

# Design and Analysis of Algorithms Lab

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- 1 Use Selection Sort and Insertion Sort techniques to sort a set of student records by considering a specified field (Hall Ticket Number, Name, or Team Number).
- 2 Use Selection Sort and Insertion Sort techniques to sort a set of student records by considering all the fields in a specific order (Team Number, Hall Ticket Number, and Name).

Note:

- ▶ Input should be read from a file **DAA Lab\_input1.txt**
- ▶ Output should be written into a file **DAA Lab\_output1.txt**

- 1 Use Merge Sort and Quick Sort techniques to sort a set of student records by considering a specified field (Hall Ticket Number, Name, or Team Number).
- 2 Use Merge Sort and Quick Sort techniques to sort a set of student records by considering all the fields in a specific order (Team Number, Hall Ticket Number, and Name).

Note:

- ▶ Input should be read from a file **DAA Lab\_input1.txt**
- ▶ Output should be written into a file **DAA Lab\_output1.txt**

- 1 Use Linear Search technique to search a student record by considering a specified field (Hall Ticket Number, Name, or Team Number).
- 2 Use Binary Search technique to search a student record by considering a specified field (Hall Ticket Number, Name, or Team Number).

Note:

- ▶ Input should be read from a file **DAALab\_input1.txt**
- ▶ Output should be written into a file **DAALab\_output1.txt**

## Bonus:

- 1 Use Fibonacci Search technique to search a student record by considering a specified field (Hall Ticket Number, Name, or Team Number).

- 1 Use a Tree Sort technique to sort a set of student records by considering Hall Ticket Number.
- 2 Develop a program to multiply two square-matrices of order  $1024 \times 1024$  using Block Matrix Multiplications by considering the block sizes: 4, 8, 16, 32, and 64. Use `gettimeofday()` for calculating *runtime* (the average of 5 runs). Draw a plot using *runtime* and block-size.

Note:

- ▶ Input should be read from a file **DAA Lab\_input1.txt**
- ▶ Output should be written into a file **DAA Lab\_output1.txt**

- 1 Develop a program for the Defective Chessboard problem ( $N=1024$ ,  $2048$ , and  $4096$ ). Use *gettimeofday()* for calculating *runtime* (the average of 5 runs).
- 2 Develop a program to multiply two square-matrices of order  $1024 \times 1024$  using Strassen's Matrix Multiplication. Use *gettimeofday()* for calculating *runtime* (the average of 5 runs).

## Bonus Problem Statements:

- 1 Given an array of  $n$  numbers and a positive integer  $i$ , write a program to find the  $i^{th}$  smallest element that runs in  $O(n)$  time.
- 2 Given two sorted arrays, each consisting of  $n$  numbers, write a program to find the median of  $2n$  elements that runs in  $O(\log n)$  time.

- ❶ **Kanpsack Problem:** We are given with  $n$  objects and a knapsack with capacity  $M$ . Let  $w_1, w_2, w_3, \dots, w_n$  and  $p_1, p_2, \dots, p_n$  be the weights and profits of  $n$  objects, respectively. If we place a fraction  $x_i$ , ( $0 \leq x_i \leq 1$ ) of object  $i$  into the Knapsack, then we get a profit  $p_i \cdot x_i$  and kanpsack capacity is reduced by  $M - w_i \cdot x_i$ . Write a program to find a solution vector  $(x_1, x_2, x_3, \dots, x_n)$  in such a way that we have to get the maximum profit.
- ❷ **Job Sequencing with Deadlines:** We are given with a machine and a set of  $n$  jobs. Each job  $i$  has an integer deadline ( $d_i$ ) and a profit ( $p_i$ ). Execution time of any job is one unit. If a job  $i$  is executed within its deadline, then we get profit  $p_i$ . Write a program to find a solution vector  $(x_1, x_2, x_3, \dots, x_n)$  in such a way that we have to get the maximum profit.



