

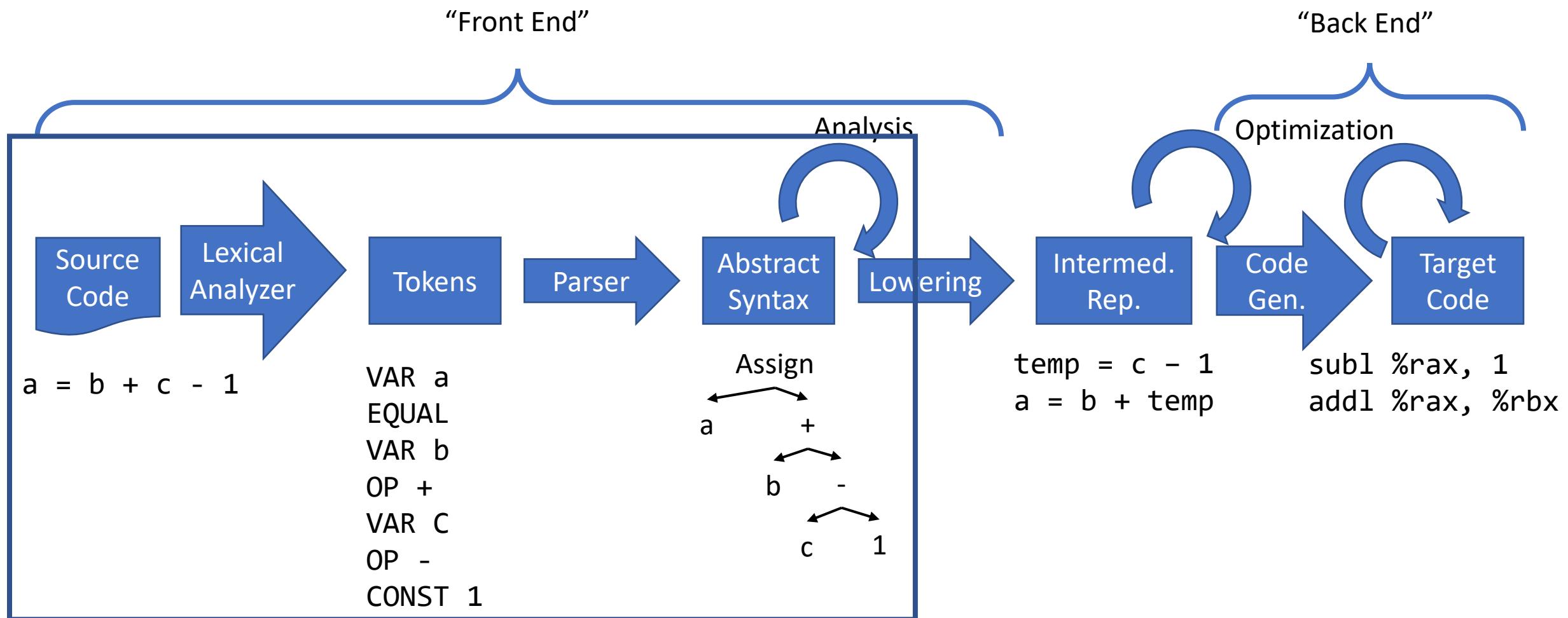
CS443: Compiler Construction

Lecture 2: Lexing, Finite State Machines, Regular Expressions

Announcements

- Project 0 out, due 9/3
- Office hour *locations* swapped this week:
 - Wednesday, 10:30-11:30 SB 218E
 - Thursday, 2-3 Zoom (link in email, I'll also put it on Canvas)

Compilers translate code in phases



Terminology

- *Lexical analysis* “lexing”
- Performed by *lexical analyzer* “lexer”
- Produces stream of *tokens*

Tokens are specified using a *regular* grammar

- Regular expressions R :
- ϵ Empty string
- abc Exactly the string abc Literal
- $R_1 R_2$ R_1 followed by R_2 Concatenation
- $R_1 \mid R_2$ R_1 or R_2 Alternation
- R^* Zero or more R Kleene Star
- R^+ One or more R
- $R?$ Optional R
- $[a-z]$ a, b, c, d, ..., z

Regex examples (Alphabet: a, b)

Write a regex that recognizes all strings:

- with at least one a $(a|b)^*a(a|b)^*$
- where every a is immediately followed by a b $b^*(ab^+)^*$
- beginning and ending in b $b | (b(a|b)^*b)$

Tokens are specified using a *regular* grammar

digit ::= [0-9]

alpha ::= [a-z]

ident ::= alpha (alpha | digit)*

num ::= digit⁺

ident → IDENT s

num → NUM s

“while” -> WHILE

“+” -> PLUS...

