

# CS443: Compiler Construction

Lecture 4: LR parsing

# Shift-reduce parsers work for LR(k) grammars

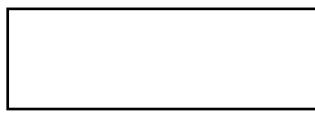


State machine with a stack and 2 actions:

- *Shift* a token onto the stack
- *Reduce* the top of the stack to a nonterminal by a production

# Shift-reduce parsers work for LR(k) grammars

Stack



$S ::= e$

Input

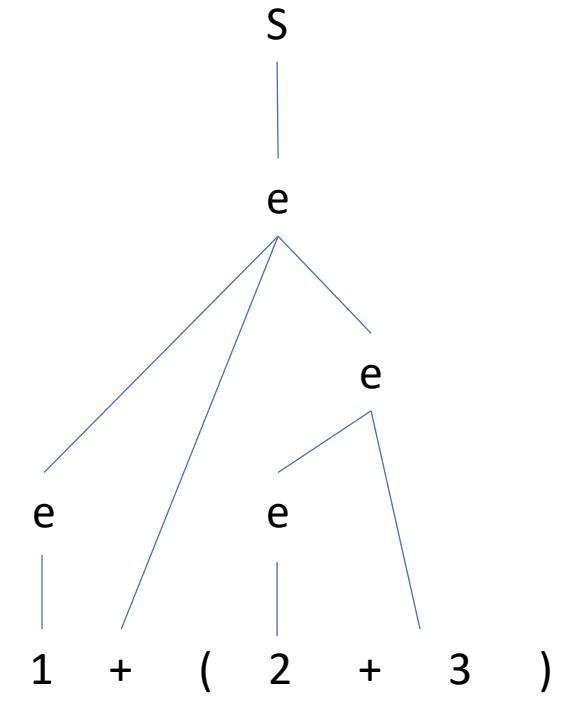
$1 + (2 + 3)\$$

1  
e  
e +  
e + (   
e + (2  
e + (e  
e + (e +  
e + (e + 3  
e + (e  
e + (e)  
e  
S

+ (2 + 3)\$  
+ (2 + 3)\$  
(2 + 3)\$  
2 + 3)\$  
+ 3)\$  
+ 3)\$  
3)\$  
)\$  
)\$  
\$  
\$

$e ::= n \mid e + n \mid e + (e)$

Shift  
Reduce  $n \rightarrow e$   
Shift  
Shift  
Shift  
Shift  
Reduce  $n \rightarrow e$   
Shift  
Shift  
Reduce  $e + n \rightarrow e$   
Shift  
Reduce  $e + (e) \rightarrow e$   
Reduce  $e \rightarrow S$ , accept



# Shift-reduce parsers make decisions based on DFAs

- Edges: terminals + nonterminals on stack
- Just treat the stack as a stack of states (can reconstruct orig. stack)
- Transition table has two parts:
  - ACTION(state, terminal)
    - $sn$  – shift state  $n$  onto stack
    - $rn$  – reduce using rule  $n$
    - $a$  – accept
    - error (leave the table blank)
  - GOTO(state, nonterminal)
    - next state

# Building the DFA for LR(0) parsing (see book for details)

- Items: Productions with a  $.$  indicating where we are
  - e.g.  $e \rightarrow e + . n$
- DFA states = sets of items

