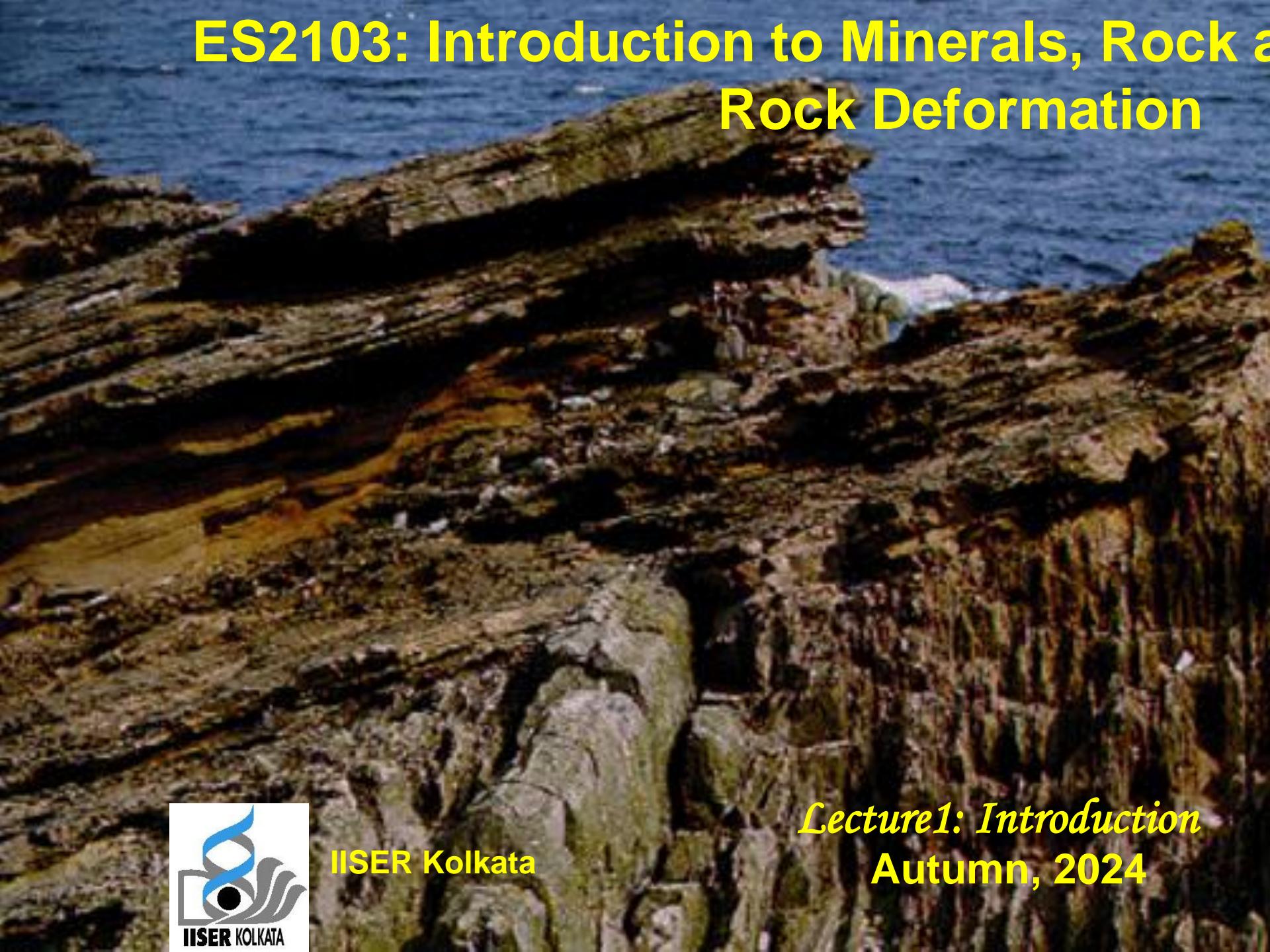


# ES2103: Introduction to Minerals, Rock and Rock Deformation

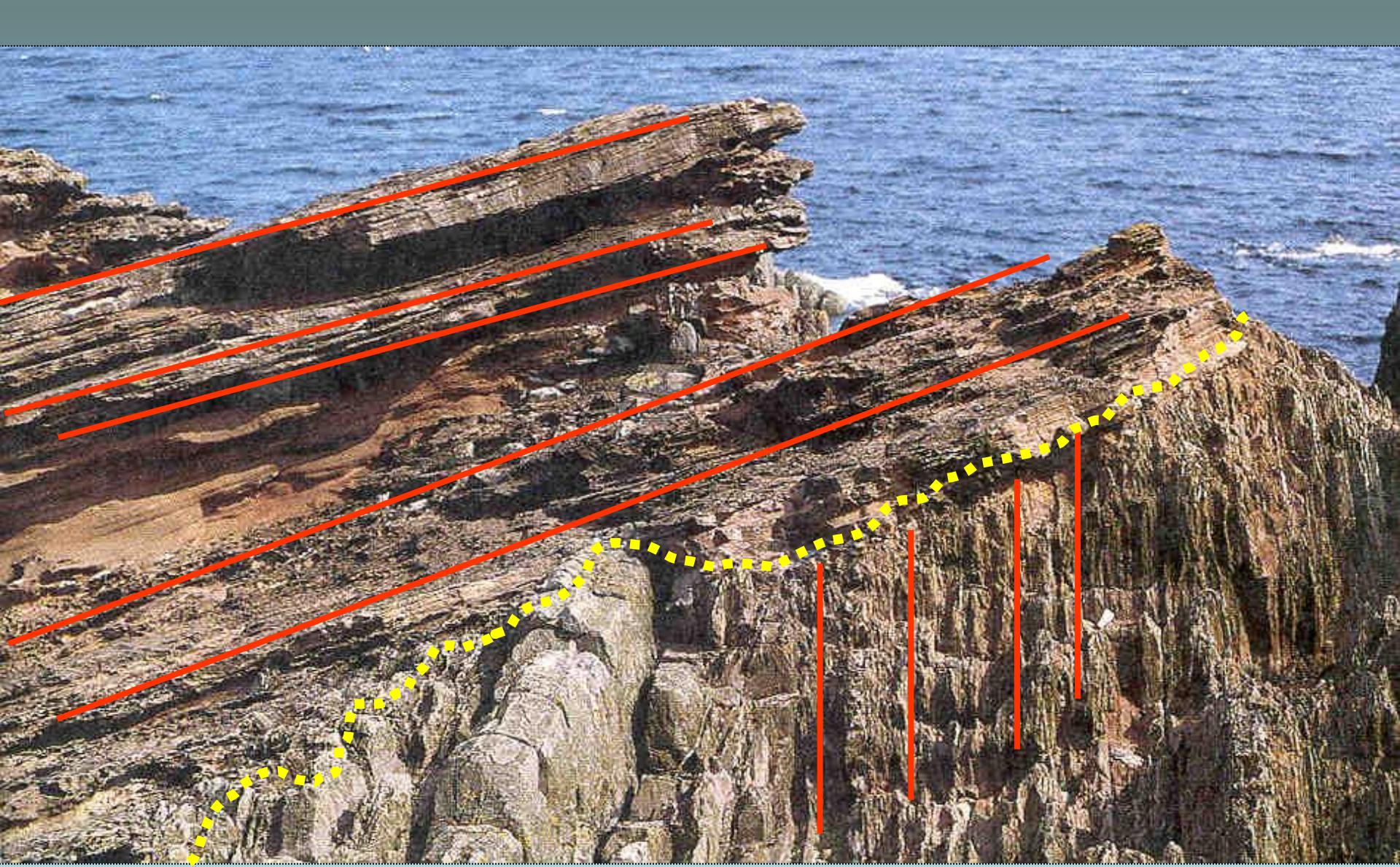


IISER Kolkata

*Lecture 1: Introduction*  
Autumn, 2024





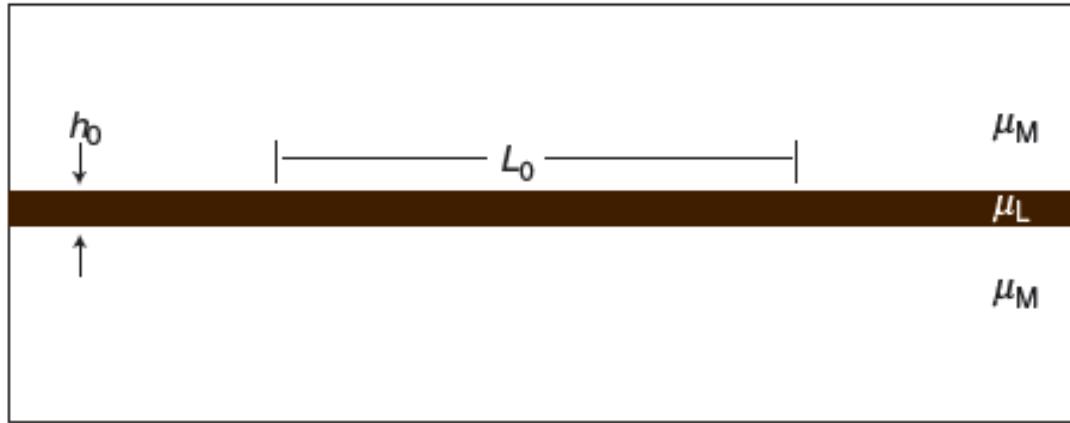


Layers that are not presently horizontal must have been some way **deformed** !

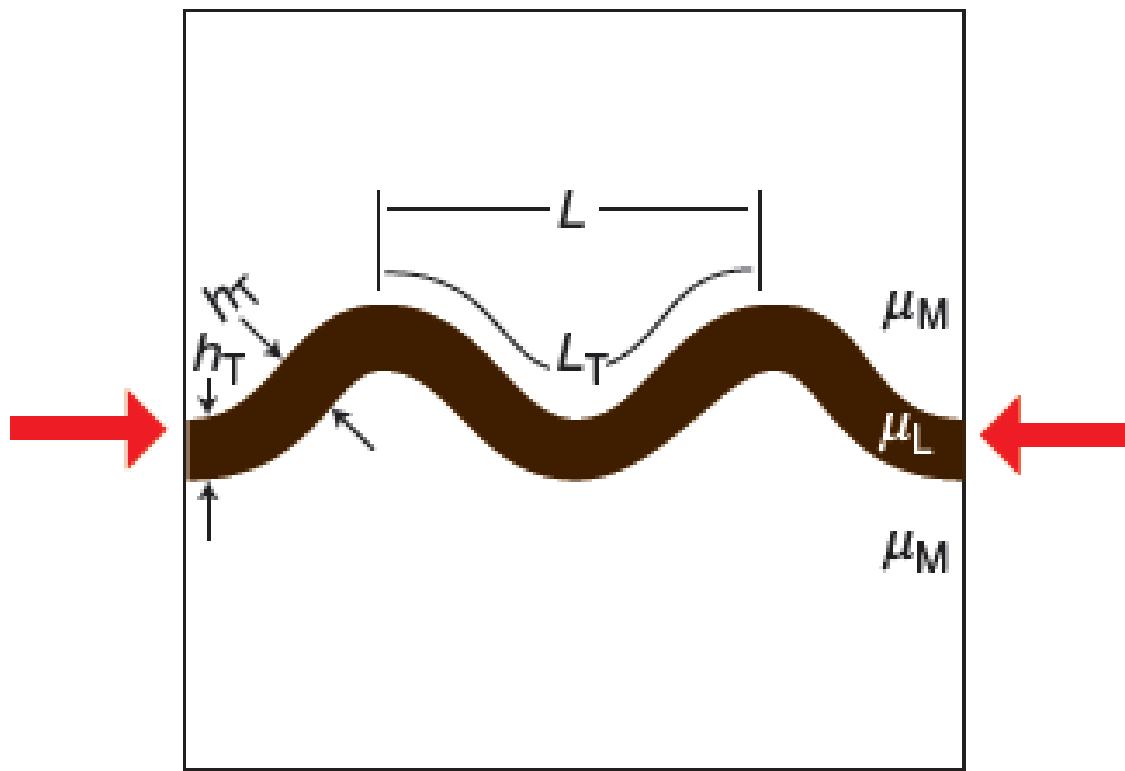
***Principle of Original Horizontality***

Nicholas Steno (17<sup>th</sup> Century)

(a)



(c)

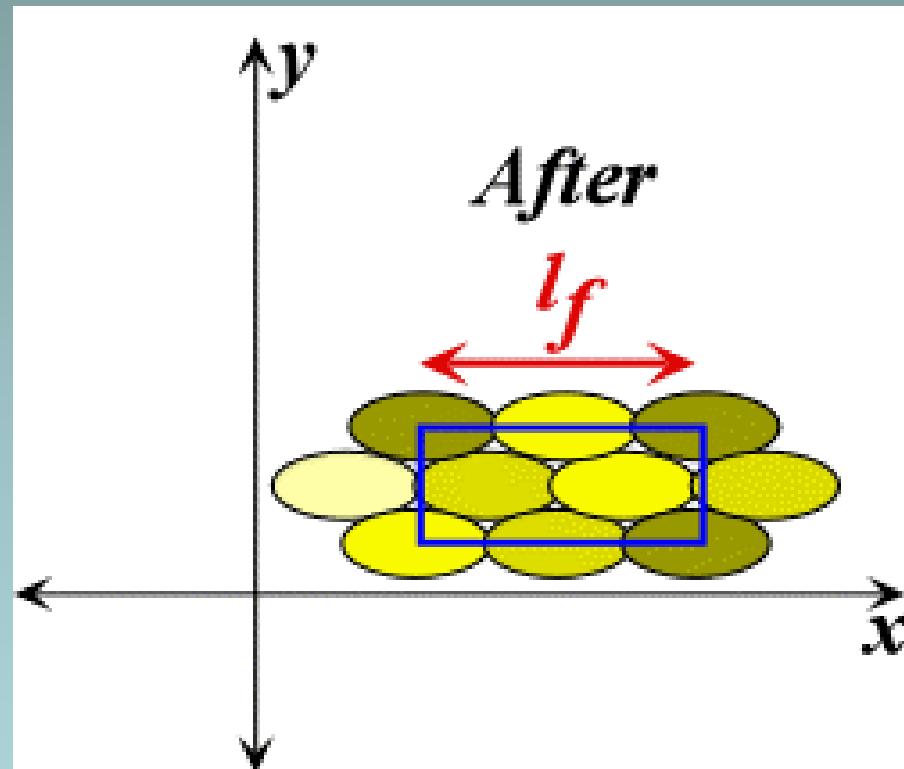
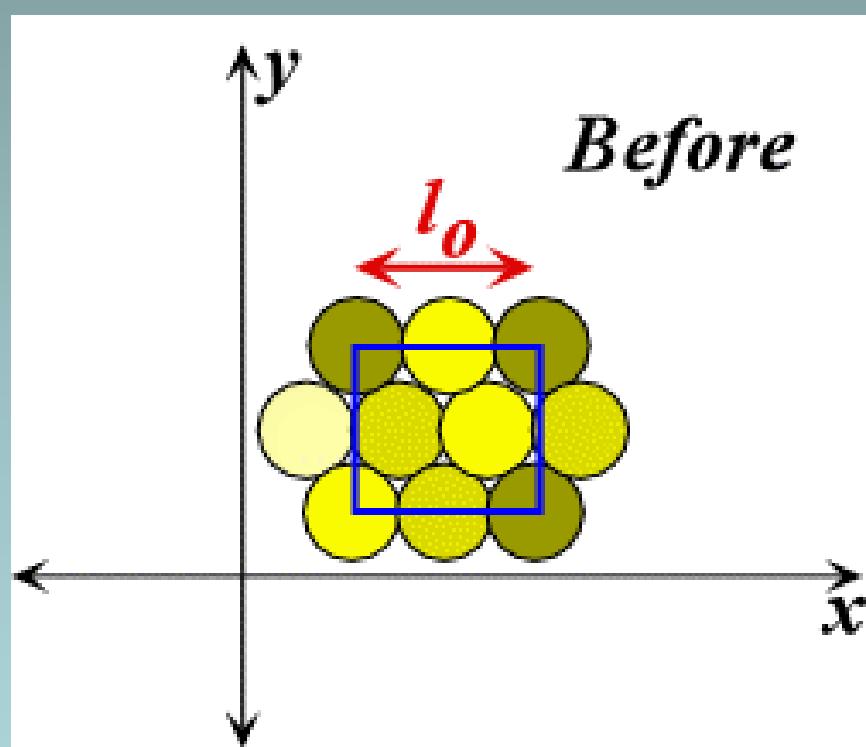


