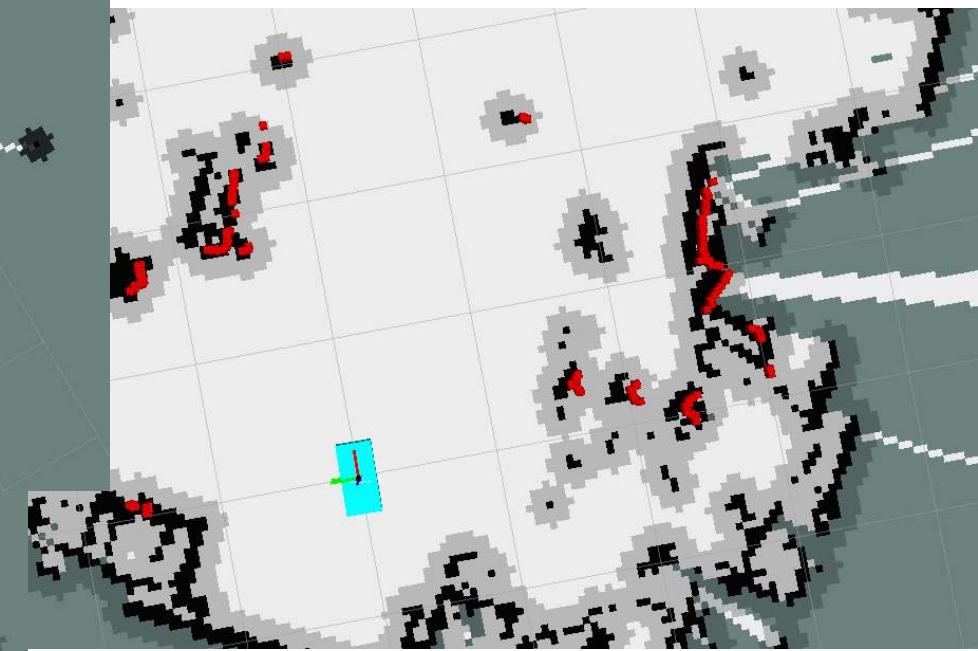
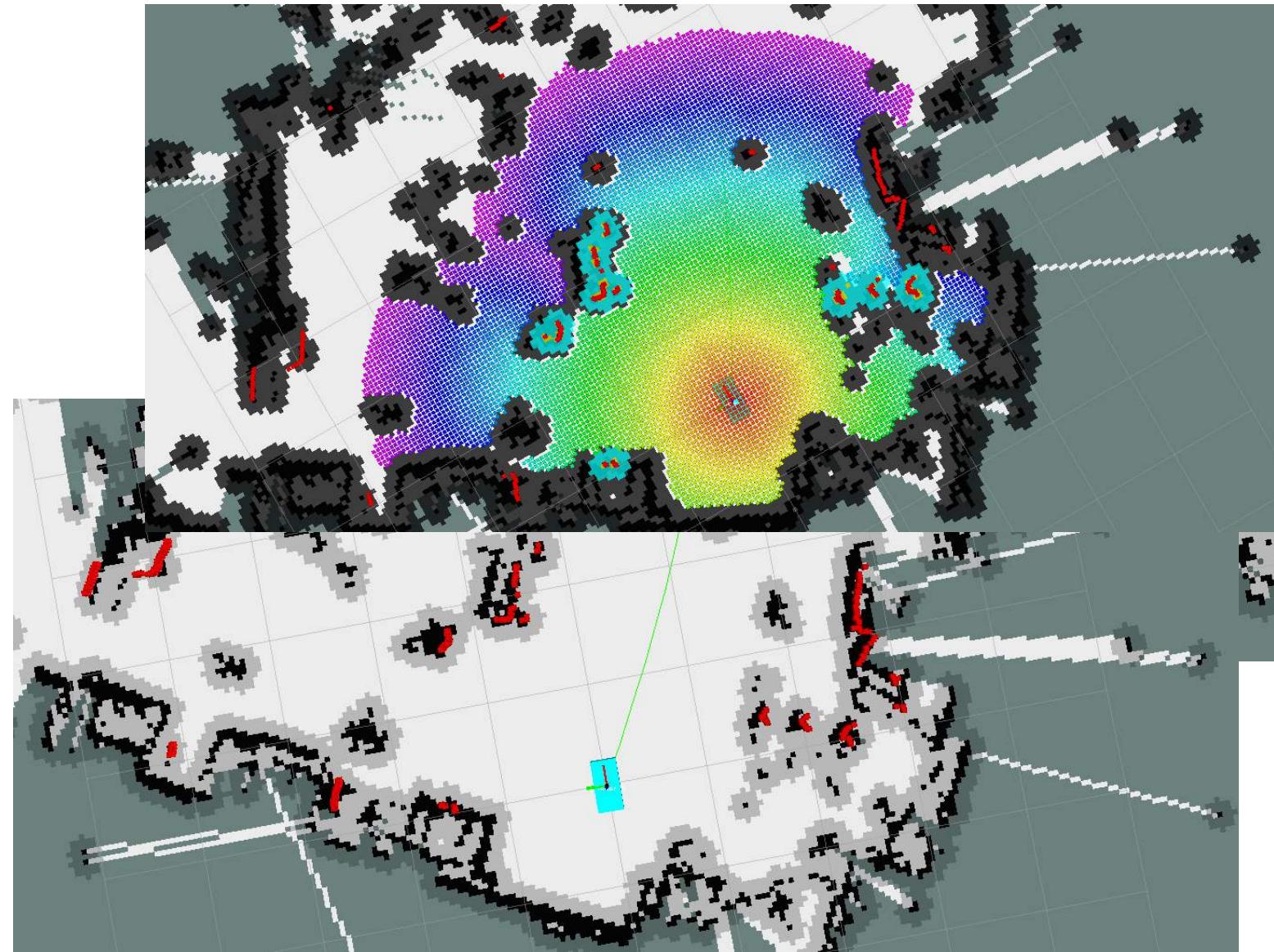




ROS Transformations and frames

Madhur Behl
(University of Virginia)

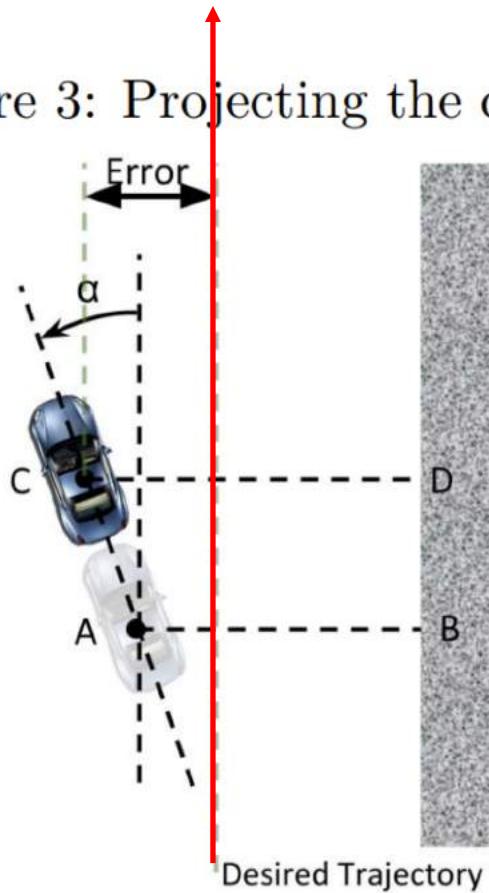
Where are we headed to



COMPLETE AUTONOMY

Account for the forward motion of the car

Figure 3: Projecting the car future in time



$$\alpha = \tan^{-1}\left(\frac{a \cos(\theta) - b}{a \sin(\theta)}\right)$$

$$AB = b \cos(\alpha)$$

$$CD = AB + AC \sin(\alpha)$$

Error = desired trajectory – CD

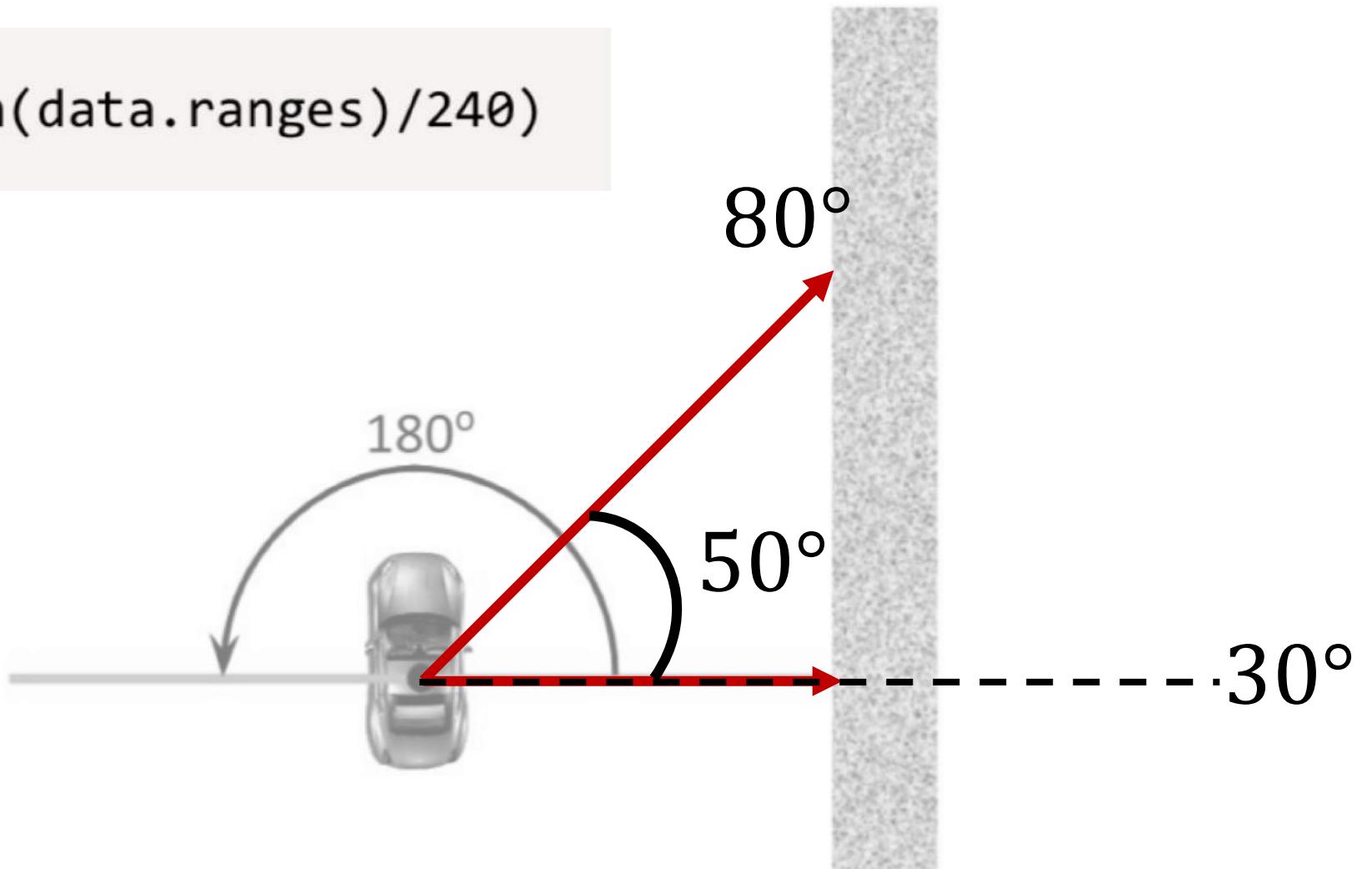
PID Steering Control

$$V_\theta = K_p \times e(t) + K_d \frac{de(t)}{dt}$$

$V_\theta = K_p \times error + K_d \times previous\ error - current\ error$

steering angle = steering angle – V_θ

```
index = theta * (len(data.ranges)/240)
```



```
zero_ray_index = 30 * (len(data.ranges)/240) = 0.125 * (len(data.ranges)/240)
```

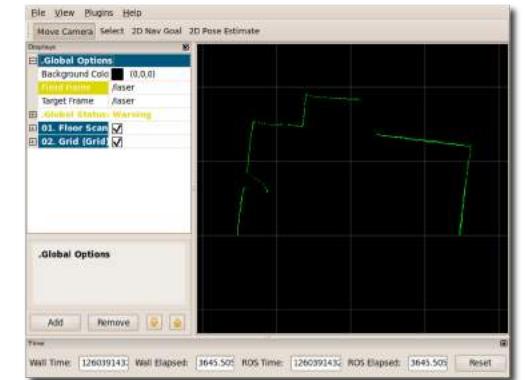
control.py

Publishes to topic – **drive_parameters**

Subscribes to : **error**



ROS over Network



Remote connection
SSH >> rviz visualization

dist_finder.py

Publishes topic – **error** | message type **pid_input.msg**

Subscribes to topic – **scan**

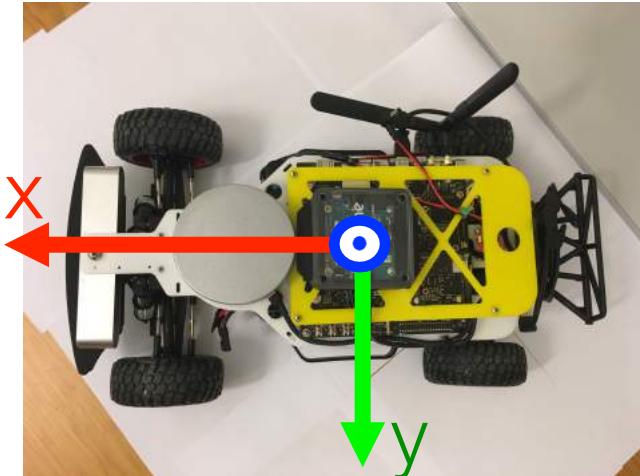
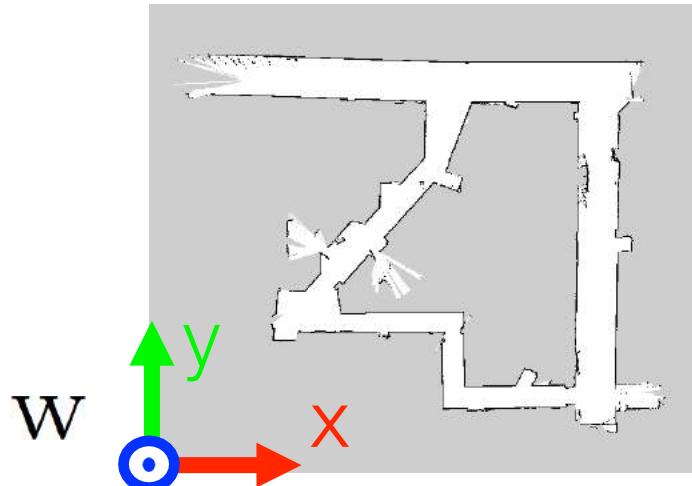
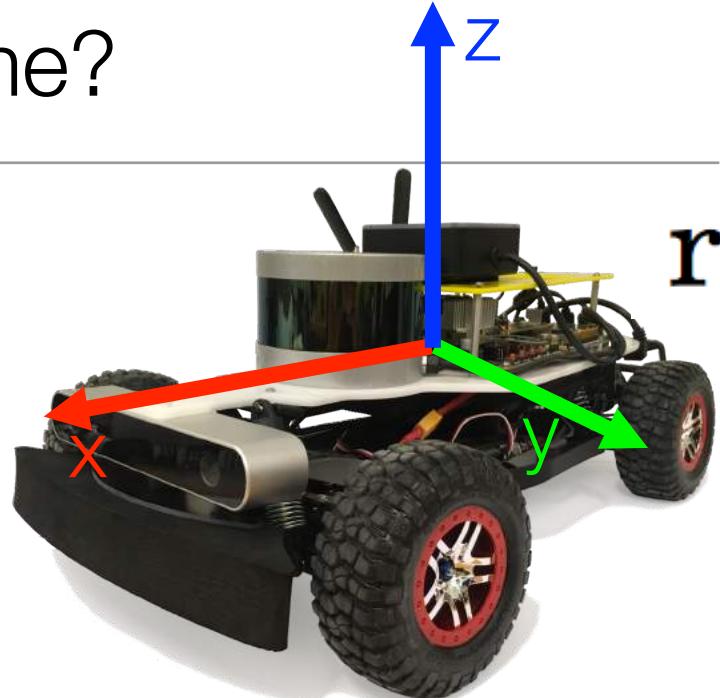
Transformations and Frames:

Map frame – where are you w.r.t the map – co-ordinates from origin



What is a Coordinate Frame?

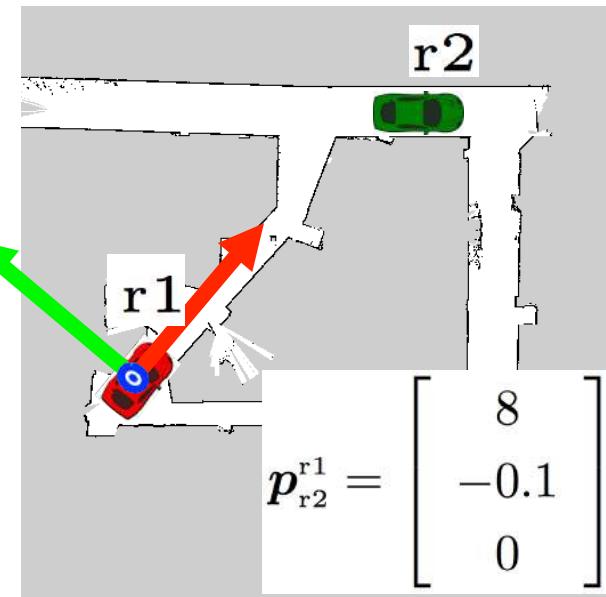
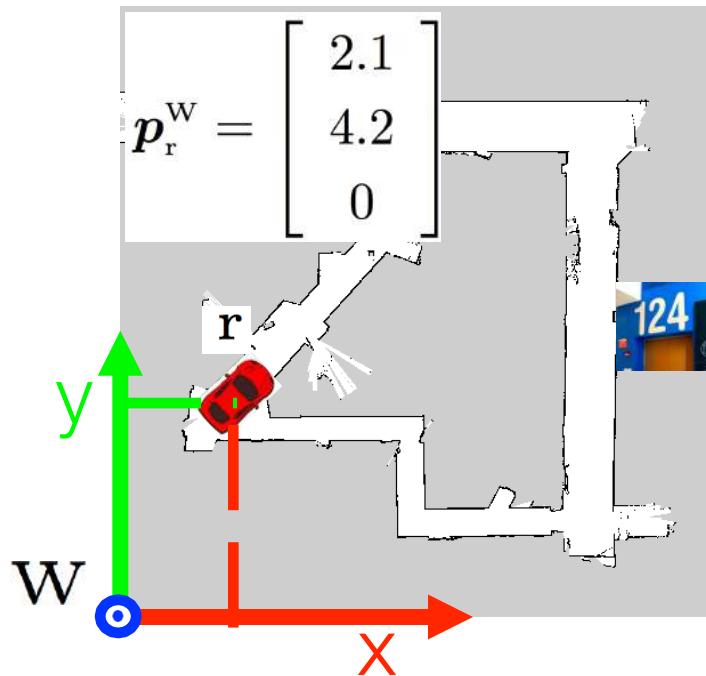
- “set of orthogonal axes attached to a body that serves to describe position of points relative to that body”
- **axes** intersect at a point known as the **origin**



In many robotics problems, the first step is to assign a coordinate frame to all objects of interest

Why do we need Coordinate Frames?

