruction “ $x = c$ ”:
  - Add  $x \rightarrow c$  to a map
- For each instruction (e.g.  $x_1 = \text{add i32 } v_1, v_2$ ):
  - Look up variable operands in map, replace with value if there

# LLVM specifics

- If  $\%x \rightarrow c$  is in the map, can we propagate  $c$  to, e.g.,  
`getelementptr i32, i32* %x, i32 5?`
  - Only if  $c$  is another variable (it should be if we're not manipulating bare memory addresses)
- What LLVM instructions have the form “ $\%x = c$ ”?
  - In LLVM.Ast: `ISet(%x, t, c)`
  - $\%x = \text{bitcast } t1 \text{ to } t2 \text{ when } t1 = t2$
  - $\%x = \text{phi } t [c1, \%l1], \dots, [cn, \%ln] \text{ when } c1 = \dots = cn$

# Constant Folding: Do arithmetic with constants when you can

```
int a[] = malloc(10000 * sizeof(int));
for (int i = 0; i < 10000; i++) {
    a[i] = f(i, 10000);
}
```

=4



```
int a[] = malloc(40000);
for (int i = 0; i < 10000; i++) {
    a[i] = f(i, 10000);
}
```

# Constant Folding: Who's written code like this?

```
int seconds_to_days (int secs) {  
    return secs / (60 * 60 * 24);  
}
```

# Constant Folding: Can extend to things that aren't just simple arithmetic

```
int x = 3;  
int y = 4;  
if (x < y) {  
    s1;  
} else {  
    s2;  
}
```

```
if (3 < 4) {  
    s1;  
} else {  
    s2;  
}
```

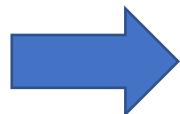
```
if (true) {  
    s1;  
} else {  
    s2;  
}
```

```
s1;
```

s2 is unreachable!  
(More on that later)

This (previous slides) kind of constant folding  
is usually safe, but don't get carried away

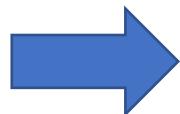
true && x && false



false && x



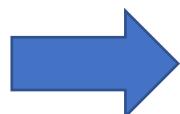
1 + x + 2



3 + x



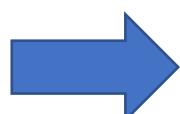
42 / 0



INTERNAL COMPILER ERROR: Divide by zero



1.0 + x + 2.0



3.0 + x



# Aside on constant folding divisions by zero

```
let a = 5 / 0
```



ocamlopt

```
000000000012cd0 <camlTest_entry>:  
12cd0:    sub    $0x8,%rsp  
12cd4:    lea    0x23bb0d(%rip),%rax      # 24e7e8 <caml_backtrace_pos>  
12cdb:    xor    %rbx,%rbx  
12cde:    mov    %ebx,(%rax)  
12ce0:    lea    0x229421(%rip),%rax      # 23c108 <caml_exn_Division_by_zero>  
12ce7:    callq  2c130 <caml_raise_exn>
```

# Aside on constant folding divisions by zero

```
return 5 / 0;
```

gcc -O0

```
0000000000005fa <main>:  
5fa: push %rbp  
5fb: mov %rsp,%rbp  
5fe: mov $0x5,%eax  
603: mov $0x0,%ecx  
608: cltd  
609: idiv %ecx  
60b: pop %rbp  
60c: retq
```

gcc -O3

```
0000000000004f0 <main>:  
4f0: ud2
```

UD2

0F 0B

Undefined  
Instruction

Generates an invalid opcode exception. This instruction is provided for software testing to explicitly generate an invalid opcode. The opcode for this instruction is reserved for this purpose.

# Related: Even if we don't have all constants, we can do algebraic simplifications

$$a * 1 = a$$

$$1 * a = a$$

$$a + 0 = a$$

$$0 + a = a$$

$$a - 0 = a$$

$$a * 0 = 0$$

$$0 * a = 0$$

Again, careful of these, e.g.

