

## Chapter 11

# Dynamic Community Discovery

### Summary

- Communities in dynamic networks
- Evaluation & Benchmarking
- Visualization

### Reading

- "Challenges in community discovery on temporal networks." Cazabet & Rossetti



# Community Discovery in Dynamic Networks

Time flies like an arrow; fruit flies like a banana



# Communities In Dynamic Networks

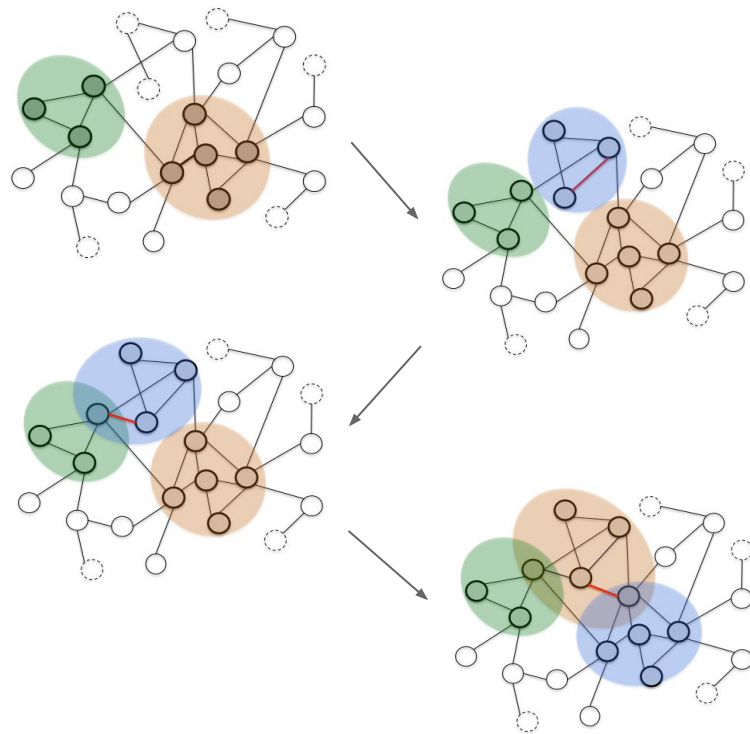
Networks change with time...

- Nodes appear and vanish
- Edges appear and vanish

...communities must change too!

DCD:

identify/track changes in community structure



Cazabet, Remy, and Giulio Rossetti. "Challenges in community discovery on temporal networks." *Temporal Network Theory*. Springer, Cham, 2019. 181-197.

A Novel Problem:

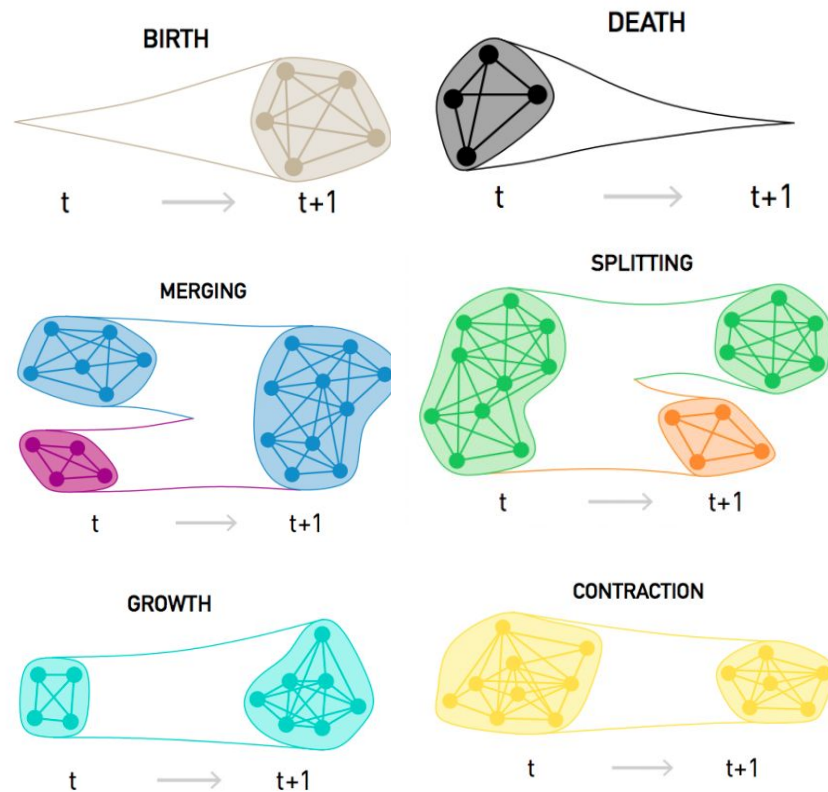
# Community life-cycle tracking

As time goes by the **rising** of novel nodes and edges (as well as the **vanishing** of old ones) led to network perturbations

Communities can be deeply affected by such changes

Three main strategies:

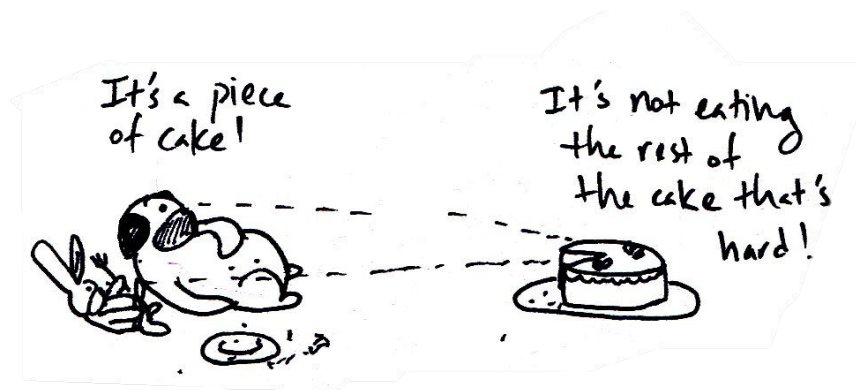
- Identify & Match
- Informed Iterative algorithms
- Stable Identification



The Optimist:

**“Ok, It’s a piece of cake!”**

1. Find communities at each network observation (using a static algorithm)
2. Match communities across consecutive network observations
3. Observe differences



Two major issues:

- Community Smoothing
- Theseus' Ship Paradox

# Community Smoothness

Communities are arbitrarily defined  
(same issue of static CD)

Most “efficient” algorithms are stochastic

- Change in communities might be due to **structural changes** OR to **arbitrary choices** of the algorithm
- The same algorithm ran twice on the same graph *might yield different results*

Desiderata:

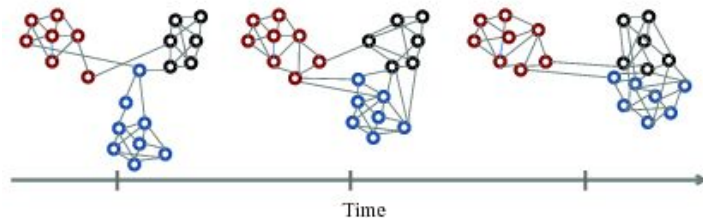
- a “simple” (parsimonious) model
- a trade-off between quality and simplicity (smoothness)