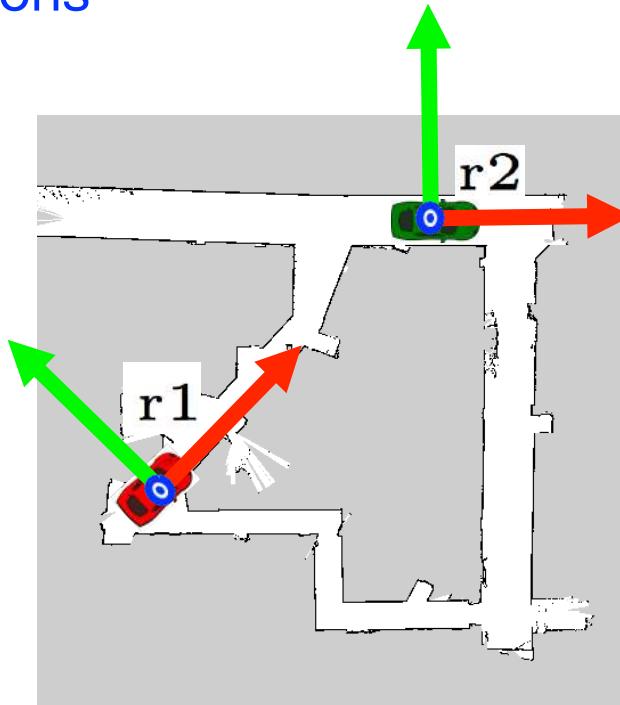
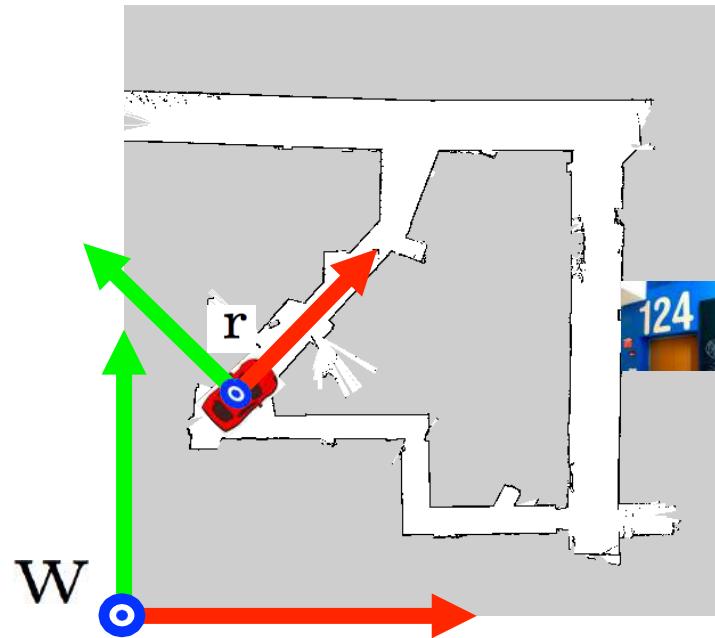
- compact representation of points



- coordinates have no meaning without specifying coordinate frame

Why do we need Coordinate Frames?

- compact representation of points
- compact representation of orientations

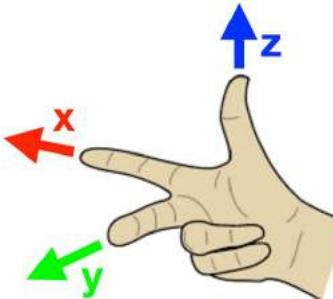


- **rotation, attitude, orientation**
- **pose** = position & rotation

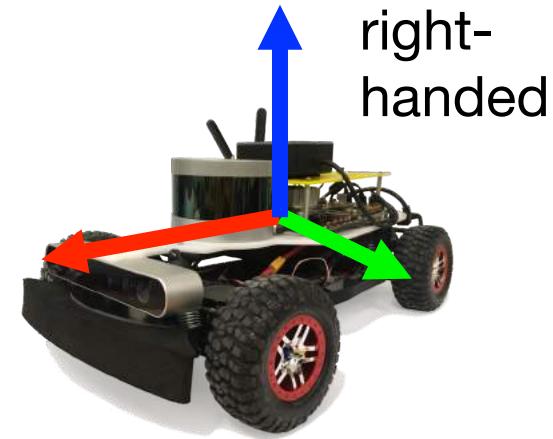
Left-handed vs Right-handed Coordinate Frames

- **Direction of axes is important!**

- There is a common mnemonic:

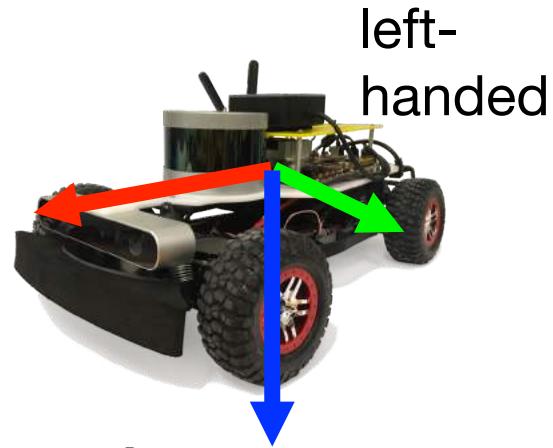


- positive **x axis** points along your **index** finger, positive **y axis** points along your **middle** finger.



- In so-called "**right-handed**" coordinate systems, positive z-axis points along the thumb of your right hand.

- In so-called "**left-handed**" coordinate systems, positive z-axis points along the thumb of your left hand.



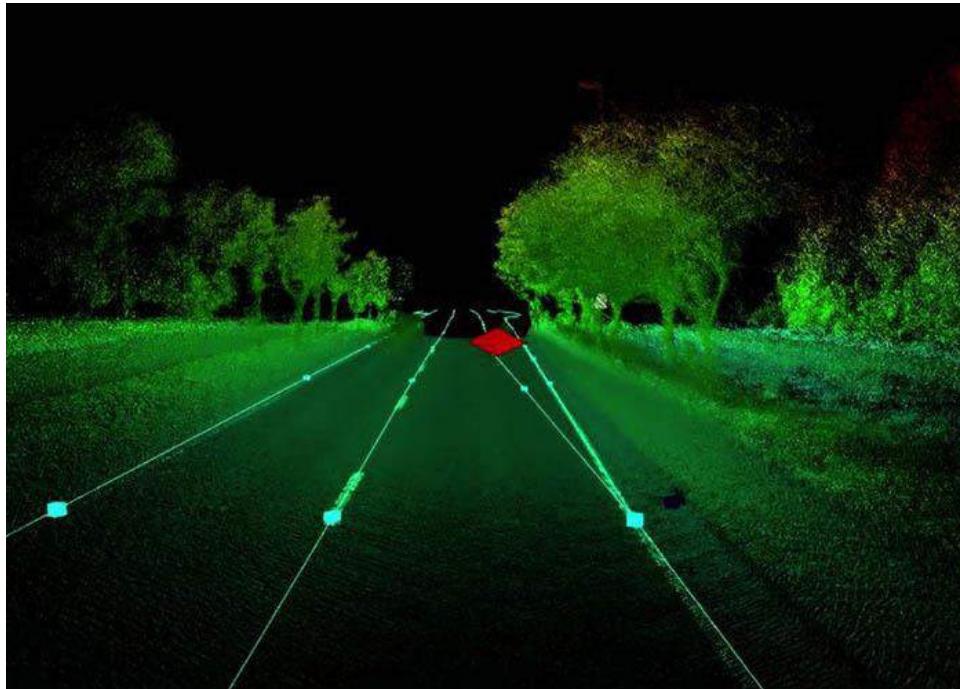
- **robotics always uses right-handed coordinate systems**

- left-handed systems are sometimes used in graphics

[slide courtesy
of Prof. Roy]

Transformations and Frames:

- The **Sensor frame** – how does the world look w.r.t the sensor



Does this tell you anything about where obstacles are in the map?

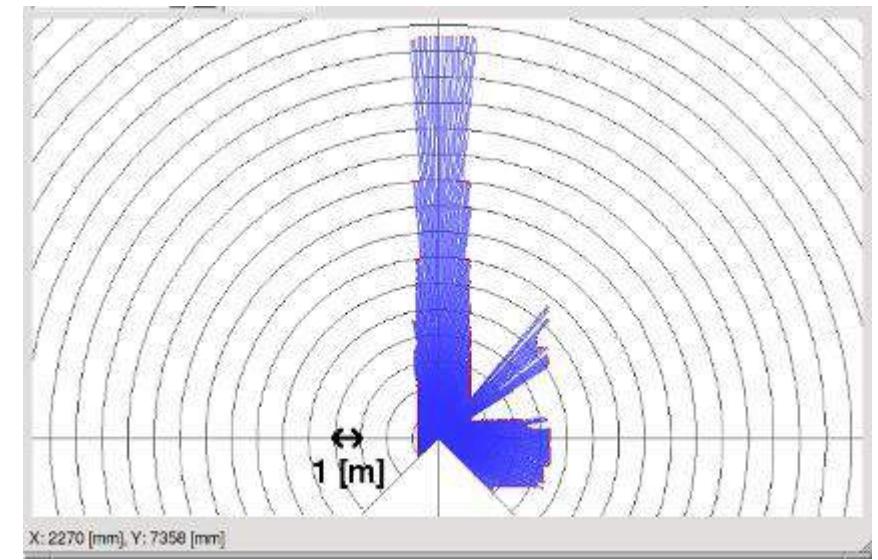
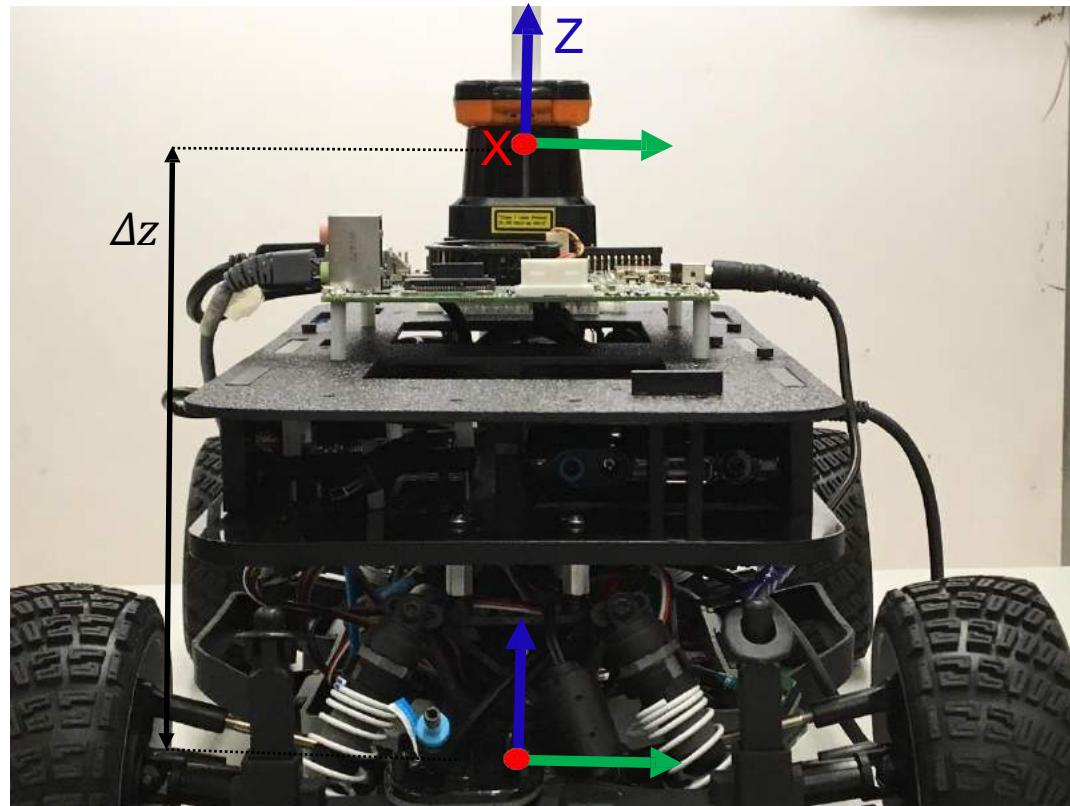
Does this tell you anything about where we are in the map?

We must link frames together

Transformations

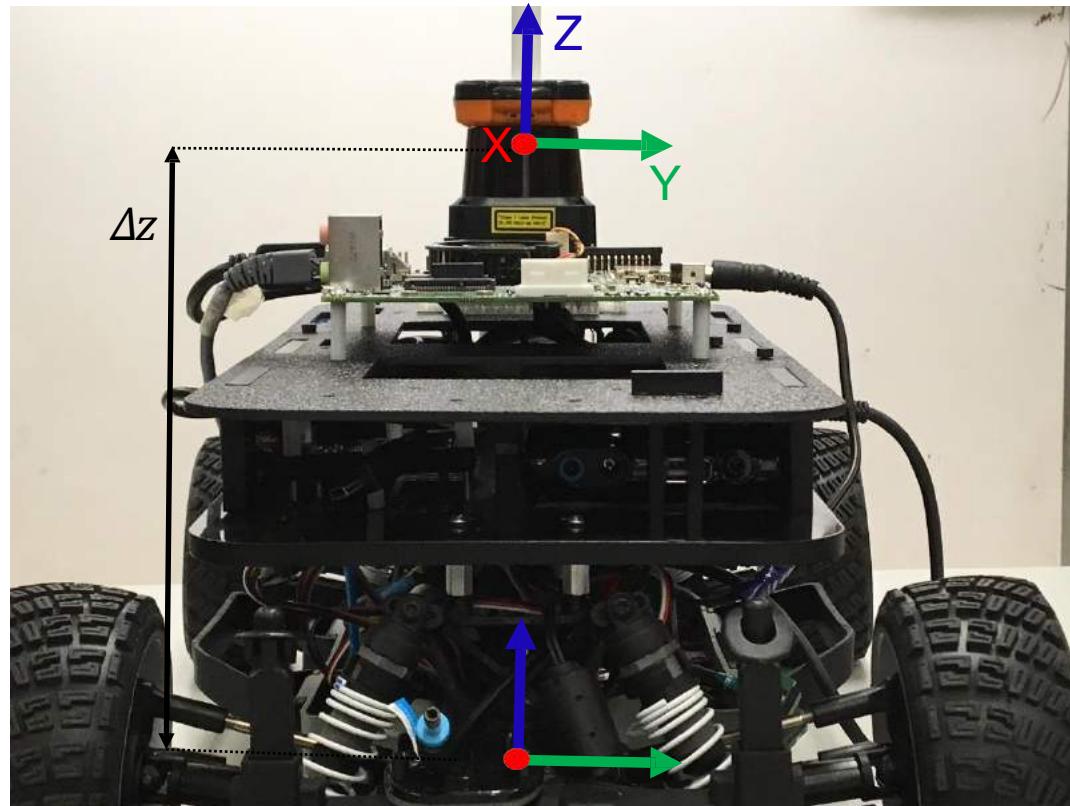
Transformations and Frames

- The frame of reference in which the measurement is taken

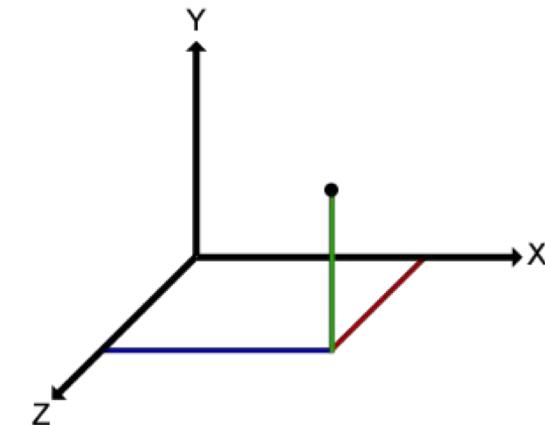
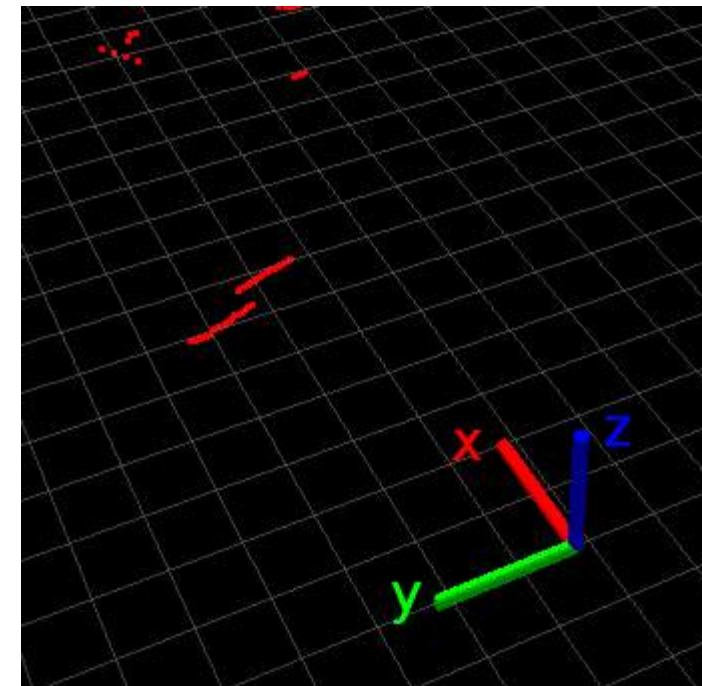


Distance measurements returned by LIDAR

Transformations and Frames

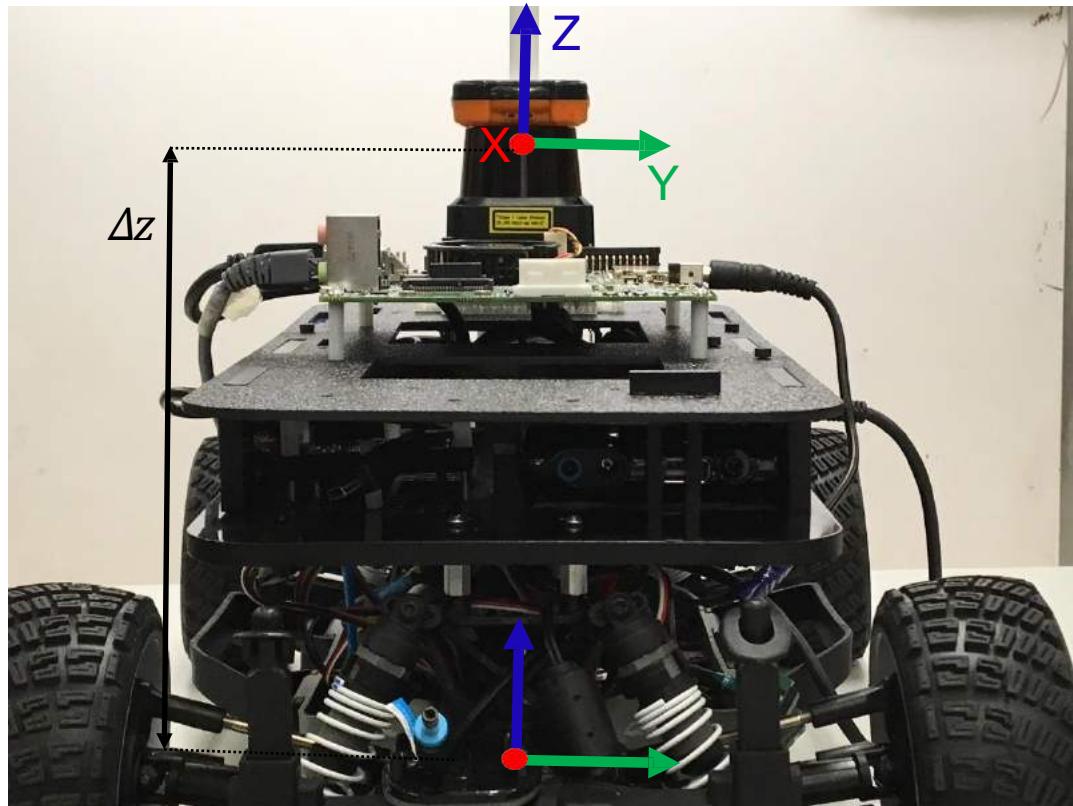


Note:
Axes X,Y,Z of Frames of Reference are orthogonal(90°) to each other.
X,Y,Z represent the axes along the 3 dimensions.

