

**THE UNIVERSITY OF QUEENSLAND**

**School of Information Technology and  
Electrical Engineering**

Mid-Semester Examination

**ENGG1300**

Introduction to Electrical Systems

Time: **TEN (10)** minutes for perusal  
**NINETY (90)** minutes for working

**THIS EXAM CONSISTS OF THIRTY (30) MULTIPLE  
CHOICE QUESTIONS. ANSWER EACH QUESTION ON THE  
MULTIPLE CHOICE ANSWER SHEET PROVIDED.**

During perusal, you are permitted to write on the rough paper provided.

This examination is closed book – No materials permitted.

No electronic aids are permitted (e.g. laptops, phones).

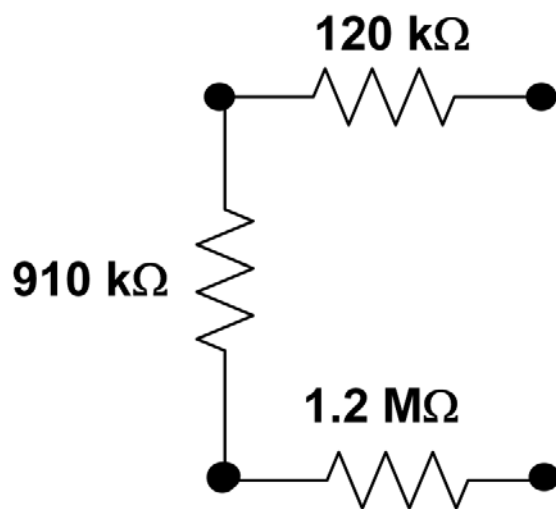
A UQ approved calculator (with label), or a casio FX-82 series calculator is allowed.

For each question, choose the one answer which is most correct.

Where "none of the above" is the correct answer option, the associated numerical answer will be different to any of the provided numerical answers by at least +/-5%.

**Question 1.**

Consider the one-port network shown below:



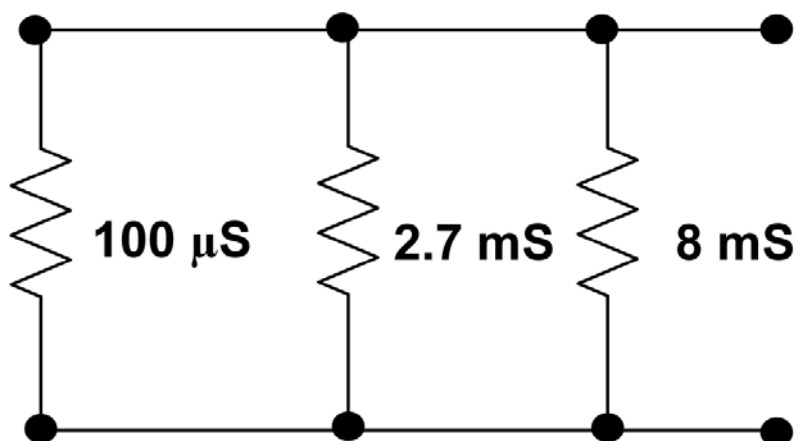
What is the equivalent resistance of this network?

- A.  $1031.2\text{ k}\Omega$
- B.  $2.230\text{ M}\Omega$
- C.  $97.41\text{ k}\Omega$
- D.  $373.4\text{ }\Omega$
- E. None of the above.

**Question 2.**

Consider the one-port network shown below.

Note that the resistor values are shown as conductances.

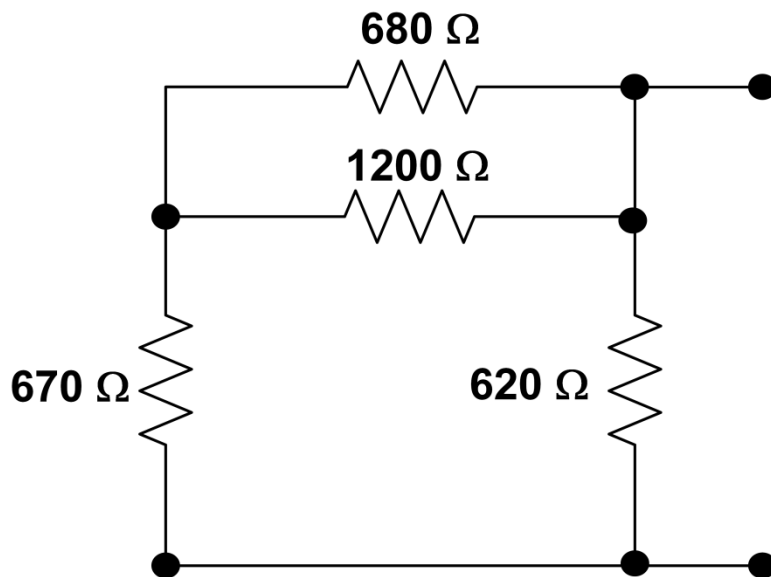


What is the equivalent resistance of this network?