**No Smoothness:**

Partition at each  $t$  should be the same as found by a static algorithm

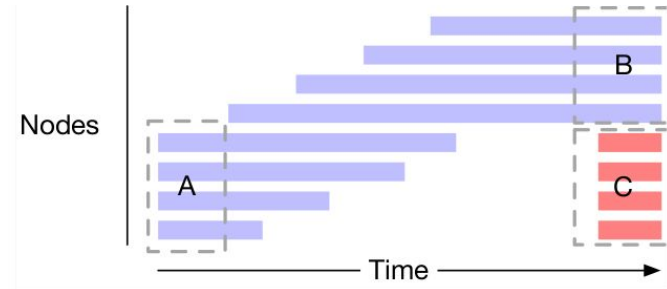
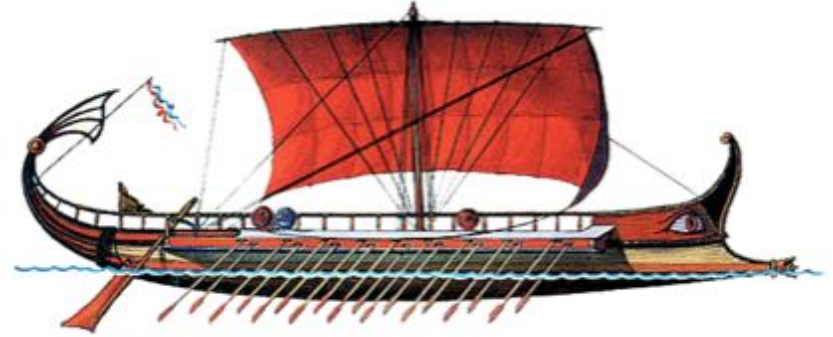
**Smoothness:**

Partition at  $t$  is a trade-off between “good” communities for the graph at  $t$  and similarity with partitions at different times



# Theseus' Ship Paradox

- I. Theseus killed the Minotaur in Crete and came back to Athen on his boat
- II. His boat was conserved as memory during a very long time
- III. The boat was deteriorating, so pieces of it were gradually replaced.
- IV. Until one day, all original parts were replaced



# Theseus' Ship Paradox

- A. Is this ship still the same as Theseus boat ?
- B. If another boat was built using all pieces of the original boat, which one would be the “real” Theseus boat ?

Community evolution/identity is an arbitrary concept

Fig. A - Ship of Theseus - Original

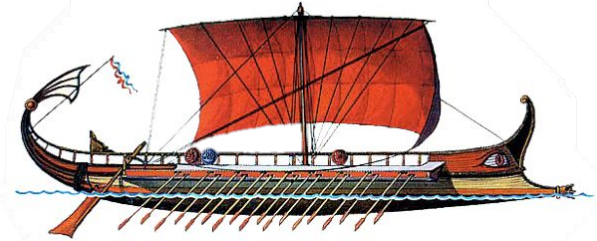
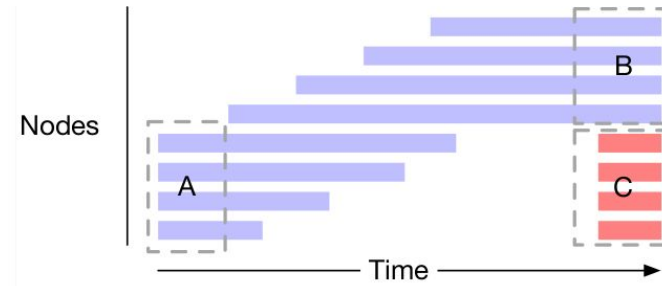
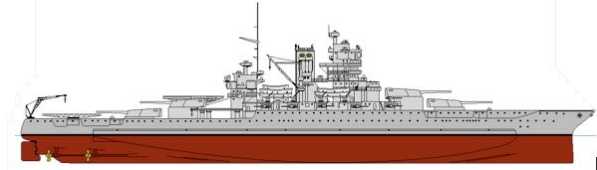