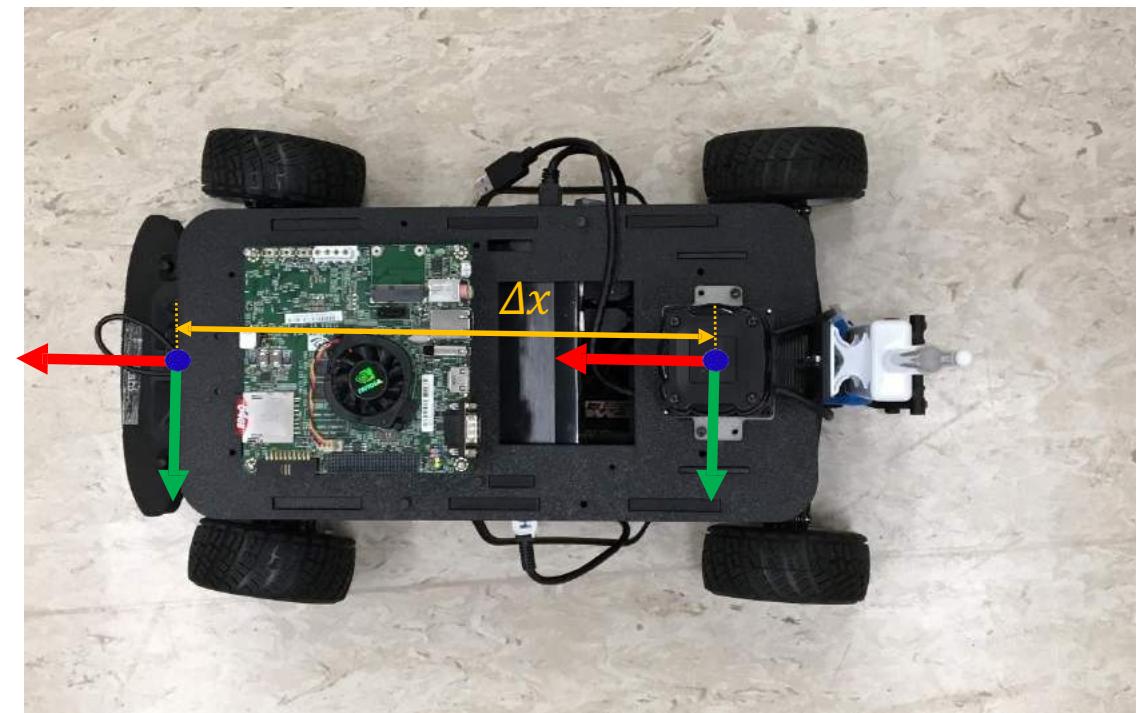


Transformations and Frames

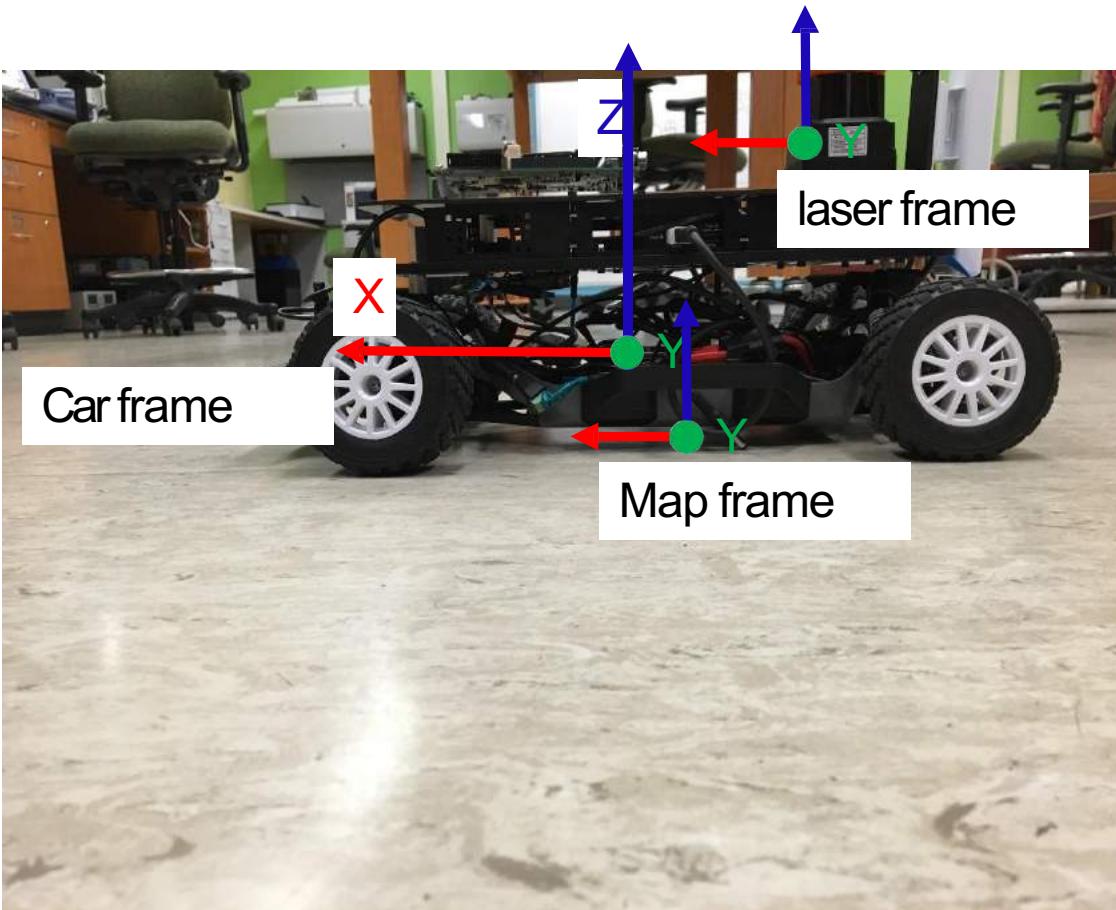
- The frame of reference in which the measurement is taken



The scan Values from the LIDAR will not tell us how far away are the obstacles. We must take care of the offsets



Transformations and Frames

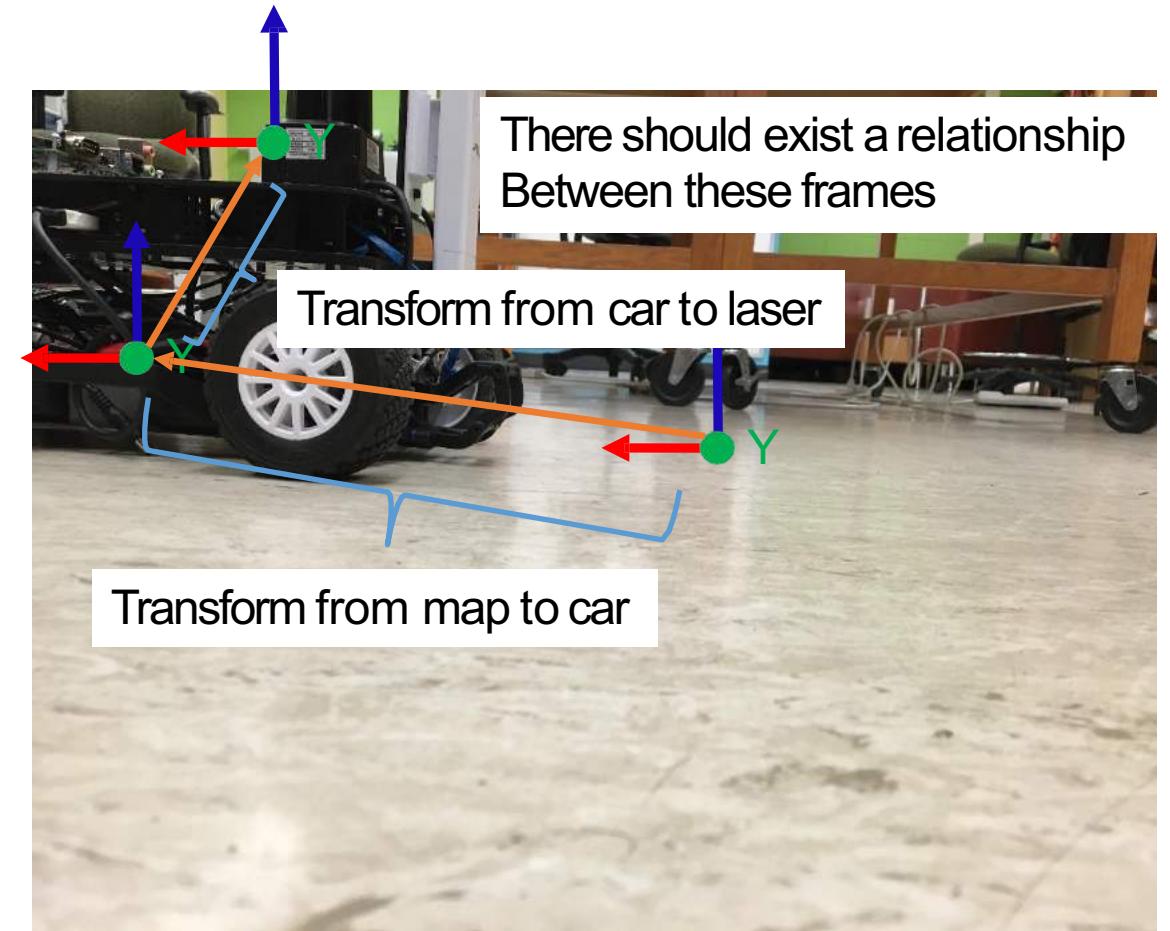
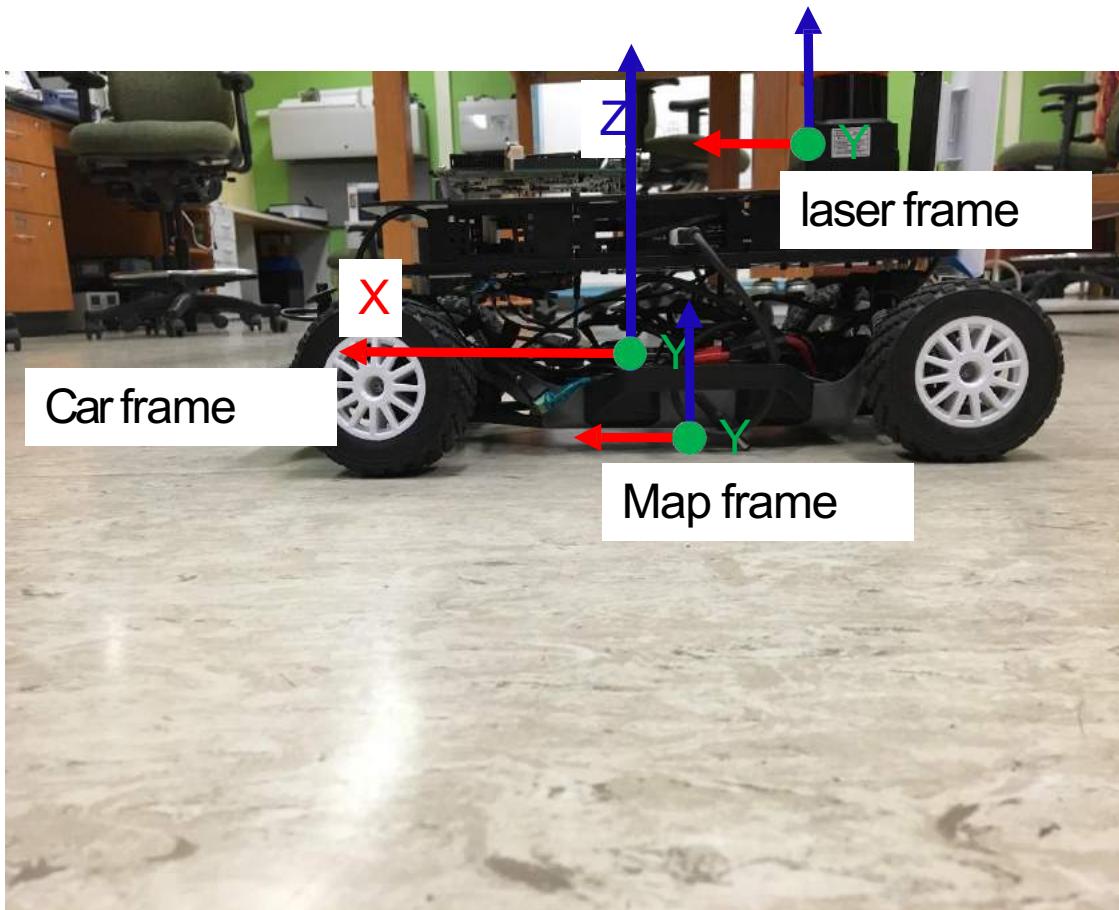


Between frames there will exist transformations that convert measurements from one frame to another

Important Point:
Note what the
transformation means
w.r.t frames

Transformations and Frames

Between frames there will exist transformations that convert measurements from one frame to another



Interact

Move Camera

Select

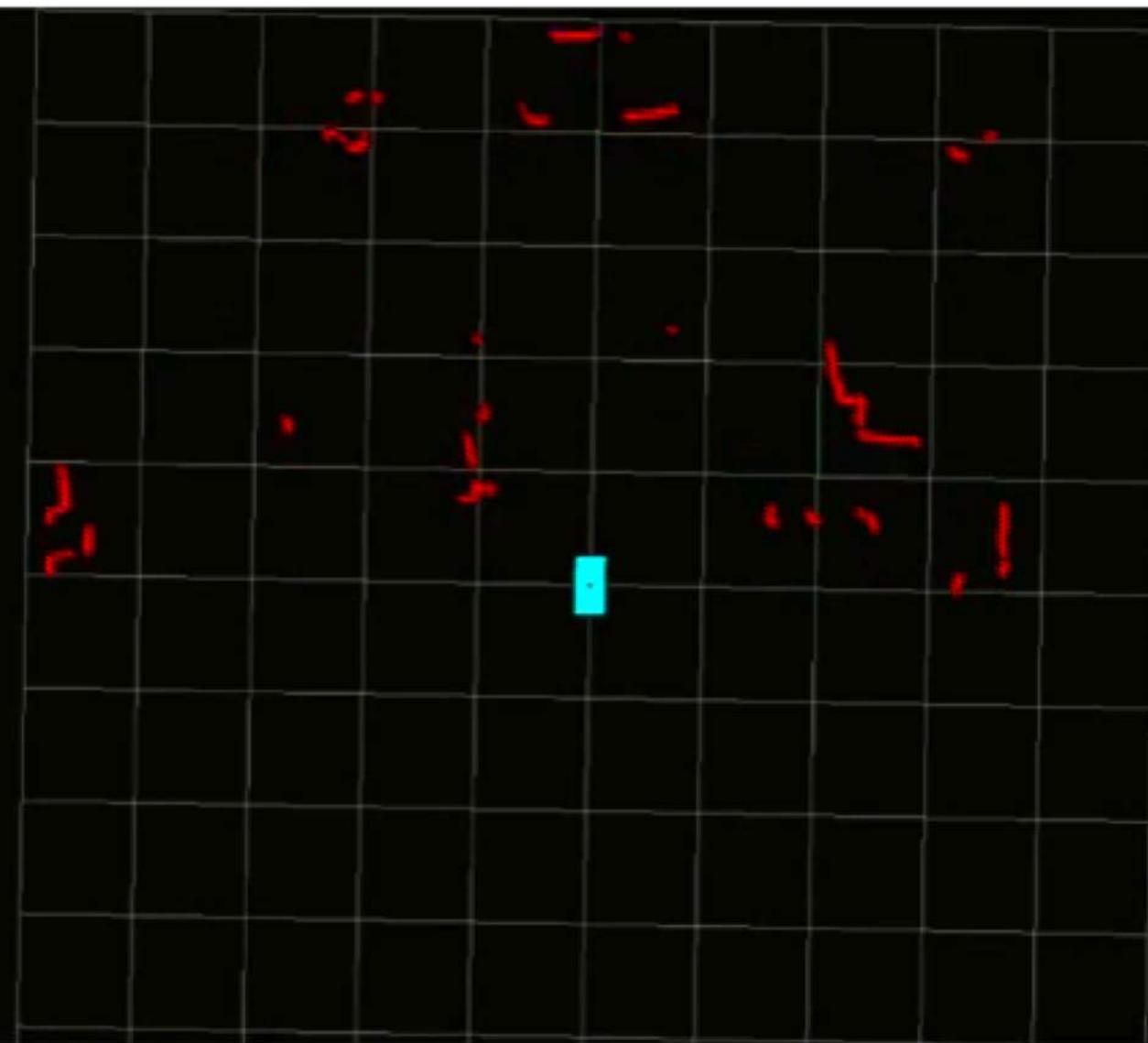
Focus Camera

Measure

2D Pose Estimate

2D Nav Goal

Publish Point



Time

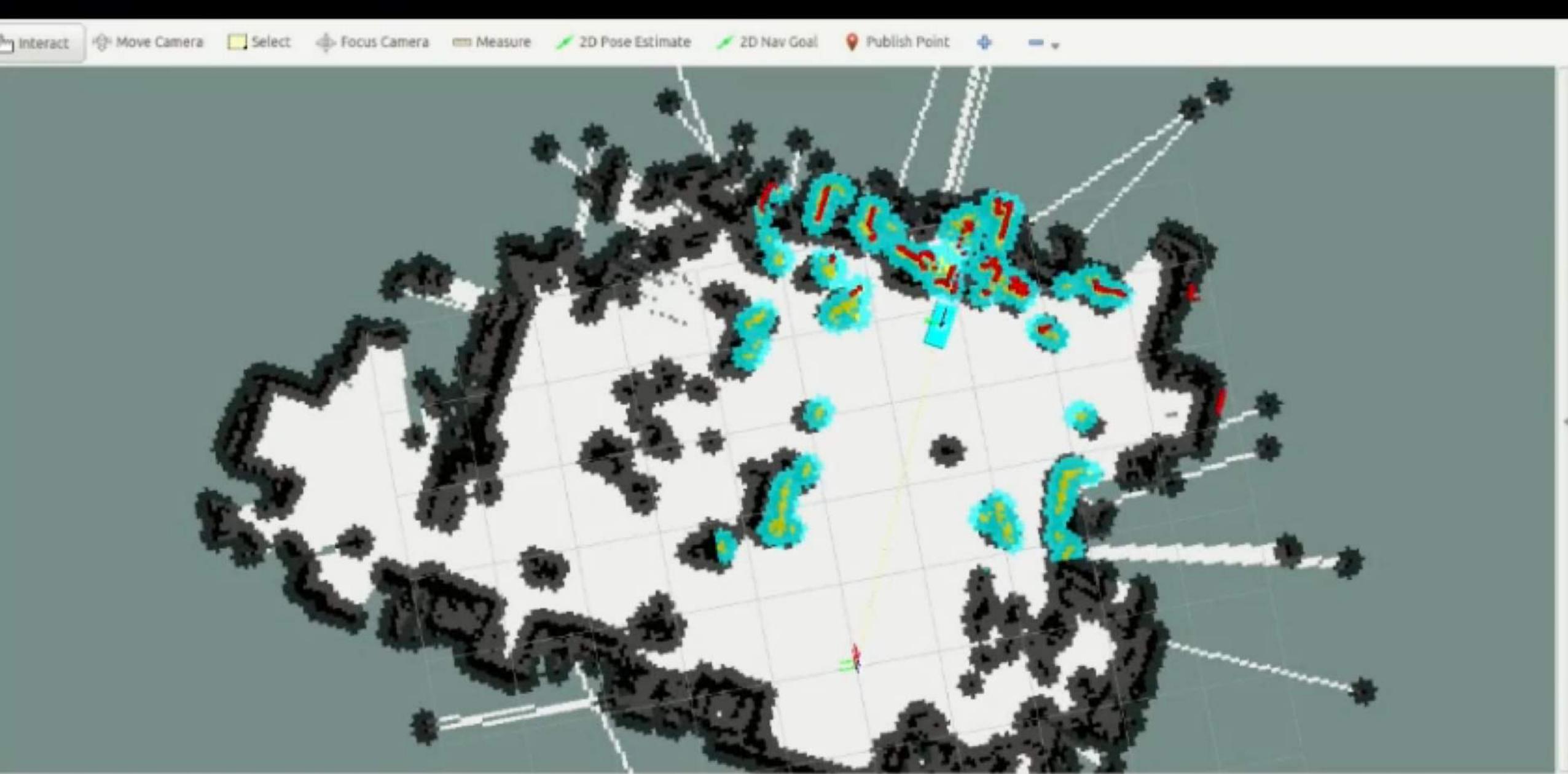
ROS Time: 1449846801.68 ROS Elapsed: 78.84

Wall Time: 1459857837.91 Wall Elapsed: 184.27

Experimental

Reset Left-Click: Rotate Middle-Click: Move X/Y Right-Click/Mouse Wheel: Zoom Shift: More options.

30 fps



Time

OS Time: 1449846795.66

ROS Elapsed: 46.17

Wall Time: 1459858888.32

Wall Elapsed: 194.04

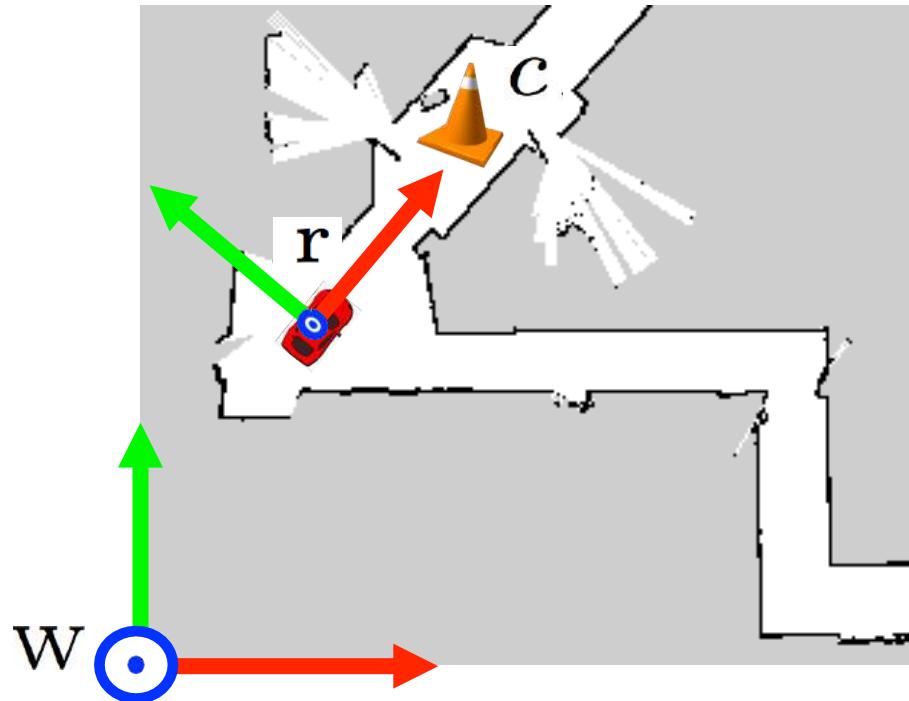
 Experimental

Reset Left-Click: Rotate. Middle-Click: Move X/Y. Right-Click/Mouse Wheel: Zoom. Shift: More options.