$(5 / z) * 0$  if  $z = 0$

or  
 $(f()) * 0$  if  $f$  has a side effect

$$a \&& \text{true} = a$$

$$\text{true} \&& a = a$$

$$a \&& \text{false} = \text{false}$$

$$\text{false} \&& a = \text{false}$$

$$a \mid\mid \text{true} = \text{true}$$

$$\text{true} \mid\mid a = \text{true}$$

$$a \mid\mid \text{false} = a$$

$$\text{false} \mid\mid a = a$$

# Implementing Constant Folding

- Hope you like pattern matching
- Can do this at the same time as copy/constant propagation

# Constant Folding: Summary

- What does it optimize?
  - Time
- When is it safe?
  - If it doesn't change side effect behavior and doesn't do weird FP stuff
- When is it an optimization?
  - Well, depends on what we do after

# Optimizations can enable other optimizations

```
int secs_per_day = 60 * 60 * 24;  
int days = secs / secs_per_day;
```

Constant Folding

```
int secs_per_day = 86400;  
int days = secs / secs_per_day;
```

Constant Propagation

```
int secs_per_day = 86400;  
int days = secs / 86400;
```

# Optimizations can enable other optimizations: Dead Code Elimination

```
int secs_per_day = 60 * 60 * 24;  
int days = secs / secs_per_day;
```

Constant Folding

```
int secs_per_day = 86400;  
int days = secs / secs_per_day;
```

Constant Propagation

```
int secs_per_day = 86400;  
int days = secs / 86400;
```

Unused assignment  
("Dead code")

# Dead Code Elimination: defs with no uses can (sometimes) be safely removed

```
int secs_per_day = 60 * 60 * 24;  
int days = secs / secs_per_day;
```

```
int secs_per_day = 86400;  
int days = secs / secs_per_day;
```

```
int secs_per_day = 86400;  
int days = secs / 86400;
```

```
int days = secs / 86400;
```

Constant Folding

Constant Propagation

Dead Code Elim.

# Dead Code Elimination: Be careful of side effects!

```
int x = printf("Hello World\n");
// Never use x, because who does error checking
// on printf?
```

Could argue that, in this class, LLVM instructions have no side effects other than the one variable assignment

# Can we eliminate dead code that raises an exception?

```
int a = 5 / 0;  
return 0;
```

```
let a = 5 / 0  
exit 0
```

Changes program behavior... but only in a “good” way?

- gcc (with `-O1` and above) eliminates assignment
- ocamlopt doesn’t

# DCE: Summary

- What does it optimize?
  - Time
  - Space
  - Instruction cache
- When is it safe?
  - If it doesn't change side effect behavior
- When is it an optimization?
  - Probably always, but processors are very weird

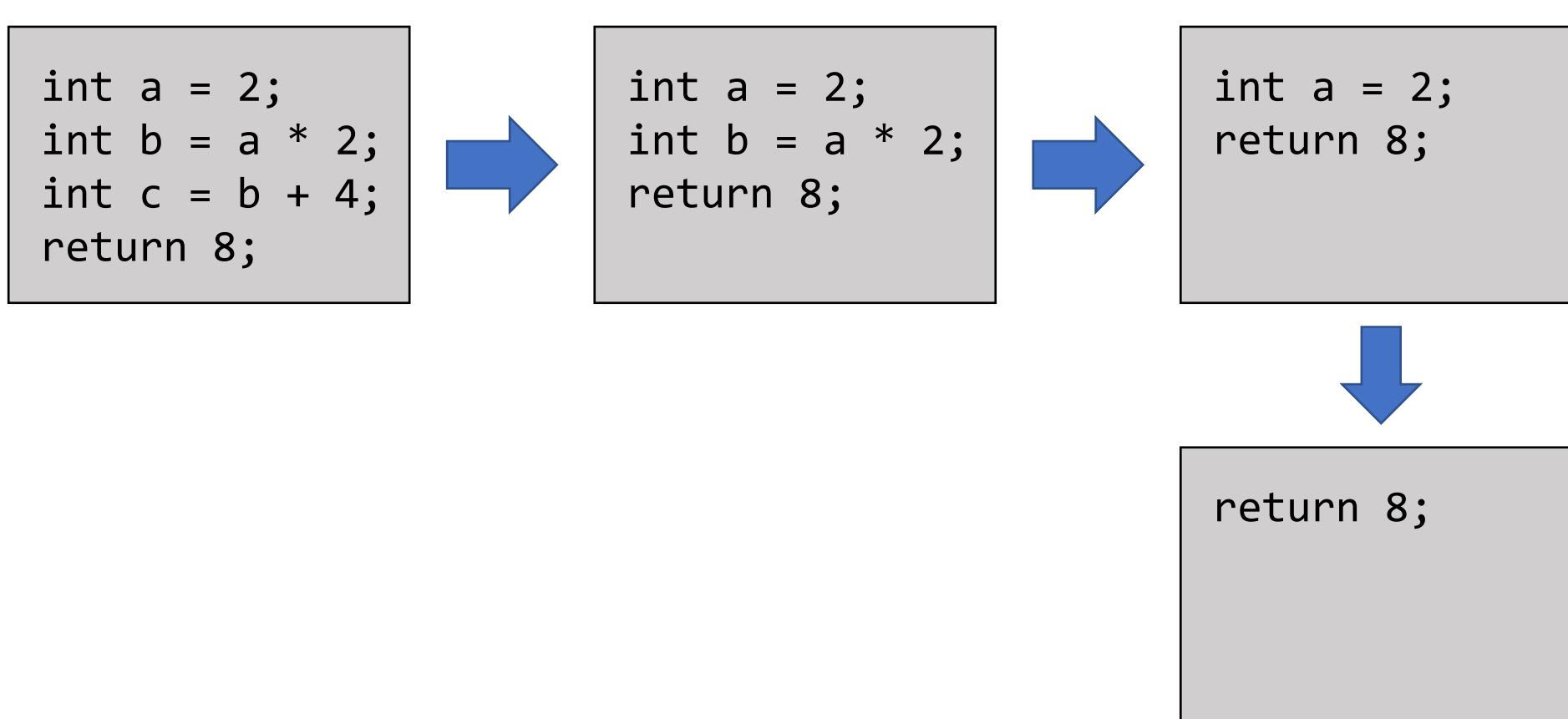
# Implementing DCE – intuitive algorithm