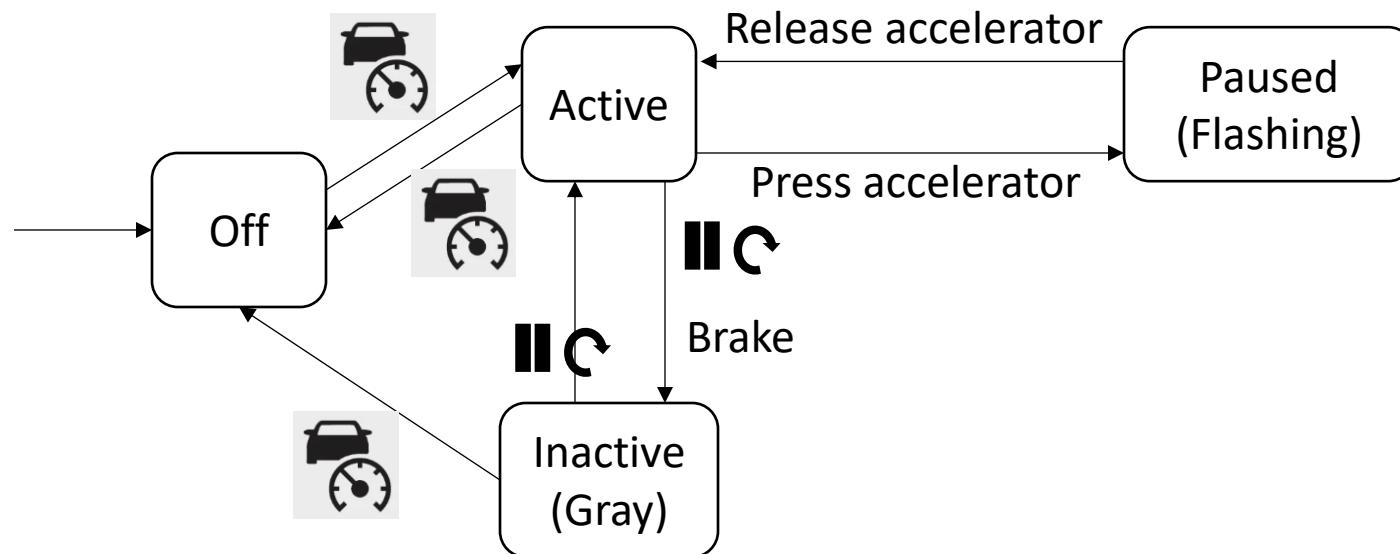
Lexing examples

- `while (i < 5)` WHILE; LPAREN; IDENT “i”; LT; NUM 5; RPAREN
- `while i < 5)` WHILE; IDENT “i”; LT; NUM 5; RPAREN
- `whole (i < 5)` IDENT “whole”; LPAREN; IDENT i; LT; NUM 5; RPAREN

Might be syntax errors
during *parsing*. Not errors
during lexing.