30 fps

Rigid-body Transformations

- How to transform points from one coordinate frame to another?



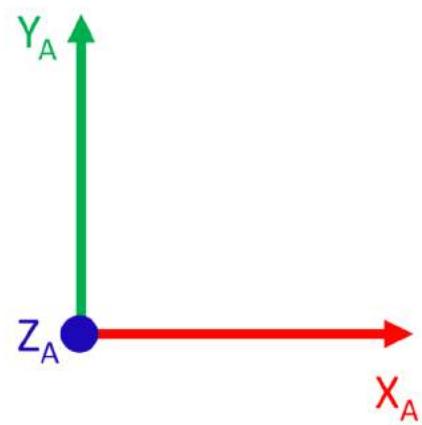
Given point “c” in coordinate frame “r” what is the position of the point in frame “w”?

$$\mathbf{p}_c^w = \mathbf{R}_r^w \mathbf{p}_c^r + \mathbf{p}_r^w$$

- **why rigid?** transformation does not change distance between points (does not deform shapes)
- translations, rotations, (reflections)



Rigid Body Transforms



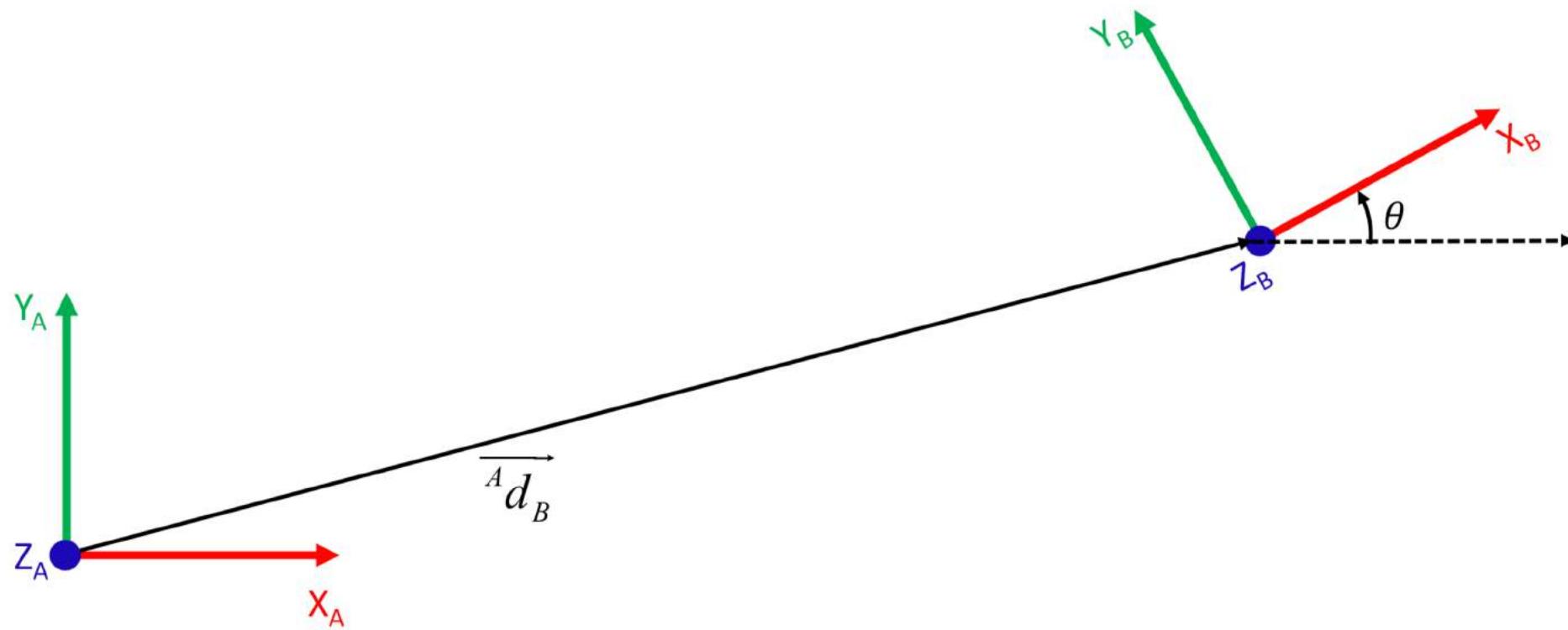
Rigid Body Transforms



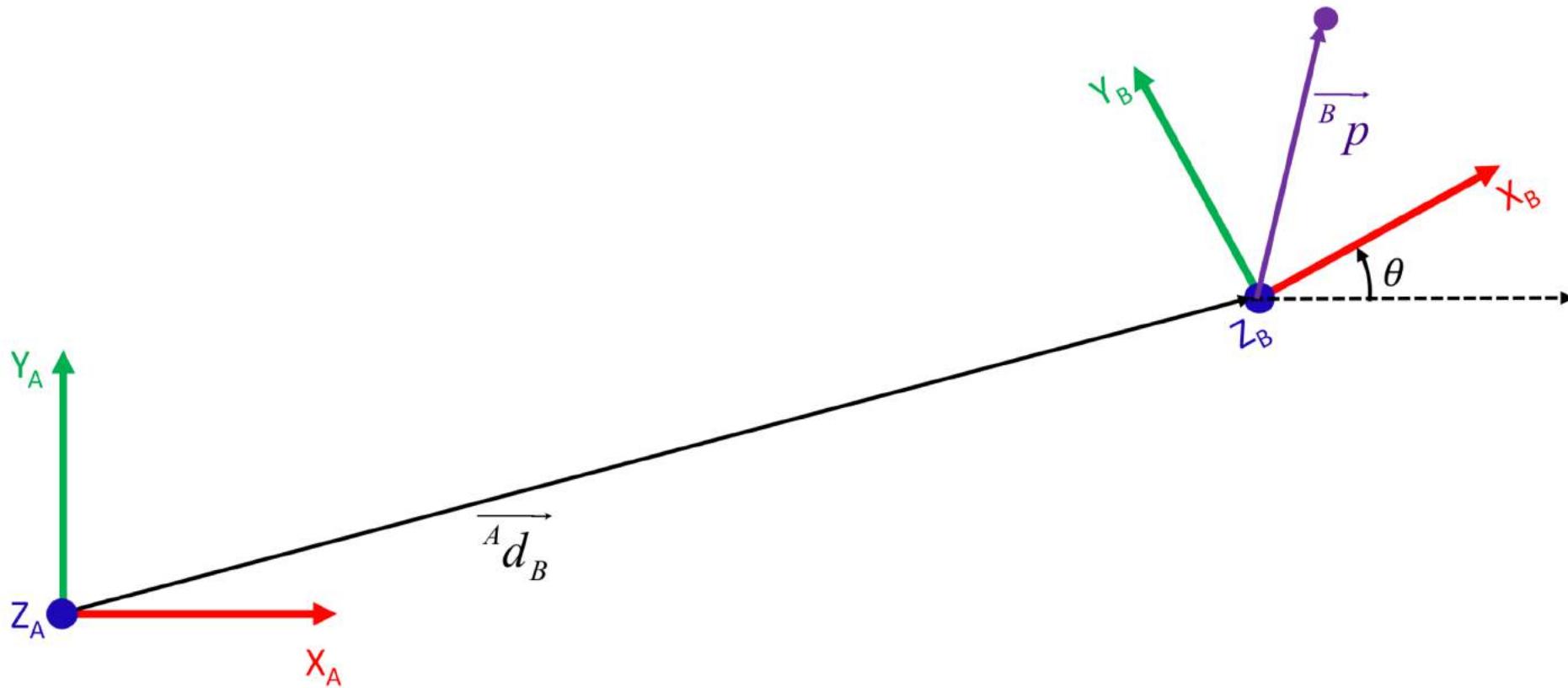
Rigid Body Transforms



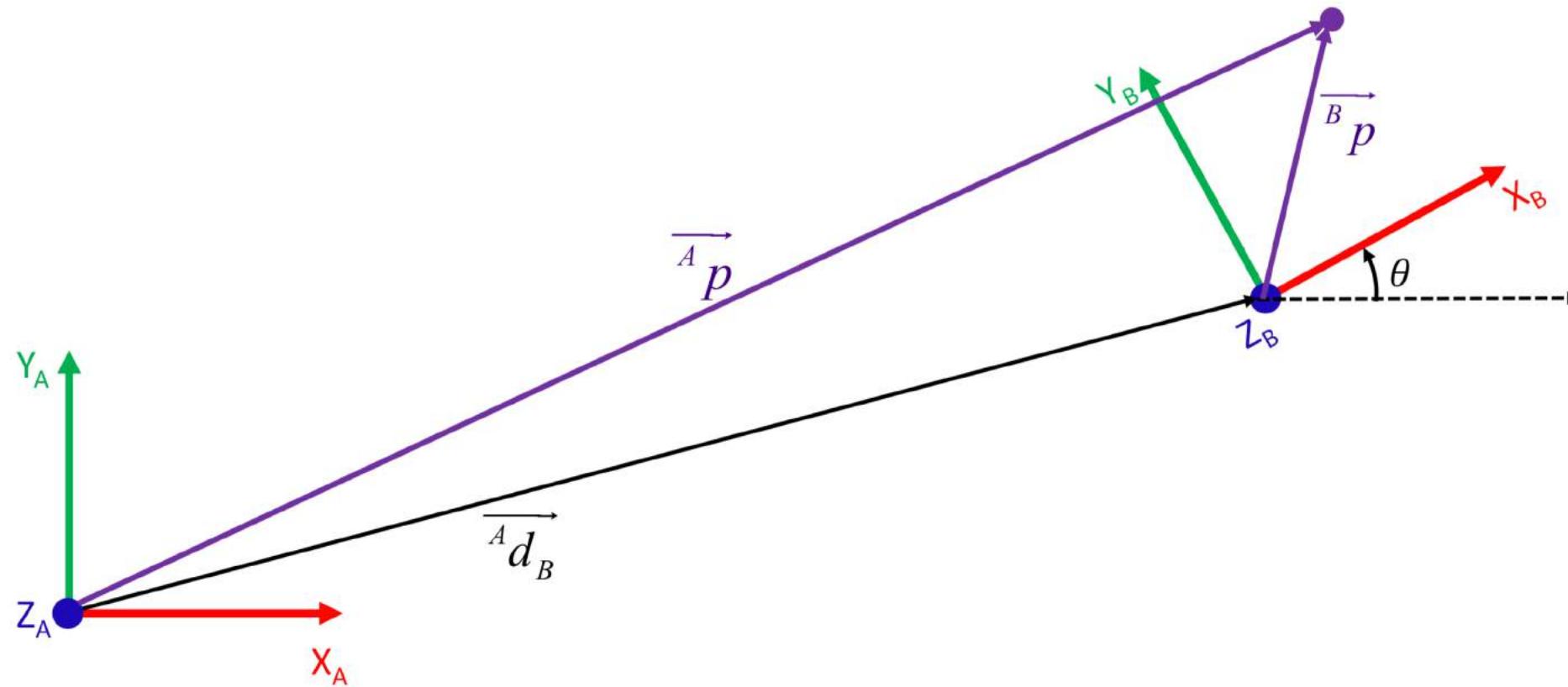
Rigid Body Transforms



Rigid Body Transforms

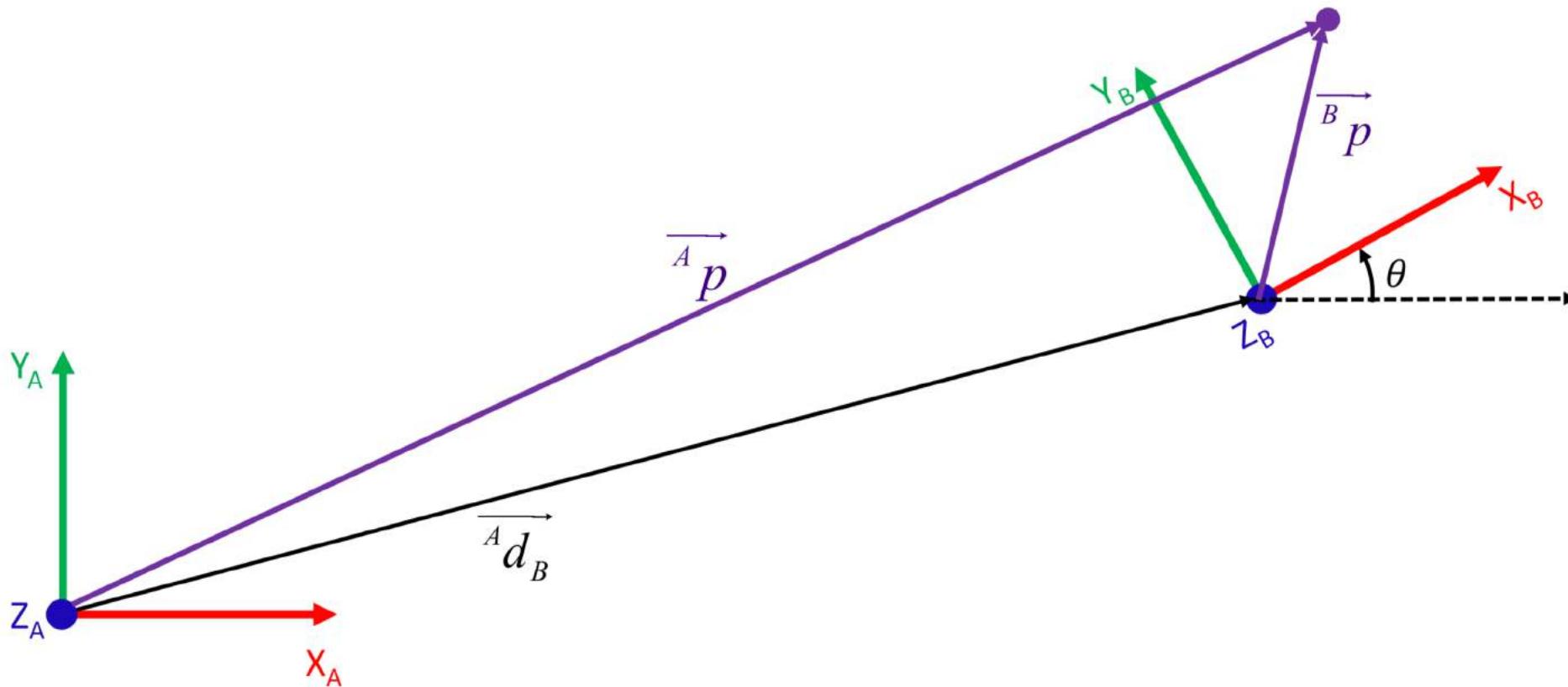


Rigid Body Transforms



Rigid Body Transforms

- What we need is Point p with respect to Frame A, given its pose in Frame B



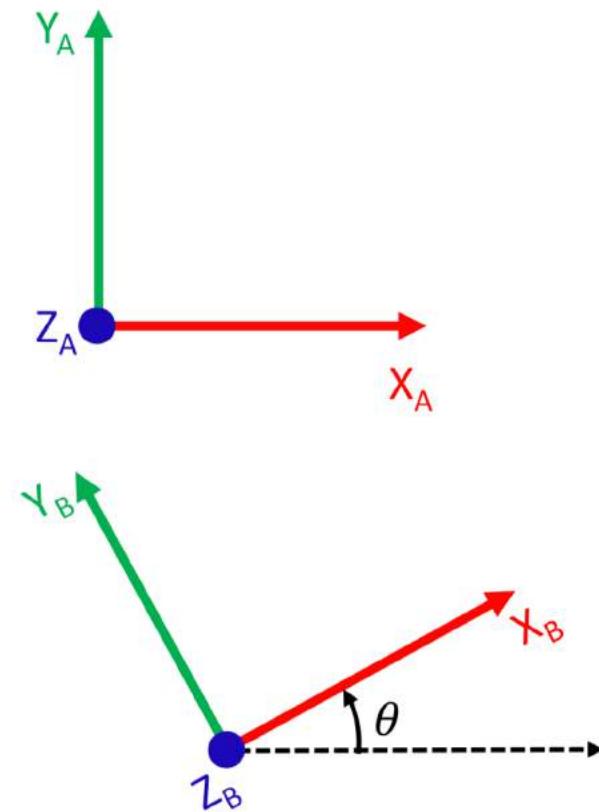
Rigid Body Transforms

- Special type of matrices called Rotation matrices

$$\widehat{X}_B = R_{11}\widehat{X}_A + R_{21}\widehat{Y}_A + R_{31}\widehat{Z}_A$$

$$\widehat{Y}_B = R_{12}\widehat{X}_A + R_{22}\widehat{Y}_A + R_{32}\widehat{Z}_A$$

$$\widehat{Z}_B = R_{13}\widehat{X}_A + R_{23}\widehat{Y}_A + R_{33}\widehat{Z}_A$$



Rigid Body Transforms

- Special type of matrices called Rotation matrices

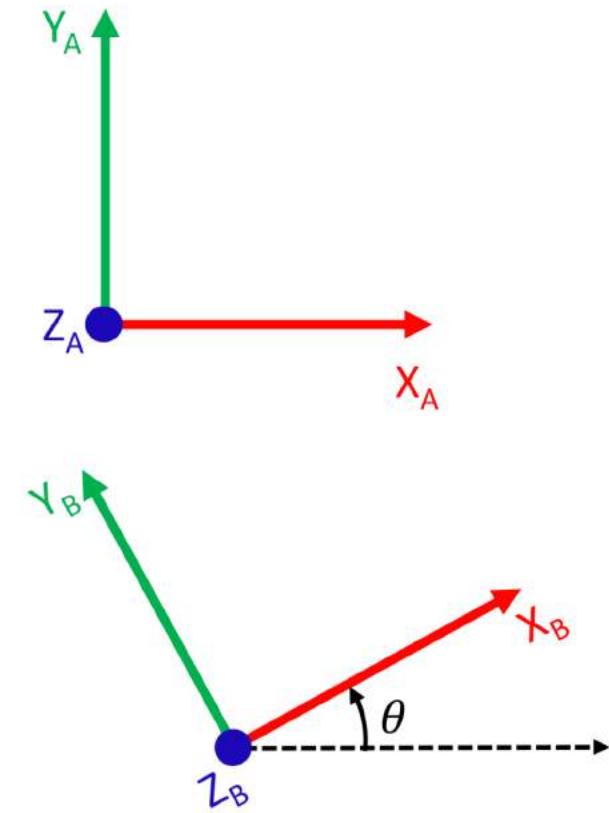
$$\widehat{X}_B = R_{11}\widehat{X}_A + R_{21}\widehat{Y}_A + R_{31}\widehat{Z}_A$$

$$\widehat{Y}_B = R_{12}\widehat{X}_A + R_{22}\widehat{Y}_A + R_{32}\widehat{Z}_A$$

$$\widehat{Z}_B = R_{13}\widehat{X}_A + R_{23}\widehat{Y}_A + R_{33}\widehat{Z}_A$$

$${}^A R_B = \begin{bmatrix} R_{11} & R_{12} & R_{13} \\ R_{21} & R_{22} & R_{23} \\ R_{31} & R_{32} & R_{33} \end{bmatrix}$$

Takes points in frame B and represents their orientation in frame A



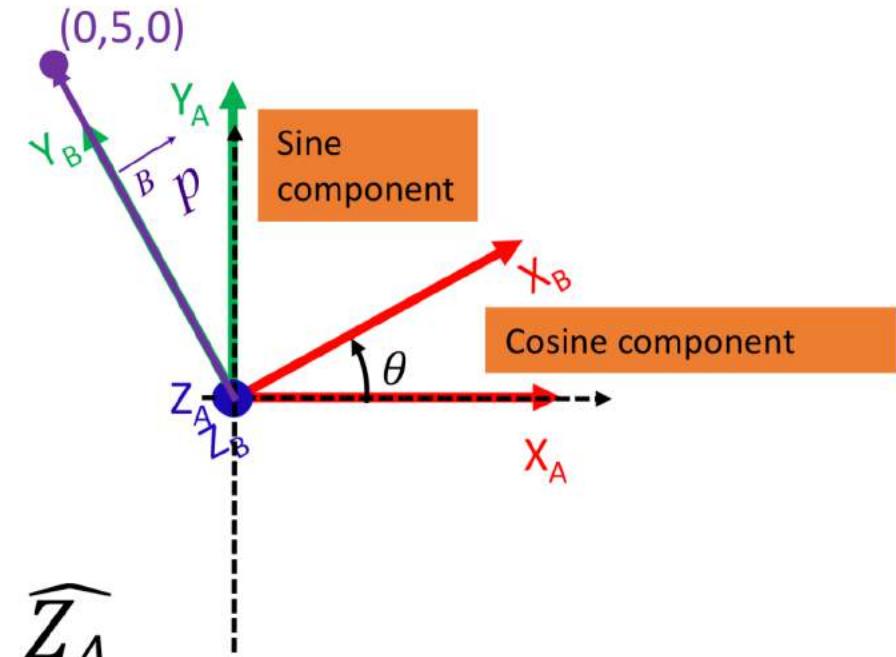
Rigid Body Transforms: Rotation Matrices

$$\widehat{X}_B = R_{11}\widehat{X}_A + R_{21}\widehat{Y}_A + R_{31}\widehat{Z}_A$$

$$\widehat{Y}_B = R_{12}\widehat{X}_A + R_{22}\widehat{Y}_A + R_{32}\widehat{Z}_A$$

$$\widehat{Z}_B = R_{13}\widehat{X}_A + R_{23}\widehat{Y}_A + R_{33}\widehat{Z}_A$$

$$\widehat{X}_B = \underbrace{\cos(\theta) \times \widehat{X}_A}_{R_{11}} + \underbrace{\sin(\theta) \times \widehat{Y}_A}_{R_{21}} + \underbrace{0 \times \widehat{Z}_A}_{R_{31}}$$



Rigid Body Transforms: Rotation Matrices

$${}^A R_B = \begin{bmatrix} \cos(\theta) & R_{12} & R_{13} \\ \sin(\theta) & R_{22} & R_{23} \\ 0 & R_{32} & R_{33} \end{bmatrix}$$

The diagram illustrates the decomposition of the rotation matrix ${}^A R_B$ into its components. The first column, containing $\cos(\theta)$ and $\sin(\theta)$, is highlighted with a red border and points to the unit vector \widehat{X}_B . The second column, containing R_{12} , R_{22} , and R_{32} , is highlighted with a red border and points to the unit vector \widehat{Y}_B . The third column, containing R_{13} , R_{23} , and R_{33} , is highlighted with a red border and points to the unit vector \widehat{Z}_B .