- Initialize  $\text{uses}(i)$  to 0 for all instructions
- For each instruction (e.g.,  $x = \text{add i32, v1, v2}$ ):
  - Increment  $\text{uses}(vi)$  for all variable operands  $vi$  ( $x$  is not used)
- Then:
- For each definition  $x = e$ :
  - If  $\text{uses}(x) = 0$  and  $e$  has no side effects, eliminate

(in SSA there's only one def of  $x$ )



# Intuitive algo might lead to more dead code

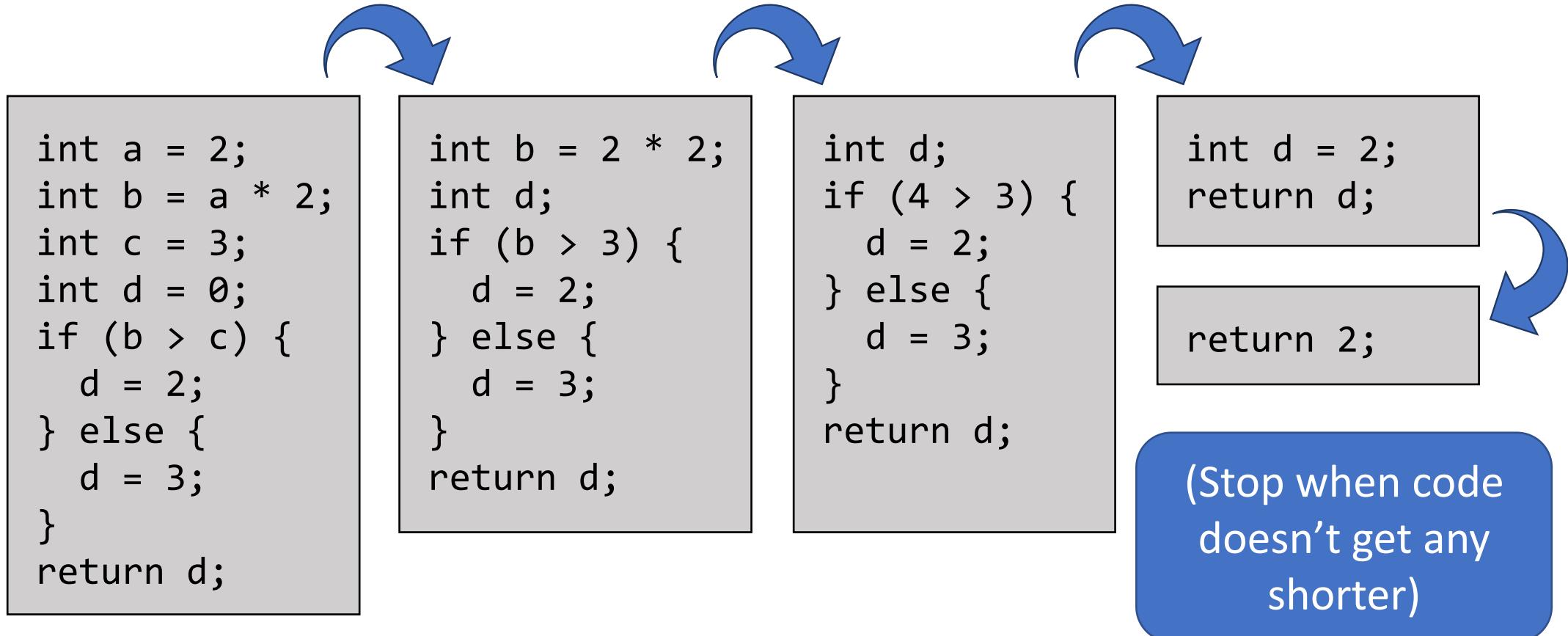


# More efficient worklist algorithm

- Let  $V = \text{all vars in the program}$
- Initialize  $\text{uses\_of}(v)$  and  $\text{def\_of}(v)$  for all vars
- while  $V$  is not empty:
  - remove  $v$  from  $V$
  - if  $\text{uses\_of}(v)$  is empty and  $\text{def\_of}(v)$  has no other side effects:
    - remove  $\text{def\_of}(v)$  from the program
    - for  $x$  in  $\text{use}(\text{def\_of}(v)) / \{v\}$ :
      - delete  $\text{def\_of}(v)$  from  $\text{uses\_of}(x)$
      - $V = V \cup \{x\}$



# For best results: Fold, propagate, eliminate, and repeat



# Example #4

```
%temp1$1 = bitcast i32 %n to i32
%temp2$2 = bitcast i32 1 to i32
%a$3 = add i32 %temp1$1, %temp2$2
%temp7$4 = bitcast i32 1 to i32
%temp8$5 = bitcast i32 2 to i32
%temp5$6 = add i32 %temp7$4, %temp8$5
%temp6$7 = bitcast i32 4 to i32
%temp4$8 = icmp sgt i32 %temp5$6, %temp6$7
br i1 %temp4$8, label %label1, label %label2
label1:
%temp3$10 = bitcast i32 %a$3 to i32
ret i32 %temp3$10
label2:
br label %label3
label3:
%temp9$9 = bitcast i32 1 to i32
