

## 信号与系统实验报告

名称: 数字信号卷积和的实现及应用

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评分: \_\_\_\_\_

## 一、实验目的

1. 掌握 Matlab 中相关函数的使用，程序代码编制与调试的流程。
2. 熟悉卷积和的运算规则及其意义，加深对离散时间信号分析的理解。

## 二、实验任务

1. 完成实验内容全部题目，分析解决调试代码过程中出现的问题。
2. 认真完成本次实验小结，思考卷积和的应用。

## 三、主要设备、软件平台

1. 硬件：计算机
2. 软件：Matlab

## 四、实验内容

1. 输出杨辉三角。
  - 1) 函数编写
  - 2) 控制台输出
  - 3) 循环语句、条件语句
  - 4) 程序运行、调试

代码：

```
1  def generate numRows):
2      """
3          :type numRows: int
4          :rtype: List[List[int]]
5      """
6
7      if numRows == 0:
8          return []
9      if numRows == 1:
10         return [[1]]
11     if numRows == 2:
12         return [[1], [1, 1]]
13     numRows -= 2
14     rList = [[1], [1, 1]]
15     while numRows > 0:
16         newList = [1]
17         for i in range(len(rList[-1]) - 1):
18             newList.append(rList[-1][i] + rList[-1][i + 1])
19         newList.append(1)
20         rList.append(newList)
21         numRows -= 1
22     return rList
```

运行结果：

```
Please input the numRows
[1]
[1, 1]
[1, 2, 1]
[1, 3, 3, 1]
[1, 4, 6, 4, 1]
[1, 5, 10, 10, 5, 1]
[1, 6, 15, 20, 15, 6, 1]
[1, 7, 21, 35, 35, 21, 7, 1]
[1, 8, 28, 56, 70, 56, 28, 8, 1]
[1, 9, 36, 84, 126, 126, 84, 36, 9, 1]
[1, 10, 45, 120, 210, 252, 210, 120, 45, 10, 1]
```

2. 编程实现信号  $x(n)$ ,  $h(n)$ 间的卷积和运算函数  $my\_cov(x, h)$ , 并绘制出下列信号卷积和波形。

- 1)  $x(n)=[1,2,3,\dots,10]$ ,  $h(n)=[1,1]$
- 2)  $x(n)=[1,2,3,9,4,5,6,0,7,8]$ ,  $h(n)=[-1,2,-1]$
- 3)  $x(n)=[1,2,3,\dots,10]$ ,  $h(n)=[1,2,3,\dots,10]$

代码：

```
import matplotlib.pyplot as plt
def draw_scatter(flag,str,path,x):
    plt.title(flag)
    plt.ylim(ymax=max(x)+ 2, ymin=-2)
    plt.xticks(range(0,len(x)+2))
    plt.xlabel("x")
    plt.ylabel(str)
    plt.plot(range(0,len(x)), x, 'ro')
    plt.savefig(path)
    plt.show()
```

```
def my_cov(x, h):
    list.reverse(h)
    x = [0]*(len(h)-1)+x
    x = x + [0]*(len(h)-1)
    tp = []
    for j in range(len(x)-len(h)+1):
        temp = 0
        for i in range(len(h)):
            temp += h[i] * x[j+i]
        tp.append(temp)
    return tp
```

```
x = list(range(1,11))
h = [1,1]
y = my_cov(x,h)
print(x,'*',h,'=',y)
draw_scatter("x1_scatter","x1","x1.png",x)
draw_scatter("h1_scatter","h1","h1.png",h)
draw_scatter("x1*h1_scatter","x1*h1","x1convh1.png",y)
```

```
x = list(range(1,9))
h = [-1,2,-1]
y = my_cov(x,h)
print(x,'*',h,'=',y)
draw_scatter("x1_scatter","x1","x2.png",x)
draw_scatter("h1_scatter","h1","h2.png",h)
draw_scatter("x1*h1_scatter","x1*h1","x2convh2.png",y)
```

```
x = list(range(1,11))
h = x[:]
draw_scatter("x1_scatter","x1","x3.png",x)
draw_scatter("h1_scatter","h1","h3.png",h)
y = my_cov(x,h)
print(x,'*',end="")
print(h,end="")
print('=',y)

draw_scatter("x1*h1_scatter","x1*h1","x3convh3.png",y)
```