Regex matching can be done by finite state machines (FSMs)

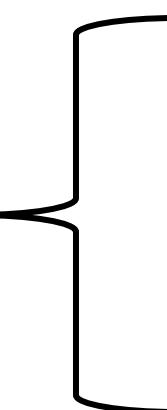
- Machine can be in one of a *finite number of states*
- Changes state by reading input



Common state machine: DFA (Deterministic Finite Automaton)

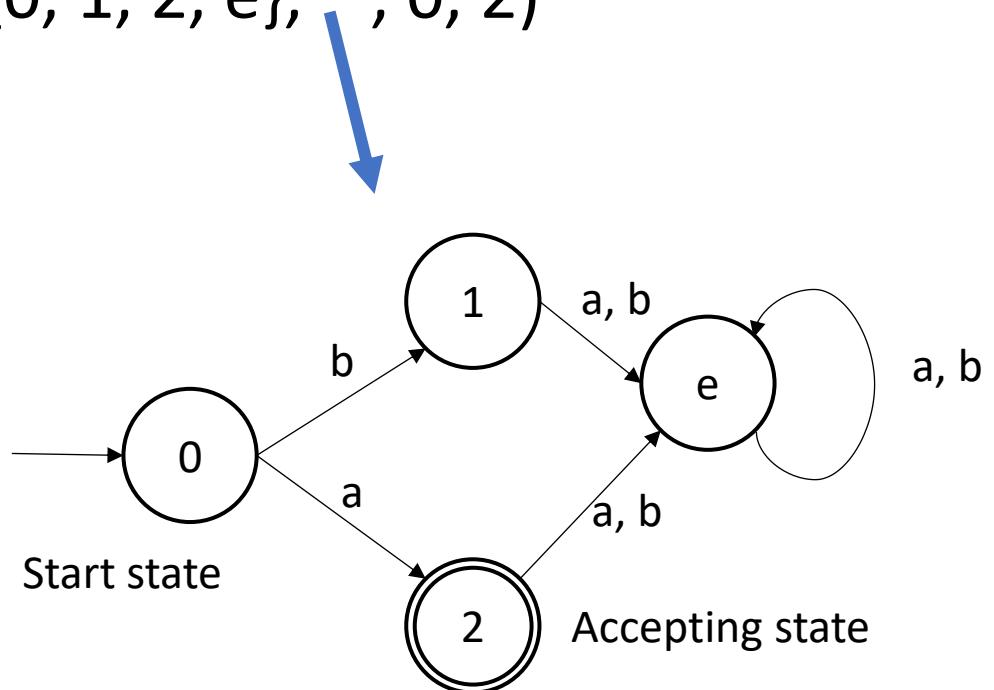
Over an alphabet Σ

Formal definition: (Q, δ, q_0, F)

- Q : A set of states
 - δ : Transition function $(Q \times \Sigma \rightarrow Q)$
 - q_0 : Start state
 - F : Set of *accepting* states
- 
- Total and deterministic –
exactly one transition for
every state, symbol

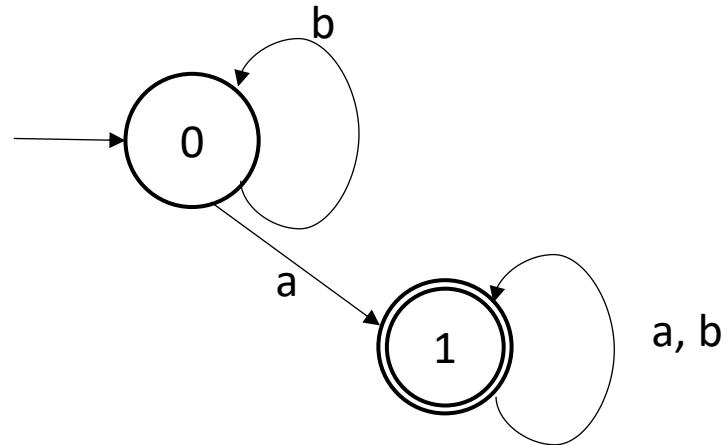
Common state machine: DFA (Deterministic Finite Automaton)

- $(\{0, 1, 2, e\}, \{a, b\}, 0, 2)$

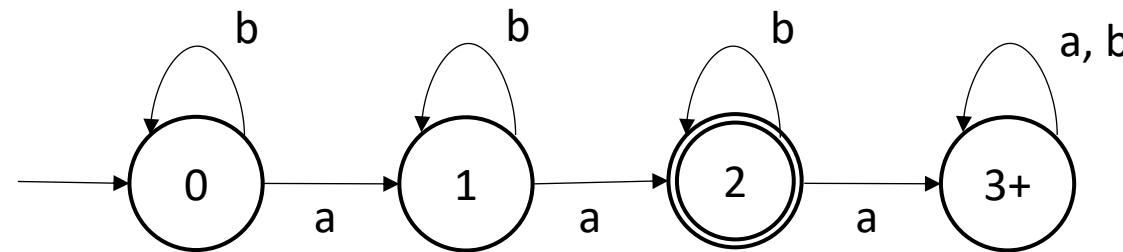


Accepts exactly “a”