- A.  $95.30\text{ }\mu\Omega$
- B.  $10.80\text{ m}\Omega$
- C.  $92.59\text{ }\Omega$
- D.  $92.59\text{ m}\Omega$
- E. None of the above.

**Question 3.**

Consider the one-port network shown below.



What is the equivalent resistance of this network?

- A.  $397.0\ \Omega$
- B.  $3170.0\ \Omega$
- C.  $465.4\ \Omega$
- D.  $184.7\ \Omega$
- E. None of the above.

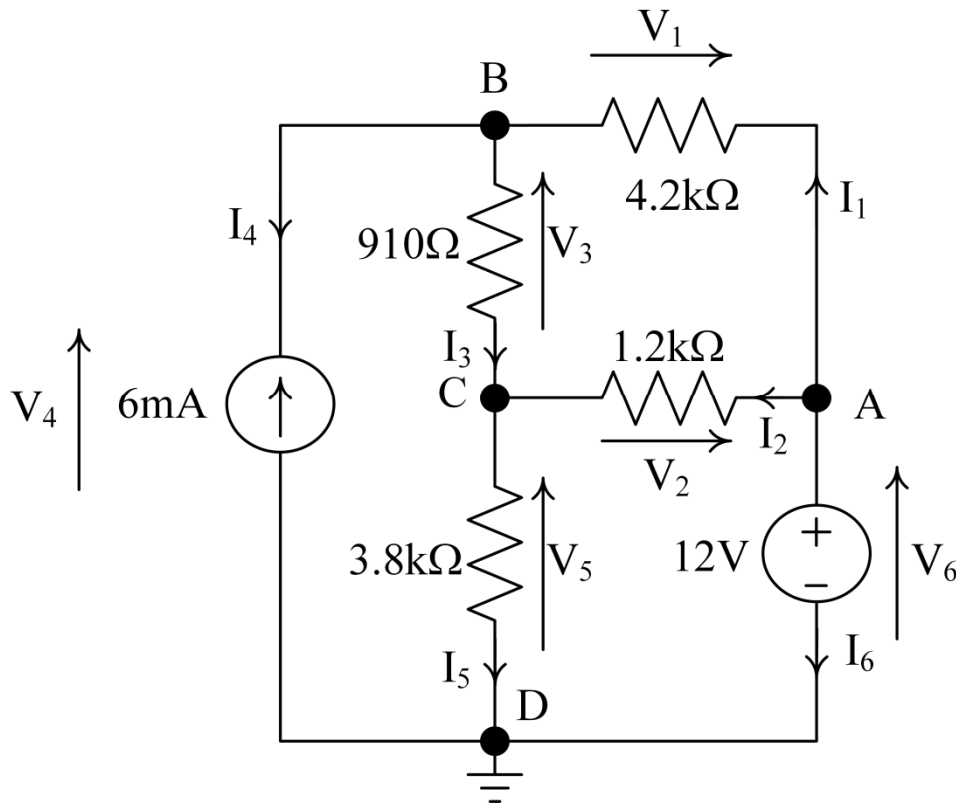
**Question 4.**

Which of the following is a unit of inductance?

- A. Ohms
- B. Siemens
- C. Amperes
- D. Farads
- E. None of the above

**Questions (5)–(15) all refer to solution of the circuit below in Figure 1. First solve this circuit, and then check your working to make sure it is correct before answering the subsequent questions.**

**In all cases be very careful about the sign of the answers.**



**Figure 1: Circuit Schematic for Question (5)-(15)**

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**Question 5**

With reference to Figure 1, which of the following is a correct Kirchoff's Voltage Law Equation?

A.  $V_1 + V_2 + V_3 = 0$

D.  $V_1 = V_2 + V_3$

B.  $V_2 = V_1 + V_3$

C.  $V_3 = V_1 + V_2$

E. None of the above.

**Question 6**

With reference to Figure 1, which of the following is a correct Kirchoff's Current Law Equation?