$$\mu_L > \mu_M$$

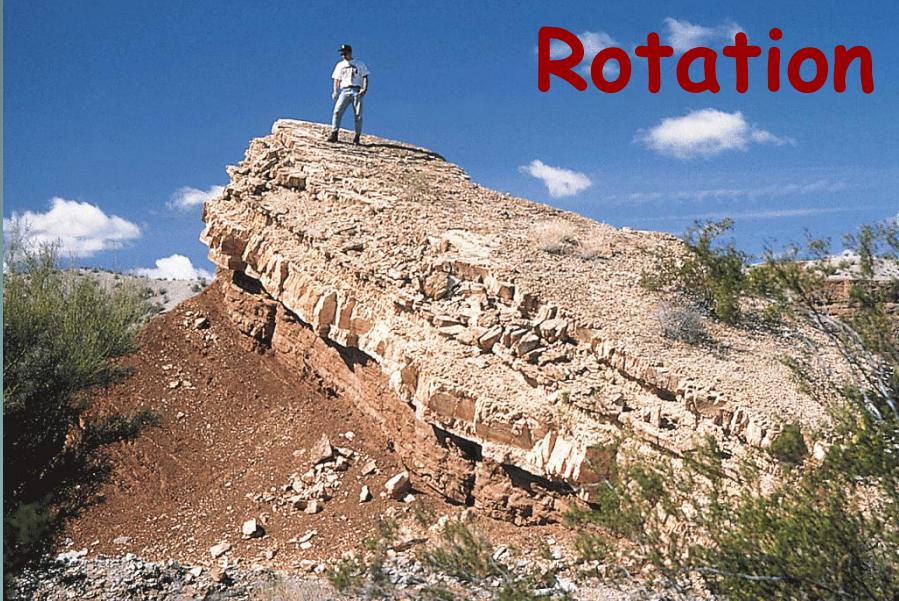
Thickening of beds  
+  
shortening of beds

# 1D strain

Change in Length of lines



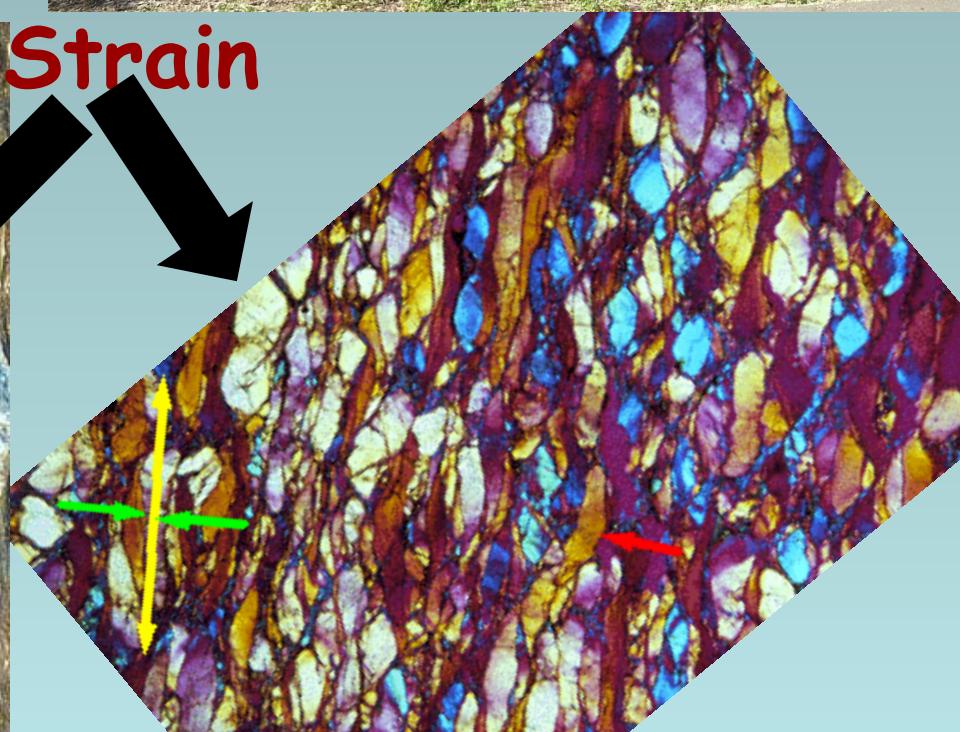
# Rotation



# Strain

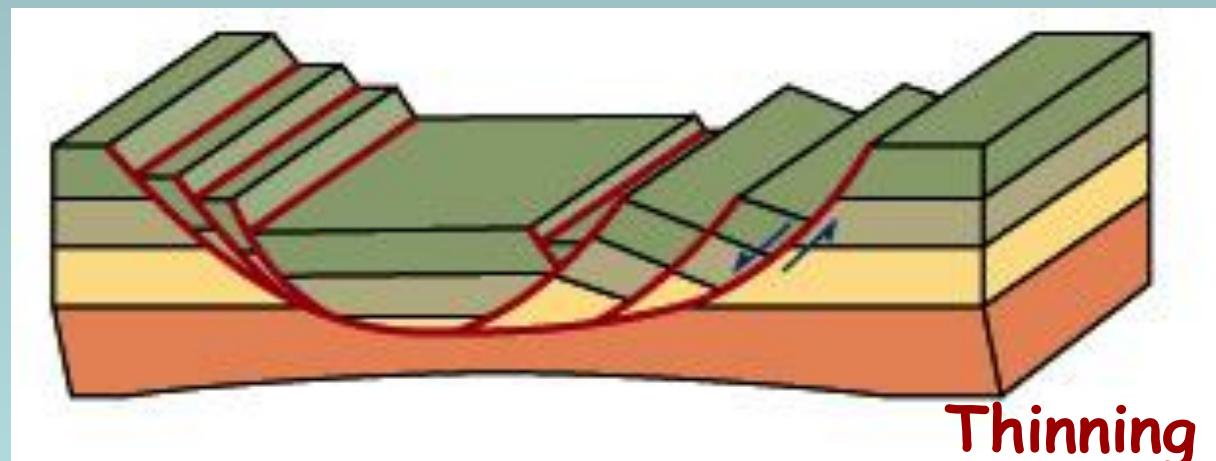
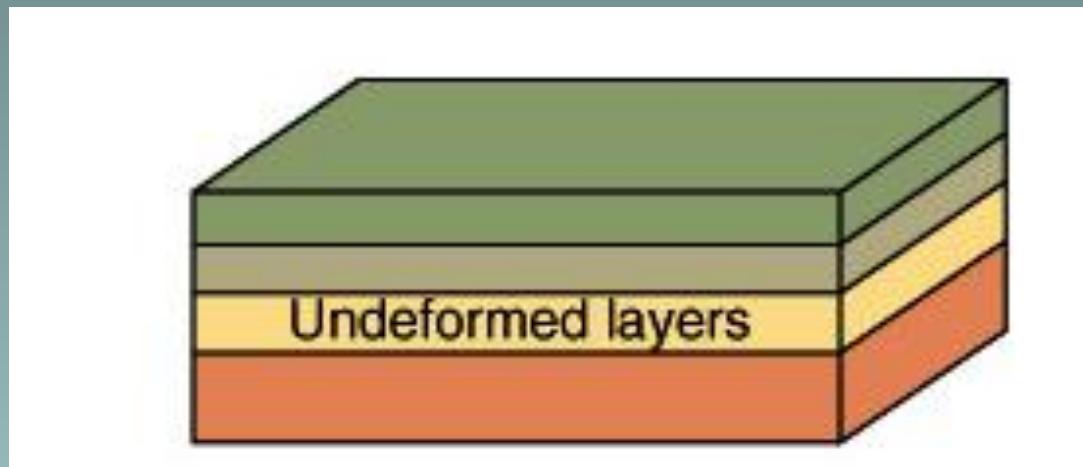


# Strain



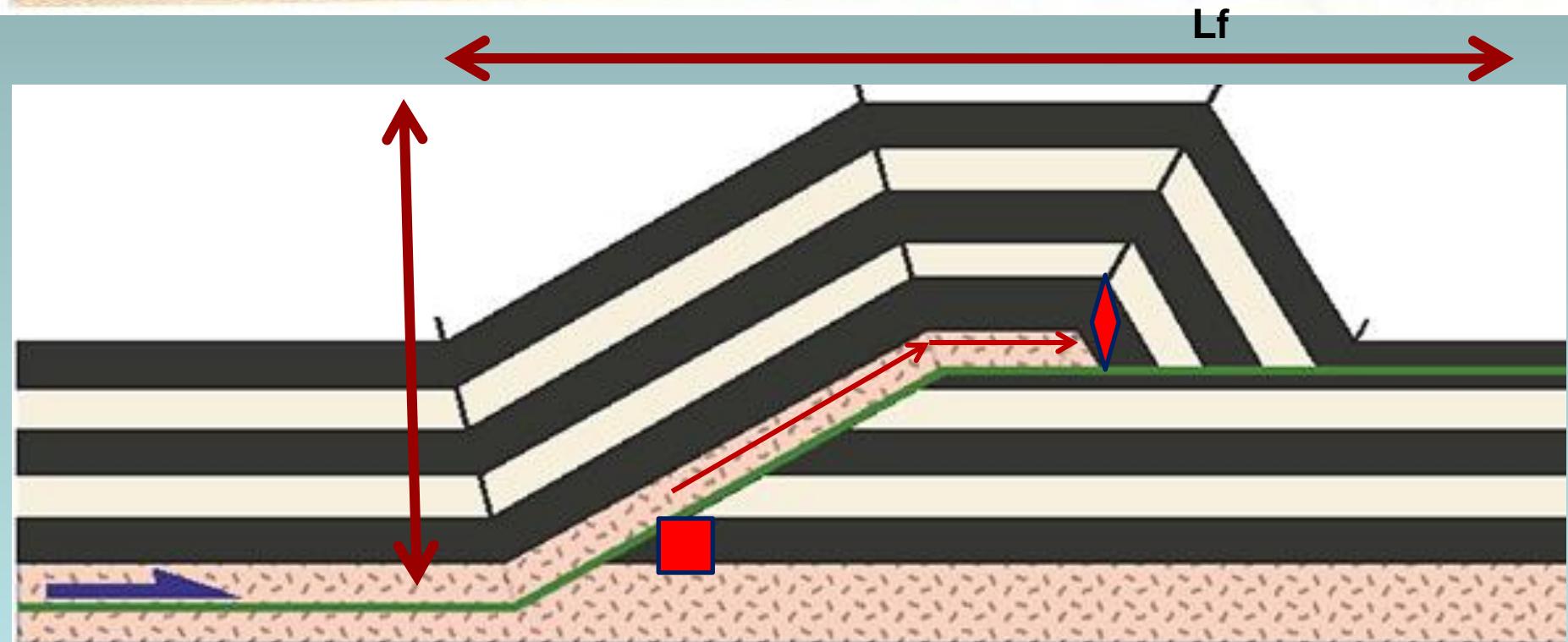
Can only shortening of rock layers?