Fig. B - Ship of Theseus - Reconstructed





# DCD Algorithms Taxonomy

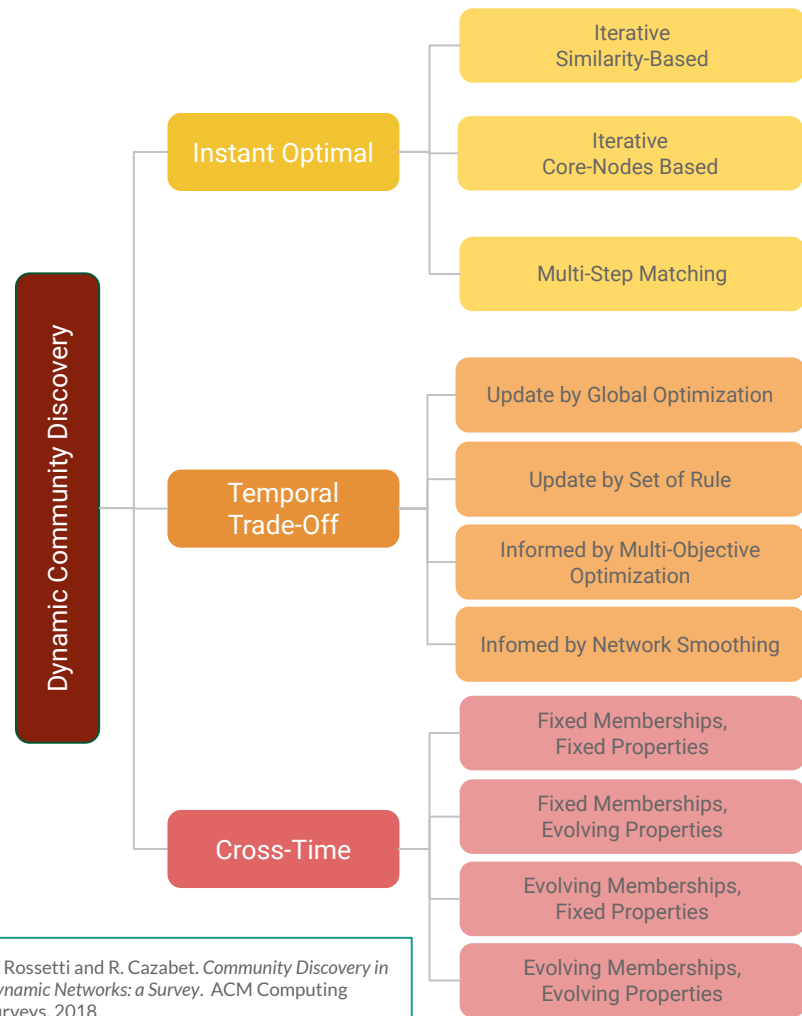
Hierarchical categorization

First Level:

Increasing degree of smoothness (*none* -> *complete*)

Second Level:

Algorithmic Approach (*how to deal with Theseus*)



## Taxonomy

# Instant Optimal

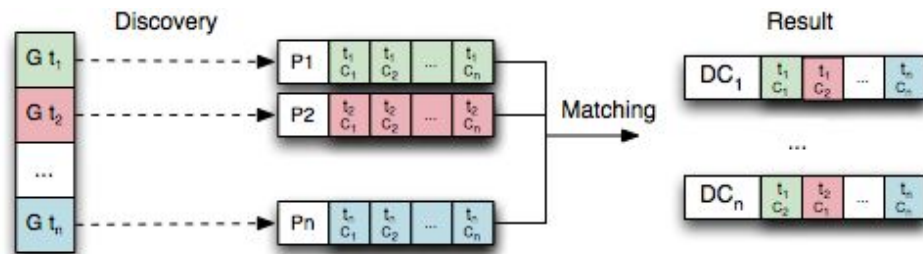
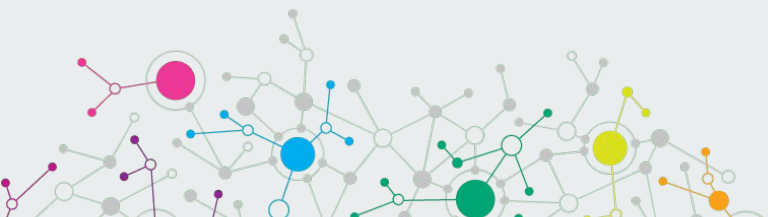
“Communities found at time  $t$  are optimal for the network at time  $t$ ”