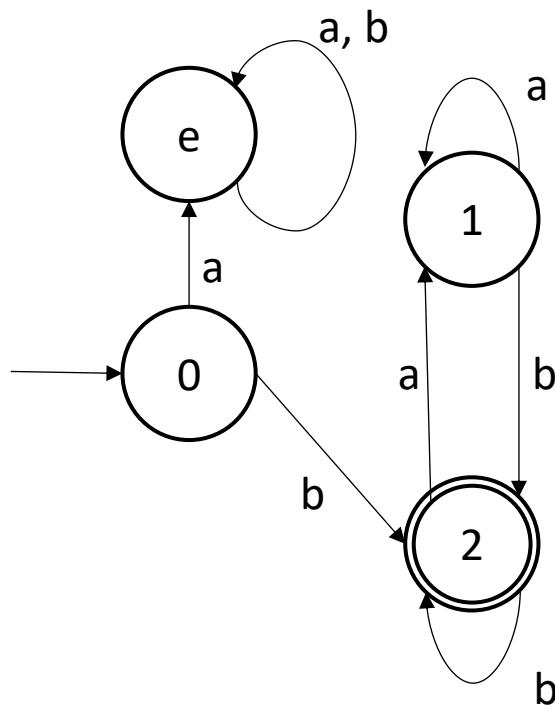
DFA for “at least one a”



DFA for “exactly two *a*s”
(Just count the number until we get to 3)

