

Question1)

Matching trigram =2 { the cat was, under the bed}

Total trigram in the actual sentence: 4

Total trigram in predicted answer=5

precision=> 2 / 5

Recall=> 2/4

Both Correct: 4 marks, single correct 2 marks

Question 2)

$$\text{MRR} = \frac{1}{|Q|} \sum_{i=1}^{|Q|} \frac{1}{\text{rank}_i} \cdot$$

1/50 * sum(1/1 + 1/2 ++ 1 /40)
ans=>> .085

4 marks for correct expression, else 0

Question 3)

Ans:

$$\text{PMI}(X, Y) = \log_2 \frac{P(x, y)}{P(x)P(y)}$$

---- 1mark

$$p_{ij} = \frac{f_{ij}}{\sum_{i=1}^W \sum_{j=1}^C f_{ij}}$$

-----1 mark

P(data)=0.37

P(information)=0.58

P(information, data)=0.32----1 mark

$$\text{pmi}(\text{information}, \text{data}) = \log_2 (.32 / (.37 * .58)) = .58$$

----- 1 mark

Question4)

Column dimension has to be **NLP, IR, Math, Interesting, else -1**

Question5)

★ **SOLUTION:** The Viterbi algorithm predicts that the most likely sequence of states is A, A, A. The relevant computations are:

$$V_1^A = 0.99 \times 0.8 = 0.792$$

$$V_1^B = 0.01 \times 0.1 = 0.001$$

$$V_2^A = 0.2(0.792)(0.99) = 0.156816$$

$$V_2^B = 0.9(0.792)(0.01) = 0.007128$$

$$V_3^A = 0.8(0.156816)(0.99) = 0.1241983$$

$$V_3^B = 0.1(0.007128)(0.99) = 0.000705672$$

Correct state sequence and relevant calculations (6 marks)

In case of wrong state sequence:

- (3 marks) State sequence is partially correct and relevant calculation
- (2 marks or 1 marks) Some calculations are correct.
- (0 marks) in case the sequence is completely wrong or question not attempted.

Question 6.

YES----- 1 mark

$$\begin{aligned}
 P(a,a) &= 0.25 \\
 P(c,c) &= 0.25 \\
 P(b,a) &= 0.125 \\
 P(b,b) &= 0 \\
 P(a,c) &= 0.25 \\
 \text{Total} &= 0.875
 \end{aligned}$$

Remaining bigram prob.

$$\begin{aligned}
 P(a,b) + P(b,c) + P(c,a) + P(c,b) \\
 = 1 - 0.875 = 0.125 \quad \text{--- (i)}
 \end{aligned}$$

$$\begin{aligned}
 P_L(a) &= 0.5 \\
 \Rightarrow P(aa) + P(ab) + P(ac) &= 0.5 \\
 \Rightarrow 0.25 + P(ab) + 0.25 &= 0.5 \\
 \Rightarrow P(ab) &= 0 \quad \text{--- (ii)}
 \end{aligned}$$

$$\begin{aligned}
 P_R(b) &= 0.125 \\
 \Rightarrow P(ab) + P(bb) + P(cb) &= 0.125 \\
 \Rightarrow 0 + 0 + P(cb) &= 0.125 \\
 \Rightarrow P(cb) &= 0.125 \quad \text{--- (iii)}
 \end{aligned}$$

Substituting (ii) & (iii) in (i), we get

$$P(b,c) + P(c,a) = 0 \Rightarrow P(b,c) = P(c,a) = 0$$

Since prob. is always positive

$$\begin{aligned}
 \text{Now, } P(b|c) &= \frac{P(c,b)}{P_L(c)} = \frac{0.125}{P(c,a) + P(c,b) + P(c,c)} \\
 &= \frac{0.125}{0 + 0.125 + 0.25} = \underline{\underline{1/3}}
 \end{aligned}$$

1 mark for eq I and II

1 mark for $p(b,c)=p(c,a)=0$

1 mark for final ans = $1/3$

Question7)

Choice of Model -> Choosing Model B over Model A (+2 marks) {calculations were unnecessary as was indicated in the question paper}

Reasons why - (These were the points that we were looking for. Explanations are awarded marks in accordance with these ideas.)