### Strengths

Definition consistent with static CD, parallelisation

### Drawbacks

Lack of smoothness, only SN



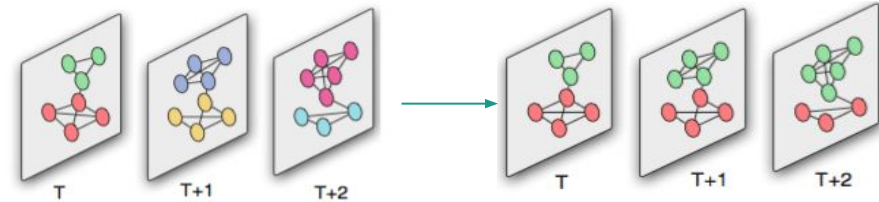
# Taxonomy

## Two-Step

1. Communities are detected at every step using a static algorithm (e.g. Louvain Algorithm)
2. Similarities are computed between communities in consecutive steps (at  $t$  and  $t+1$  (e.g., Jaccard index))

$$J(A, B) = \frac{|A \cap B|}{|A \cup B|} = \frac{|A \cap B|}{|A| + |B| - |A \cap B|}$$

3. Most similar communities are matched between  $t$  and  $t+1$



### Advantages:

- Easy to model, can extend smoothly static approaches

### Drawbacks:

- The reduction to static scenarios through temporal discretization is not always a good idea
  - How to choose the temporal threshold?
  - To what extent can we trust the obtained results?

## Taxonomy

# Temporal Trade-Off

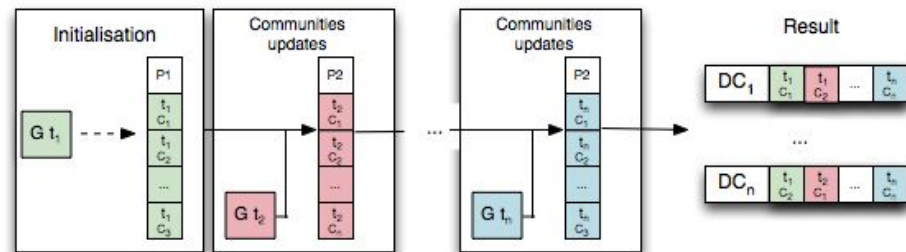
*"Communities found at time  $t$  represent a trade-off between the graph at  $t$  and its previous states"*

### Strengths

Online, incremental, natural smoothness

### Drawback

Iterative, risk of avalanche effect



# Taxonomy

## Tiles

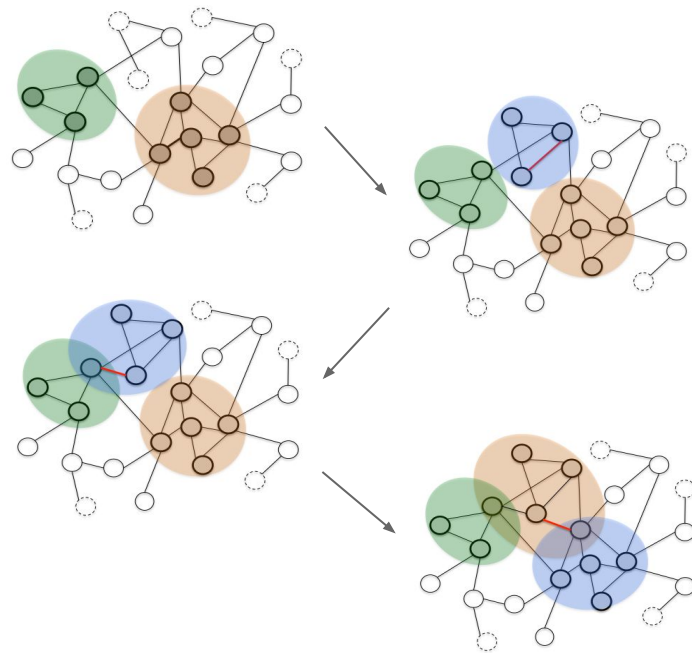
1. Social Interactions define the communities a user belongs to
2. Dynamic graphs as *edge streams*
3. Online updates of communities as nodes/edges appear/vanish