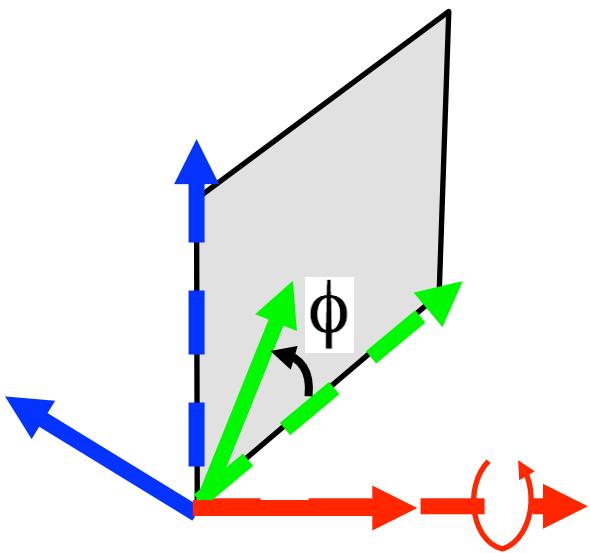
\widehat{X}_A
 \widehat{Y}_A
 \widehat{Z}_A

$${}^A R_B = \begin{bmatrix} C_\theta & -S_\theta & 0 \\ S_\theta & C_\theta & 0 \\ 0 & 0 & 1 \end{bmatrix}$$

$$\begin{aligned} C_\theta &= \cos(\theta) \\ S_\theta &= \sin(\theta) \end{aligned}$$

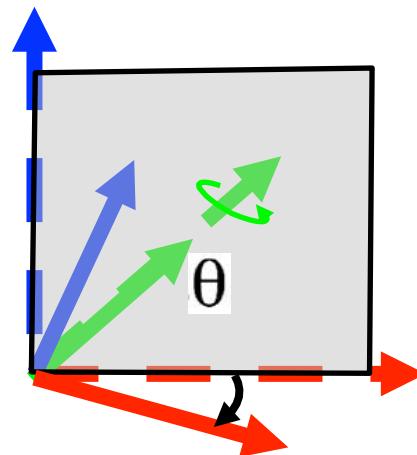
Elementary Rotations

Rotation around
the **x** axis



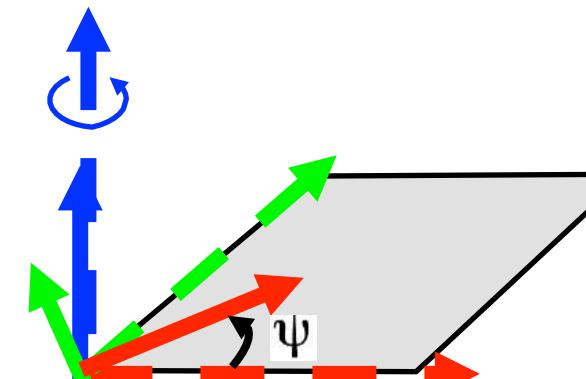
$$R_x(\phi) = \begin{bmatrix} 1 & 0 & 0 \\ 0 & \cos\phi & -\sin\phi \\ 0 & \sin\phi & \cos\phi \end{bmatrix}$$

Rotation around
the **y** axis



$$R_y(\theta) = \begin{bmatrix} \cos\theta & 0 & \sin\theta \\ 0 & 1 & 0 \\ -\sin\theta & 0 & \cos\theta \end{bmatrix}$$

Rotation around
the **z** axis



$$R_z(\psi) = \begin{bmatrix} \cos\psi & -\sin\psi & 0 \\ \sin\psi & \cos\psi & 0 \\ 0 & 0 & 1 \end{bmatrix}$$

Euler Angles

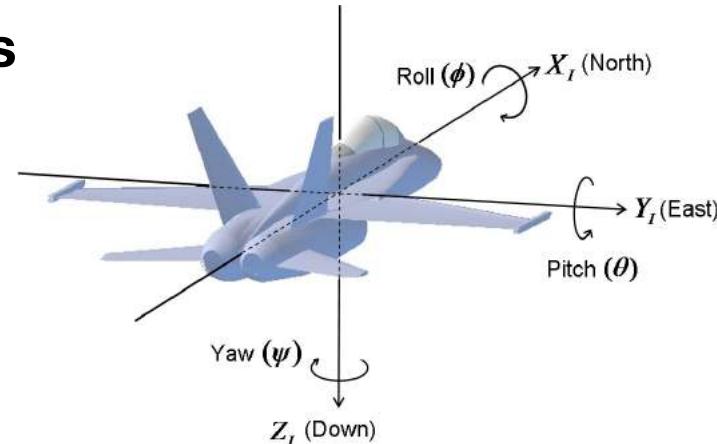
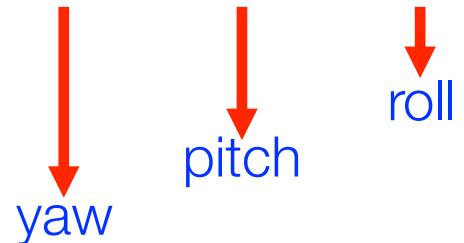
Euler's rotation theorem (1.0): Any rotation can be written as the product of no more than 3 elementary rotations (no two consecutive rotations along the same axis).

$$\mathbf{R} = \mathbf{R}_z(\gamma) \mathbf{R}_y(\beta) \mathbf{R}_x(\alpha)$$

$$\mathbf{R} = \mathbf{R}_y(\gamma) \mathbf{R}_z(\beta) \mathbf{R}_y(\alpha)$$

- why not x-y-z, y-x-z, x-x-z, ...?
- α, β, γ are generally called **Euler angles**

$$\mathbf{R} = \mathbf{R}_z(\gamma) \mathbf{R}_y(\beta) \mathbf{R}_x(\alpha)$$



- We only need 3 numbers to represent a rotation!

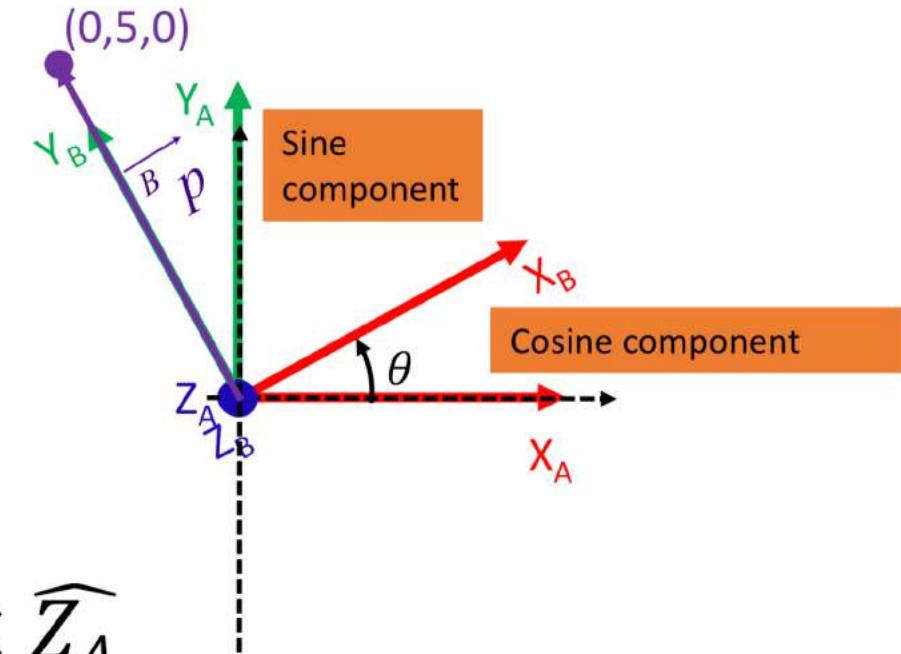
Rigid Body Transforms: Rotation Matrices

$$\widehat{X}_B = R_{11}\widehat{X}_A + R_{21}\widehat{Y}_A + R_{31}\widehat{Z}_A$$

$$\widehat{Y}_B = R_{12}\widehat{X}_A + R_{22}\widehat{Y}_A + R_{32}\widehat{Z}_A$$

$$\widehat{Z}_B = R_{13}\widehat{X}_A + R_{23}\widehat{Y}_A + R_{33}\widehat{Z}_A$$

$$\widehat{X}_B = \underbrace{\cos(\theta) \times \widehat{X}_A}_{R_{11}} + \underbrace{\sin(\theta) \times \widehat{Y}_A}_{R_{21}} + \underbrace{0 \times \widehat{Z}_A}_{R_{31}}$$



We have the Rotation Matrix, so now what?

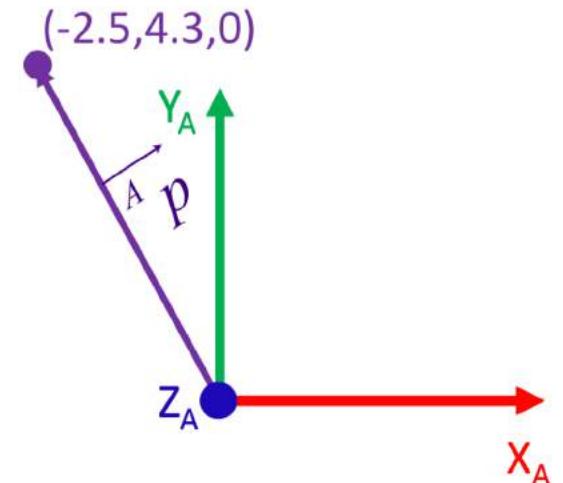
$$\overrightarrow{^A p} = {}^A R_B \times \overrightarrow{^B p}$$

We now have the point P as referenced in frame A

$$R = \begin{bmatrix} 0.86 & -0.5 & 0 \\ 0.5 & 0.86 & 0 \\ 0 & 0 & 1 \end{bmatrix}$$

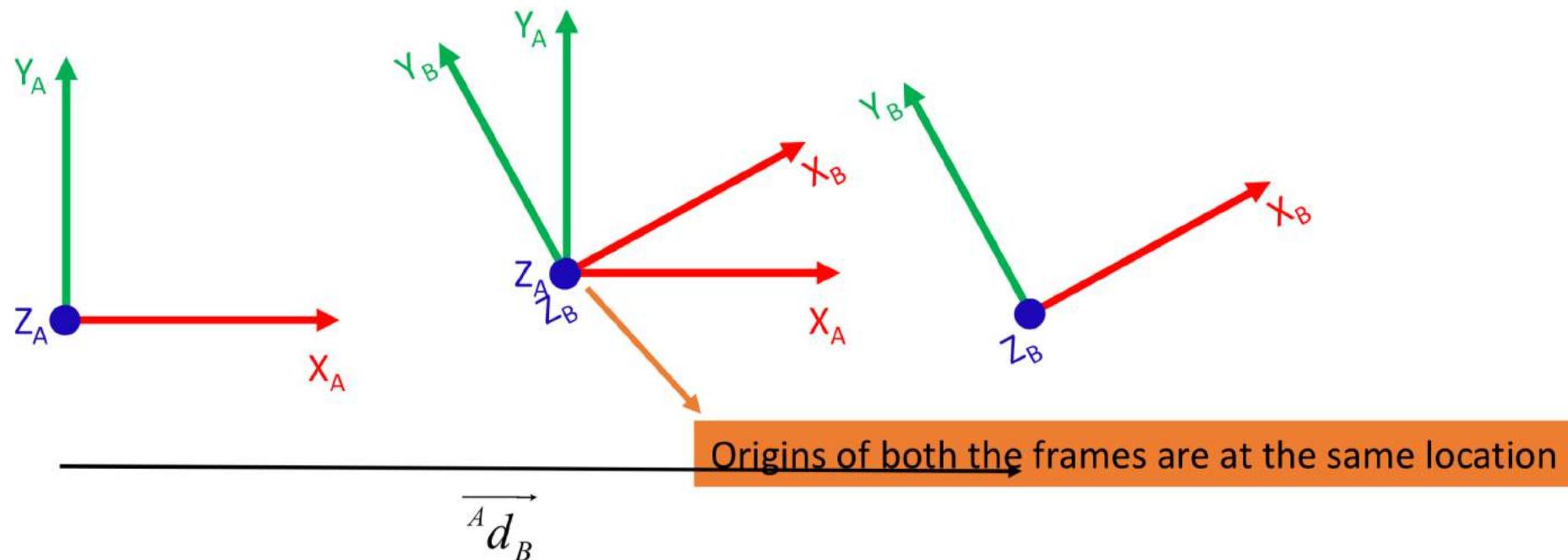
For example

$$\theta = \pi/6 \Rightarrow \overrightarrow{^A p} = (-2.5, 4.3, 0)$$

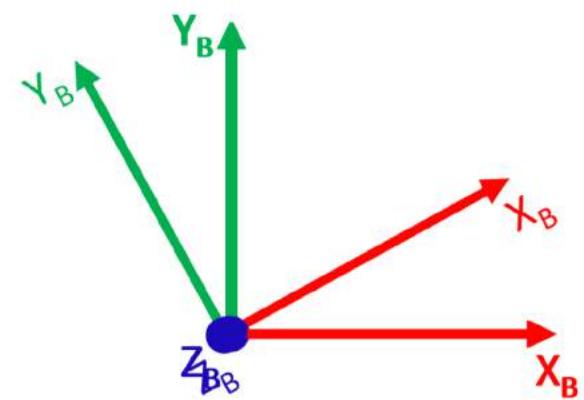
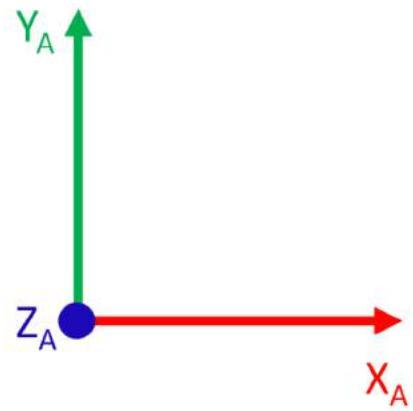


Important point to remember

- The rotation matrix will take care of perspectives of orientation, what about displacement?



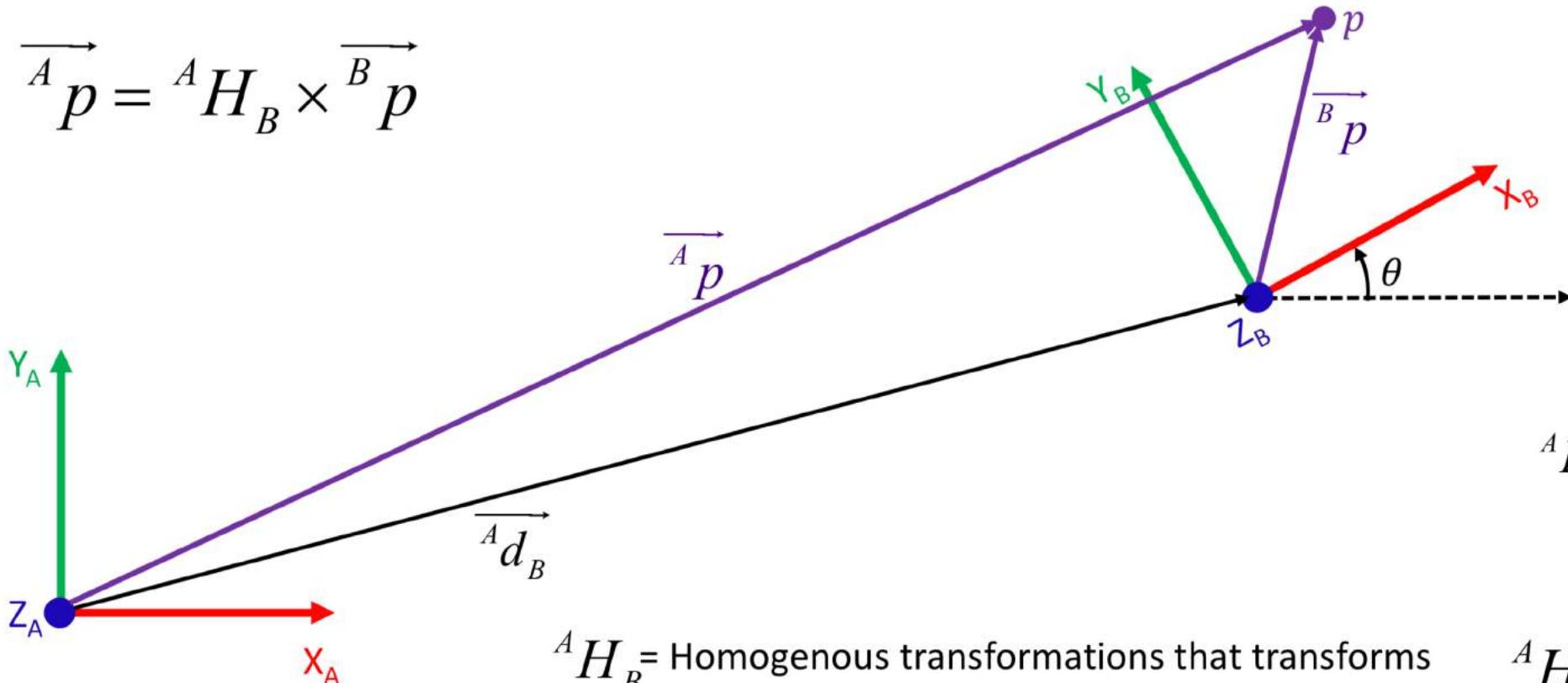
$$\overrightarrow{^A p} = {}^A R_B \times {}^B p + {}^A d_B$$



