

### Computer Exercise 3: Binary Dependent Variable Models

**Exercise 1** *Spread betting (such as handicap betting in William Hill) is often seen in sports gambling. The file `pntsprd.csv` contains the data related to the Las Vegas (renowned for gambling) point spread for college basketball games in the USA.*

1. *A linear probability model to estimate the probability that the favored team wins is*

$$P(\text{favwin} = 1 | \text{spread}) = \beta_0 + \beta_1 \text{spread}. \quad (1)$$

*Explain why, if the spread incorporates all relevant information, we expect  $\beta_0 = 0.5$ .*

2. *Suppose now we use the probit model*

$$P(\text{favwin} = 1 | \text{spread}) = \Phi(\beta_0 + \beta_1 \text{spread}). \quad (2)$$

*If the spread incorporates all relevant information, what shall we expect  $\beta_0$  to be?*

3. *Use the data to estimate the linear probability model in (1). Test  $H_0 : \beta_0 = 0.5$  against a two-sided alternative. Use both the usual and heteroskedasticity-robust standard errors.*
4. *Is spread statistically significant? What is the estimated probability that the favored team wins when  $\text{spread} = 10$ ?*
5. *Test  $H_0 : \beta_0 = 0$  in the probit model.*
6. *Use the probit model to estimate the probability that the favored team wins when  $\text{spread} = 10$ . Compare this with the LPM estimate.*
7. *Add the variables `favhome`, `fav25`, and `und25` to the probit model. Can you notice an improvement in the McFadden  $R$ -squared measure?*
8. *Test the joint significance of these variables using the likelihood ratio test ( $2 [\ln L(\hat{\beta}_U) - \ln L(\hat{\beta}_R)]$ ) and Wald test. How many degrees of freedom should be used for the chi-square distribution? Interpret this result and check whether the spread incorporates all observable information prior to a game.*