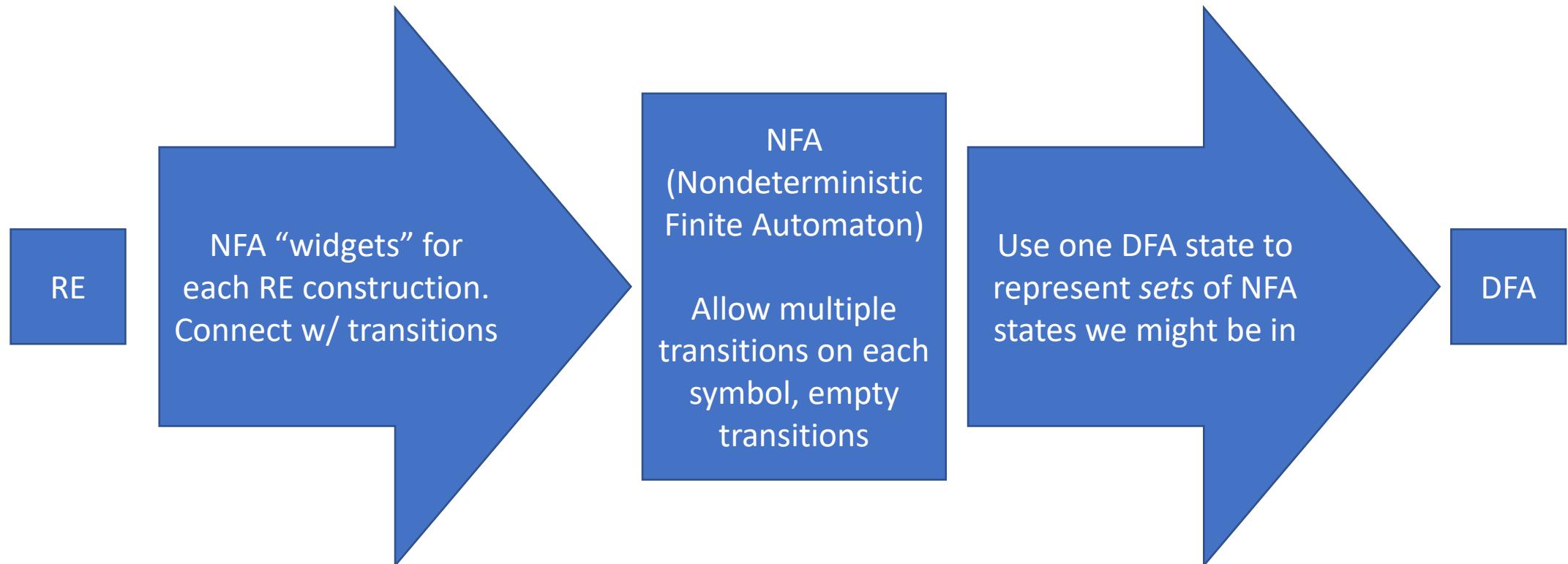


DFA for “beginning and ending with b ”



Can convert regexes to DFAs-but we don't do it directly

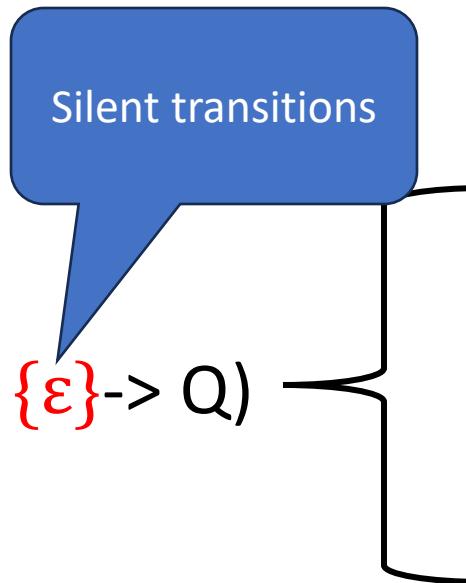
- Full algorithm in Appel, PDB. General idea:



NFAs

Formal definition: (Q, δ, q_0, F)

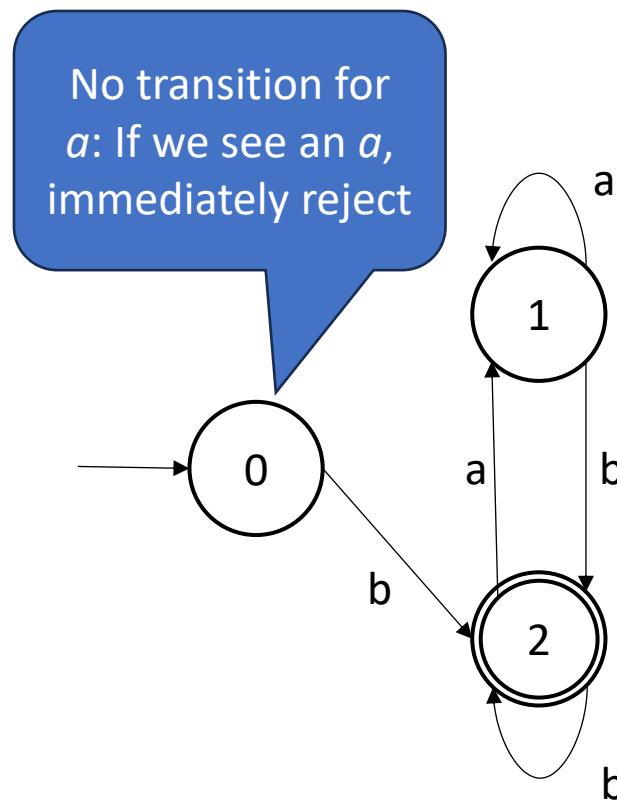
- Q : A set of states
- δ : Transition function $(Q \times \Sigma \cup \{\varepsilon\}) \rightarrow Q$
- q_0 : Start state
- F : Set of *accepting* states