ret i32 %temp9$9
```

## Example #4

```
%a$3 = add i32 %n, 1
%temp5$6 = add i32 1, 2
%temp4$8 = icmp sgt i32 %temp5$6, 4
br i1 %temp4$8, label %label1, label %label2
label1:
    ret i32 %a$3
label2:
    br label %label3
label3:
    ret i32 1
```

## Example #4

```
%a$3 = add i32 %n, 1
%temp5$6 = bitcast i32 3 to i32
%temp4$8 = icmp sgt i32 %temp5$6, 4
br i1 %temp4$8, label %label1, label %label2
label1:
    ret i32 %a$3
label2:
    br label %label3
label3:
    ret i32 1
```

## Example #4

```
%a$3 = add i32 %n, 1
%temp4$8 = icmp sgt i32 3, 4
br i1 %temp4$8, label %label1, label %label2
label1:
    ret i32 %a$3
label2:
    br label %label3
label3:
    ret i32 1
```

## Example #4

```
%a$3 = add i32 %n, 1
%temp4$8 = bitcast i1 0 to i1
  br i1 %temp4$8, label %label1, label %label2
label1:
  ret i32 %a$3
label2:
  br label %label3
label3:
  ret i32 1
```

## Example #4

```
%a$3 = add i32 %n, 1
br i1 0, label %label1, label %label2
label1:
    ret i32 %a$3
label2:
    br label %label3
label3:
    ret i32 1
```

## Example #4

```
%a$3 = add i32 %n, 1
br label %label2
label1:
    ret i32 %a$3
label2:
    br label %label3
label3:
    ret i32 1
```

## Example #4

```
%a$3 = add i32 %n, 1  
br label %label2  
label2:  
  br label %label3  
label3:  
  ret i32 1
```



A large yellow starburst shape with a red outline, centered on the right side of the slide. It has several points radiating outwards. Inside the starburst, the text "Later: Delete unreachable code!" is written in black.