A.  $\frac{V_B - V_C}{910} + \frac{V_C - V_D}{3800} + \frac{V_C - V_A}{1200} = 0$

B.  $\frac{V_B - V_C}{910} + \frac{V_D - V_C}{3800} + \frac{V_C - V_A}{1200} = 0$

C.  $\frac{12 - V_B}{4200} + \frac{V_C - V_B}{910} = 0.006$

D.  $\frac{V_B - 12}{4200} + \frac{V_B - V_C}{910} = 0.006$

E. None of the above.

**Question 7**

With reference to Figure 1, which of the following is a correct Kirchoff's Current Law Equation at node D?

A.  $I_4 = I_5 + I_6$

B.  $I_5 = I_4 + I_6$

C.  $I_6 = I_4 + I_5$

D. It is impossible to write this equation because the current entering the earth connection is unknown.

E. None of answers (A)-(C) are correct, but it is possible to write a correct Kirchoff's Current Law Equation at node D

**Question 8**

In the circuit shown in Figure 1, what is the value of current  $I_4$ ?

A. 0.600 A

B. -0.600 A

C. 6 mA

D. -6 mA

E. None of the above.

**Question 9**

In the circuit shown in Figure 1, what is the value of current  $I_5$ ?

- A. 4.66 mA
- B. -6.00 mA
- C. 3.52 mA
- D. -3.52 mA
- E. None of the above.

**Question 10**

In the circuit shown in Figure 1, what is the value of node voltage  $V_B$ ?

- A. 17.63 V
- B. 12.0 V
- C. 24.0 V
- D. -13.42 V
- E. None of the above

**Question 11**

In the circuit shown in Figure 1, what is the value of branch voltage  $V_6$ ?

- A. 14.67 V
- B. -14.67 V
- C. 12 V
- D. -12 V
- E. None of the above.

**Question 12**

In the circuit shown in Figure 1, what is the value of branch voltage  $V_2$ ?

- A. 12.0 V
- B. 1.381 V
- C. 13.381 V
- D. 16.95 V
- E. None of the above.

**Question 13**

In the circuit shown in Figure 1, what is the value of the power consumed by the 6mA current source?

- A. 105.7 mW
- B. -105.7 mW
- C. 0 W
- D. -72 mW
- E. None of the above

**Question 14**

In the circuit shown in Figure 1, what is the value of the power **consumed** by the  $910\Omega$  resistor?

- A. 19.8 mW
- B. -19.8mW
- C. 0 W
- D. 22 mW
- E. None of the above

**Question 15**

In the circuit shown in Figure 1, what is the value of the power **consumed** by all the components in the circuit in total (i.e. including the  $4200\Omega$ ,  $1200\Omega$ ,  $910\Omega$  and  $3800\Omega$  resistors; the 12V voltage source; and the 6mA current source)?

- A. 0 W
- B. 135.6mW
- C. 152.1 mW
- D. 76.04 mW
- E. None of the above.



Questions (16)–(21) all involve analysis of the one-port network shown below in Figure 2. In particular, you will be asked to calculate the Thevenin and Norton equivalent circuits.