Rigid Body Transforms

- What we need is Point p with respect to Frame A, given its pose in Frame B

$$\overrightarrow{^A p} = {}^A H_B \times \overrightarrow{^B p}$$

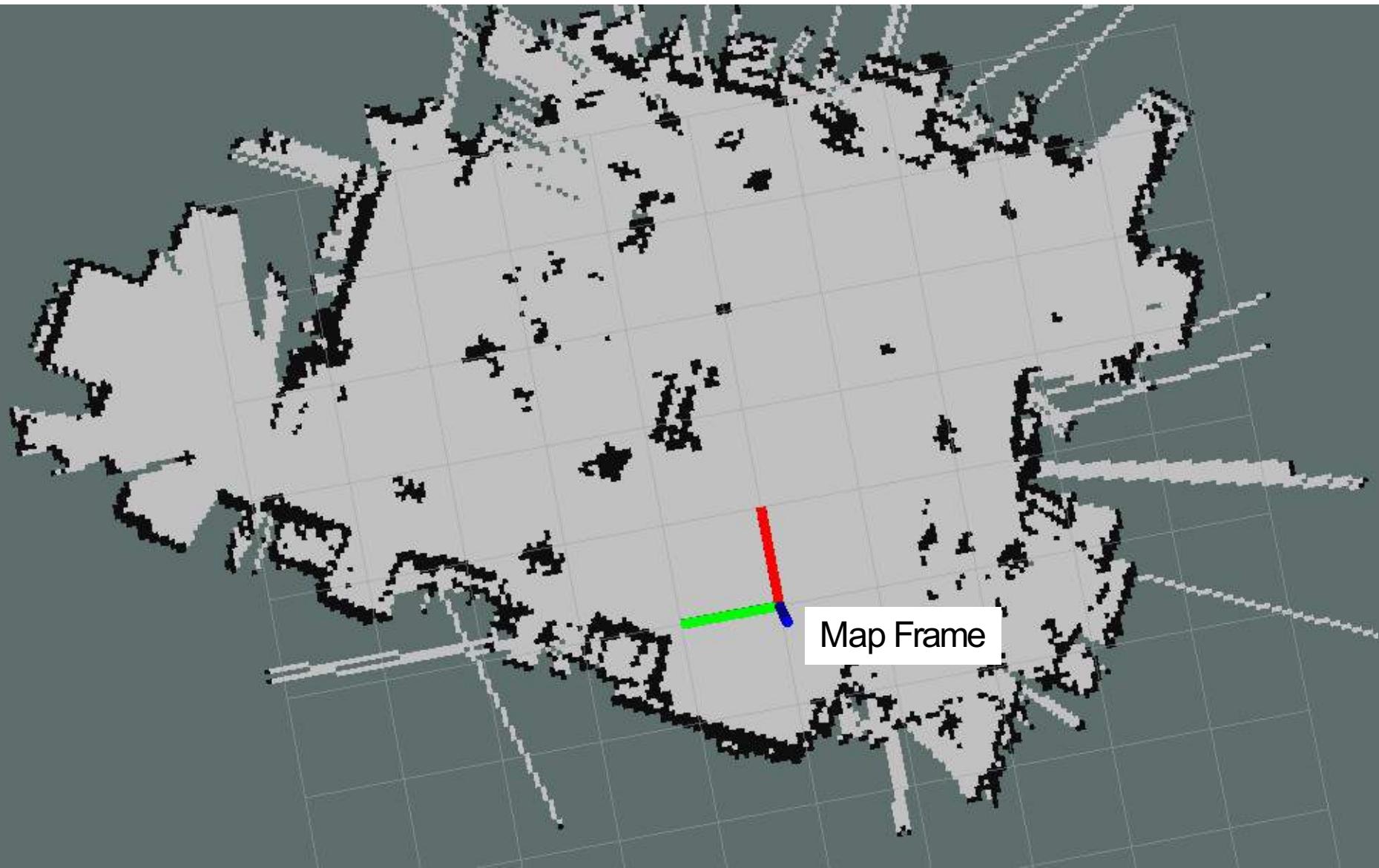


${}^A H_B$ = Homogenous transformations that transforms measurements in Frame B to those in Frame A

$${}^A R_B = \begin{bmatrix} C_\theta & -S_\theta & 0 \\ S_\theta & C_\theta & 0 \\ 0 & 0 & 1 \end{bmatrix}$$

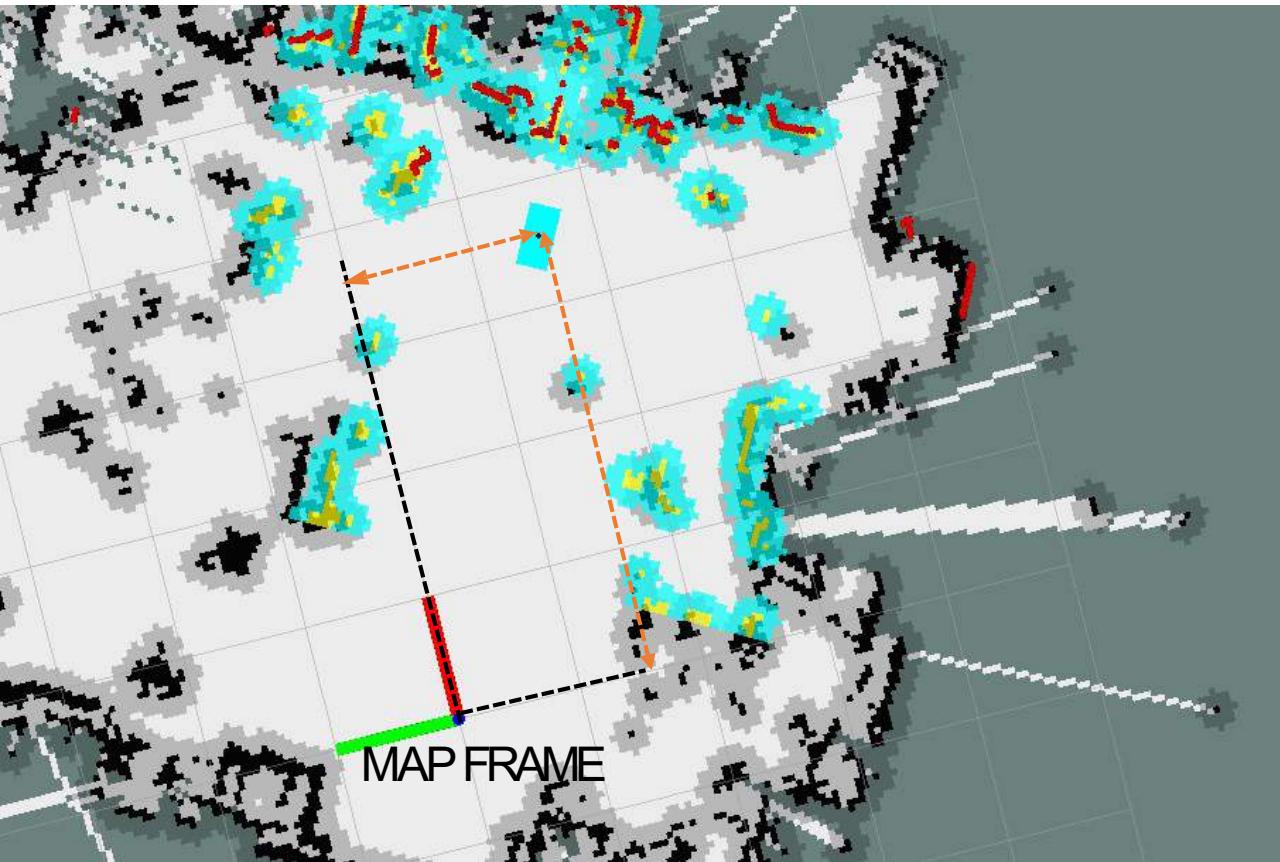
$${}^A H_B = \begin{bmatrix} {}^A R_B & {}^A d_B \\ 0 & 1 \end{bmatrix}$$

Map frame



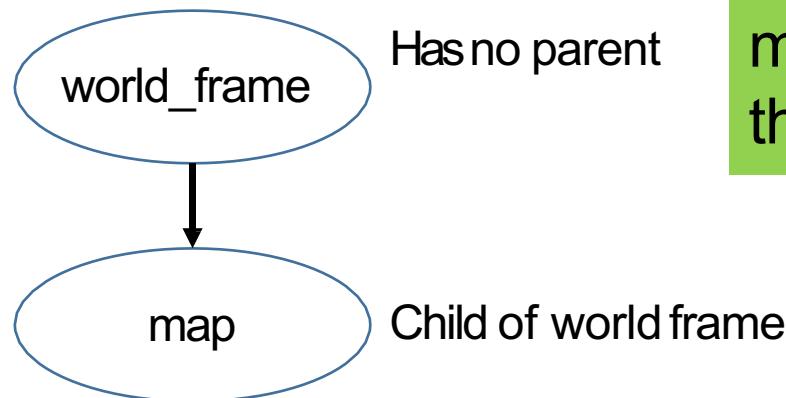
Map frame: Importance

- Position with respect to map



Map Frame: ROS

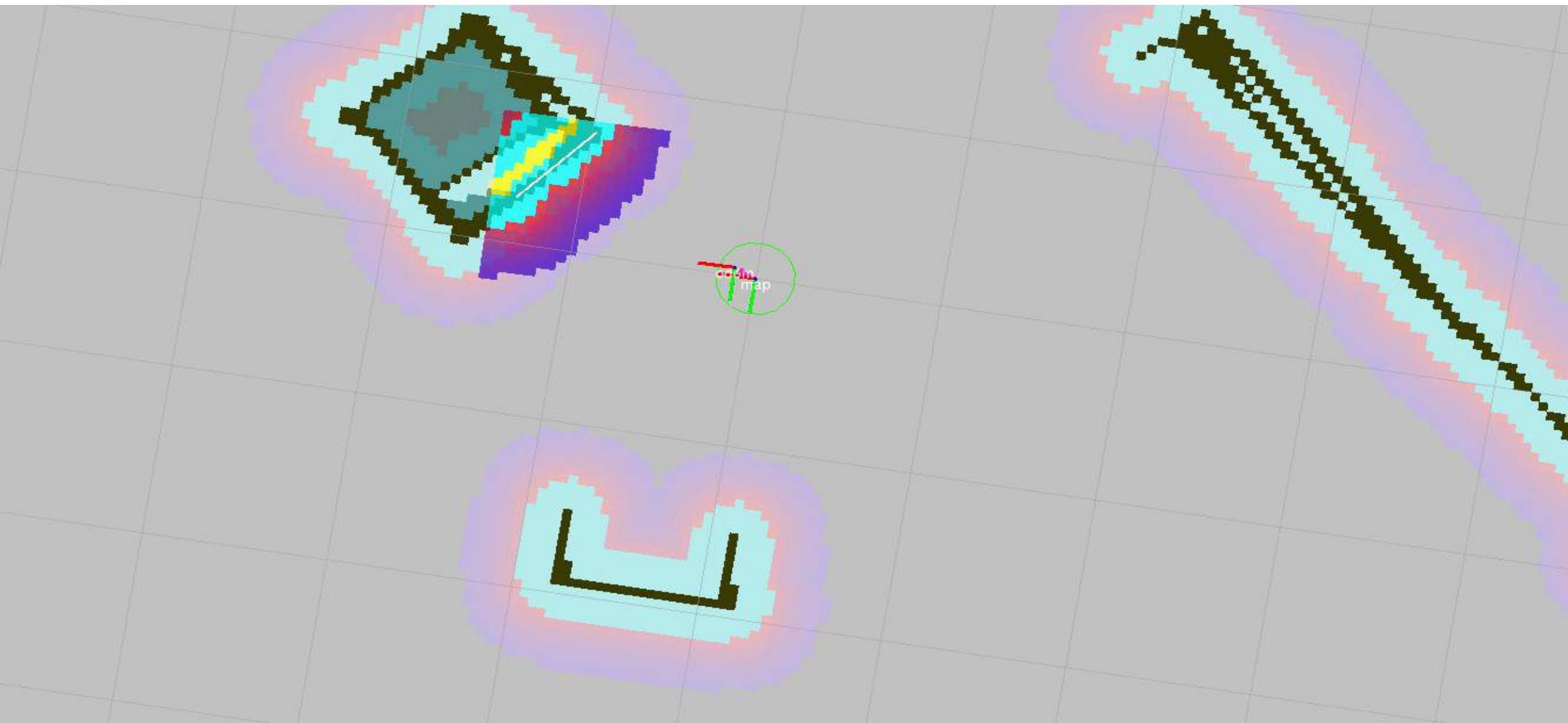
- The `tf` package – tracks multiple 3D coordinate frames - maintains a tree structure b/w frames – **access relationship b/w any 2 frames at any point of time**
- ROSREP(ROSEnhancement Proposals) 105 describes the various frames involved
- Normal hierarchy



A tf tree is a structure that maintains relations between the linked frames.

Note:
Tf = transformer class

Odom Frame



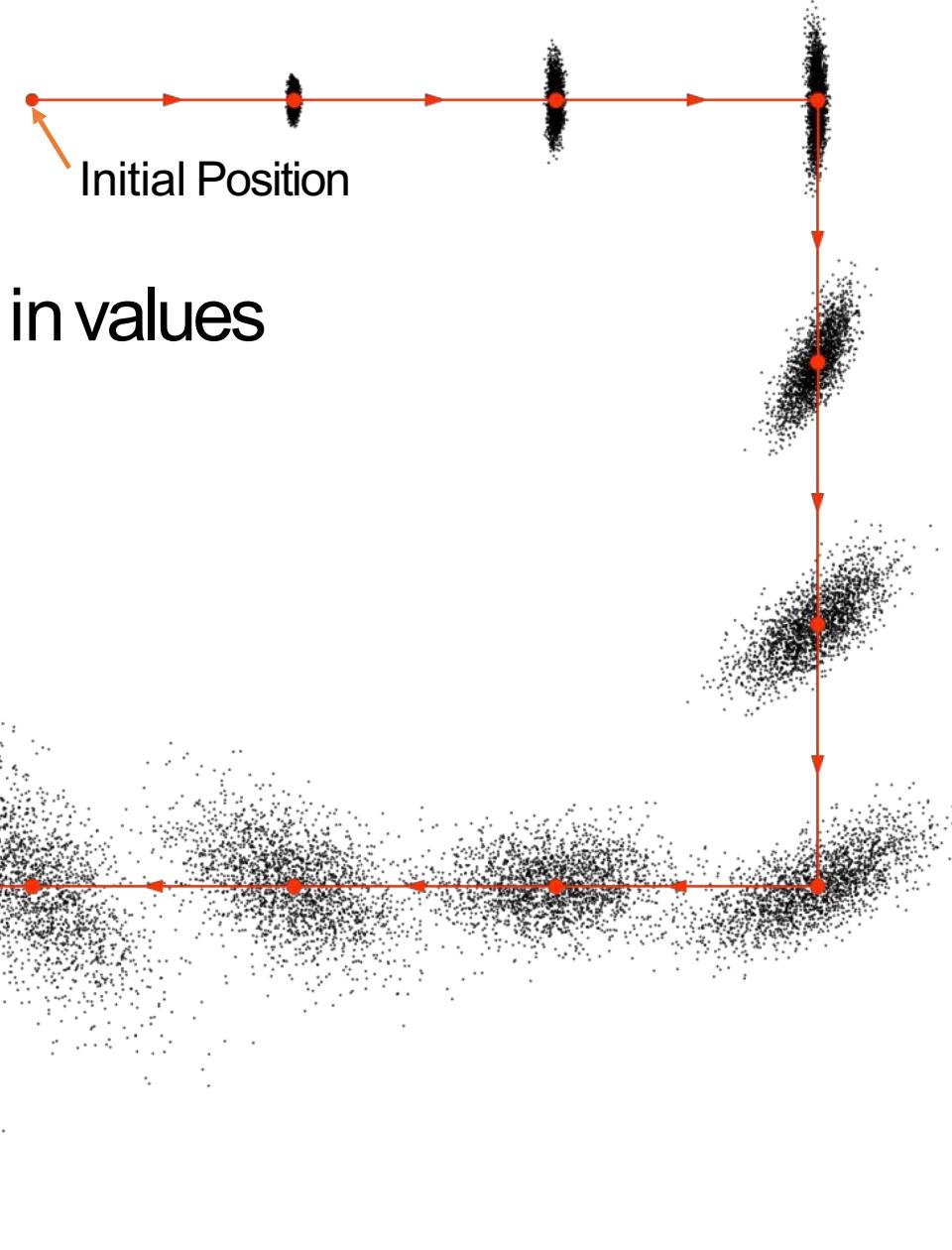
Odom Frame: Calculation

- Difference in count of ticks of wheels – orientation
- Integrating the commanded velocities/accelerations
- Integrating values from IMU
- Scan Matching

Odom Frame: Uncertainty

- Error can accumulate – leading to a drift in values
- Incorrect diameter used?
- Slippage?
- Dead Reckoning

Notice how the uncertainty increases

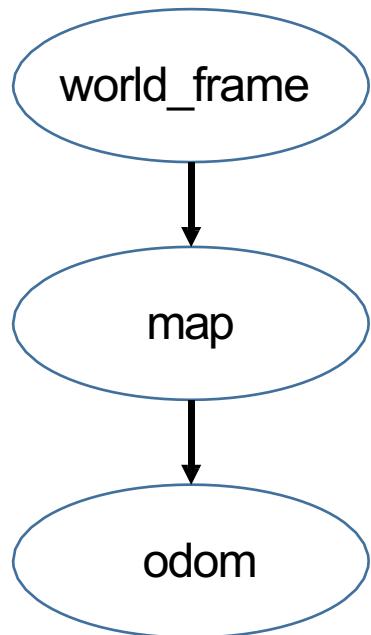


Odom Frame: Properties

- Continuous – actual data from actuators/motors
- Evolves in a smooth manner, without discrete jumps
- Short term ; accurate local reference