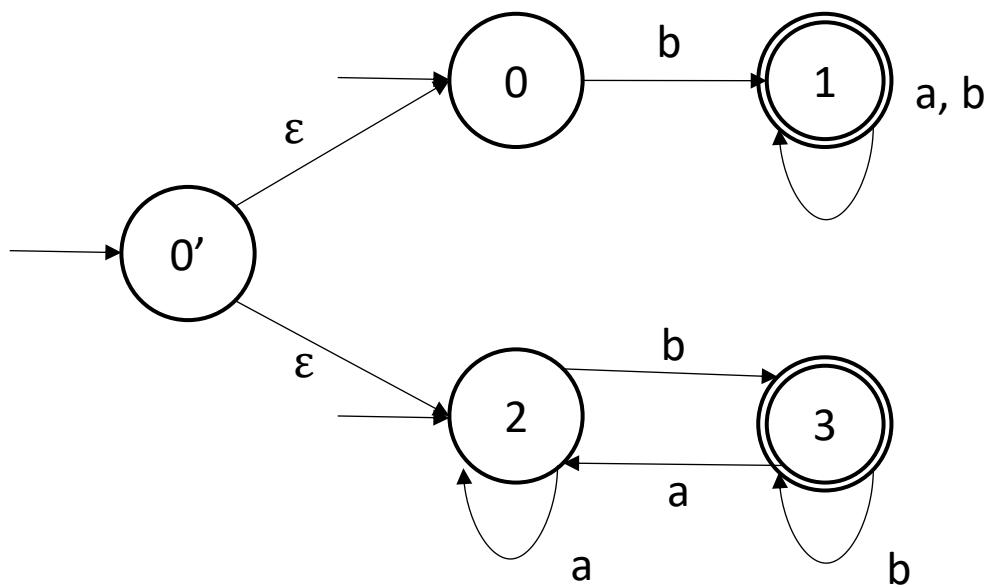
~~Total and deterministic – exactly one transition for every state, symbol~~
Zero or more transitions

Accept if there's a way to reach a final state ("try all paths at once")

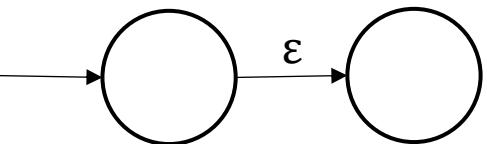
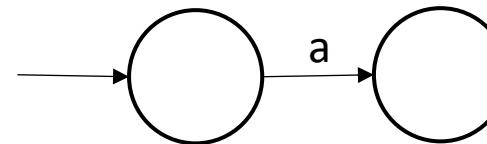
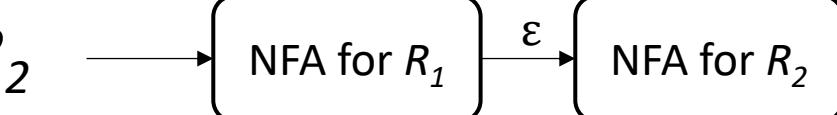
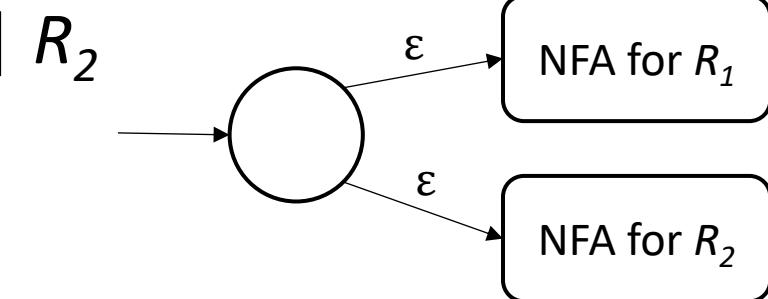
NFA for “beginning and ending with b ”

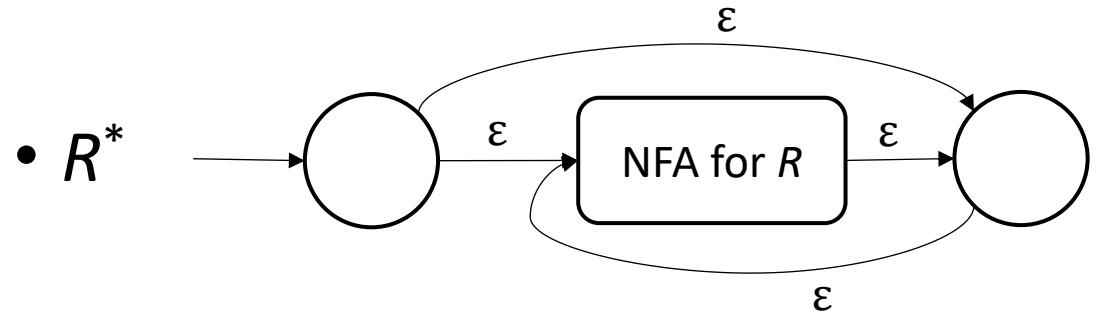


NFA for “beginning or ending with b ”



