

1) Aproximación Bessel

$$T(j\omega) = |T| e^{j\phi} = 1 \cdot e^{-j\omega t_0} = e^{-\frac{j\omega}{1/t_0}} = e^{-j\omega} \Big|_{\omega=\frac{s}{j}} = e^{-s}$$

\uparrow
 $1/t_0 = 1$

$$T(s) = e^{-s} = \frac{1}{\sinh(s) + \cosh(s)} = \frac{1/\sinh(s)}{1 + \coth(s)} \Rightarrow \coth(s) = \frac{\cosh(s)}{\sinh(s)} //$$

$$\left. \begin{aligned} \cosh(s) &= 1 + \frac{s^2}{2!} + \frac{s^4}{4!} + \frac{s^6}{6!} + \dots \\ \sinh(s) &= s + \frac{s^3}{3!} + \frac{s^5}{5!} + \frac{s^7}{7!} + \dots \end{aligned} \right\} \coth(s) = \frac{1}{s} + \frac{\frac{3}{5} + \frac{1}{\frac{5}{s} + \frac{1}{\frac{7}{s} + \dots}}}{\frac{3}{5} + \frac{1}{\frac{5}{s} + \frac{1}{\frac{7}{s} + \dots}}}$$

Método de storch: $T(s) = \frac{B_n(0)}{B_n(s)}$

Para n=2

$$\coth(s) = \frac{1}{s} + \frac{3}{5} = \frac{3+s^2}{3s} \Rightarrow B_2(s) = s^2 + 3s + 3 //$$

$$T_2(s) = \frac{B_2(0)}{B_2(s)} \Rightarrow T_2(s) = \frac{3}{s^2 + 3s + 3}$$

Para n=3

$$\coth(s) = \frac{1}{s} + \frac{1}{\frac{3}{5} + \frac{s}{5}} = \frac{6s^2 + 15}{s^3 + 15s} \Rightarrow B_3(s) = s^3 + 6s^2 + 15s + 15 //$$

$$T_3(s) = \frac{B_3(0)}{B_3(s)} \Rightarrow T_3(s) = \frac{15}{s^3 + 6s^2 + 15s + 15}$$

Para n=4

$$\coth(s) = \frac{1}{s} + \frac{1}{\frac{3}{5} + \frac{1}{\frac{5}{s} + \frac{1}{\frac{7}{s} + \frac{1}{\frac{9}{s} + \dots}}}} = \frac{s^4 + 45s^2 + 105}{105s^3 + 105s} \Rightarrow B_4(s) = s^4 + 105s^3 + 45s^2 + 105s + 105 //$$

$$T_4(s) = \frac{B_4(0)}{B_4(s)} \Rightarrow T_4(s) = \frac{105}{s^4 + 105s^3 + 45s^2 + 105s + 105}$$