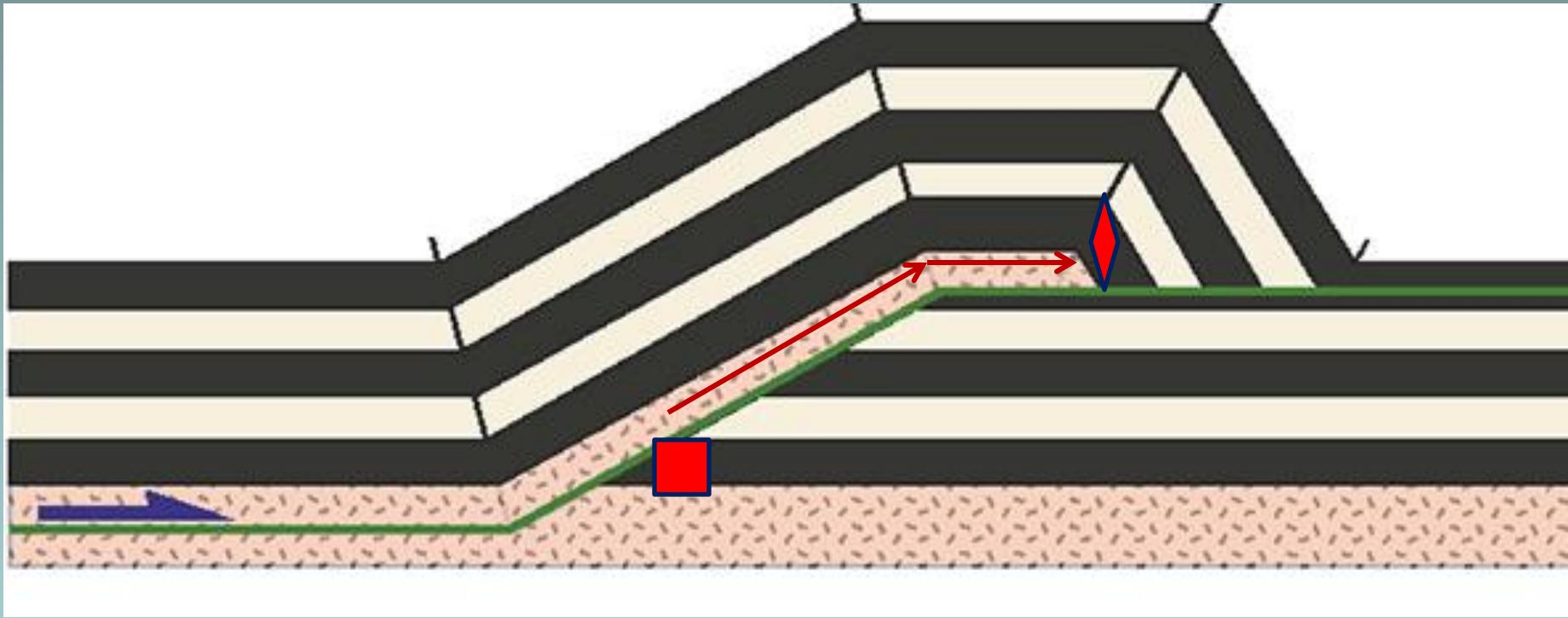


Thinning of strata  
+  
Lengthening of beds

# Deformation?



# Deformation?



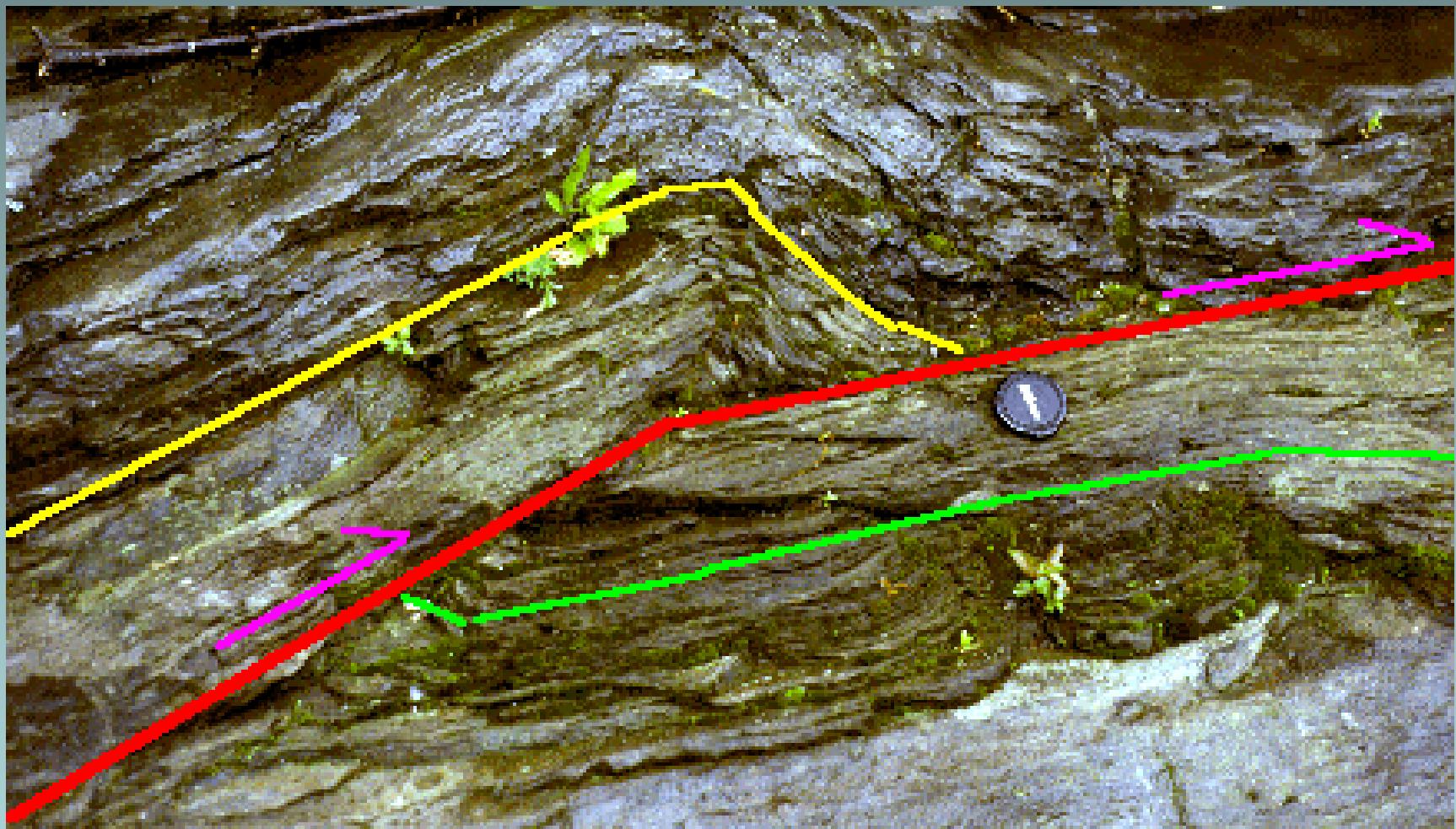
Total Displacement field: 1. Bulk Translation

2. General Deformation

Rigid Body Rotation

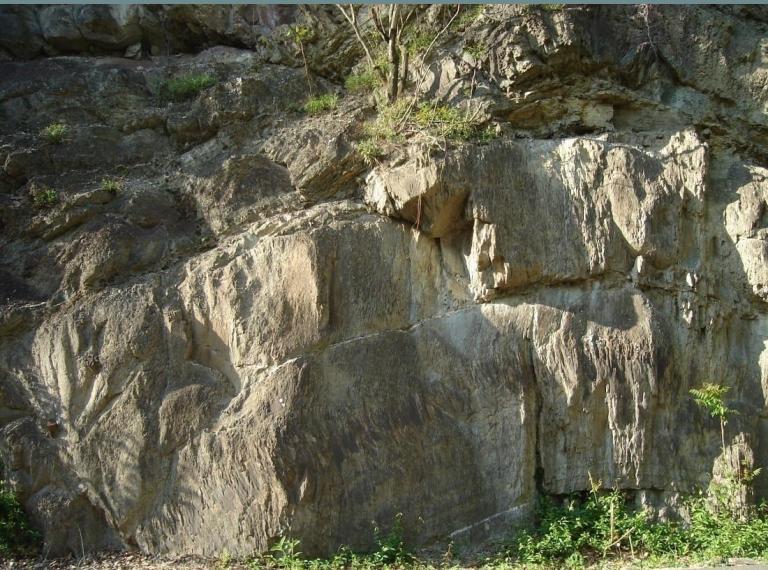
Strain

*All of these quantities are independent of each other*



**Various types of structures in same outcrop**

# Deformation in rocks: Structural Geology

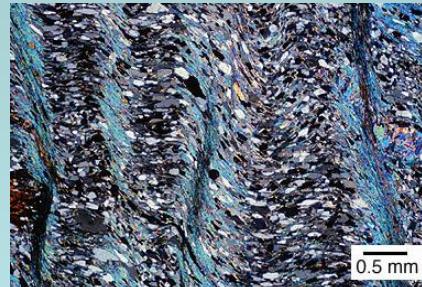
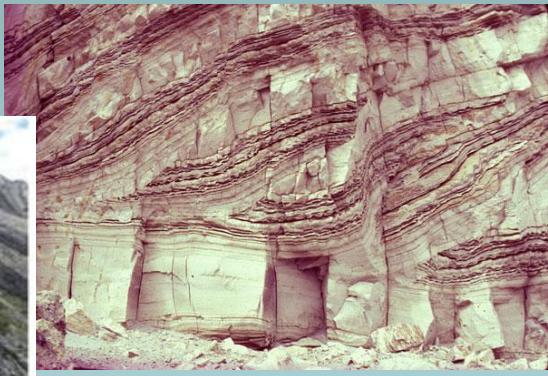


What?  
How?  
Why?

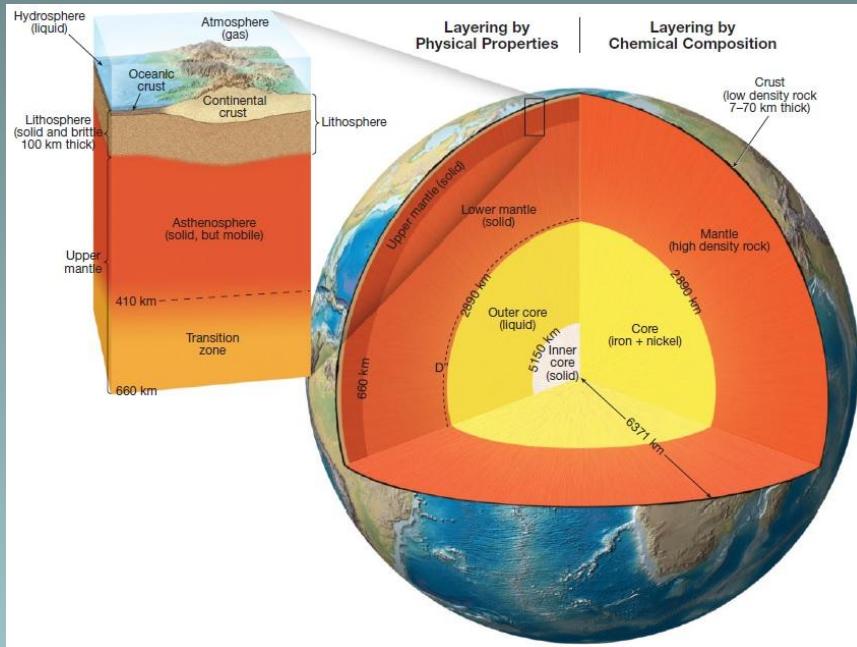


"The study of the architecture of rocks from submicroscopic to regional scales, resulting from deformation."

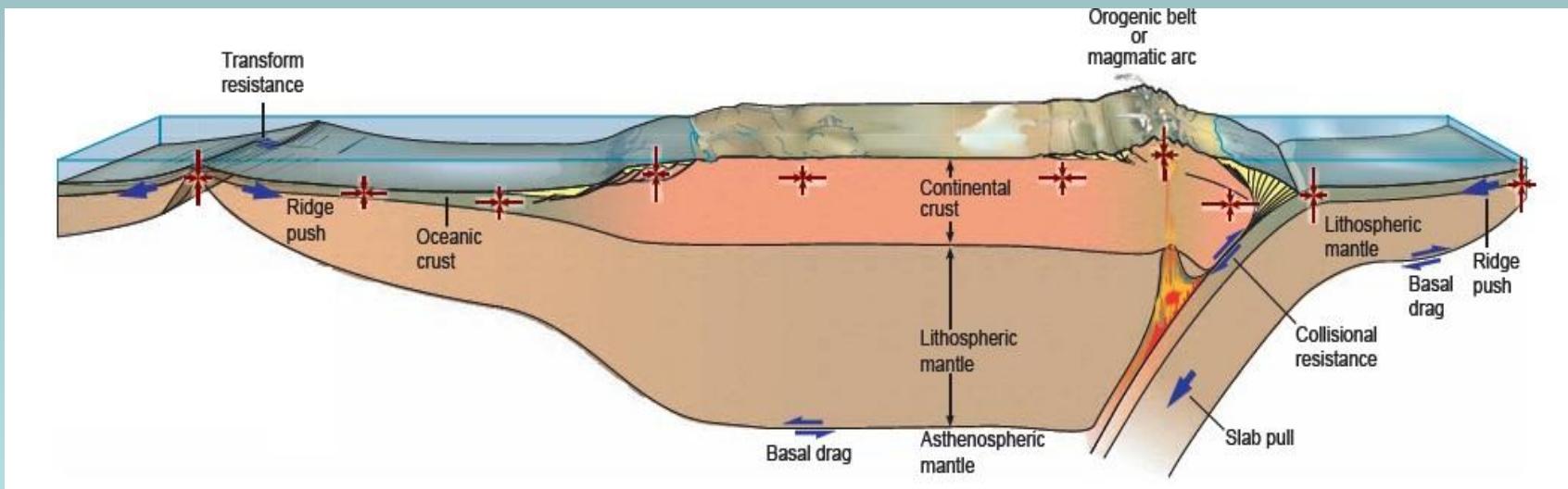
<https://blogger.googleusercontent.com/img/bua4JI0zRXOofseaKx8DLTg/s1440/recumbent-fold.jpg>



# What caused the deformation in these rocks?!

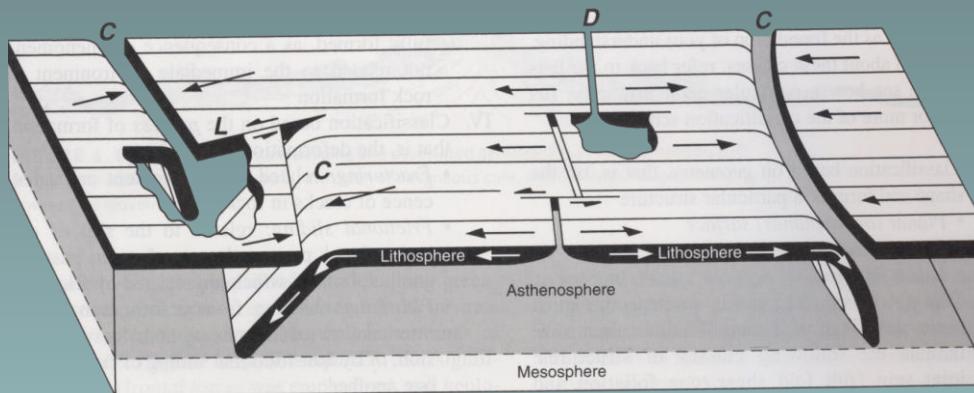


## Tectonic Forces?!



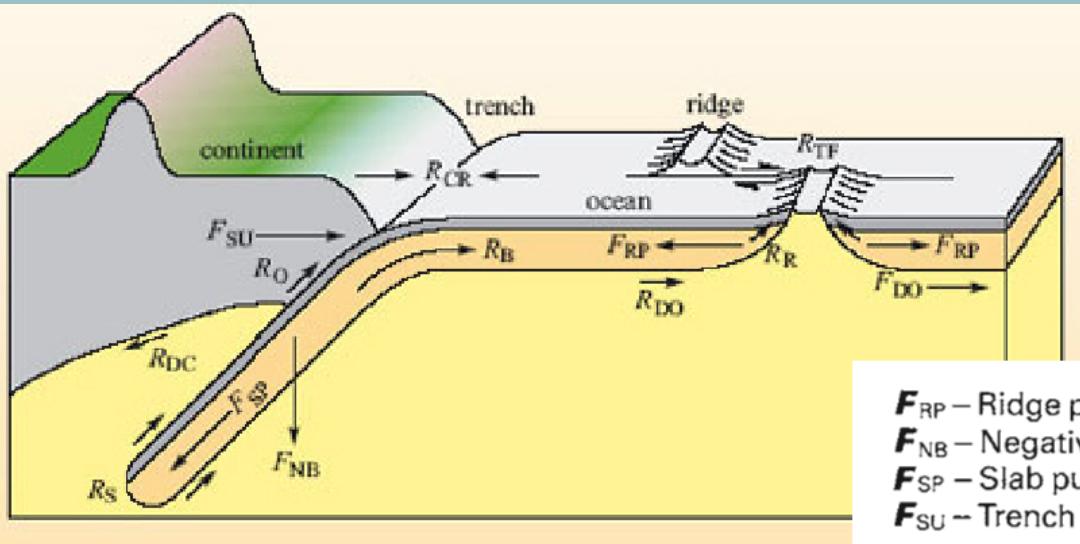
(Fossen, 2010)

# What caused the deformation in these rocks?!



Relative movement of lithospheric plates:

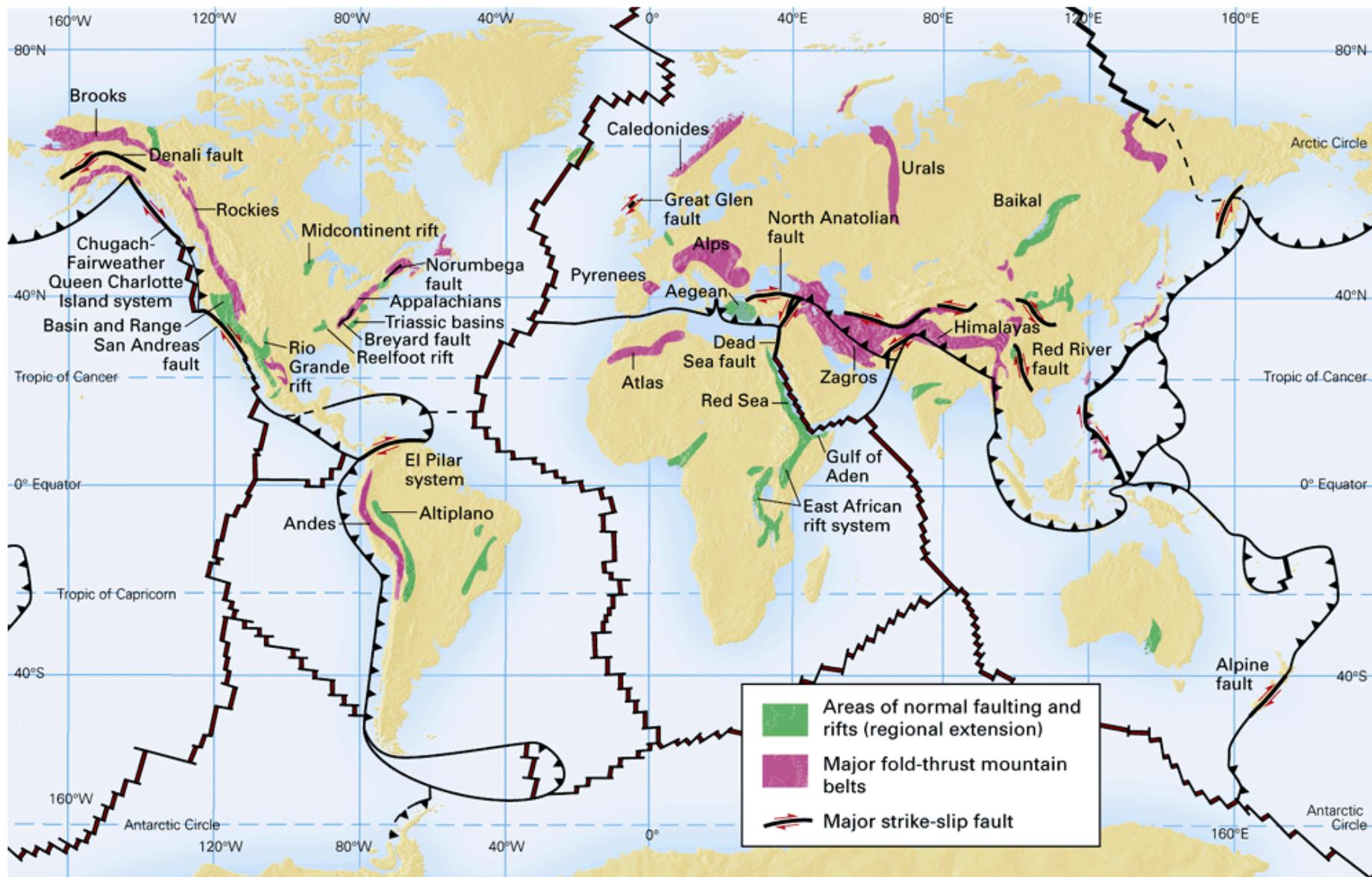
- Convergent boundary (C)
- Divergent Boundary (D)
- Transform boundary (L)



$F_{RP}$  – Ridge push  
 $F_{NB}$  – Negative buoyancy  
 $F_{SP}$  – Slab pull  
 $F_{SU}$  – Trench suction

$R_R$  – Ridge resistance  
 $R_B$  – Bending resistance  
 $R_S$  – Slab resistance  
 $R_O$  – Overriding plate resistance  
 $R_{DO}$  – Mantle drag under ocean  
 $R_{DC}$  – Mantle drag under continent

(after Forsyth and Uyeda, 1975)



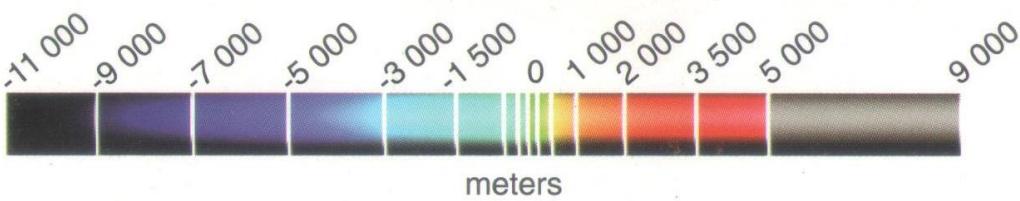
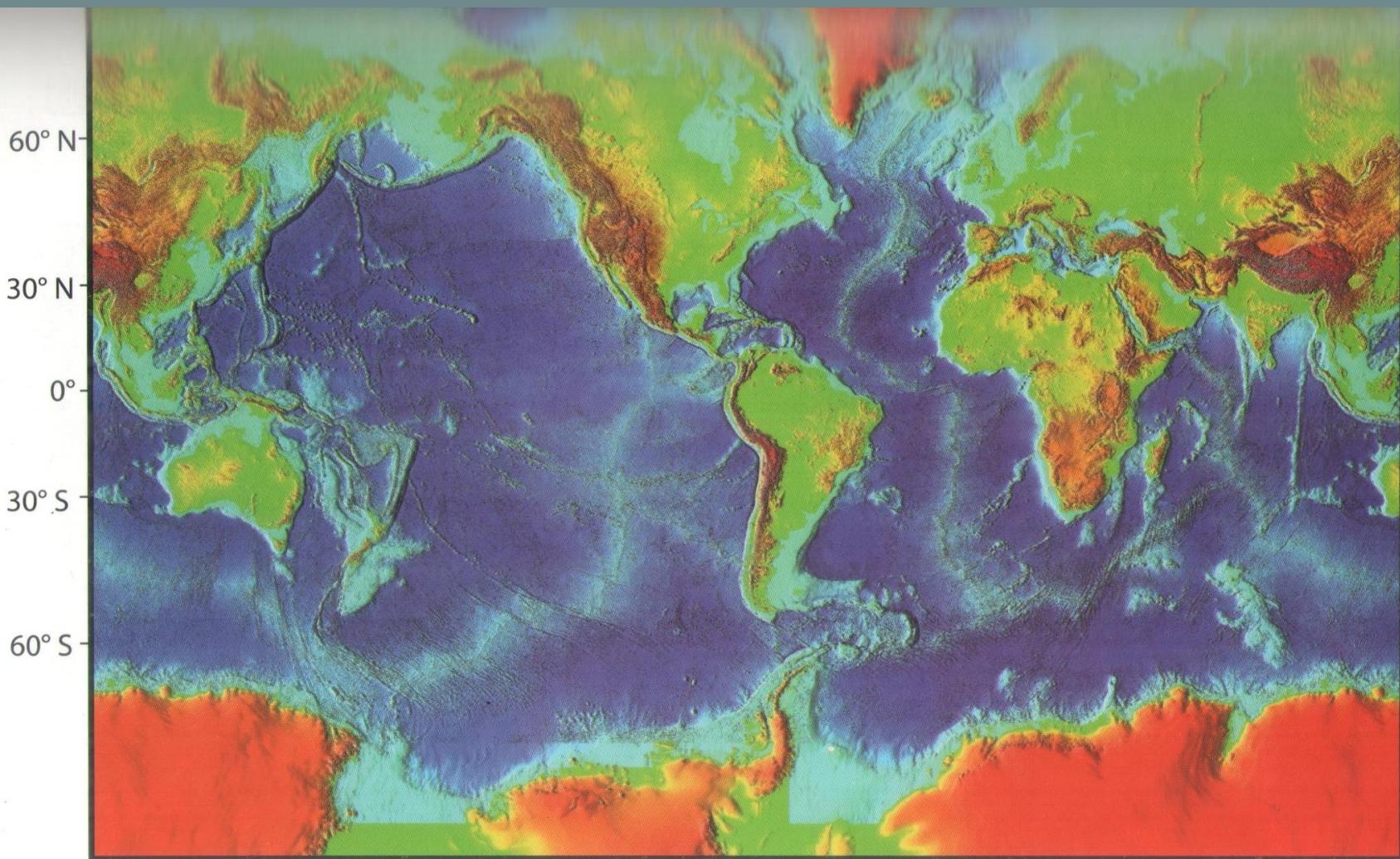


Plate 1.1 Global relief map (reproduced courtesy of the National Geophysical Data Center of the US National Oceanic and Atmospheric Administration).

**Geologic Structure:** Any definable shape/fabric  
in a rock body

**(a) Primary structures**

- Form during or shortly after deposition of sediments/formation of rocks

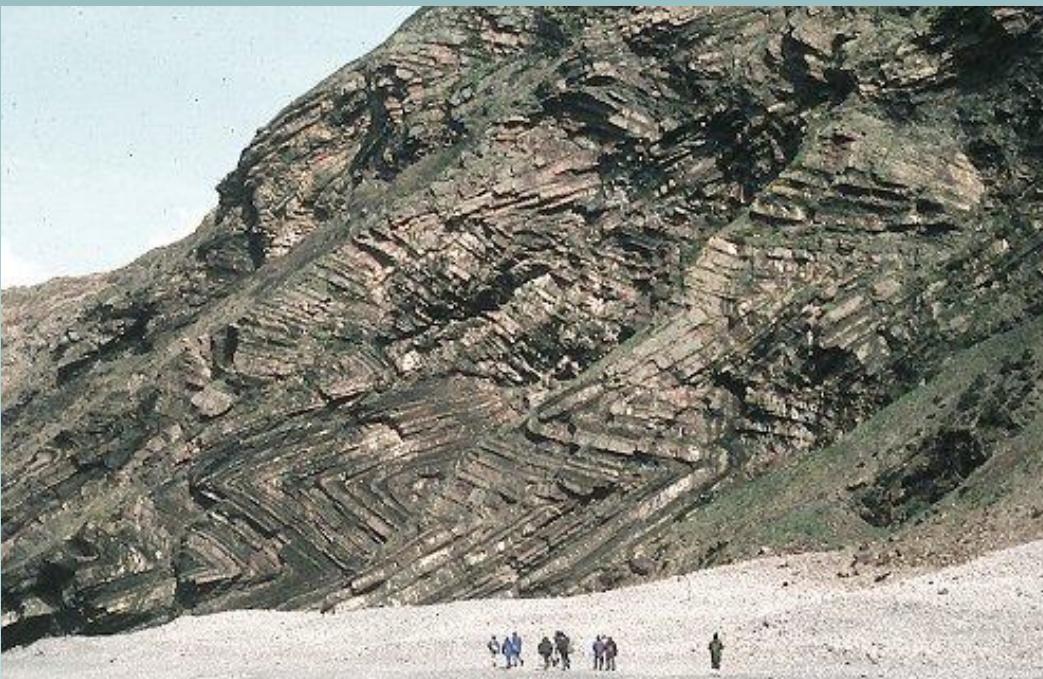
**(b) Secondary structures**

- Tectonic structures: Form in response to forces generated by plate interactions.

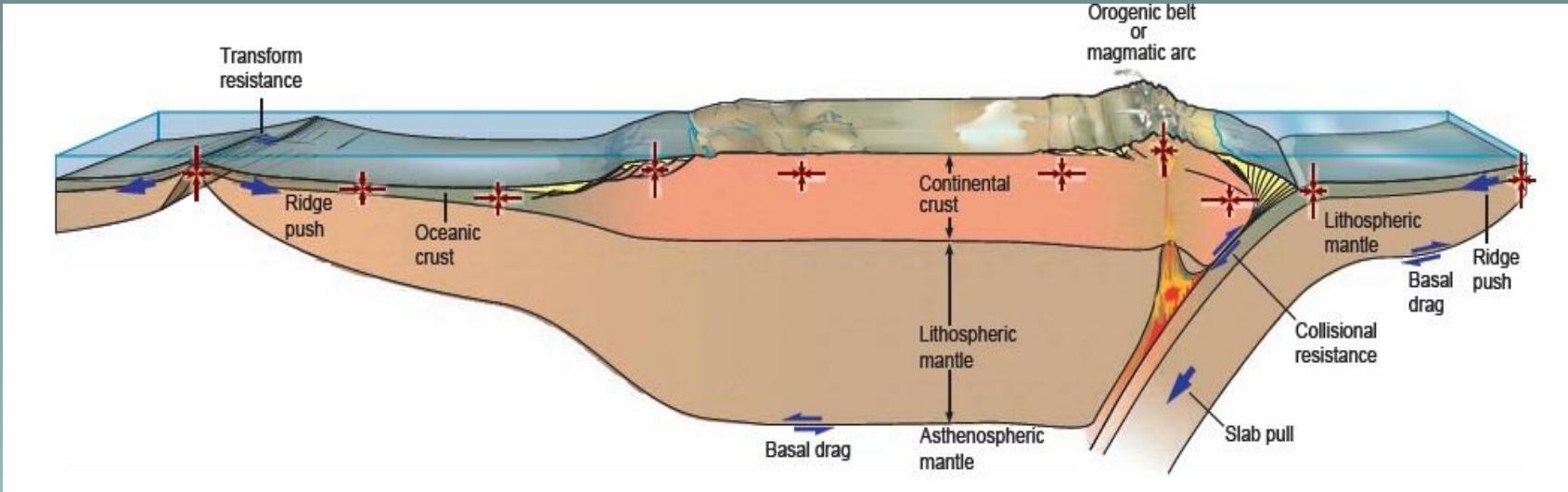
# Quiz: Can you distinguish?



[https://en.wikipedia.org/wiki/Cross-bedding#/media/File:Trough\\_xbed\\_mcr1.JPG](https://en.wikipedia.org/wiki/Cross-bedding#/media/File:Trough_xbed_mcr1.JPG)



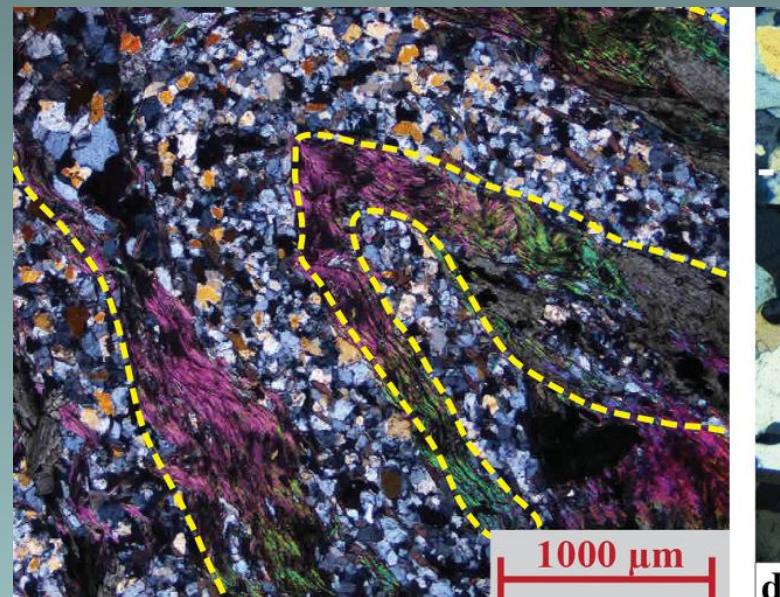
# Why Structural Geology?