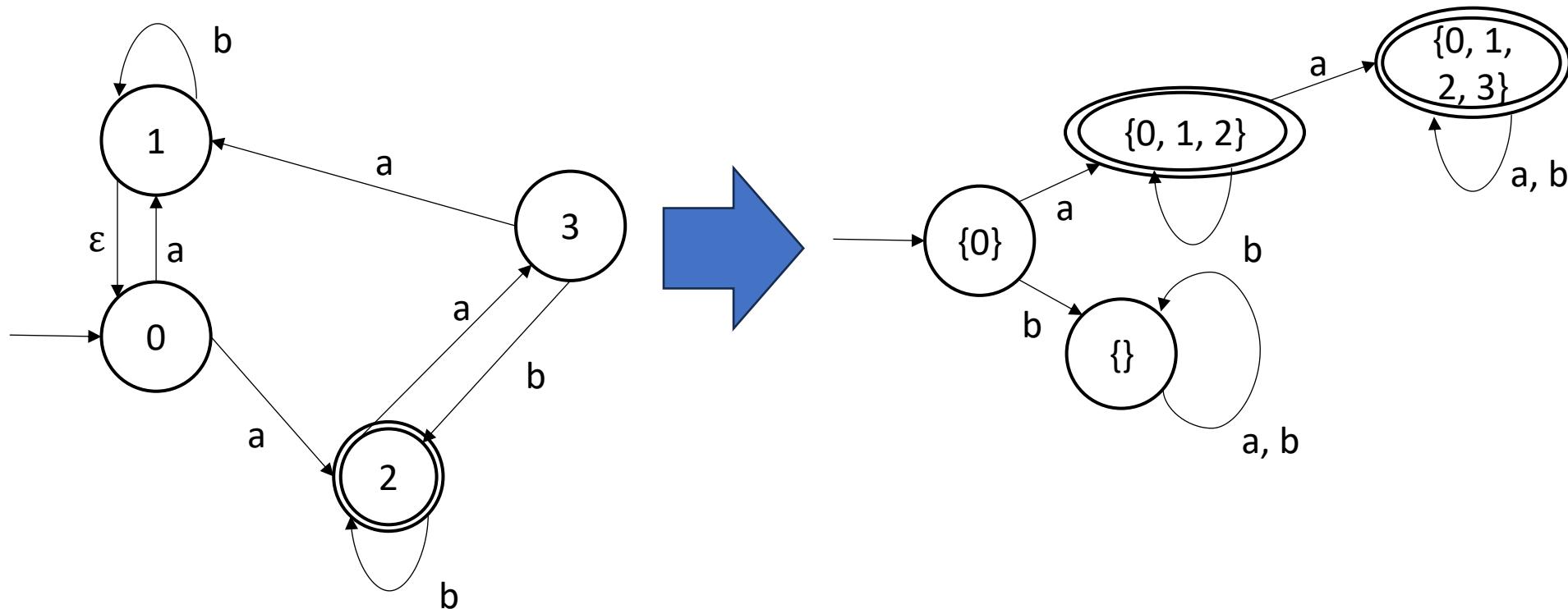
Convert Regexes to NFAs with “widgets”

- ϵ 
- a 
- $R_1 R_2$ 
- $R_1 \mid R_2$ 



Convert NFAs to DFAs with “subset construction”

- DFA states = *sets of NFA states*
- Final DFA states = contain ≥ 1 final NFA state



DFAs/regexes can't do everything

- Make a Regex/DFA for “open and close parens match”
- Impossible!
- Proof sketch: Need different states for (, (), ((), ...
- “DFAs can’t count”