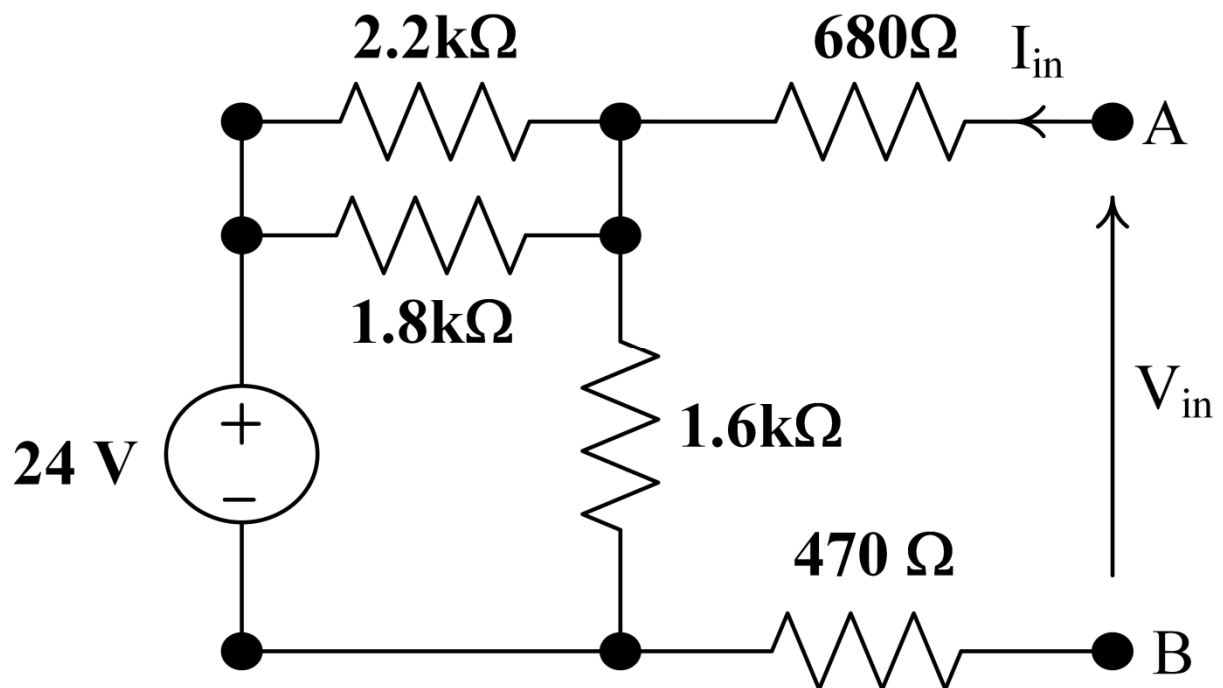


Figure 2: Circuit Schematic for Question's (16)-(21)

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**Question 16**

If the one-port network of Figure 2 is replaced by its Thevenin Equivalent Circuit, what is the value of the voltage source in that equivalent circuit,  $V_T$ ?

- A. 24.0 V
- B. 9.17 V
- C. 14.83 V
- D. 6.67 V
- E. None of the above.

**Question 17**

If the one-port network of Figure 2 is replaced by its Thevenin Equivalent Circuit, what is the value of the series resistor in that equivalent circuit,  $R_T$ ?

- A. 1761.6  $\Omega$
- B. 611.6  $\Omega$
- C. 6750.0  $\Omega$
- D. 2750.0  $\Omega$
- E. None of the above.

**Question 18**

If the one-port network of Figure 2 is replaced by its Norton Equivalent Circuit, what is the value of the current source in that equivalent circuit,  $I_N$ ?

- A. 6.92 mA
- B. -6.92 mA
- C. 8.42 mA
- D. -8.42 mA
- E. None of the above.

For Questions (20)-(23), a non-linear diode is placed across the terminals of the one port network shown in Figure 2 to give the circuit of Figure 3. The  $I$ - $V$  characteristic of the diode is shown in Figure 4.

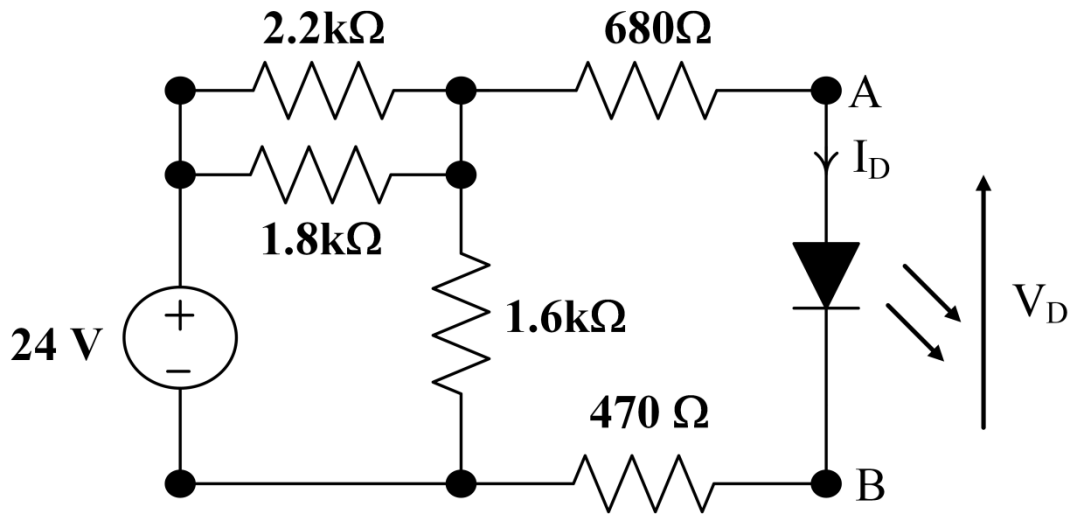


Figure 3: Circuit Schematic for Questions (19)-(21)