(Fossen, 2010)

- How rocks accommodate deformation?
- Manifestation & Quantification
- Mechanics & Kinematics
- Formation of Mountain Belts, Basins, Climate, Erosion
- Evolution of Crust through space and time



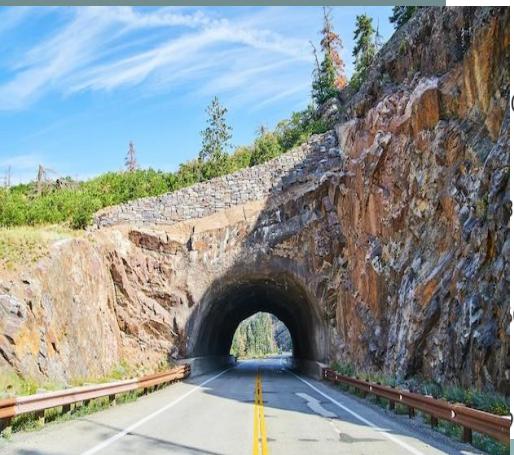


(Ghosh et al., 2020)

<https://link.springer.com/article/10.1007/s00531-017-1486-5>

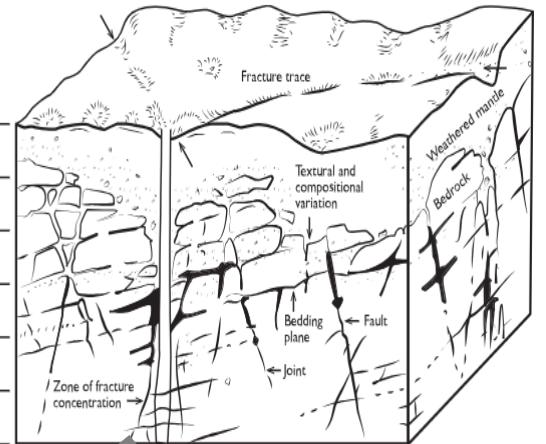
# Engineering Geology

[https://www.freepik.com/premium-photo/image-view-center-road-tunnel-through-mountains-with-stone-wall\\_21634376.htm](https://www.freepik.com/premium-photo/image-view-center-road-tunnel-through-mountains-with-stone-wall_21634376.htm)



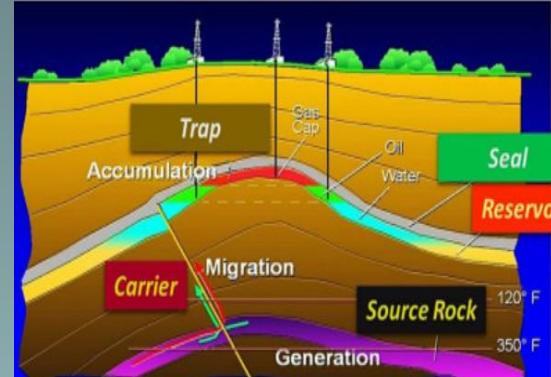
# Groundwater studies

<https://fc79.gw-project.org/english/chapter-4/>



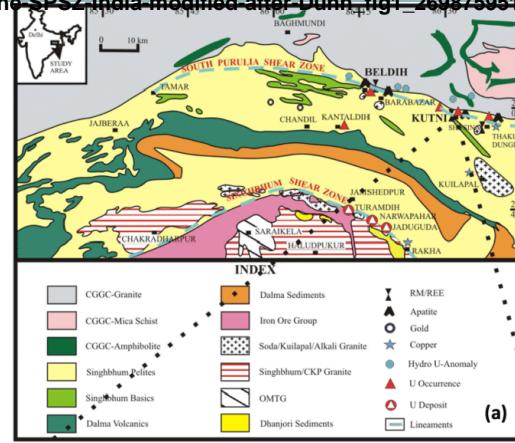
# Oil & Gas Exploration

<https://www.sciencedirect.com/topics/earth-and-planetary-sciences/petroleum-geology>



# Mineral Exploration

<https://www.researchgate.net/figure/a-General-geological-map-of-South-Purulia-Shear-Zone-SPSZ-India-modified-after-Dunn-fig1-269875051>



## Structural Geology

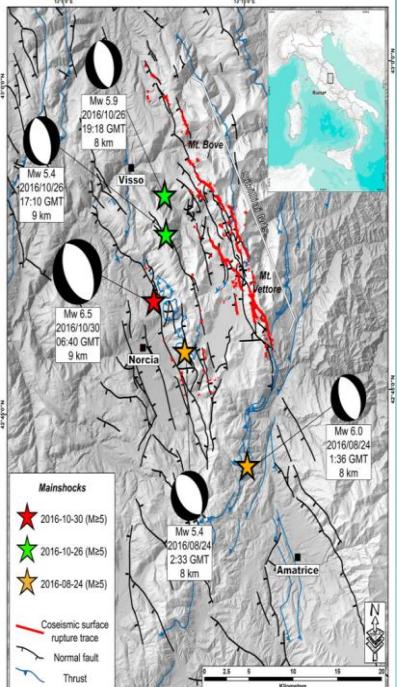
## Extraterrestrial processes

<https://geology.com/stories/13/rocks-on-mars/cross-bedding-outcrop-lg.jpg>

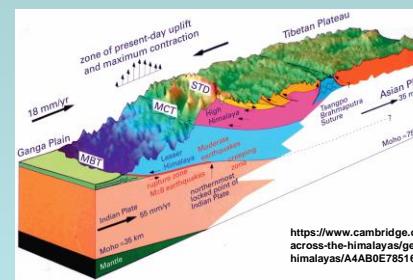


## Earthquakes risk assessment

DOI:10.1029/2018EA000490



# Climate Sciences

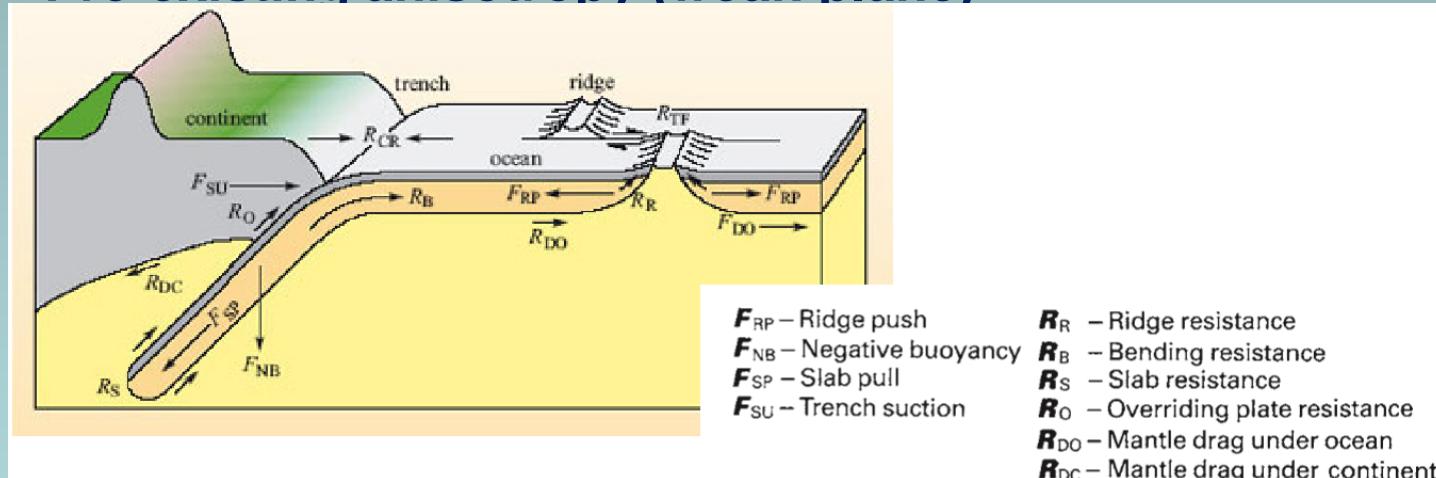


<https://www.cambridge.org/core/books/abs/bird-migration-across-the-himalayas/geological-origin-and-evolution-of-the-himalayas/A4AB0E78516E6761F52EDDE9B5D2125B>

# Mechanics of Structures

## How Rocks Deform Depend on:

- Force applied
- Temperature
- Pressure (rock or lithostatic pressure)
- Pore fluid pressure
- Composition of rocks
- Rate of deformation
- Grain size
- Pre-existing anisotropy (weak-plane)



$\mathbf{F}_{RP}$  – Ridge push  
 $\mathbf{F}_{NB}$  – Negative buoyancy  
 $\mathbf{F}_{SP}$  – Slab pull  
 $\mathbf{F}_{SU}$  – Trench suction

$\mathbf{R}_R$  – Ridge resistance  
 $\mathbf{R}_B$  – Bending resistance  
 $\mathbf{R}_S$  – Slab resistance  
 $\mathbf{R}_O$  – Overriding plate resistance  
 $\mathbf{R}_{DO}$  – Mantle drag under ocean  
 $\mathbf{R}_{DC}$  – Mantle drag under continent

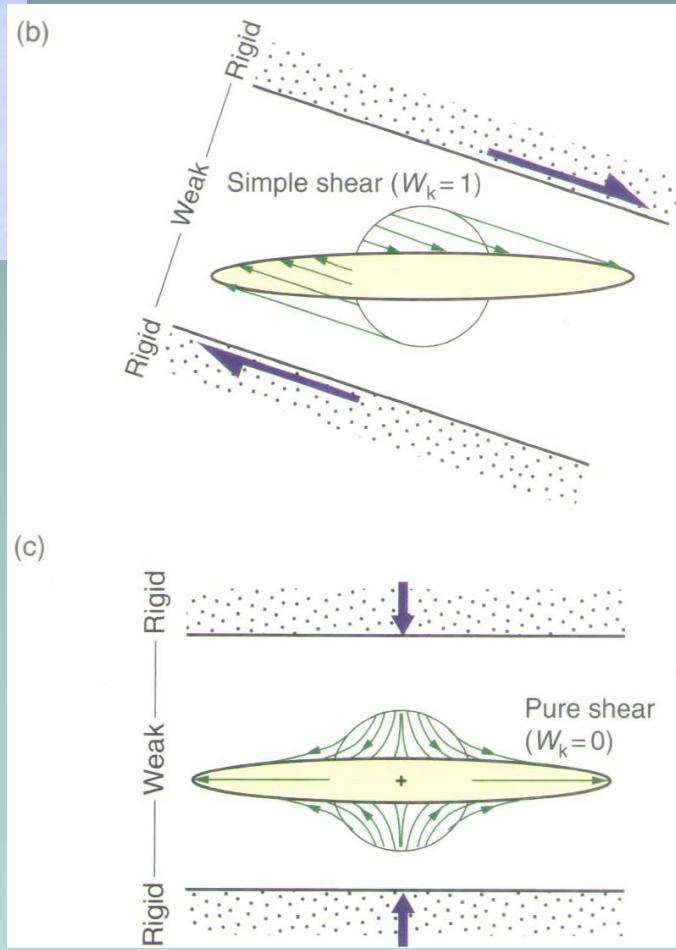
## Forces: Push or Pull.

Vector quantity (SI Unit = Newton =  $\text{kg} \cdot \text{m/s}^2$ )

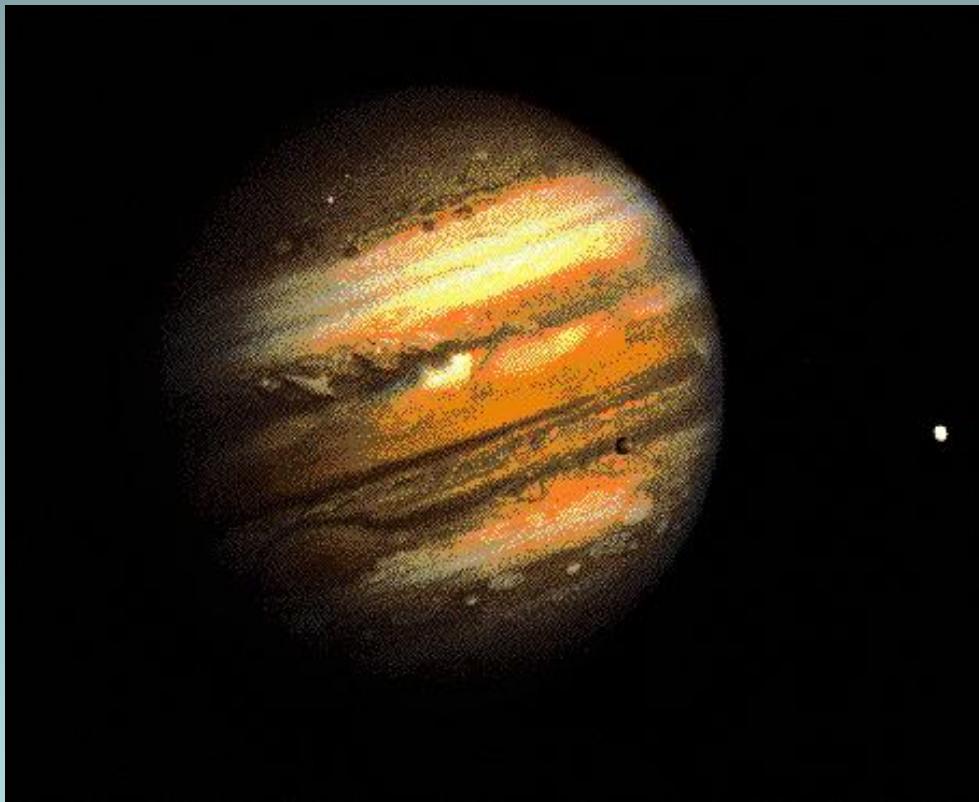
- Body force
- Surface force



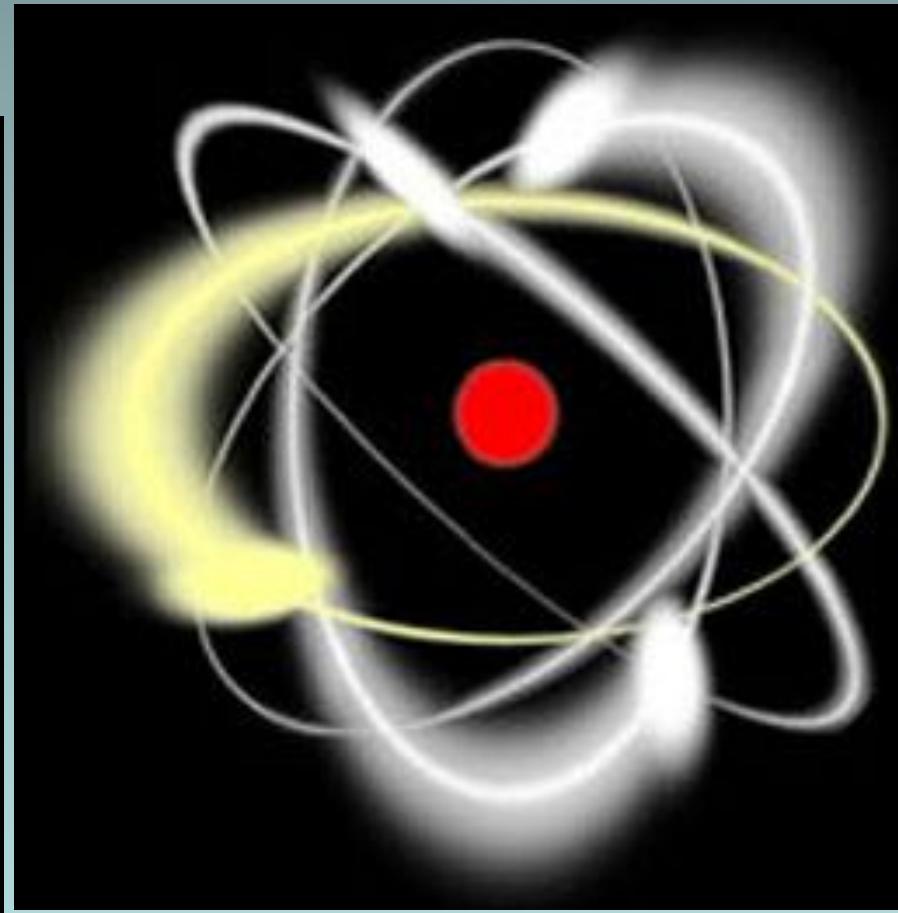
<https://www.stockfood.com/images/13180975-Flowing-honey>



**Body Force:** They act on each particle of rock in a volume, and its magnitude is proportional to the mass within that volume.