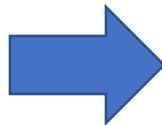
Later:  
Delete unreachable  
code!

## Example #4

```
br label %label2
label2:
    br label %label3
label3:
    ret i32 1
```

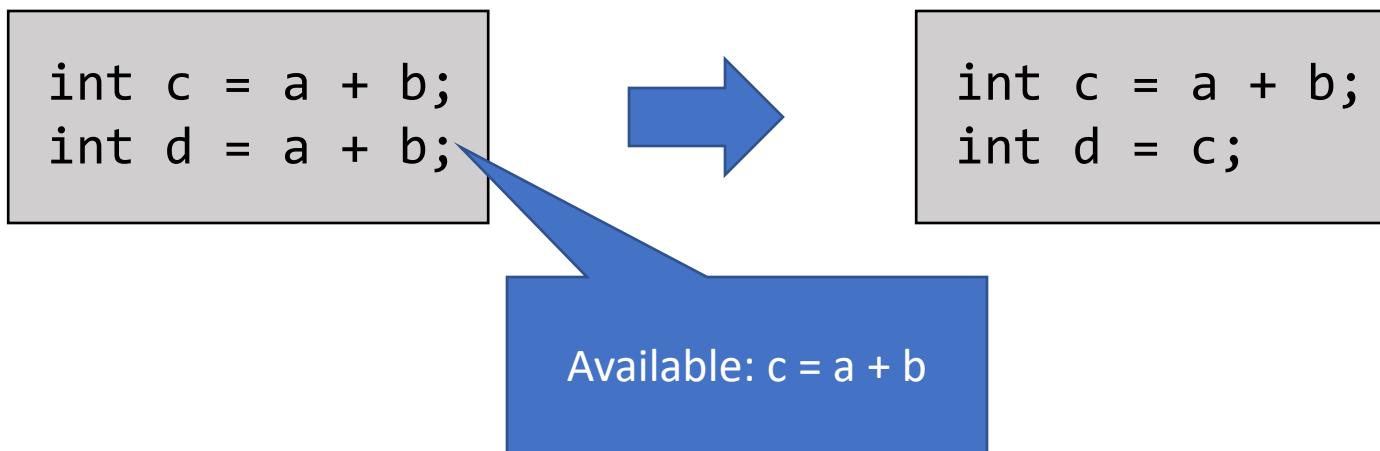
# Reusing available expressions

```
int c = a + b;  
int d = a + b;
```



```
int c = a + b;  
int d = c;
```

# Recall: Available expressions dataflow analysis



# Available expressions analysis takes care of safety for reusing expressions

```
int c = a + b;  
c = c + 1;  
int d = a + b;
```



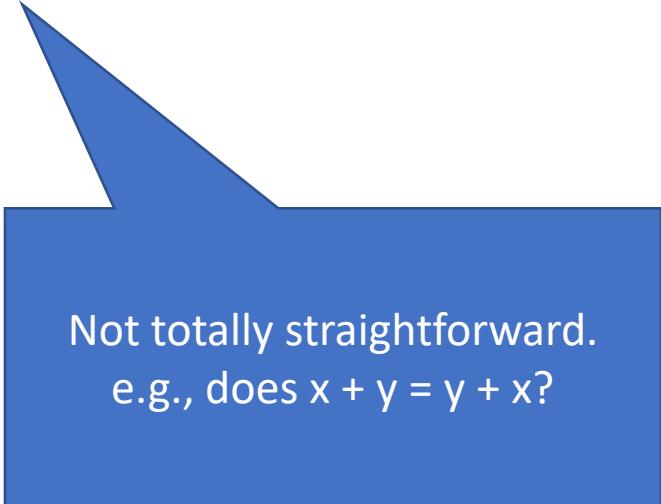
```
int c = a + b;  
c = c + 1;  
int d = a + b;
```

(and this isn't a concern in SSA, anyway, but there is still one concern)



# Algorithm for reusing expressions

- Perform available expressions dataflow analysis
- For each node  $n$  where  $\text{stmt}(n)$  is “ $v = e_1$ ”:
  - If an assignment “ $a = e_2$ ” is available where  $e_1 = e_2$ 
    - Replace  $n$  with “ $v = a$ ”



Not totally straightforward.  
e.g., does  $x + y = y + x$ ?