- Occam's Razor, choosing the simplest model available.

- An unbiased model is a model with higher entropy (**randomness**). We want to reduce the bias in model.

Students who have mentioned these key points in their arguments are awarded **2 marks**.

Some common errors:

- Entropy for MEMM has little relation with the number of features (0.5 marks awarded)
- Entropy of MEMM has effect on the predictions of regressor for sure, but this is not the reason for maximum entropy in a model.

Question 12)

1)

$S \rightarrow$

$X \rightarrow aY \mid bY \mid \epsilon$

$Y \rightarrow X \mid c$

The variable X is nullable; and so therefore is Y .

After elimination of ϵ , we obtain:

$S \rightarrow aXbX \mid abX \mid aXb \mid ab$

$X \rightarrow aY \mid bY \mid a \mid b$

$Y \rightarrow X \mid c$

After elimination of the unit production $Y \rightarrow X$,
we obtain:

$S \rightarrow aXbX \mid abX \mid aXb \mid ab$

$X \rightarrow aY \mid bY \mid a \mid b$

$Y \rightarrow aY \mid bY \mid a \mid b \mid c$

Now, break up the RHSs of S; and replace a by A,
b by B and c by C wherever not units:

$S \rightarrow EF \mid AF \mid EB \mid ABP$

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$X \rightarrow AY \mid BY \mid a \mid b$

$Y \rightarrow AY \mid BY \mid a \mid b \mid c$

$E \rightarrow AX$

$F \rightarrow BX$

$A \rightarrow a$
 $B \rightarrow b$
 $C \rightarrow c$

ii)

$S \rightarrow ASA \mid aB$
 $A \rightarrow B \mid S$
 $B \rightarrow b \mid \epsilon$ (epsilon)

After adding the new start symbol S_0 , we get the following grammar.

(G1)

\Rightarrow

S
 $S \rightarrow ASA \mid aB$
 $A \rightarrow B \mid S$
 $B \rightarrow b \mid$

Removing nullable variables In the above grammar, both A and B are the nullable variables. We have the rule $S \rightarrow ASA$. Since A is nullable, we need to add $S \rightarrow SA$ and $S \rightarrow AS$ and $S \rightarrow S$ (which is of course a silly rule, so we will not waste our time putting it in). We also have $S \rightarrow aB$. Since B is nullable, we need to add $S \rightarrow a$. The resulting grammar is the following.

(G2)

$\Rightarrow S_0 \rightarrow S$
 $S \rightarrow ASA \mid aB \mid a \mid SA \mid AS$
 $A \rightarrow B \mid S$
 $B \rightarrow b$

Removing unit rules. The unit pairs for this grammar are $\{A \rightarrow B, A \rightarrow S, S_0 \rightarrow S\}$. We need to copy the productions for S up to S_0 , copying the productions for S down to A , and copying the production $B \rightarrow b$ to $A \rightarrow b$.

(G3)

$\Rightarrow S_0 \rightarrow ASA \mid aB \mid a \mid SA \mid AS$
 $S \rightarrow ASA \mid aB \mid a \mid SA \mid AS$
 $A \rightarrow b \mid ASA \mid aB \mid a \mid SA \mid AS$
 $B \rightarrow b$

Final restructuring. Now, we can directly patch any places where our grammar rules have the wrong form for CNF. First, if the rule has at least two symbols on its righthand side but some of them are terminals, we introduce new variables which expand into these terminals. For our example, the offending rules are $S_0 \rightarrow aB$, $S \rightarrow aB$, and $A \rightarrow aB$. We can rid these by replacing the a 's with a new variable U , and adding a rule $U \rightarrow a$.

(G4)

$\Rightarrow S_0 \rightarrow ASA \mid UB \mid a \mid SA \mid AS$

$S \rightarrow ASA \mid UB \mid a \mid SA \mid AS$

$A \rightarrow b \mid ASA \mid UB \mid a \mid SA \mid AS$

$B \rightarrow b$

$U \rightarrow a$