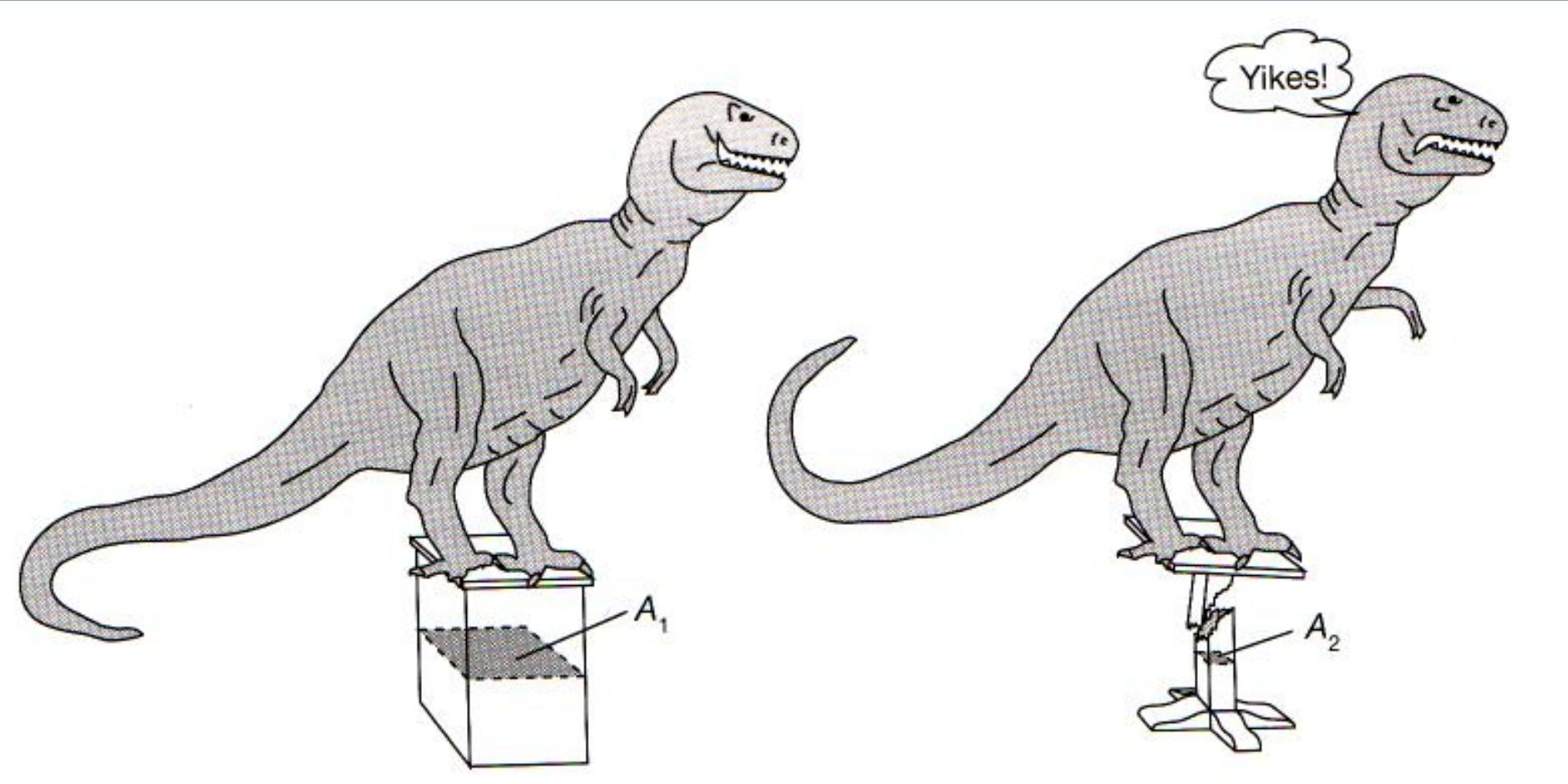


**Gravitational Forces**

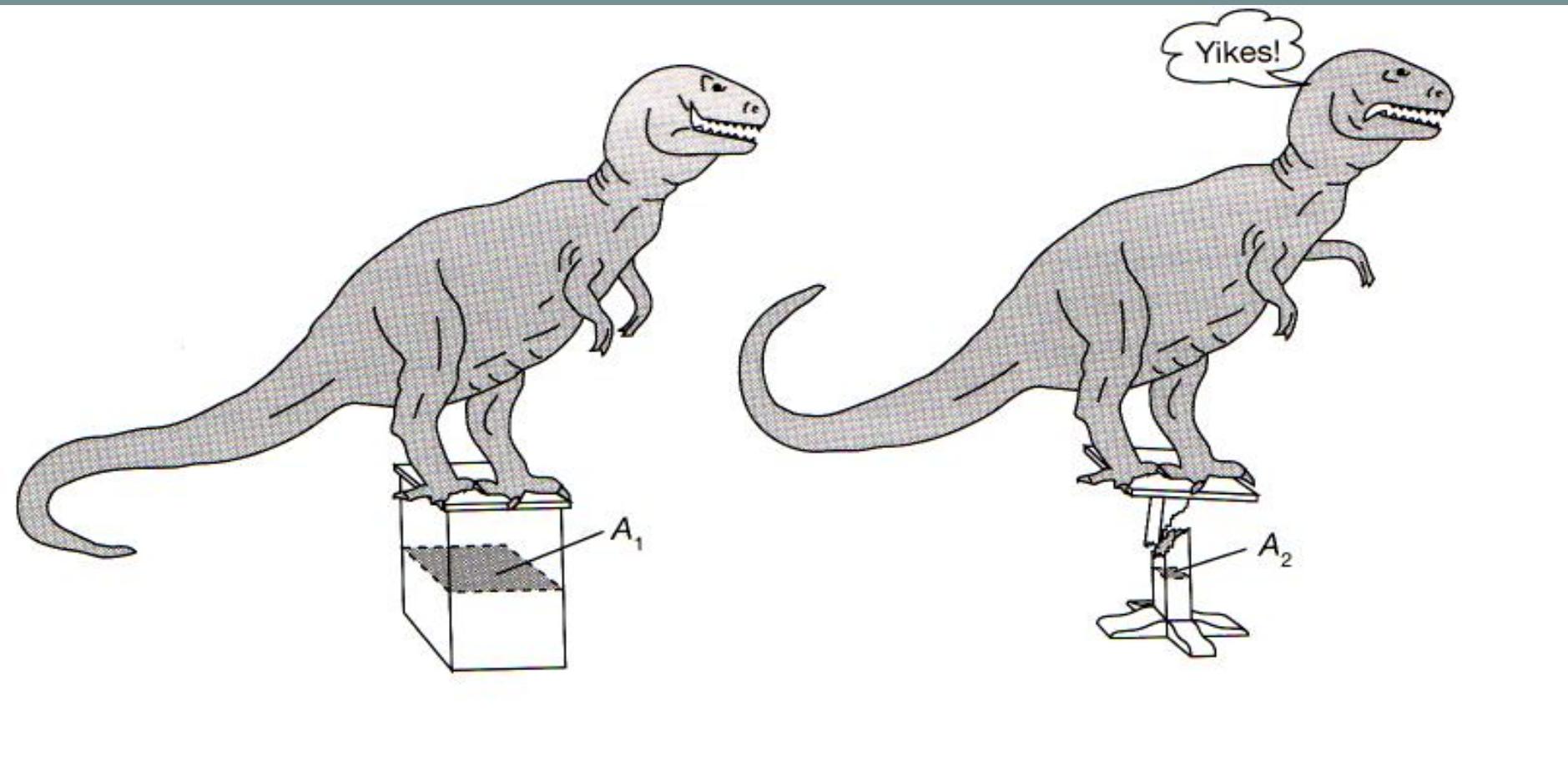


**Electromagnetic Forces**

**Surface Force:** Forces that result from the action of one body / part of a body on another across a shared surface. They act on a specific surface of a body.

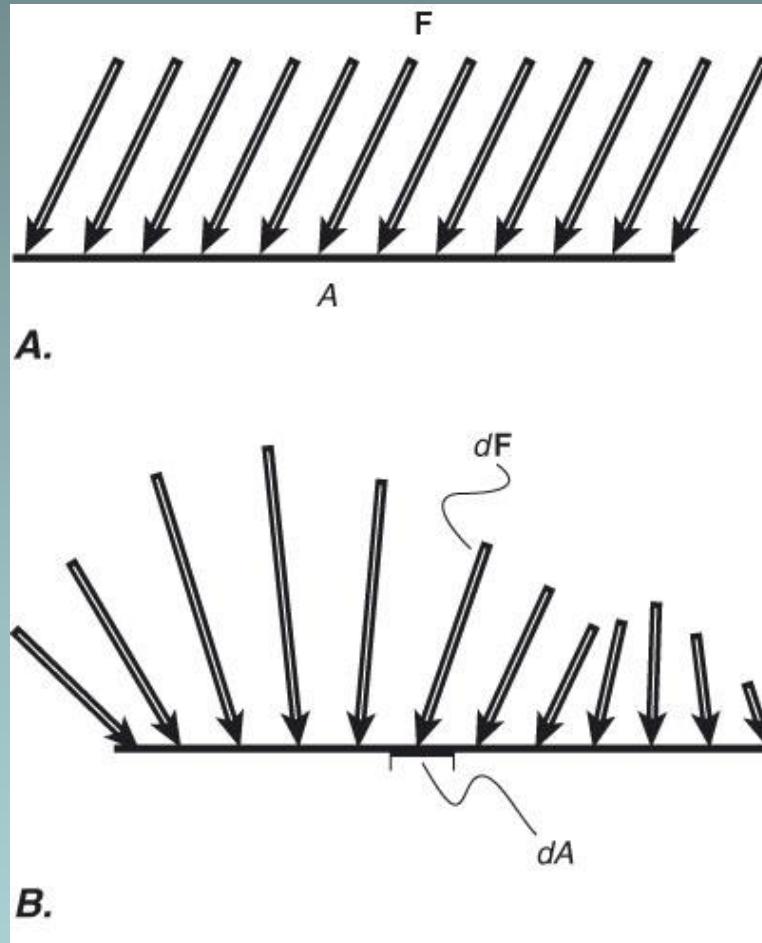


# Traction: Intensity of Force



$$\Sigma = F/A$$

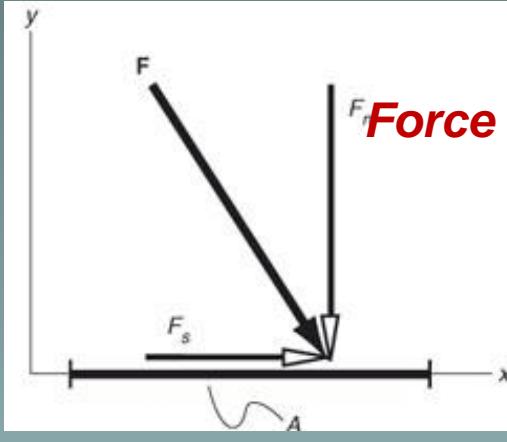
*But...*



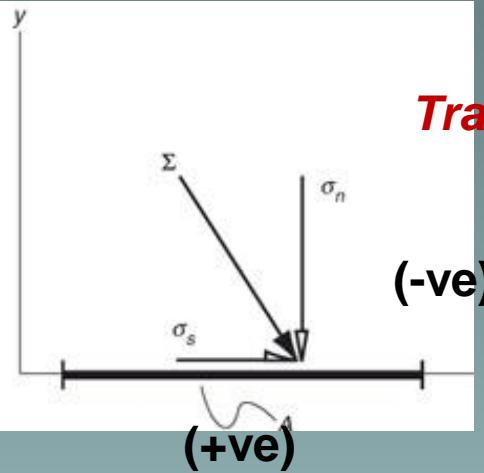
Traction at a point,

$$\Sigma = dF/dA$$

*Magnitude & direction of traction can vary from point to point across a surface.*

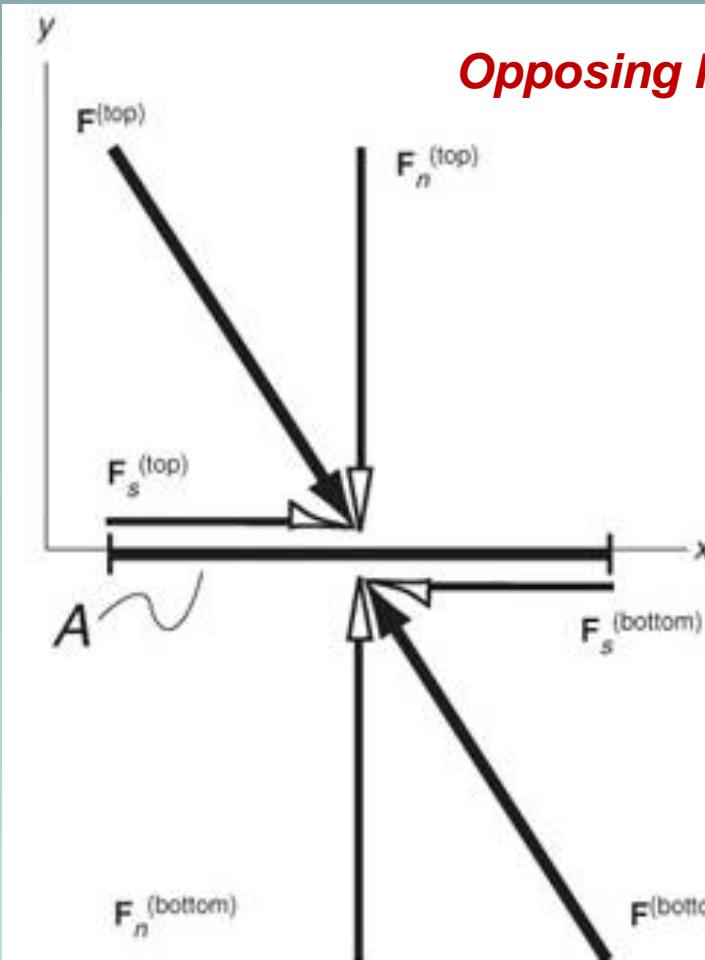


**Force**

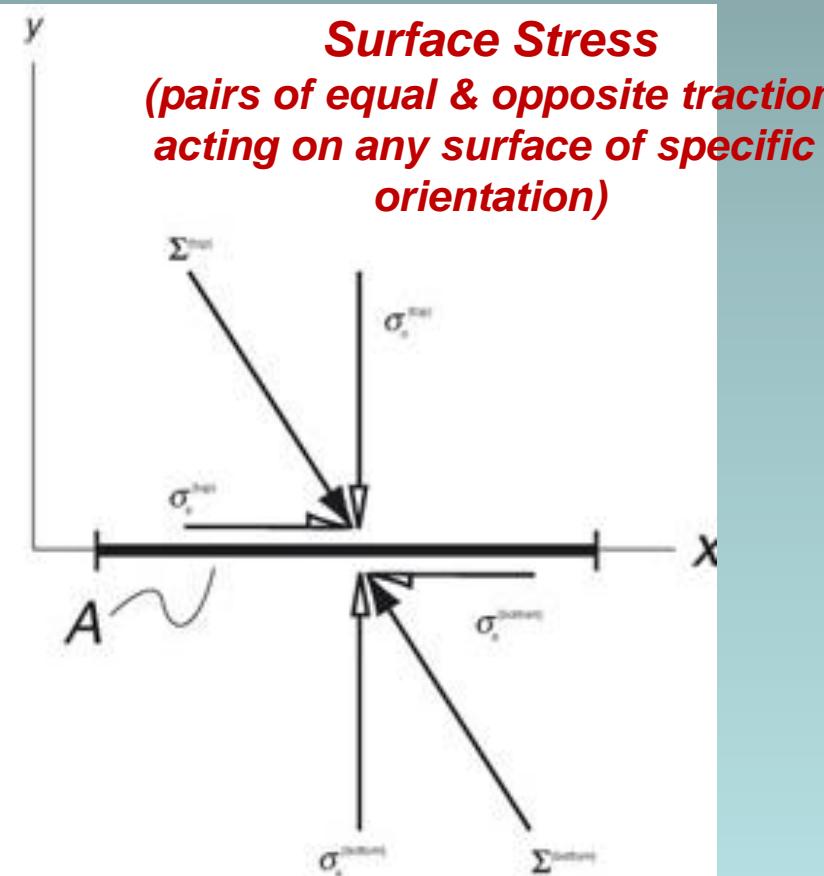


**Traction**

(-ve)  
(+ve)