Odom Frame: ROS

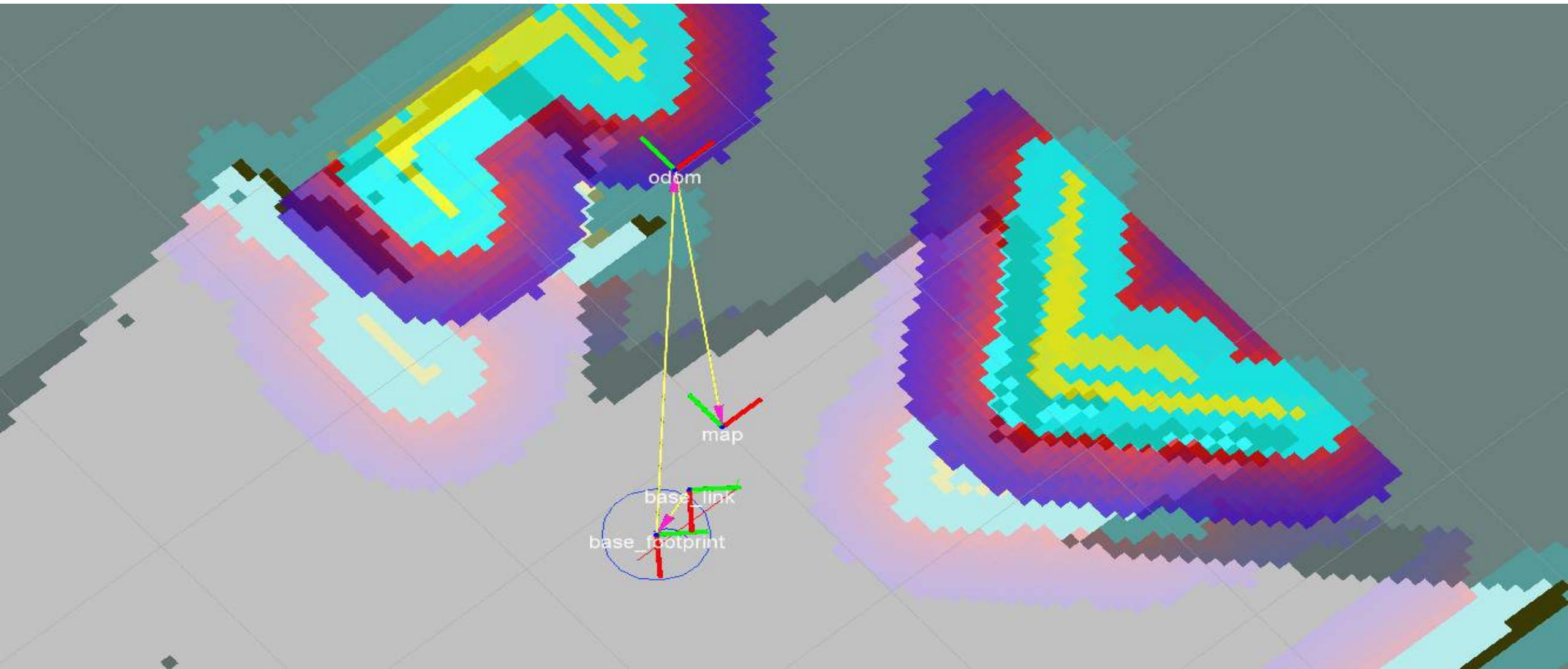
- General ROS frame hierarchy



Tf tree

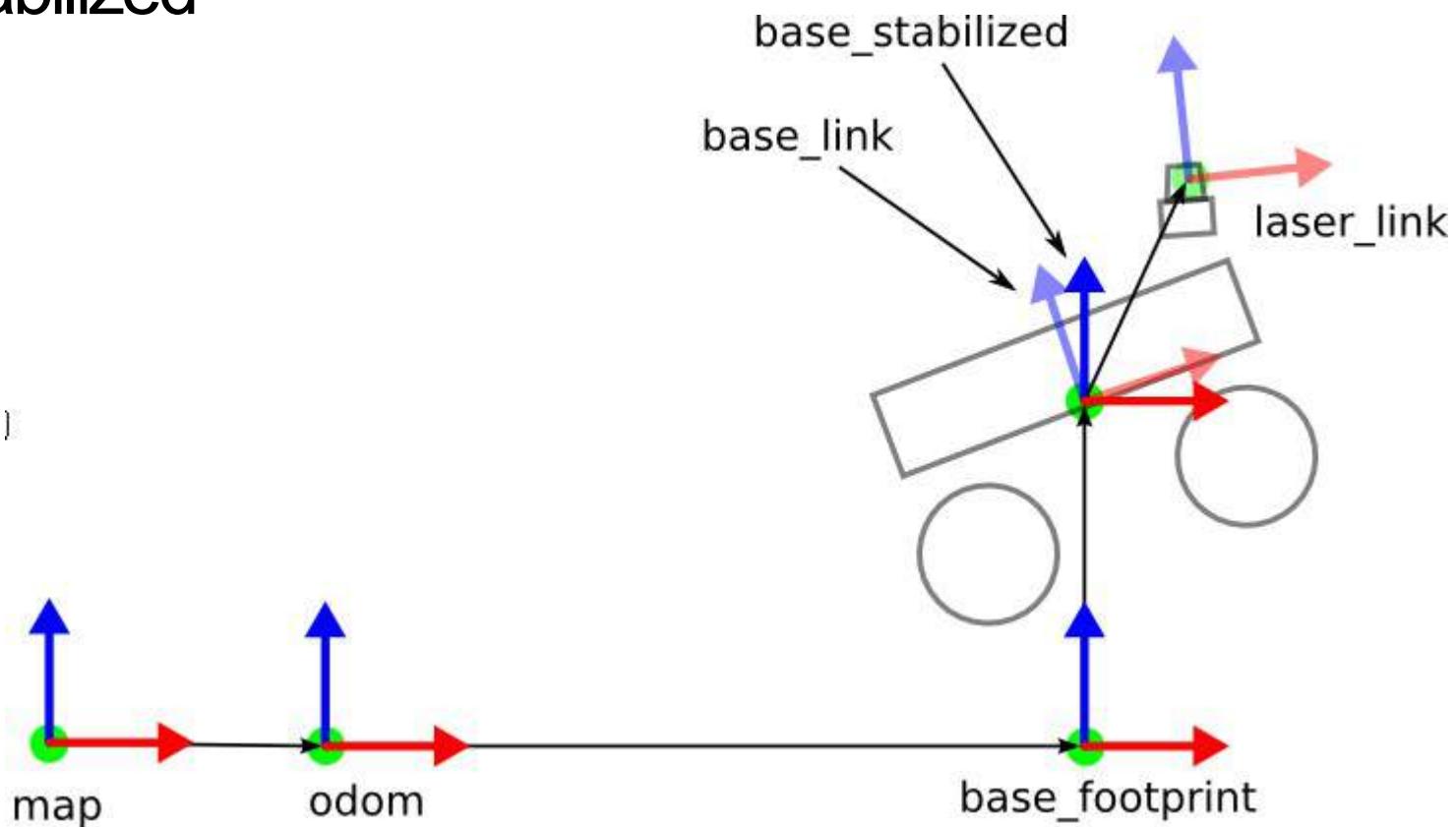
Note that if the frame is connected in the tf tree, we can obtain a representation of that frame with any other frame in the tree

Base_link and fixed frames attached to the robot



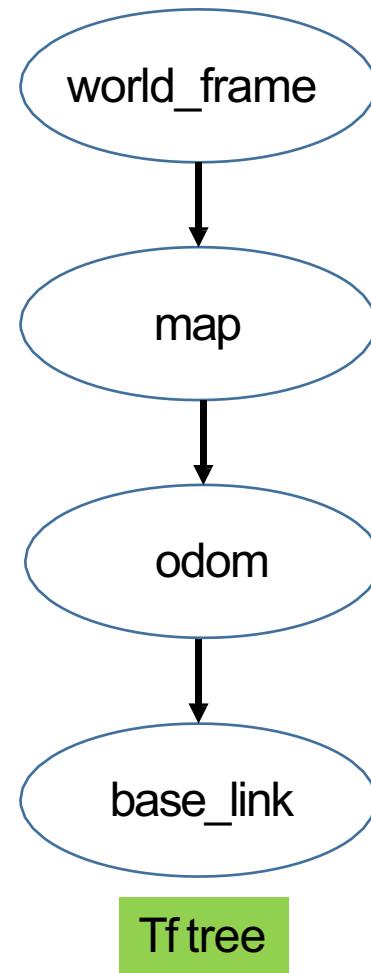
Base link: What is it

- Attached to the robot itself – `base_footprint`; `base_link`; `base_stabilized`



Base_link Frame: ROS

- General ROS frame hierarchy



Base link: Properties

- Odom -> base link transform provided by Odometry source
- Map -> base_link transform provided by localization component

ROS.W.T.F

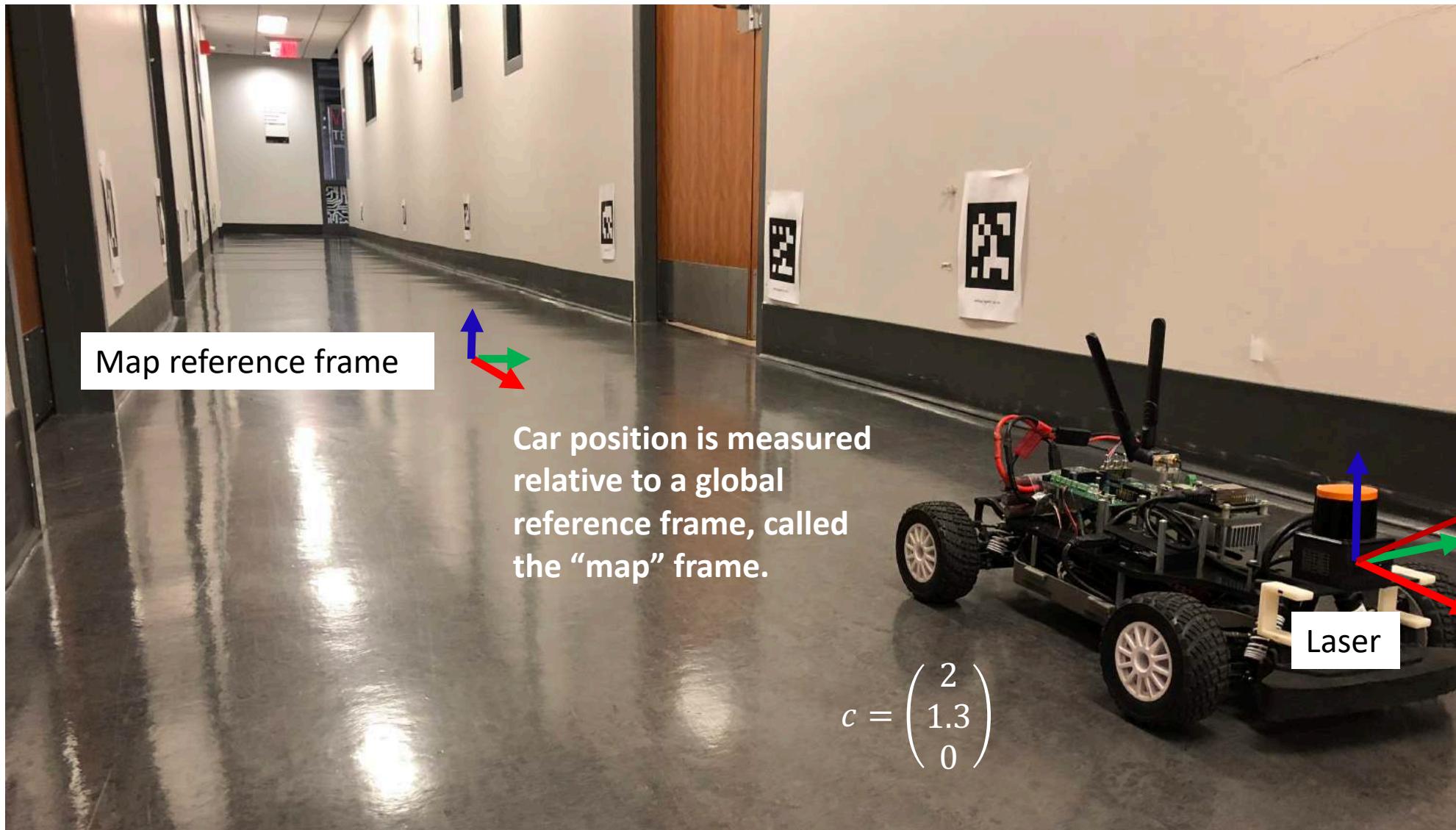
- Host of tf debugging tools provided by ROS
- ROS tf tutorial for further details

```
$ rosrun tf view_frames
```

```
$ rosrun tf view_monitor
```

```
$ rosytic
```

Why do we have multiple frames?

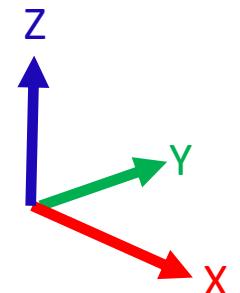
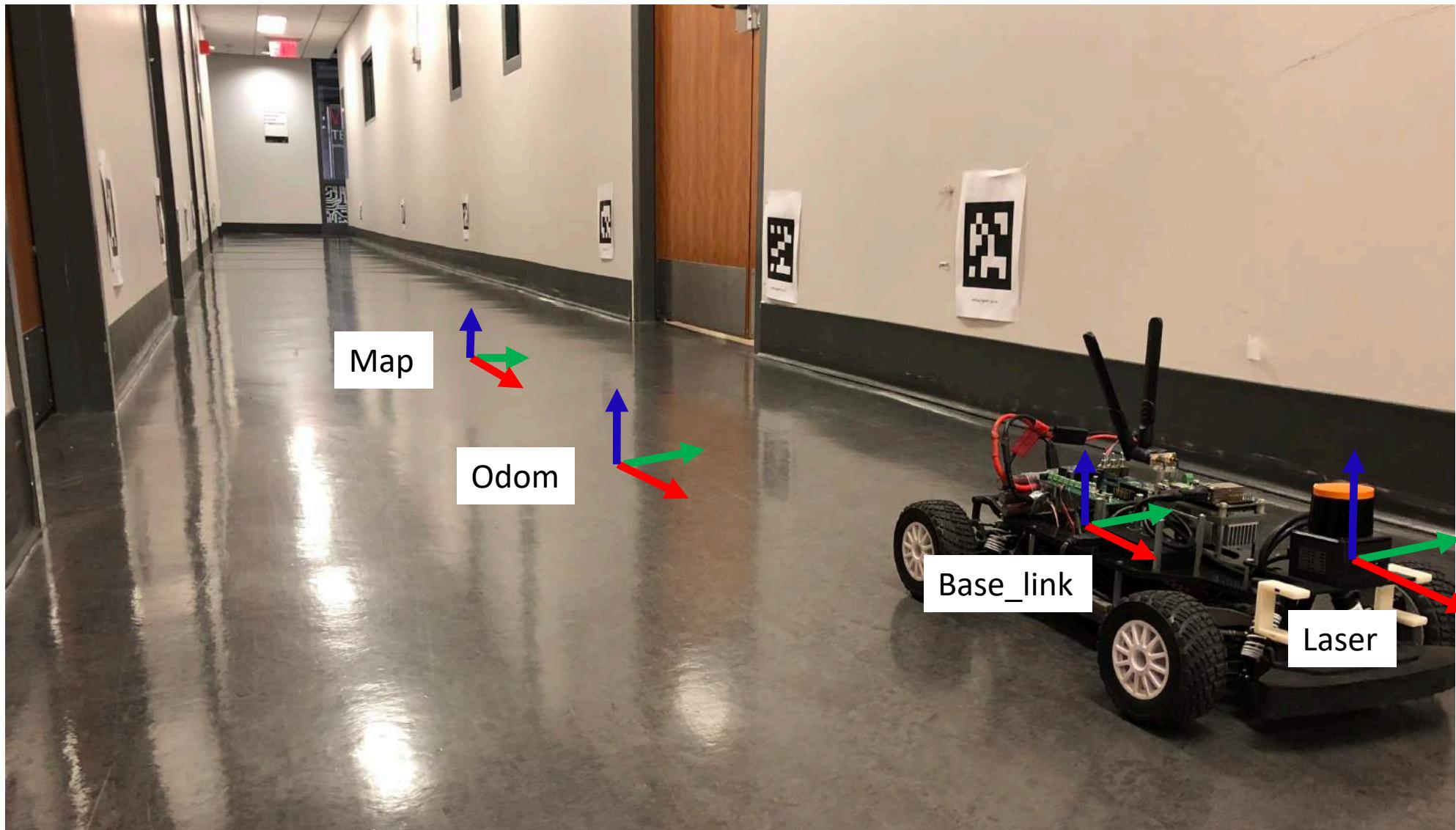


Lidar measurements are relative to the LiDAR itself, i.e., in the laser reference frame. (After all, LiDAR doesn't know where the car is)

$$o = \begin{pmatrix} 2 \\ 3 \\ 2 \end{pmatrix}$$

What other frames might be useful?

Other frames we will use

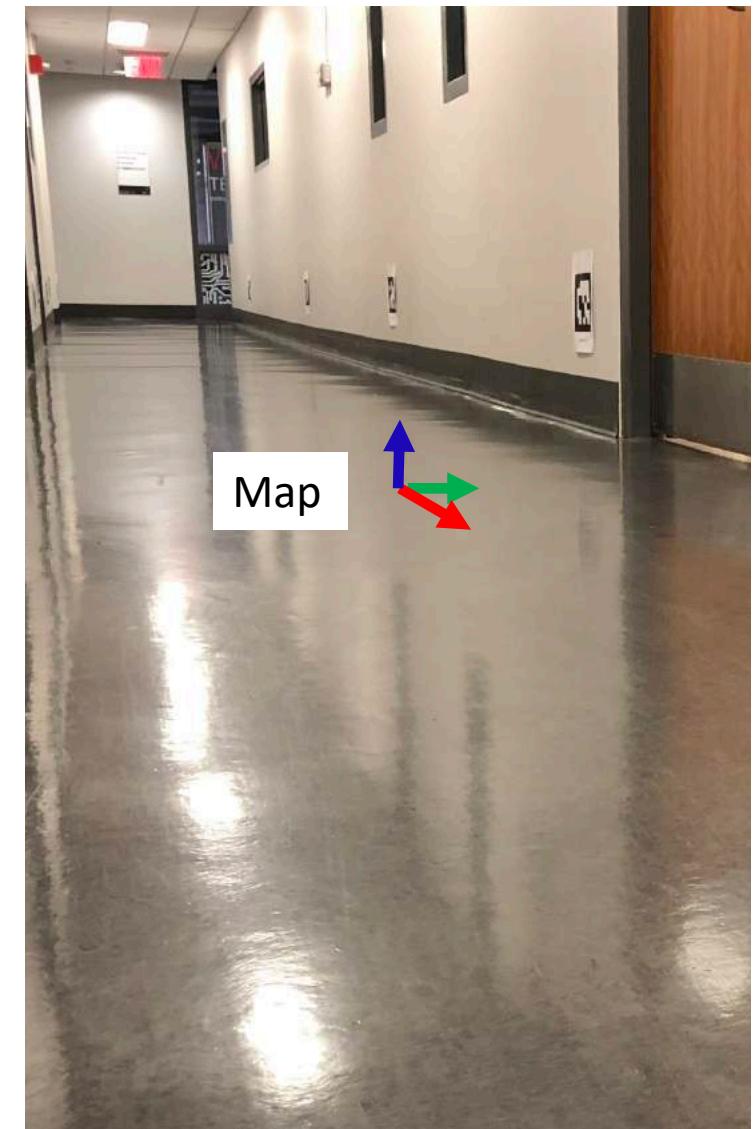
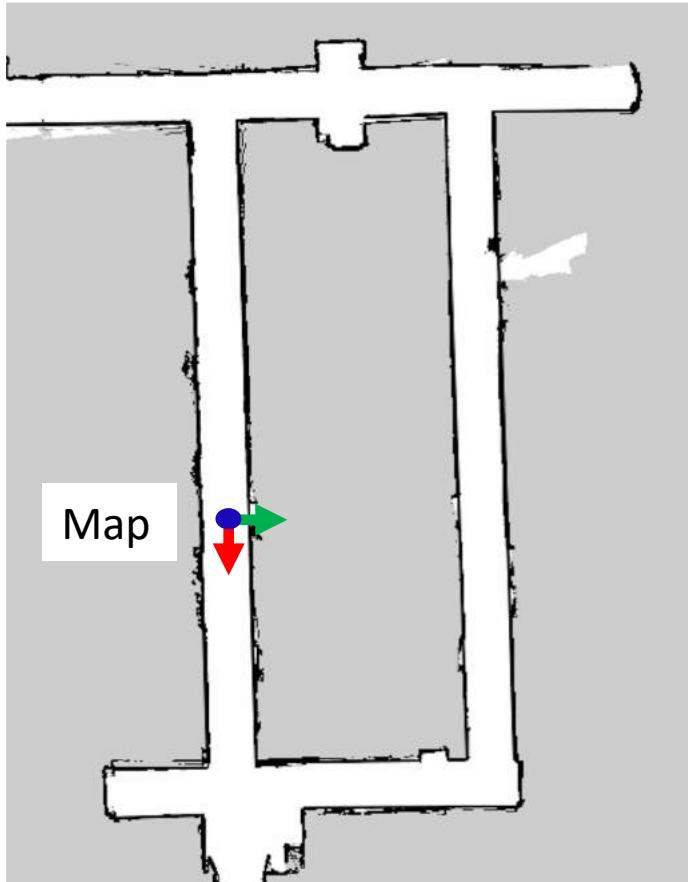


Memory trick:
RGB \rightarrow XYZ

* ROS convention is having positive x direction in front of the link and positive y direction to left of the link. [REP 103]

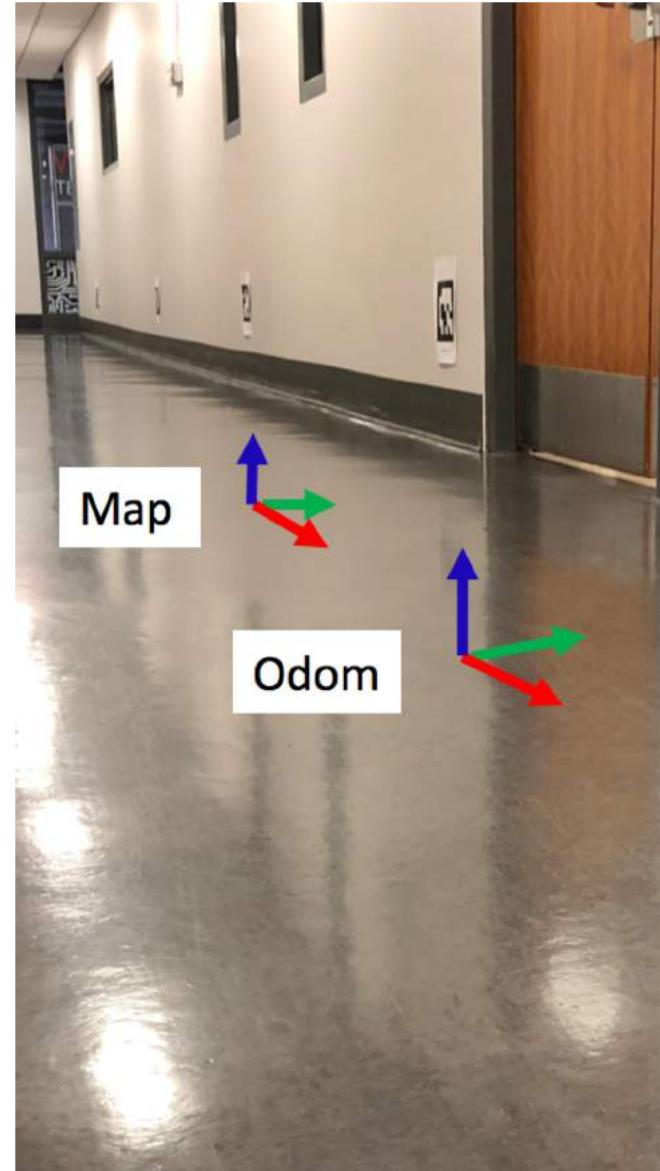
Map Frame

- Map frame origin is set arbitrarily, meaning we can choose it.