# Reusing expressions example

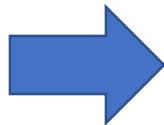
- Can we optimize this?

```
int d = a[i] + b[i];
c[j] = d;
int e = a[i] + b[i];
```

- A: Not necessarily.  $c[j]$  might alias  $a[i]$  or  $b[i]$ .
- Available expressions should handle this (recall:  $c[j] = d$  will kill any uses that might alias  $c[j]$ ).
- Conservative approximation: stores kill all available expressions

# Common Subexpression Elimination (CSE)

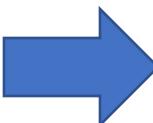
```
int c = (a + b) * 2;  
int d = (a + b) * 3;
```



```
int temp = a + b;  
int c = temp * 2;  
int d = temp * 3
```

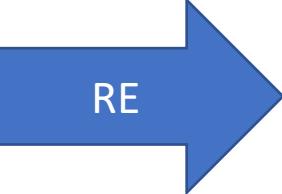
# In LLVM, CSE = reusing expressions!

```
int c = (a + b) * 2;  
int d = (a + b) * 3;
```



```
int temp = a + b;  
int c = temp * 2;  
int d = temp * 3
```

```
%temp1 = add i32 %a %b  
%c = mul i32 %temp1 2  
%temp2 = add i32 %a %b  
%d = mul i32 %temp2 3
```



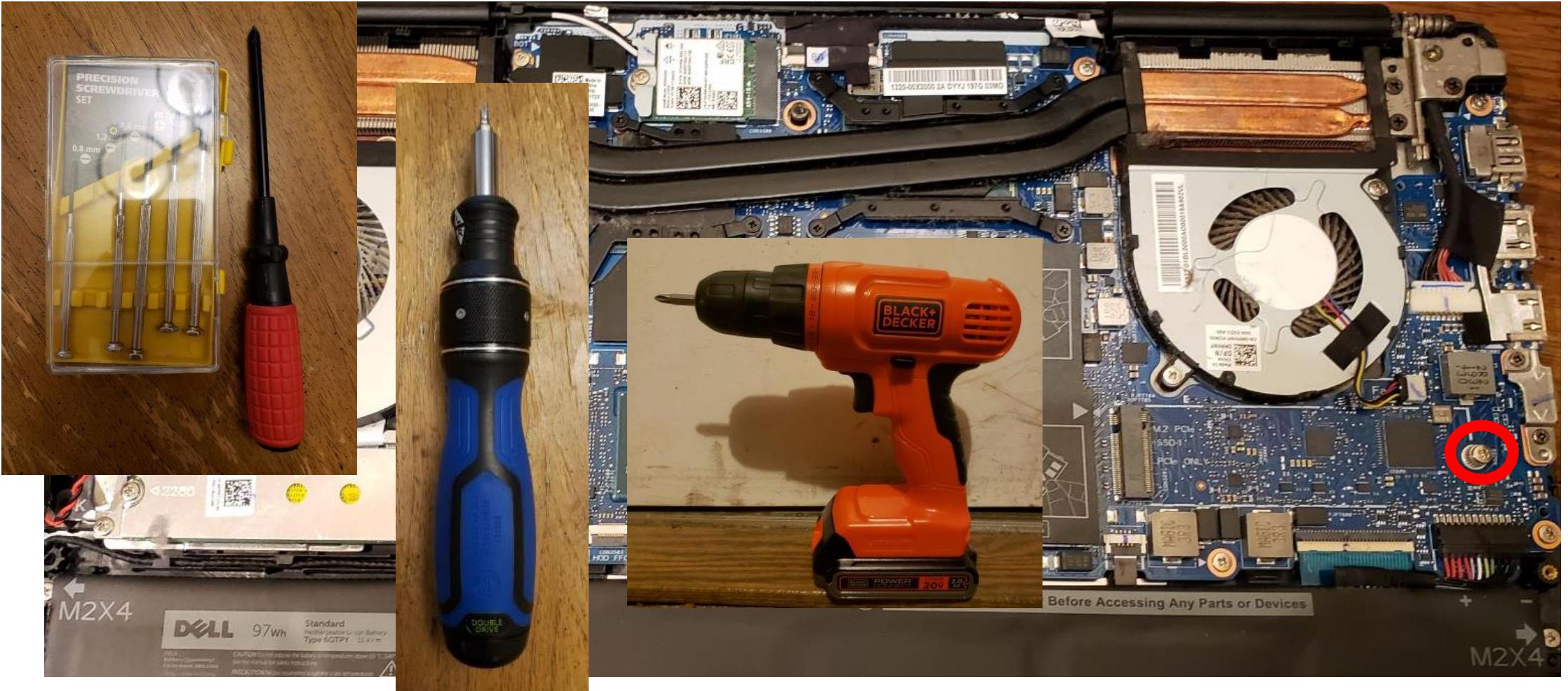
```
%temp1 = add i32 %a %b  
%c = mul i32 %temp1 2  
%temp2 = %temp1  
%d = mul i32 %temp2 3
```

