Estimating HRF and covariance structure

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Estimating HRF and amplitudes

- Use one block at a time
- Code the twelve stimuli as 1-12, the "null" signal as 13, and the 6 "calibration" signals as 14-19
- Transform stimuli assignments to a matrix S, dimension of S is $T \times K$, T is the time of time points, K the number of stimuli types

Estimating HRF and amplitudes

Transform estimated or assumed HRF $h = (h_1, ..., h_L)$ to matrix H(h). Dimension of H(h) is $T \times T$

$$h = \begin{bmatrix} h_1 \\ h_2 \\ h_3 \\ h_4 \\ h_5 \\ \vdots \end{bmatrix} \rightarrow H(h) = \begin{bmatrix} h_1 & 0 & 0 & \cdots \\ h_2 & h_1 & 0 & \cdots \\ h_3 & h_2 & h_1 & \cdots \\ h_4 & h_3 & h_2 & \cdots \\ h_5 & h_4 & h_3 & \cdots \\ \vdots & \vdots & \vdots & \vdots \end{bmatrix}$$

Estimating amplitudes

Estimate the stimuli-specific amplitudes $\alpha = (\alpha_1, \dots, \alpha_K)$ by fitting the model

Estimating HRF

Suppose instead that α is known and h is unknown. Then let $t = S\alpha = (t_1, t_2, ...)$ and define

$$A(S\alpha) = \begin{bmatrix} t_1 & 0 & 0 & \cdots \\ t_2 & t_1 & 0 & \cdots \\ t_3 & t_2 & t_1 & \cdots \\ t_4 & t_3 & t_2 & \cdots \\ t_5 & t_4 & t_3 & \cdots \\ \vdots & \vdots & \vdots & \vdots \end{bmatrix}$$

Dimension of $A(S\alpha)$ is $T \times L$, where L is duration of HRF. Then fit

$$y \sim A(S\alpha)h + \text{const}$$