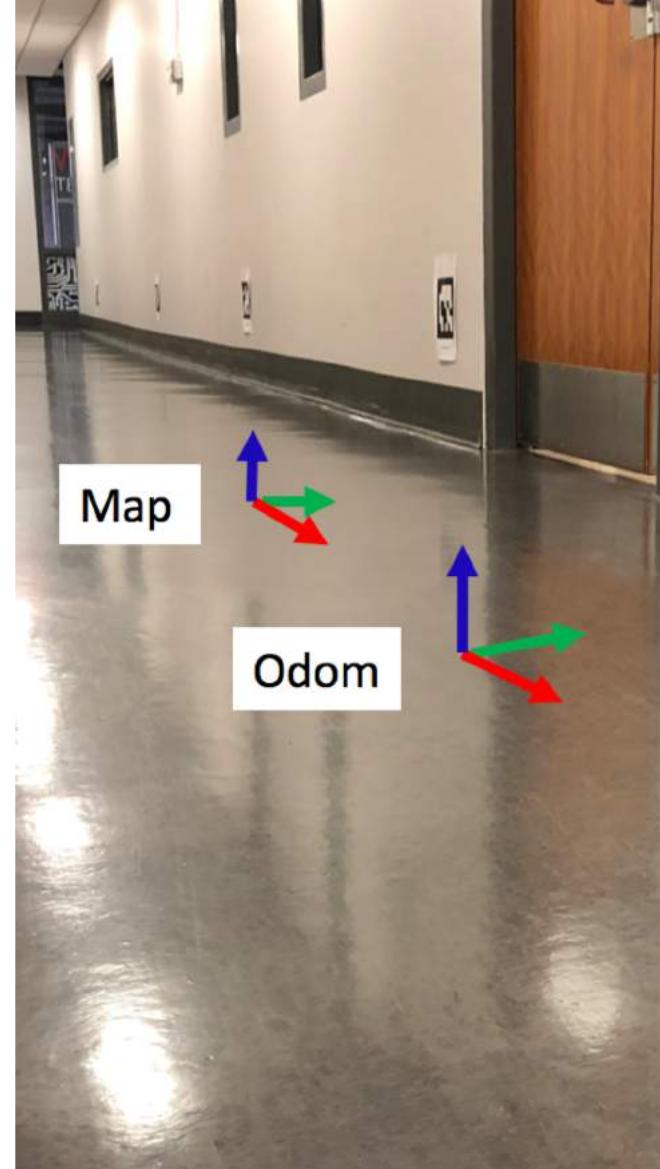
Odom Frame

- Odom frame originates where the car starts at. In this case the car started a meter in front of the map origin. Hence map \rightarrow odom transform is 1m in x direction.
- Odom frame stays fixed – it does not move with the robot.



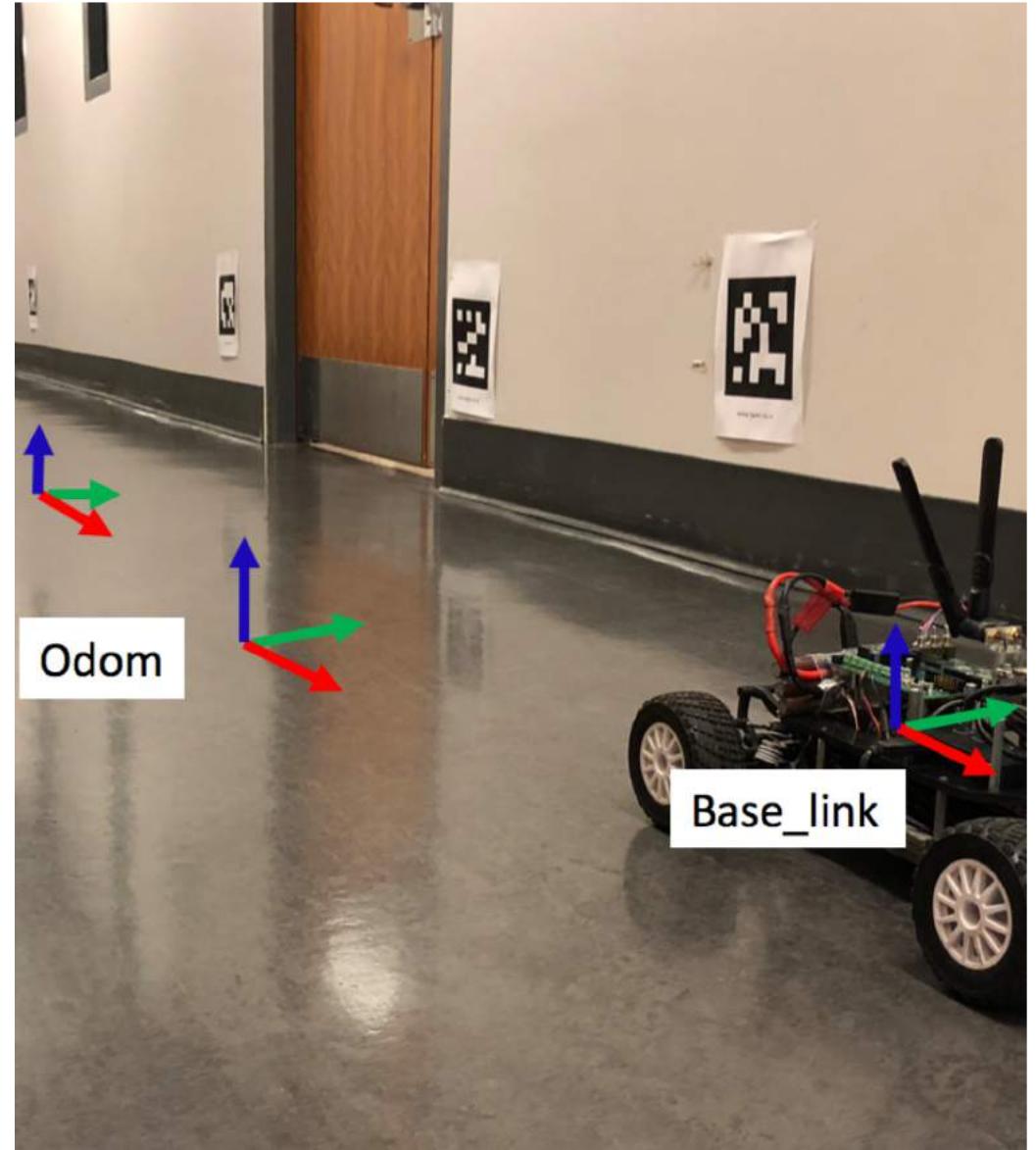
Burdened by history

- *Historically*, localization is done relative to map frame.
- Terminology: Localization = fusing multiple sources of location information, including odometry, into one best estimate
- Pose of a robot in map frame can have jumps, meaning discontinuous, because the best estimate (e.g., provided by an Extended Kalman Filter) can jump

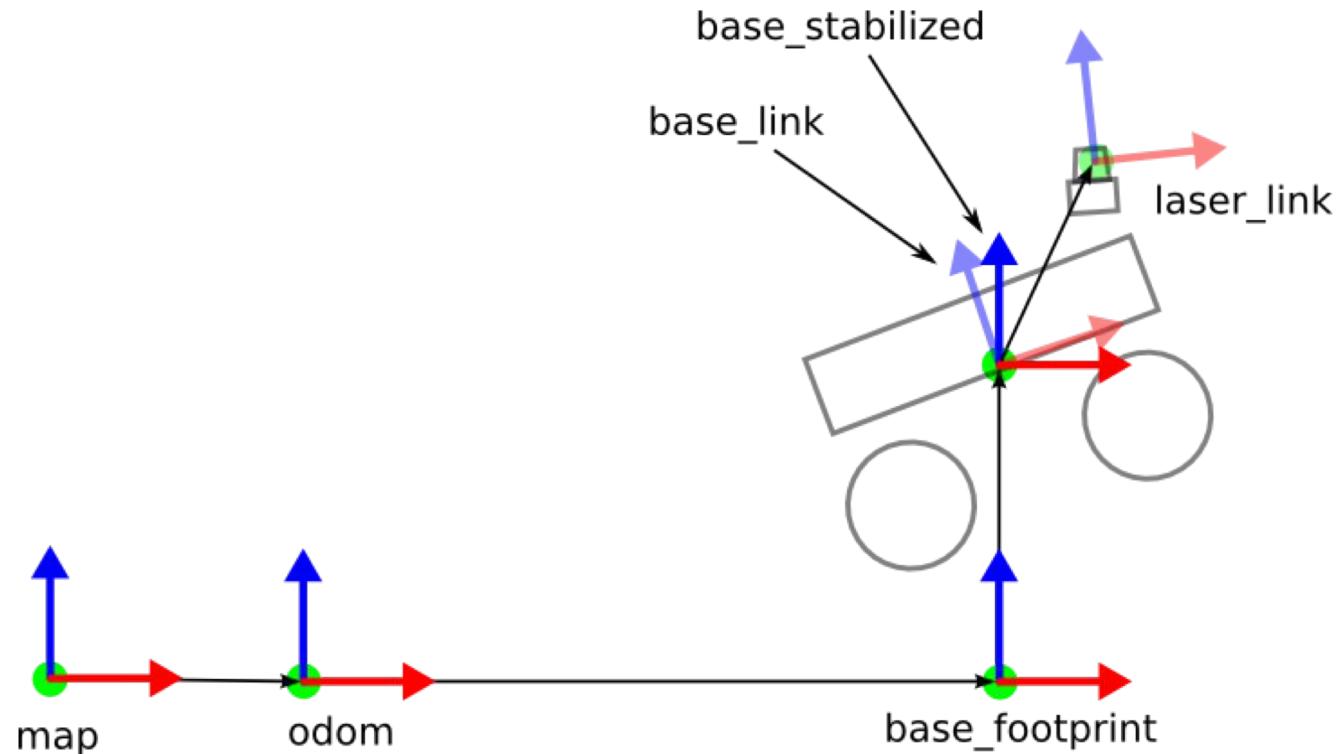


Base_link Frame

- Defined as the center of the car's rear axle
- Base_link frame moves with the car (it is not fixed)
- You really control where to place the base_link on the car. Just be consistent, and be aware that algorithms you re-use have their assumptions (usually, center of car's rear axle).



All the single frames, all the single frames



You might also see:
base_stabilized (no roll or pitch) and base_footprint.
(E.g. these are used by hector_slam).

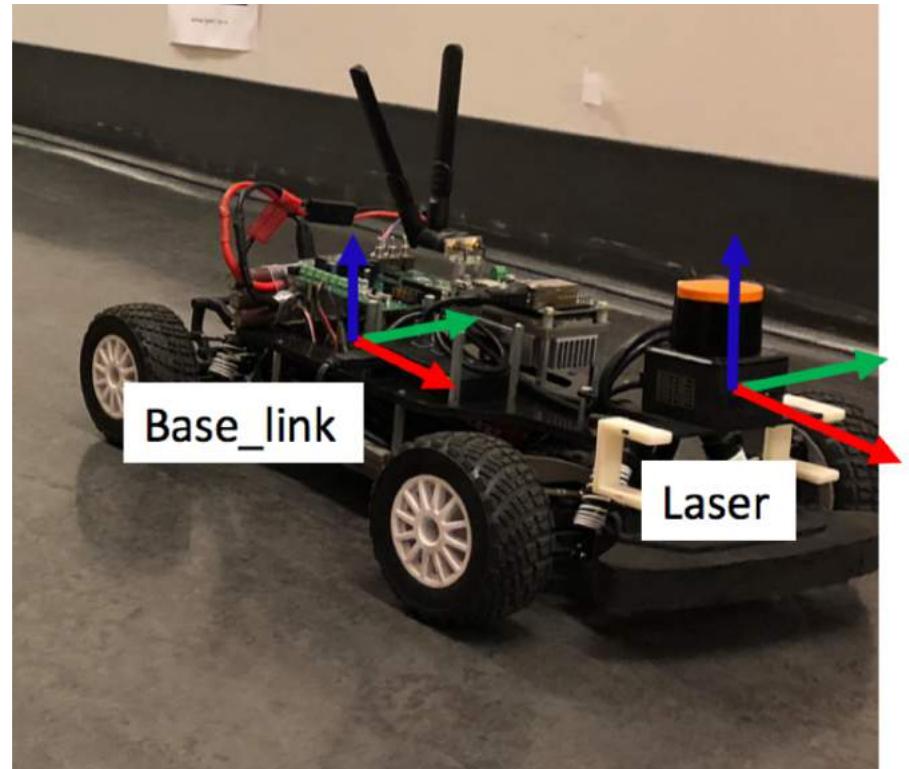
If we assume a flat world for our car, we only need **map**, **odom**, **base_link**, and **laser** (no motion in Z direction)

Why do we need to transform between frames?

- Data is usually provided in the most convenient frame to the data source (e.g. laser scans).
- If an obstacle is detected in the *base_link*, we want to know where it is in the world, i.e. in *map*.
- When we do laser scanning, we need to know the transformation between the lidar position (*laser*) and the *base_link* of the car.
- If we had two disconnected maps, we might want to know their location with respect to each other within a global world frame.

Static transform

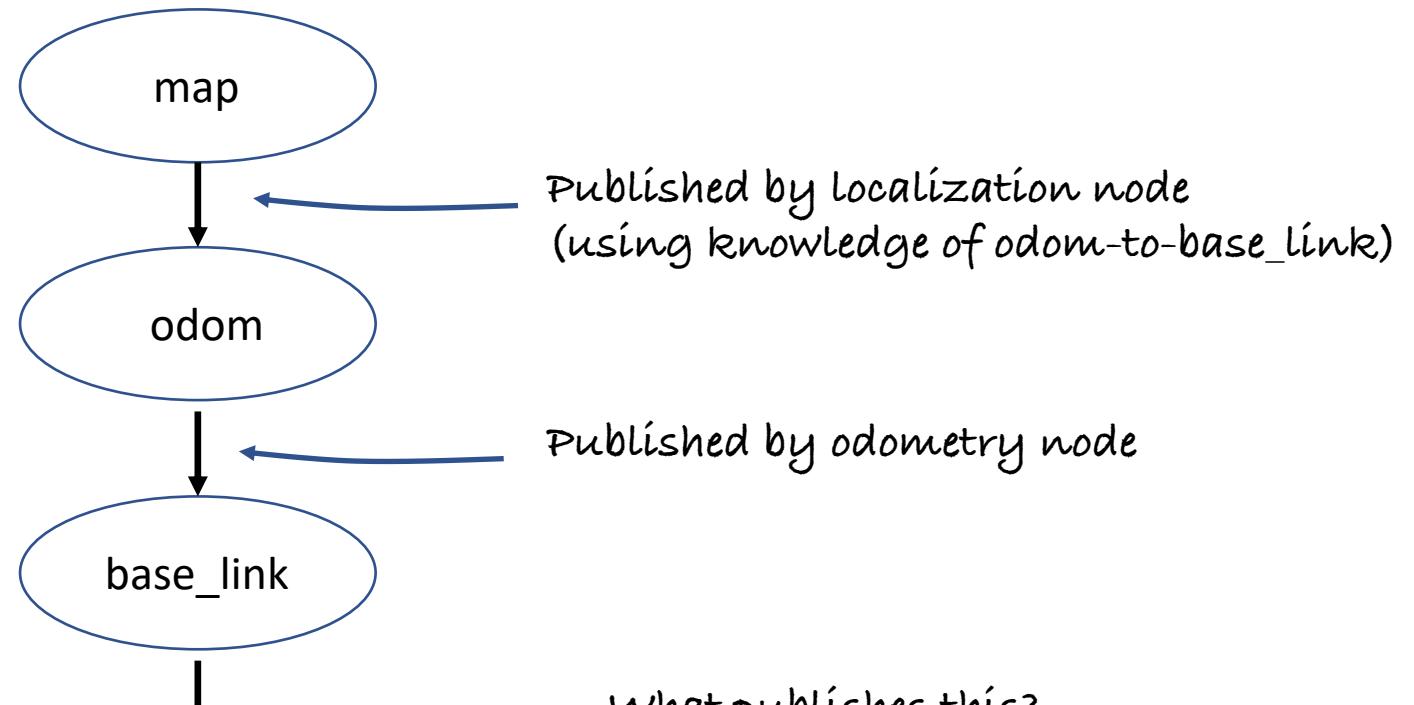
- There exists a static transform between laser and base_link (why?)
- What are the translation and rotation of laser relative to base_link?



TF Tree

- The TF tree in ROS gives us all the frames and their transforms.
- We can visualize the TF Tree by running

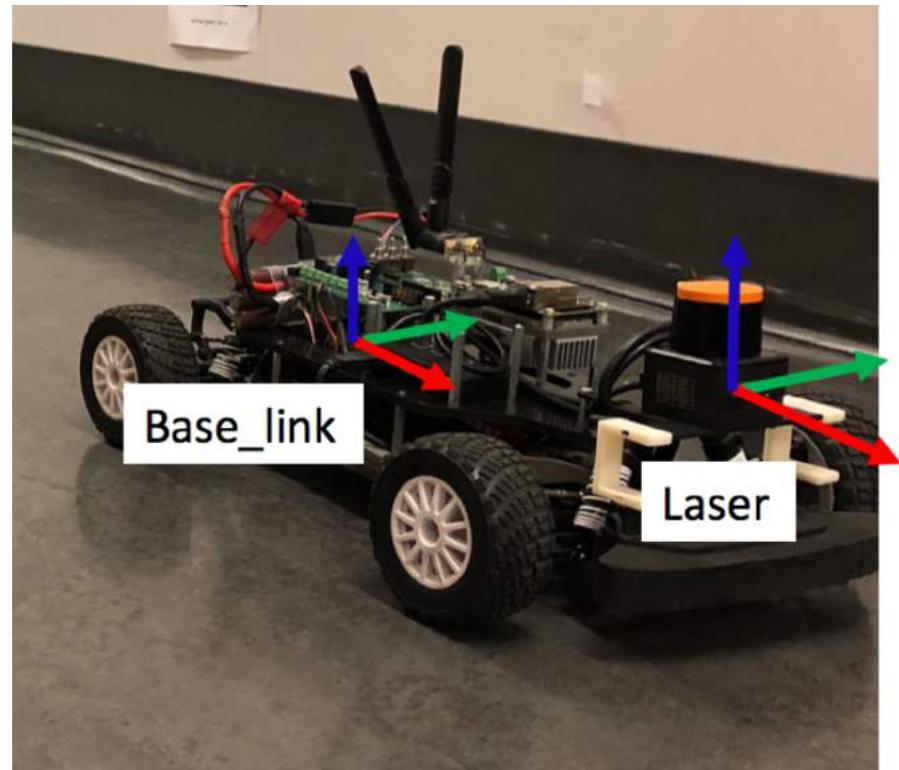
```
>> rosrun rqt_tf_tree rqt_tf_tree
```
- If a localization package doesn't work, check if the ROS TF tree is connected.
- If a frame is connected in the tf tree, we can transform between it and any other frame in the tree.



Tf tree

Static transform

- There exists a static transform between laser and base_link (why?)
- Here, relative to base_link, laser has transform of 0.285 in x direction and 0.127 in z direction. No rotation in quaternions.



```
<node pkg="tf2_ros" type="static_transform_publisher" name="base_link_to_laser"  
args="0.285 0.0 0.127 0.0 0.0 0.0 0.0 1.0 /base_link /laser" />
```

```
static_transform_publisher x y z qx qy qz qw frame_id child_frame_id
```

Child_frame relative to frame

ROS Implementation of Static Transform Publisher

```
<node pkg="tf2_ros" type="static_transform_publisher" name="base_link_to_laser"  
args="0.285 0.0 0.127 0.0 0.0 0.0 1.0 /base_link /laser" />
```

static_transform_publisher x y z qx qy qz qw frame_id child_frame_id

- Placing this line above in the launch file creates a static transform between base_link and laser.
- Published on the topic /tf_static
- X offset of 0.285 meters and z offset of 0.127
- No rotation in quaternions (qx, qy, qz, and qw)
- http://wiki.ros.org/tf2_ros