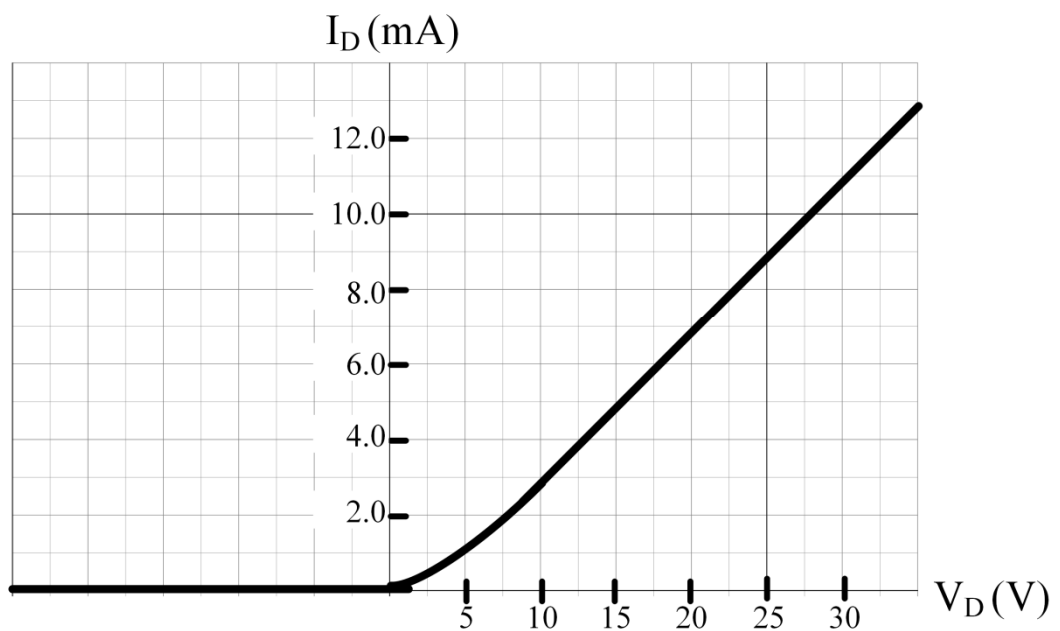


Figure 4: The characteristics of the LED described in questions (19)-(23)

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**Question 19**

Which of the following equations must the solution to the circuit in figure 4 satisfy?

Note,  $R_{TH}$  refers to the Thevenin resistance as calculated in Question (17);  $I_N$  refers to the Norton current calculated in Question (18);  $V_D$  refers to the voltage across the diode, and  $I_D$  refers to the current through the diode (as labelled in figure 4).

- A.  $I_D = -(R_{TH}V_D + I_N)$
- B.  $I_D = R_{TH}V_D - I_N$
- C.  $I_D = I_N - \frac{1}{R_{TH}}V_D$
- D.  $I_D = \frac{1}{R_{TH}}V_D - I_N$
- E. It is not possible to express the solution to this circuit as a linear relationship between  $I_D$  and  $V_D$  because the diode is a non-linear component.

**Question 20**

Given the circuit in Figure 3, and the diode I–V characteristic of Figure 4, which of the following is **closest** to the value of  $V_D$ ?

- A.  $V_D$  is 5V or less
- B. 10 V
- C. 15 V
- D. 20 V
- E.  $V_D$  is 25V or greater.

**Question 21**

Given the circuit in Figure 3 and the diode I–V characteristic of Figure 4, which of the following is closest to the value of  $I_D$ ?

- A. 2.0 mA or less
- B. 3mA
- C. 5mA
- D. 7mA
- E.  $I_D$  is 9mA or greater.

*Questions 22 and 23 refer to the  $I$ – $V$  characteristic of the diode as shown in Figure 4 above. These questions introduce a new design problem and DO NOT require information provided in either of Figure 2 or Figure 3.*

**Question 22**

You are designing an LED light. This will consist of a 24V lead-acid battery connected in series with a single resistor and the LED characterised in figure 4 above. The battery can be modelled as a 24V ideal voltage source. The datasheet for the diode recommends that for maximum operational life, the voltage across the diode should be set to 15V. Which of the following values for the series resistor will result in a voltage across the diode ( $V_D$ ) that is **closest** to 15V?