### Advantages:

- Punctual updates of the community structure
- Low computational complexity

### Drawbacks:

- Ad-Hoc model



# Taxonomy

## Cross-Time

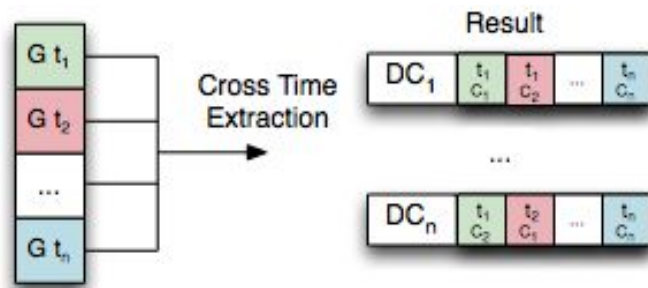
“Communities at  $t$  are defined relatively to all other steps”

### Strengths

Perfectly smoothed, stable, solution

### Drawback

Non online, batch computation, lacks incrementality

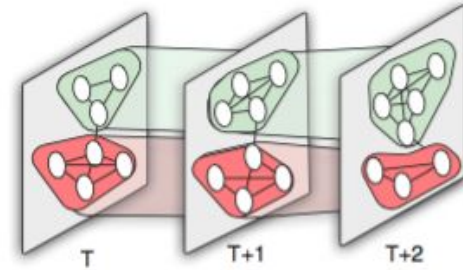


## Taxonomy

# Transversal Network

1. A transversal network is built: nodes are couples (nodes, time), edges link the same node in adjacent snapshots
2. A community detection algorithm is run on this transversal network

(Note: modified Modularity to avoid overestimating expected edges between nodes in different time steps, i.e., custom random graph)



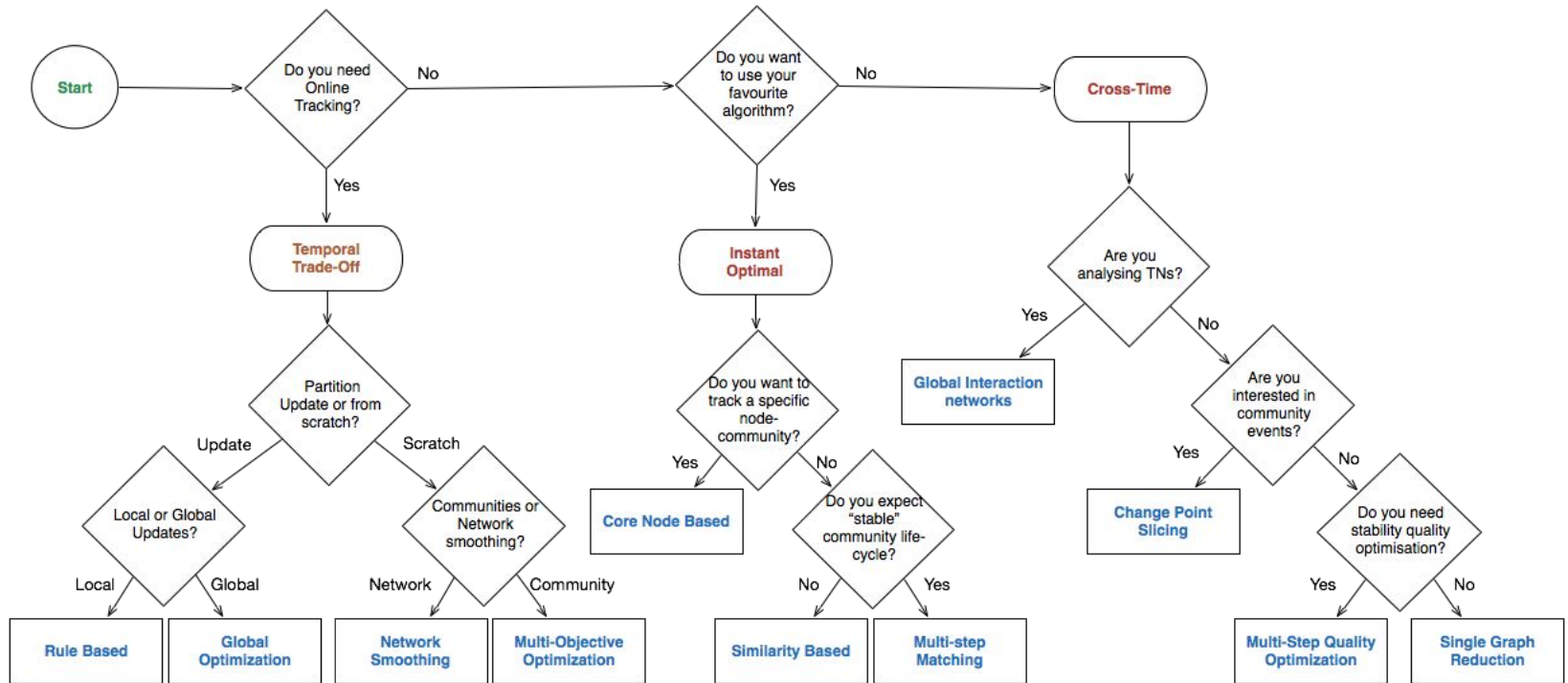
### Advantages:

- Maximal smoothing and stability

### Drawbacks:

- No Community Events are detected
- All the network history needs to be known in advance

Mucha, Peter J., et al. "Community structure in time-dependent, multiscale, and multiplex networks." *science* 328.5980 (2010): 876-878



Choosing the correct approach: one of many possible roadmaps...



# Community Discovery in Dynamic Networks

Evaluation Strategies



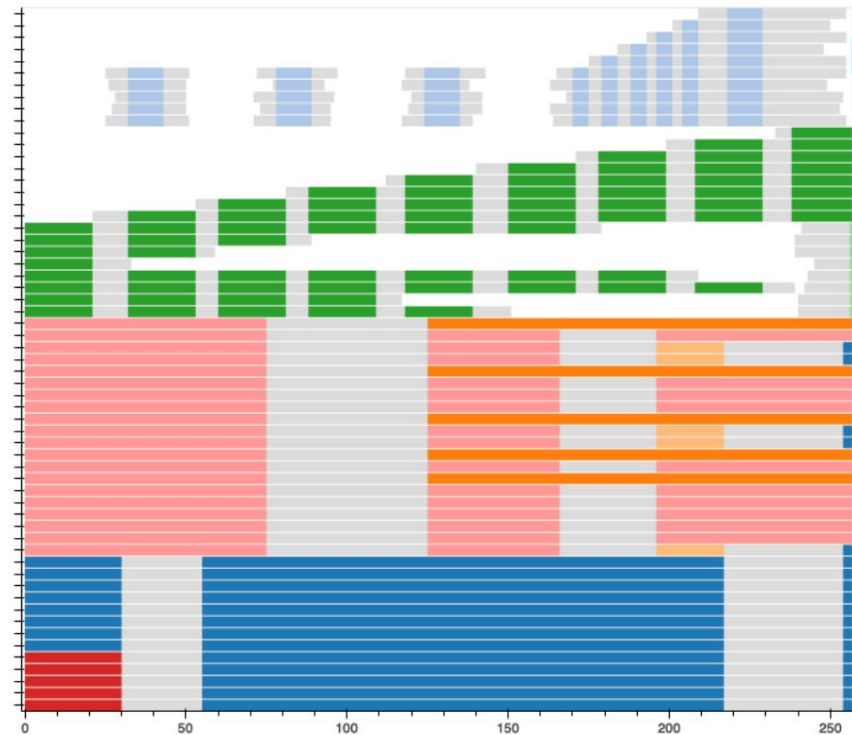
# Strategies

## Internal Evaluation

- Partition quality function  
(i.e., modularity, conductance, density...)
- Community characterization  
(i.e., size distribution, overlap distribution...)
- Execution time and Complexity

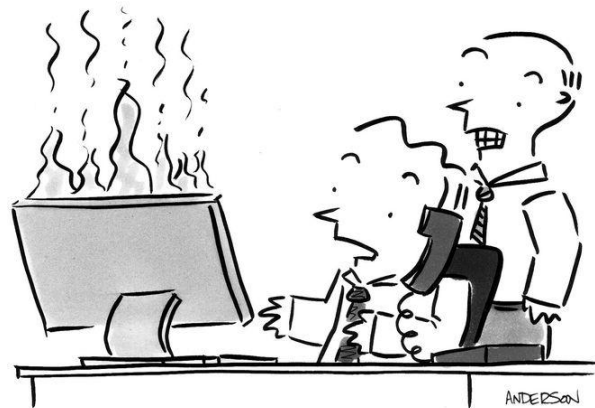
## External Evaluation

- Ground truth testing (or partitions comparison)