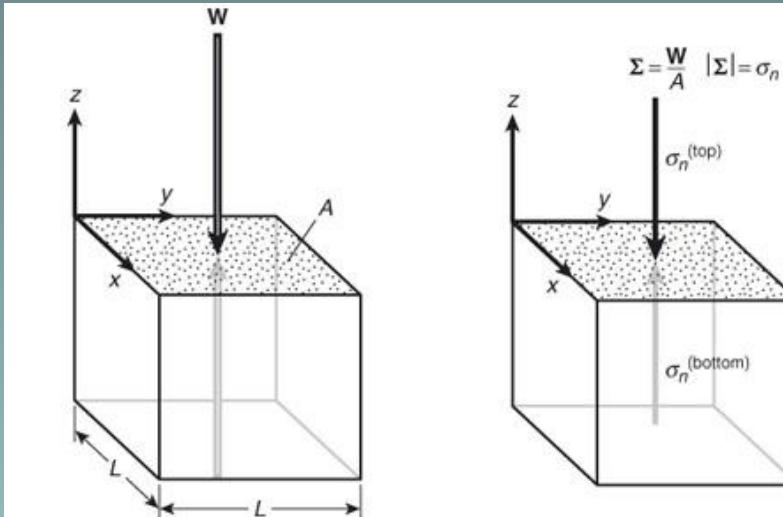


**Opposing Forces**



**Surface Stress**  
*(pairs of equal & opposite traction acting on any surface of specific orientation)*

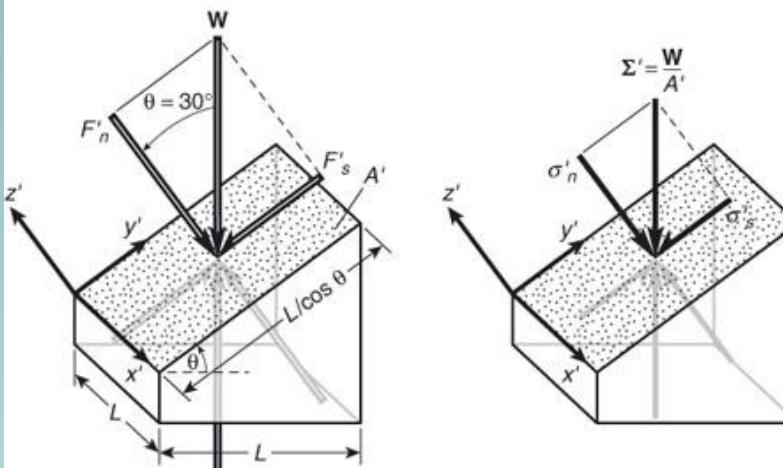
# Stress across planes of different orientations



A. Force W acting on A

$$\sigma_n = W/A$$

$$\sigma_s = 0$$



Force W acting on inclined A'

$$F'_n = W \cos\theta$$

$$F'_s = W \sin\theta$$

$$F = \sigma^* A$$

$$\sigma'_n = W \cos \Theta / L \cdot L' = W \cos \Theta / L \cdot (L / \cos \theta) = W \cos \Theta / [A / \cos \Theta] = \sigma_n \cos^2 \theta$$

$$\sigma'_s = W \sin \Theta / [A / \cos \Theta] = \sigma_n \cos \Theta \sin \Theta = (\sigma_n / 2) \sin 2\theta$$

Transformation eqn for stress

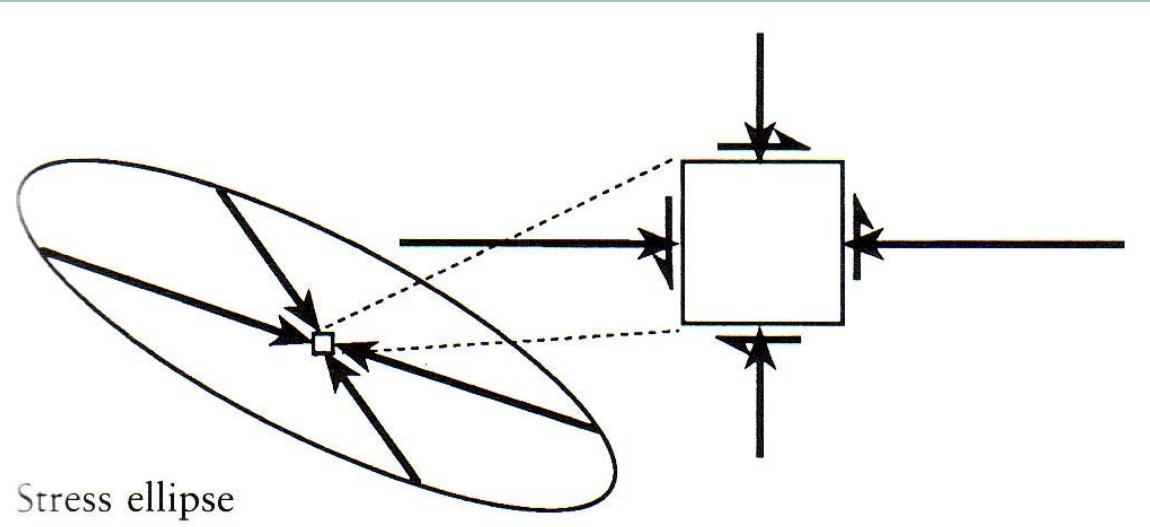
# Stress ellipse:

**State of Stress at a point ( $\sigma$ ) :**

*Defined by  $\sigma_n$ ,  $\sigma_s$  that act on planes of all possible orientations passing through the point.*

**Plotting surface stresses on all possible orientations through a point –ends of all arrows fall on an ellipse (2D; arrows are radii of ellipse) – stress ellipse → state of stress at that point**

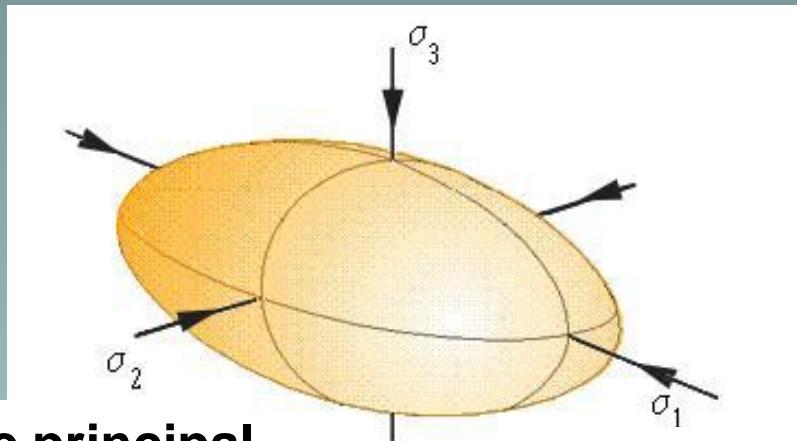
***shape & orientation of ellipse → complete state of stress at that point***



$$\begin{aligned}1 \text{ Pa} &= 1 \text{ N/m}^2 = 1 \text{ kg/(ms}^2\text{)} \\1 \text{ MPa} &= 10 \text{ bar} = 10.197 \text{ kg/cm}^2 \\100 \text{ MPa} &= 1 \text{ kbar}\end{aligned}$$

# Stress Ellipsoid

Minimum principal stress axis



Intermediate principal  
stress axis

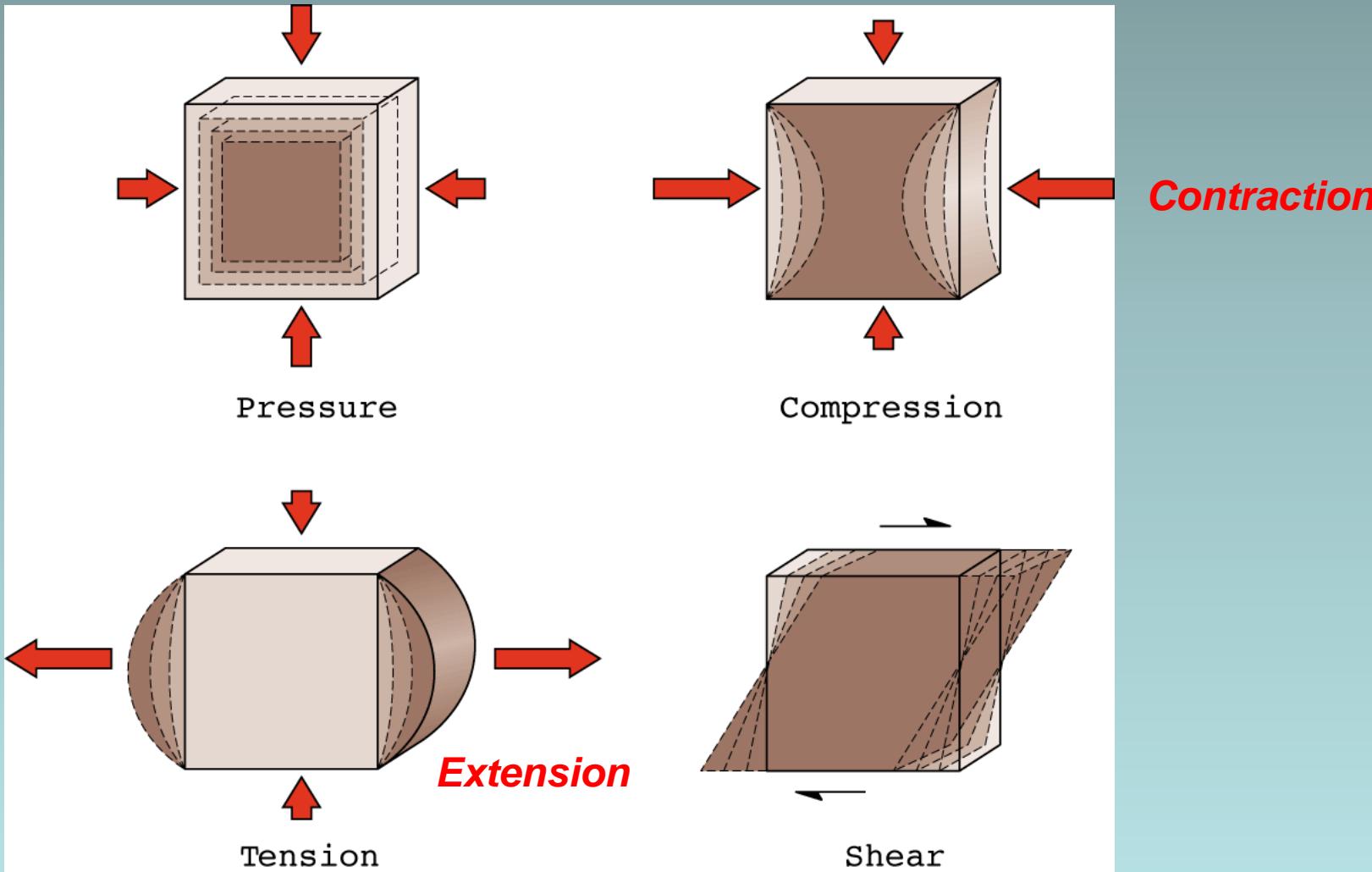
Maximum principal  
stress axis

$$\sigma_1 \geq \sigma_2 \geq \sigma_3$$

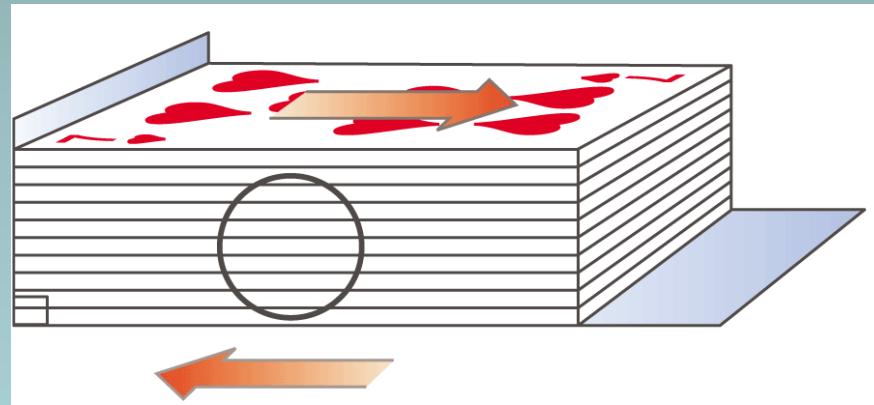
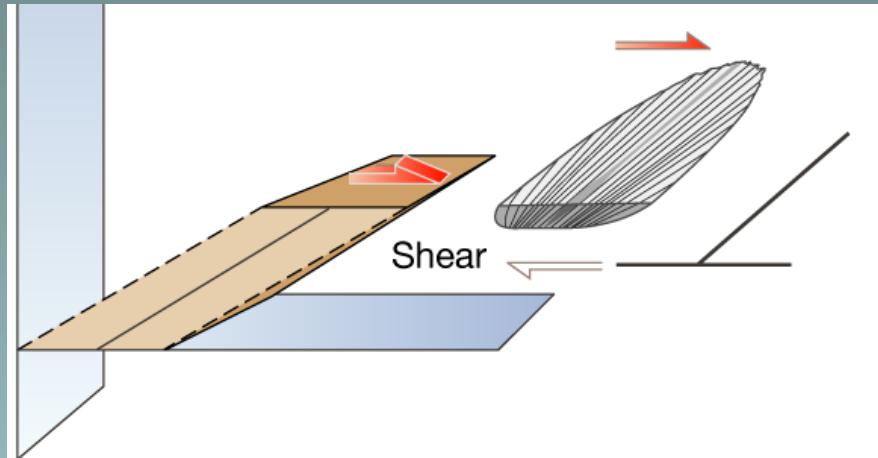
Stress ellipsoid

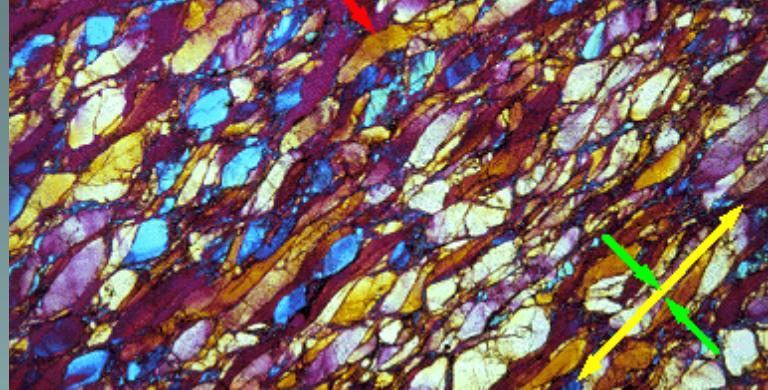
# Stress causes Strain

**Strain** – A shape change or volume loss (size change) that is a response to an applied stress

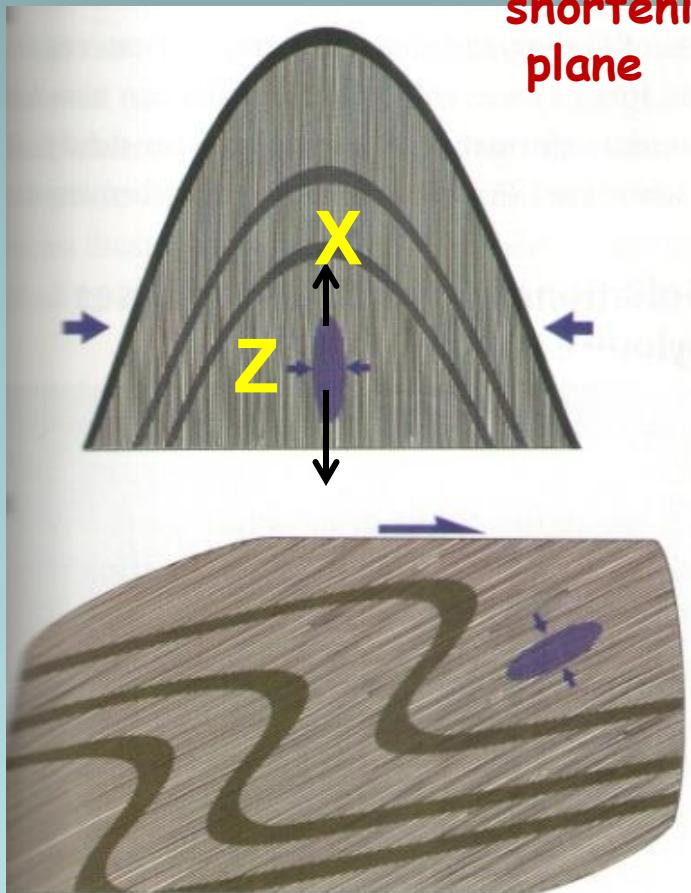


# Shear





Tracks XY/  
shortening  
plane



**Figure 12.17** Simple relationship between shortening direction (arrows), strain ellipse and cleavage for (a) upright veins, for instance in slate belts, and (b) shear zones.