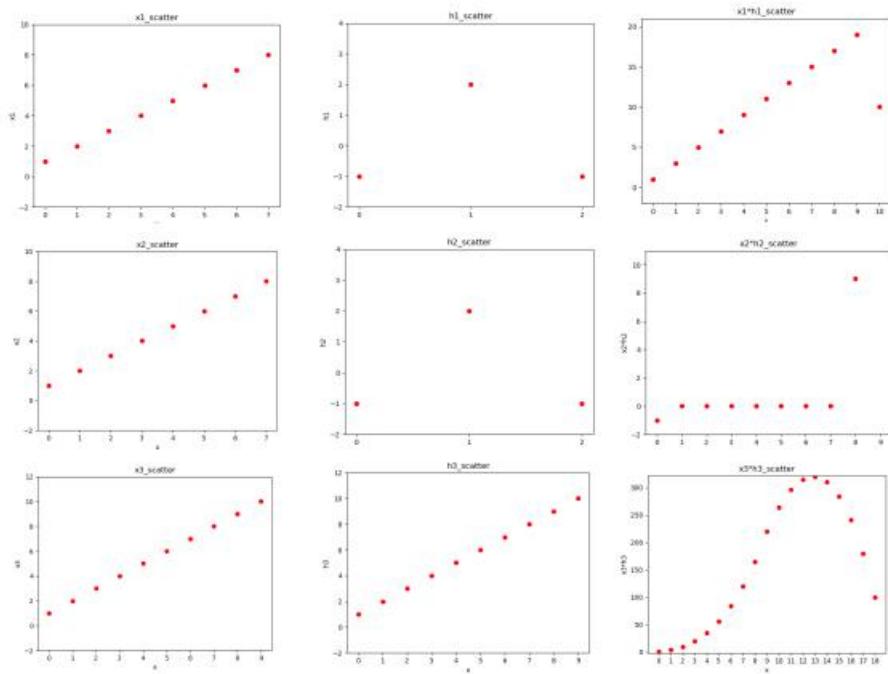
运行结果：

$$[1, 2, 3, 4, 5, 6, 7, 8, 9, 10] * [1, 1] = [1, 3, 5, 7, 9, 11, 13, 15, 17, 19, 10]$$

$$[1, 2, 3, 4, 5, 6, 7, 8] * [-1, 2, -1] = [-1, 0, 0, 0, 0, 0, 0, 0, 9, -8]$$

$$[1, 2, 3, 4, 5, 6, 7, 8, 9, 10] * [1, 2, 3, 4, 5, 6, 7, 8, 9, 10] =$$

$$[1, 4, 10, 20, 35, 56, 84, 120, 165, 220, 264, 296, 315, 320, 310, 284, 241, 180, 100]$$

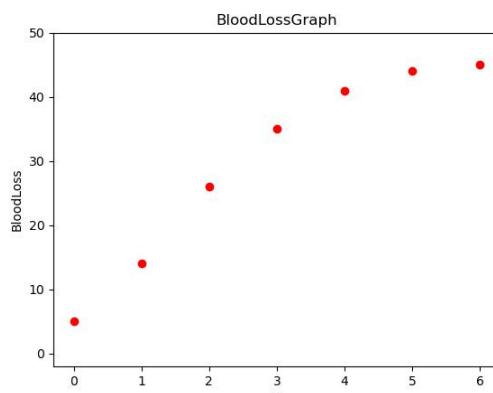


3. 设计游戏时，若对小怪使用一次技能的效果是“小怪会在接下来 5 秒内持续掉血，每秒掉血量分别为 $[5, 4, 3, 2, 1]$ ”；如果间隔 1 秒连续发动 3 次技能，请绘制出每次攻击后小怪的累计掉血量情况。

代码：

```
4 import matplotlib.pyplot as plt
5
6 def affence(i, x, y):
7     y = [0]*i + y
8     x2 = x + [0]
9
10    return np.sum([y, x2], axis=0).tolist()
11
12 def draw_scatter(path, x):
13     plt.title("BloodLossGraph")
14     plt.ylim(ymax=max(x)+5, ymin=-2)
15     plt.xticks(range(0, len(x)+3))
16     plt.xlabel("x")
17     plt.ylabel("BloodLoss")
18     plt.plot(range(0, len(x)), x, 'ro')
19     plt.savefig(path)
20     plt.show()
21
22 x = [5, 4, 3, 2, 1]
23 y = x[:]
24 x = affence(1, x, y)
25 x = affence(2, x, y)
26 for j in range(1, len(x)):
27     x[j] += x[j - 1]
28 print(x)
29 draw_scatter("BloodLoss.png", x)
```

运行结果: [5, 14, 26, 35, 41, 44, 45]



## 五、探究拓展

1. 给定一个如下所示的二维矩阵，实现其自身的卷积运算。

$$\begin{bmatrix} 0 & 1 & 0 \\ 1 & 1 & 1 \\ 0 & 1 & 0 \end{bmatrix}$$

代码：

```
import numpy as np

f = np.array([[0, 1, 0],
              [1, 1, 1],
              [0, 1, 0]], dtype=np.int_)

def cov2(f):
    f1 = f.T
    inw, inh = f.shape[0], 3
    outw = inw + 4#7
    outh = inh + 4#7
    arr = np.zeros(shape=(outw - 2, outh - 2), dtype=np.int_)
    f2 = np.zeros(shape=(outw, outh), dtype=np.int_)
    for i in range(inw):
        for j in range(inh):
            f2[i+2][j+2] = f[i][j]
    print(f2)

    for j in range(outw - inw + 1):
        for i in range(outw - inw + 1):
            s = 0
            for g in range(inw):
                for k in range(inh):
                    s += f1[g][k] * f2[g+j][k+i]
            arr[j][i] = s
    return arr

print(cov2(f))
```

运行结果：

```
[[0 0 1 0 0]
 [0 2 2 2 0]
 [1 2 5 2 1]
 [0 2 2 2 0]
 [0 0 1 0 0]]
```

## 六、实验小结

经过此次的实验我更加清楚地了解了卷积以及卷积计算方面的原理。