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> with (combinat) :
  T := j →  $\frac{1}{j+1} \cdot \text{binomial}(2 \cdot j, j)$  :
  S2 := (i, j) → stirling2(i, j) :
  B2 := (i, j) → binomial(i, j) :
  FF := n → doublefactorial(n) :
  idemp := n → sum  $\left( \text{binomial}(n, 2 \cdot k) \cdot \text{FF}(2 \cdot k - 1), k = 0 \dots \text{floor}\left(\frac{n}{2}\right) \right)$  :

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(1)

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>
> EZ := proc( $a, b$ ) local  $E, p, q, s, E1, E2, E3$ ;
    if ( $a < b$ ) then
         $E := 0$ ;
        for  $p$  from 1 to  $a + 1$  do
            for  $q$  from 1 to  $b + 1$  do
                for  $s$  from 0 to  $\min(p, q)$  do
                     $E := E + S2(a + 1, p) \cdot S2(b + 1, q) \cdot B2(p, s) \cdot B2(q, s) \cdot s!$ ;
                od; od; od;
             $E := T(a) \cdot T(b) \cdot E$ ;
        return( $E$ );
    end if;

    if ( $a = b$ ) then
         $E := 0$ ;
        if  $a = 0$  then
            return(2);
        else
            for  $p$  from 1 to  $a + 1$  do
                for  $q$  from 1 to  $a + 1$  do
                    for  $s$  from 0 to  $\min(p, q)$  do
                         $E := E + S2(a + 1, p) \cdot S2(a + 1, q) \cdot B2(p, s) \cdot B2(q, s) \cdot s!$ ;
                    od; od; od;
                 $E1 := \left( \frac{1}{2} \right) \cdot T(a)^2 \cdot E$  ;

                 $E := 0$ ;
                for  $p$  from 1 to  $a + 1$  do
                    for  $s$  from 0 to  $p$  do

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         $E := E + S2(a + 1, p) \cdot B2(p, s) \cdot idemp(s);$ 
    od; od;
     $E2 := \left( \frac{1}{2} \right) \cdot T(a) \cdot E;$ 

     $E := 0;$ 
    for  $p$  from 1 to  $a + 1$  do
         $E := E + S2(a + 1, p);$ 
    od;
     $E3 := T(a) \cdot E;$ 

    end if;
     $E := E1 + E2 - E3 ;$ 
end if;
return ( $E$ );
end proc:

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> EQNZ := proc( $n$ ) local  $a, E$ ;

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     $E := 0;$ 

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    for  $a$  from 0 to floor( $\frac{n}{2}$ ) do
         $E := E + EZ(a, n - a) ;$ 
    od;
    return( $E$ );
end proc:

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EQNT := proc( $n$ ) local  $a, E$ ;
     $E := 0;$ 
    for  $a$  from 0 to  $n$  do
         $E := E + EQNZ(a);$ 
    od;
    return( $E$ );
end proc;

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EQNT := proc( $n$ )

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    local  $a, E$ ;

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     $E := 0;$  for  $a$  from 0 to  $n$  do  $E := E + EQNZ(a)$  end do; return  $E$ 

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end proc

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(2)

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> for a from 0 to 5 do
  for b from a to 5 do
    printf("%a ", EZ(a, b));
  od;
  printf("\n");
od;
2  5  30  260  2842  36834
9  104  1015  12278  173880
427  8770  115920  1776348
52085  1480290  24354750
11371815  398999160
3716527689

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> for a from 0 to 10 do
  printf("%a ", EQNZ(a));
od;
  printf("\n");
2  5  39  364  4284  57882  888365  15120105  281941490
5698630860  123850391756

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> for a from 0 to 10 do
  printf("%a ", EQNT(a));
od;
  printf("\n");
2  7  46  410  4694  62576  950941  16071046  298012536
5996643396  129847035152

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>

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