# Quantification of Strain

## Length Change



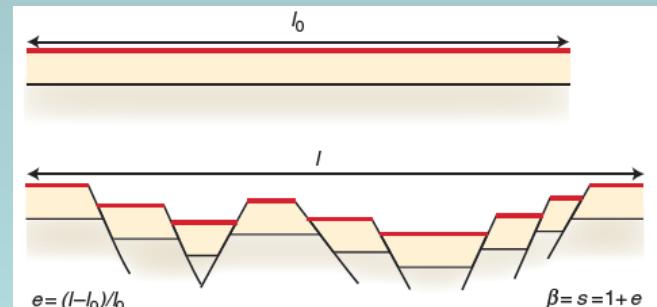
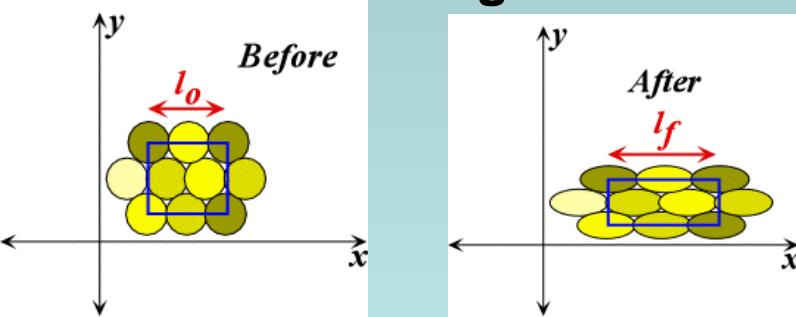
Dimensionless Number

$$\text{Elongation (engineer's extension)} = e = (l_f - l_o)/l_o$$

Useful for small strains  
e (-) = shortening  
e (+) = extension

$$\text{Stretch} = T \text{ (or } S) = l_f/l_o = 1 + e$$

Used in expressing axial ratios



**Figure 2.7** Extension of layers by faulting. The red layer has an original ( $l_0$ ) and a new length, and the extension  $e$  is found by comparing the two. The beta-factor ( $\beta$ ) is commonly used to quantify extension across extensional basins.

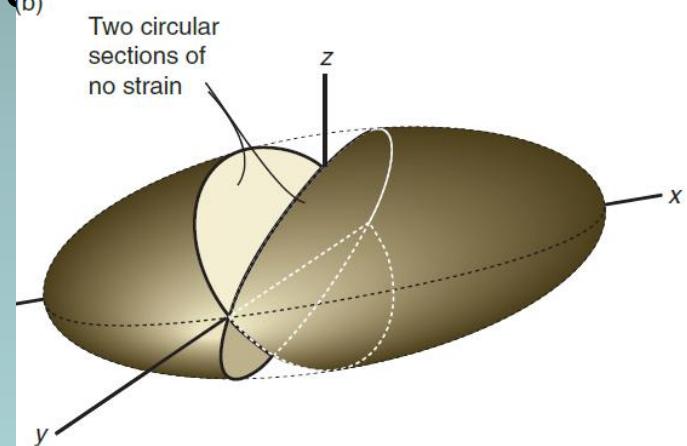
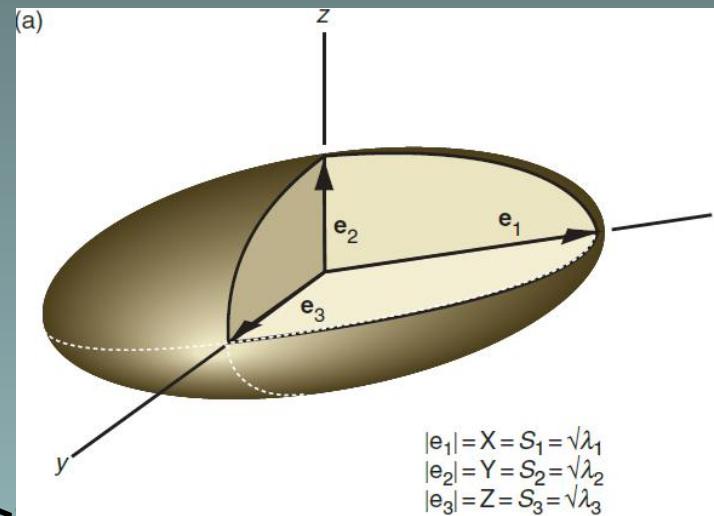
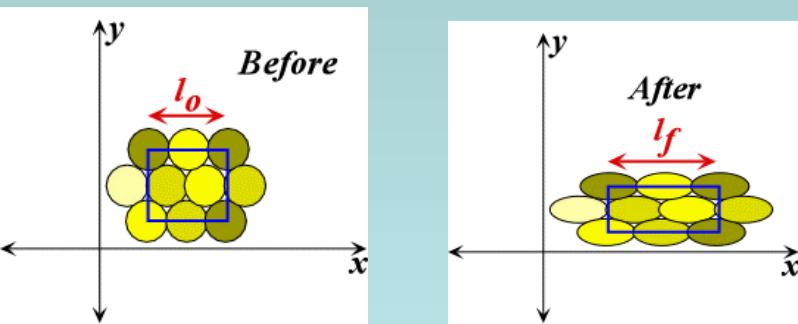
# Strain ellipsoid

Deformed shape of imaginary sphere with unit radius that is deformed along with rock volume under consideration

$$X > Y > Z$$

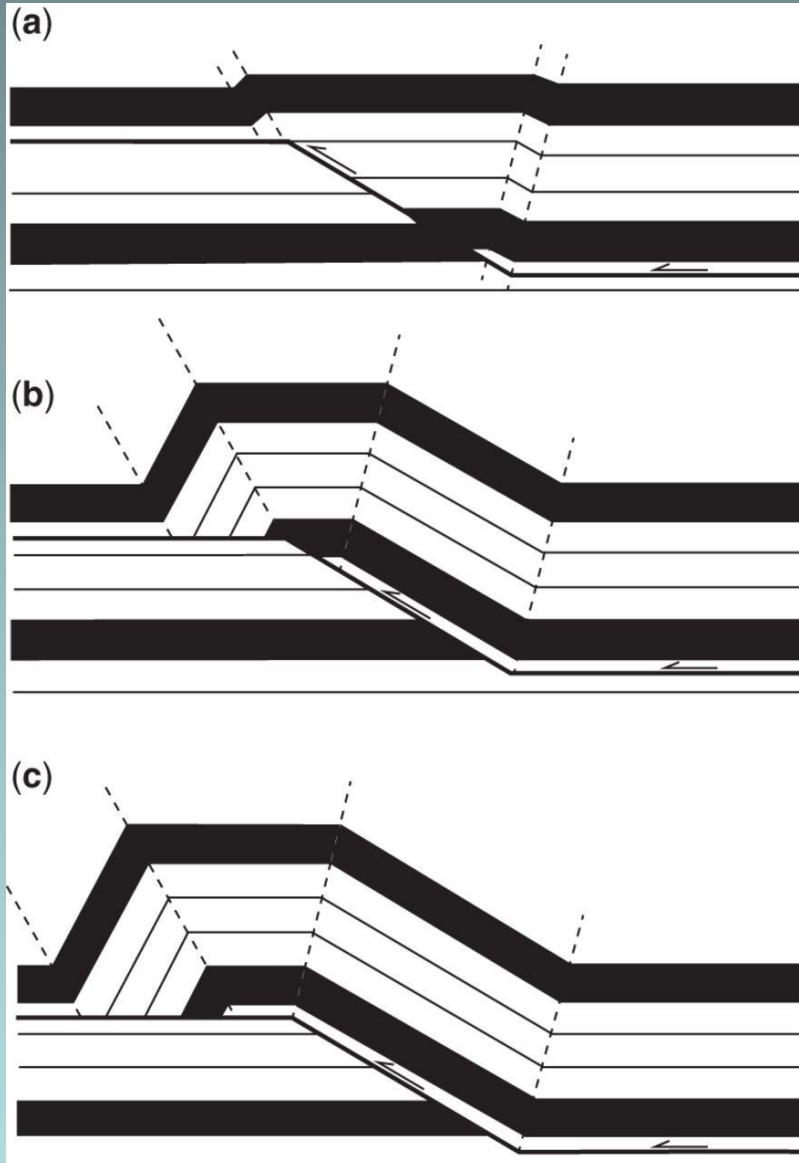
Magnitudes of axes  $\rightarrow$  Principal stretches (or,  $s_1 > s_2 > s_3 = \sqrt{\lambda_1}, \sqrt{\lambda_2}, \sqrt{\lambda_3}$ ; or,  $1+e_1 > 1+e_2 > 1+e_3$ )

$$\text{Ellipticity} = R = X/Y$$



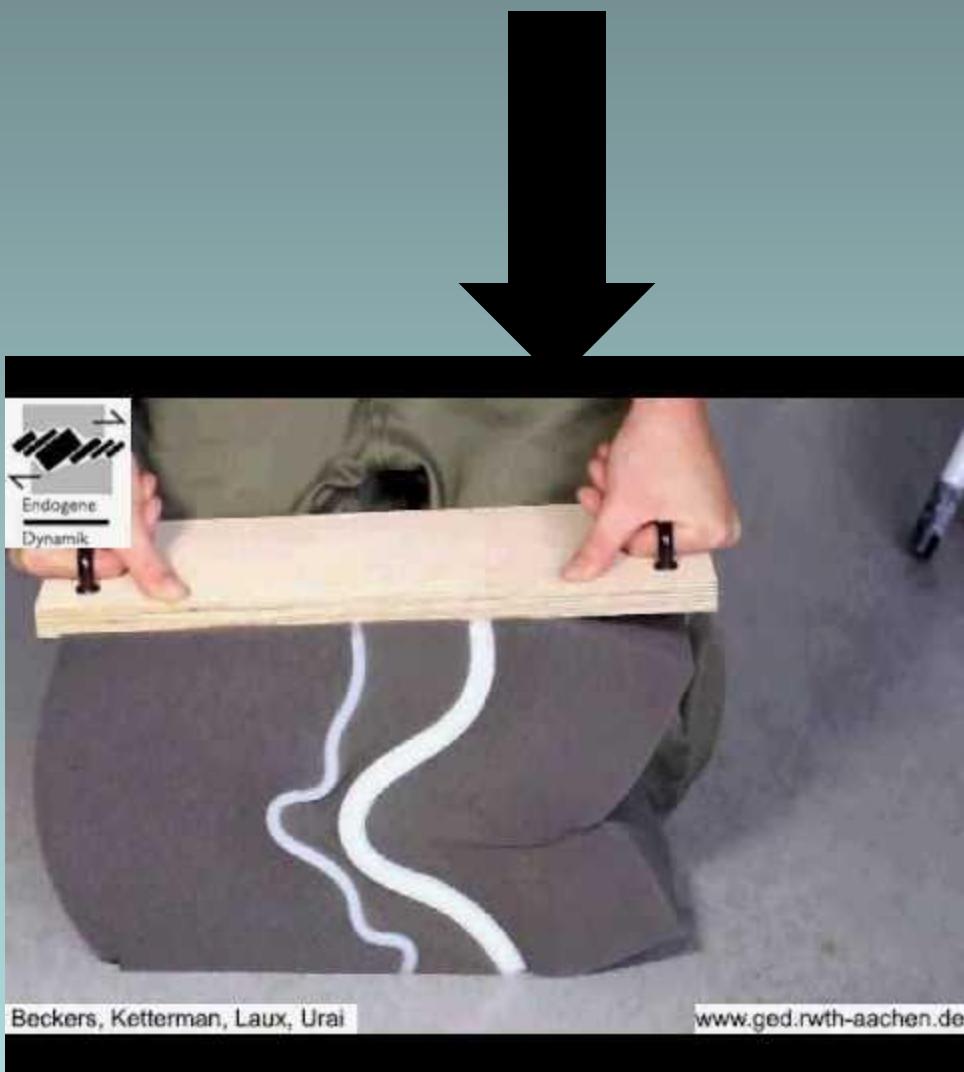
**Figure 2.13** (a) The strain ellipsoid is an imaginary sphere that has been deformed along with the rock. It depends on homogeneous deformation and is described by three vectors  $e_1$ ,  $e_2$  and  $e_3$ , defining the principal axes of strain ( $X$ ,  $Y$  and  $Z$ ) and the orientation of the ellipsoid. The length of the vector thus describes the shape of the ellipsoid, which is independent of choice of coordinate system. (b) The ellipsoid for plane strain, showing the two sections through the ellipsoid that display no strain.

Compression (stress)  $\Rightarrow$  Contraction/Shortening (strain)



Change in Length (thickening)  
Is this the only possibility?

# Compression (stress) $\Rightarrow$ Contraction/Shortening (strain)



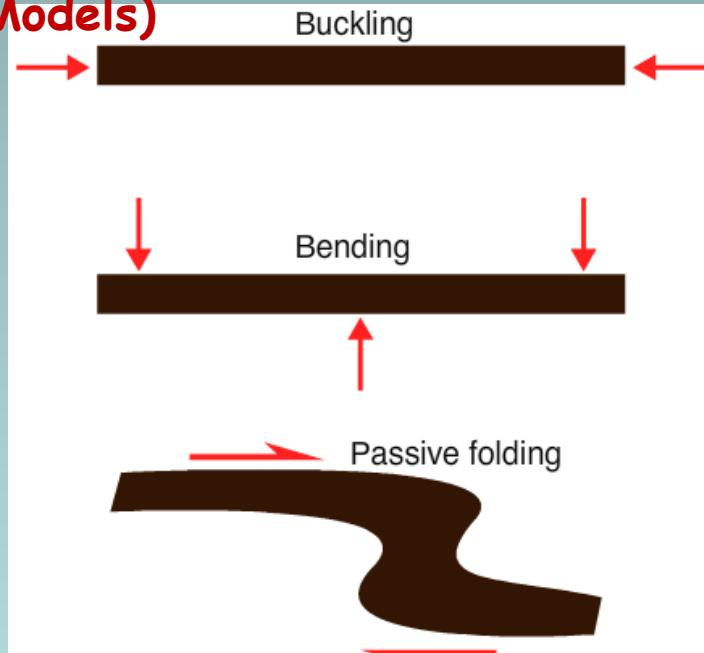
Change in Length (thickening)



# Stress & Strain Not correlatable



• How stress acts on  
layered rocks (Mechanical  
Models)



Kinematic models of Folding

Motion of the deforming body ,  
but generally, do not relate the  
motion to the mechanical properties  
of the folded layer &/ to the stress

Ref: 11.2; Fossen

Whether the beds respond actively/passively  
to the imposed strain field