# An Example of Knapsack Problem

Objects	1	2	3	4	5	6	7
Profit	10	5	15	7	6	18	3
Weight	2	3	5	7	1	4	1

M 15

# An Example of Job Sequencing with Deadlines Problem

Job	Deadline	Profit
1	2	40
2	4	15
3	3	60
4	2	20
5	3	10
6	1	45
7	1	55

- 1 **Single Source Shortest Path (SSSP):** Given a connected weighted graph (weights represent the distances between two vertices), write a program to find a shortest path from a given source vertex 's' to every other vertex.

**Using the SSSP program find a shortest path between every pair of vertices.**

- 2 **Huffman Coding:** Write a program to compress and decompress a file using a Huffman Coding. The uncompressed text file and the original text file should be the same.  
(**Size of orizinal file should be  $\geq 1$  MB**).

- 1 **Travelling Salesperson Problem (TSP):** Given a connected weighted graph (weights represent the distances between two vertices), we have to find a tour with minimum distance (cost). Write a program to find an optimal tour.
- 2 **Reliability Design Problem:** Let us consider, we have to design an  $n$ -stage system with maximum reliability under the give cost constraints using device duplication technique. Write a program to identify the number of devices that can be connected in parallel.

$$f_n(C) = \max_{1 \leq m_i \leq u_i} \left\{ \phi_n(m_n) \cdot f_{n-1}(C - c_n \cdot m_n) \right\}$$

Where  $m_n$  is the number of devices that can be connected in  $n^{th}$  Stage.  
 $\phi_n(m_n)$  is the reliability of Stage  $n$ .

**Base case:**  $f_0(x) = 1$ , where  $x \geq 0$

$f_i(-ve) = 0$ , where  $0 \leq i \leq n$

- 1 **Matrix Chain Multiplication:** Given a chain of  $n$  matrices (i.e.,  $A_1, A_2, A_3, \dots, A_n$ ) and dimensions (rows and columns) of the matrices are  $p_0 \times p_1, p_1 \times p_2, p_2 \times p_3 \dots p_{n-1} \times p_n$ , respectively. Write a program to find an order(or parenthesize the matrices) to compute the product  $A_1.A_2.A_3. \dots .A_n$  using minimum number of scalar multiplications.
- 2 **Longest Common Sub-Sequence (LCS):** Let  $X_i = (x_1, x_2, \dots, x_i)$  and  $Y_j = (y_1, y_2, \dots, y_j)$  are two strings, then write a program to a Longest Common Sub-Sequence of  $X_i$  and  $Y_j$ .

**Bonus:** Write a program to find LCS of  $n$  strings. For example LCS of 4 strings { **aaabb**, **baaaa**, **ccbb**, **bbccc** } is **bb**.

- 1 **N-Queens Problem:** Given an  $N \times N$  chessboard and N-Queens. Place N-Queens on the chessboard in non-attackable positions. Consider the different values of  $N = 8, 12, 16$ , and  $20$ . Store all the solutions in a file.
- 2 **Sum of Subsets Problem:** We are given with  $n$  distinct positive numbers (usually called weights) and a value  $m$ . Write a program to find all the subsets of these  $n$  numbers whose sums are  $m$  (Use Backtracking).
- 3 **Graph Coloring Problem:** Let  $G$  be a graph with  $n$  vertices. Write a program to assign colors to the vertices of  $G$  (using minimum number of colors) in such a way that no two adjacent vertices have the same color.
- 4 **Develop programs for 3-Puzzle, 8-Puzzle and 15-Puzzle Problems:**

8-Puzzle

1	2	
4	5	3
7	8	6

Initial State

1	2	3
4	5	6
7	8	

Goal State

15-Puzzle

4	5	7	10
8	1	2	12
3	6	9	11
14	13	15	

Initial State

1	2	3	4
5	6	7	8
9	10	11	12
13	14	15	

Final State