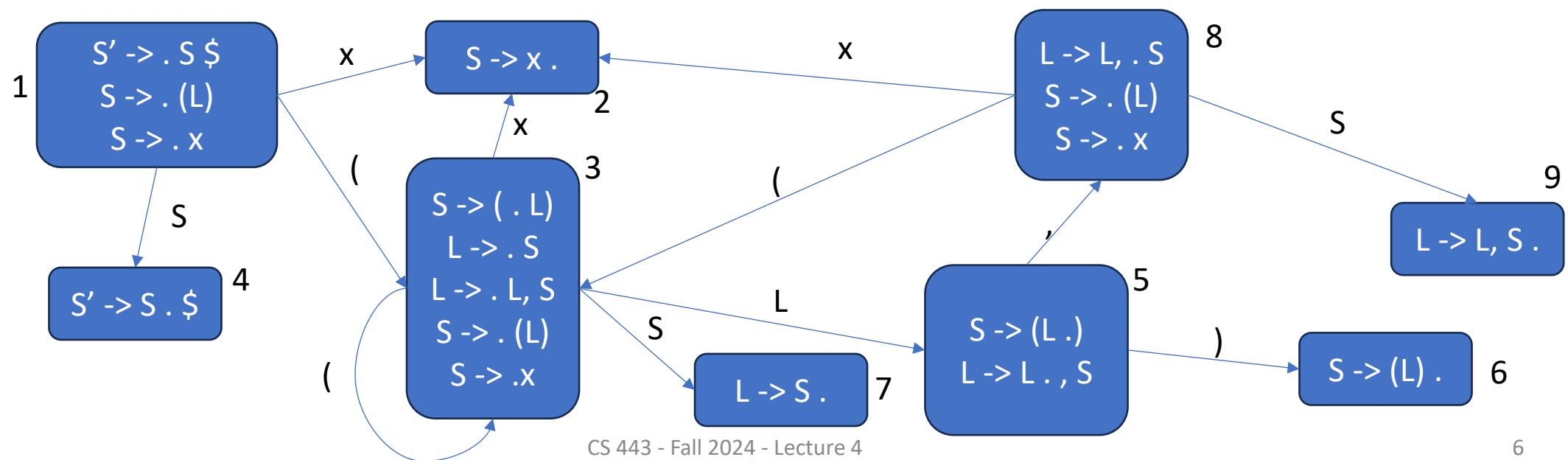
1  $S' \rightarrow S\$$   
2  $S \rightarrow (L)$   
3  $S \rightarrow x$   
4  $L \rightarrow S$   
5  $L \rightarrow L, S$



$S' \rightarrow . S\$$   
 $S' \rightarrow S . \$$   
 $S \rightarrow . (L)$   
 $S \rightarrow ( . L)$   
 $S \rightarrow (L . )$   
 $S \rightarrow (L) .$   
 $S \rightarrow . x$   
 $S \rightarrow x .$   
 $L \rightarrow . S$   
 $L \rightarrow S .$   
 $L \rightarrow . L, S$   
 $L \rightarrow L . , S$   
 $L \rightarrow L, . S$   
 $L \rightarrow L, S .$

	(	)	x	,	\$	s	L
1	s3		s2			4	
2	r3	r3	r3	r3	r3		
3	s3		s2			7	5
4					a		
5		s6		s8			
6	r2	r2	r2	r2	r2		
7	r4	r4	r4	r4	r4		
8	s3		s2			9	
9	r5	r5	r5	r5	r5		

- 1  $S' \rightarrow S\$$   
 2  $S \rightarrow (L)$   
 3  $S \rightarrow x$   
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 5  $L \rightarrow L, S$



	(	)	x	,	\$	s	L
1	s3		s2			4	
2	r3	r3	r3	r3	r3		
3	s3		s2			7	5
4					a		
5		s6		s8			
6	r2	r2	r2	r2	r2		
7	r4	r4	r4	r4	r4		
8	s3		s2			9	
9	r5	r5	r5	r5	r5		

1  $S' \rightarrow S\$$

2  $S \rightarrow (L)$

3  $S \rightarrow x$

4  $L \rightarrow S$

5  $L \rightarrow L, S$

Stack of states	Stack	Input
1		$(x, (y))\$$
13	(	$x, (y))\$$
132	(x	$, (y))\$$
13	(S	$, (y))\$$
137	(S	$, (y))\$$
13	(L	$, (y))\$$
135	(L	$, (y))\$$
1358	(L,	$(y))\$$
13583	(L, (	$y))\$$
135832	(L, (y	$))\$$
13583	(L, (S	$))\$$
135837	(L, (S	$))\$$
13583	(L, (L	$))\$$
135835	(L, (L	$))\$$
1358356	(L, (L)	$)\$$
1358	(L, S	$)\$$
13589	(L, S	$)\$$
13	(L	$)\$$
135	(L	$)\$$
1356	(L)	$\$$
1	S	$\$$
14	S	$\$$