CP, DCE can further optimize

# Common Subexp. Elim.: Summary

- What does it optimize?
  - Time, space
- When is it safe?
  - As long as expressions are available
- When is it an optimization?
  - Probably always

# Strength Reduction



# Strength Reduction – Replace expensive operations w/ cheaper ones



$x * 2$

$x * 3$



$x + x$

$x + x + x$



$x \ll 1$

# Strength Reduction: Summary

- What does it optimize?
  - Time (at proc. cycle level)
- When is it safe?
  - Always
- When is it an optimization?
  - When assumptions about architecture hold

# Function Inlining: function calls are *expensive*

```
int double(int a) {  
    return a * 2;  
}  
  
int main() {  
    int a = 2;  
    int b = double(a);  
    int c = double(b);  
    return c;  
}
```

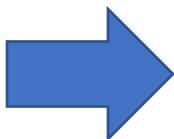
```
_double:  
addi sp,sp,-8  
sw fp,4(sp)  
sw ra,0(sp)  
addi fp,sp,4  
addi sp,sp,0
```

```
...  
double_exit:  
addi sp,fp,-4  
lw fp,4(sp)  
lw ra,0(sp)  
addi sp,sp,8  
jalr zero,ra,0
```

```
lw t0,double  
jalr ra,t0,0  
addi sp,sp,-32  
addi s1,a0,0
```

# Function Inlining: function calls are *expensive*

```
int double(int a) {  
    return a * 2;  
}  
  
int main() {  
    int a = 2;  
    int b = double(a);  
    int c = double(b);  
    return c;  
}
```



```
int main() {  
    int a = 2;  
    int b = a * 2;  
    int c = b * 2;  
    return c;  
}
```

# Function Inlining Exercise

```
define i32 @f(i32 %a, i1 %b) {
    f_entry:
        br i1 %b, label %ltrue, label %lfalse
    ltrue:
        %temp1 = add i32 %a 1
        ret %temp1
    lfalse:
        %temp2 = sub i32 %a 1
        ret %temp2
}

define @g(i32 %c) {
    %r = call i32 @f(i32 %c, i1 1)
    return i32 %r
}
```

# Function Inlining Exercise

```
define i32 @f(i32 %a, i1 %b) {  
f_entry:  
    br i1 %b, label %ltrue, label %lfalse  
ltrue:  
    %temp1 = add i32 %a 1  
    ret %temp1  
lfalse:  
    %temp2 = sub i32 %a 1  
    ret %temp2  
}
```

1. Substitute arguments
2. Rename variables in the function if they conflict
3. Replace returns with assignments to the dest. of the call (in SSA, these will need to be different versions of the var)
4. Add branches back to main code (may not be necessary if only one ret)  
In SSA: Add phi function here

```
define @g(i32 %c) {  
    br i1 1, label %ltrue, label %lfalse  
ltrue:  
    %temp1 = add i32 %c 1  
    %r = %temp1  
    br label %ldone  
lfalse:  
    %temp2 = sub i32 %c 1  
    %r = %temp2  
    br label %ldone  
ldone:  
    return i32 %r  
}
```

# Inlining: Tradeoffs

- Saves instructions for function call overhead (optimizes *time*)
- But makes code bigger—makes instruction cache usage worse
- Tradeoff: usually only inline smaller functions
  - Some compilers give the inlining threshold as an option

# Eliminating unreachable code: if there are no branches to a label, can get rid of the block