# Ground truth testing: Issues

- Few real world datasets with annotated ground truth partition are available (mostly static networks)
- Reliability of partition labelling (semantic partitions not always reflect topological ones)
- Scarcity of network generators handling community dynamics (i.e. birth, death, merge, split)



"I think we're past the point where rebooting will help."

# Benchmark

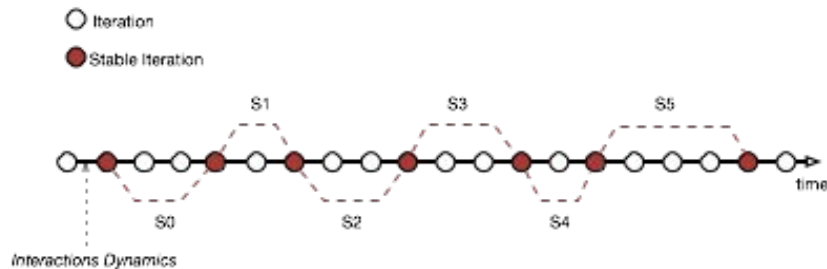
## RDyn

Dynamic network generator that

- Guarantee power law degree distribution
- Guarantee small-world effect
- Exploit planted communities (having power law size distribution)
- Handle node/edge rise/fall
- Handle Community Dynamics (merge/split)
- Generate tunable-quality time-aware network partitions (i.e. conductance/modularity/density)

Expected outputs:

- Synthetic graph (TN/SN)
- Temporal communities with planted events



Events are handled by:

1. "Semantically" planting updated communities;
2. Converging to the final stable state by leveraging intra-community edge probability side effects

A state (iteration) is called stable when a minimum partition quality is reached (i.e. modularity/conductance/density)

# Summarizing



# Mesoscale Evolutions

Node/edge local dynamics affect community structures

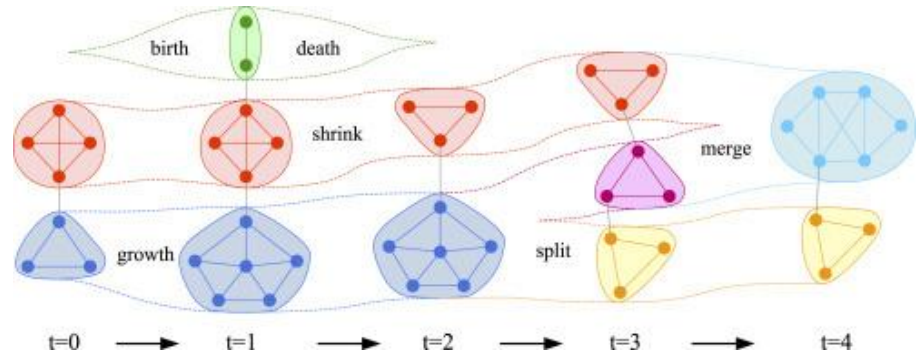
- Communities are subject to events/operations
- Life-cycles can be identified and studied

The complexity behind such ill posed problem grows

- Stability/Persistence
- Smoothness

Every family of approaches depend on

- Specific analytical needs
- Dynamic Network Representation adopted



## Chapter 11

# Conclusion

### Take Away Messages

1. As topology evolve, community do too
2. Smoothness and stability are key issues
  - a. Theseus ship paradox
3. Communities are subject to events
  - a. Life-cycle tracking

### Suggested Readings

- *"Challenges in community discovery on temporal networks."* Cazabet & Rossetti
- *"Community Discovery in Dynamic Networks: a Survey."* Rossetti & Cazabet

### What's Next

Chapter 12:  
**Diffusion: Decision based models**