- A. 2200 $\Omega$
- B. 3100 $\Omega$
- C. 4800 $\Omega$
- D. The resistor should be less than 1600 $\Omega$ , or greater than 750 $\Omega$
- E. It is not possible to estimate the required resistor value with the information provided

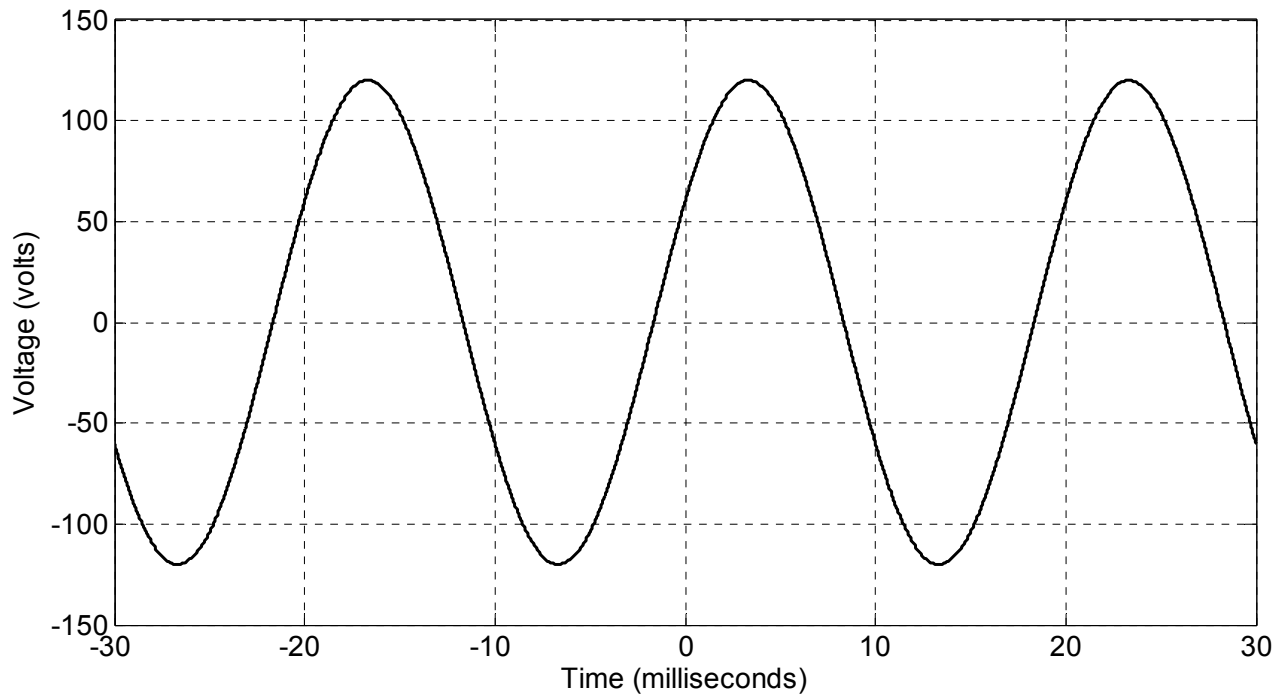
**Question 23**

The LED characterised in figure 4 can be assumed to be 100% efficient (i.e. all power dissipated by the LED is converted to light). What is the overall efficiency of the circuit described in Question (22) when the voltage across the diode is set to 15V (i.e. what percentage of total power supplied by the battery is converted to light)?

- A. 0%
- B. 37.5%
- C. 62.5%
- D. 100%
- E. The overall efficiency of the circuit cannot be estimated with the information provided.

**Question 24**

A sinusoidal voltage is displayed in the figure below.



Which of the following equations best models the sinusoidal voltage displayed?

- A.  $V_s(t) = 120\cos(50t + 0.003)$
- B.  $V_s(t) = 240\sin(50t - 0.003)$
- C.  $V_s(t) = 240\cos(315t + 1.0)$
- D.  $V_s(t) = 120\cos(315t - 1.0)$
- E.  $V_s(t) = 240\sin(315t - 1.0)$

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Questions (25) and (26) refer to the schematic in Figure 5 where  $L_1 = 220\text{mH}$ ,  $R_2 = 120\Omega$ ,  $C_3 = 47\mu\text{F}$ .

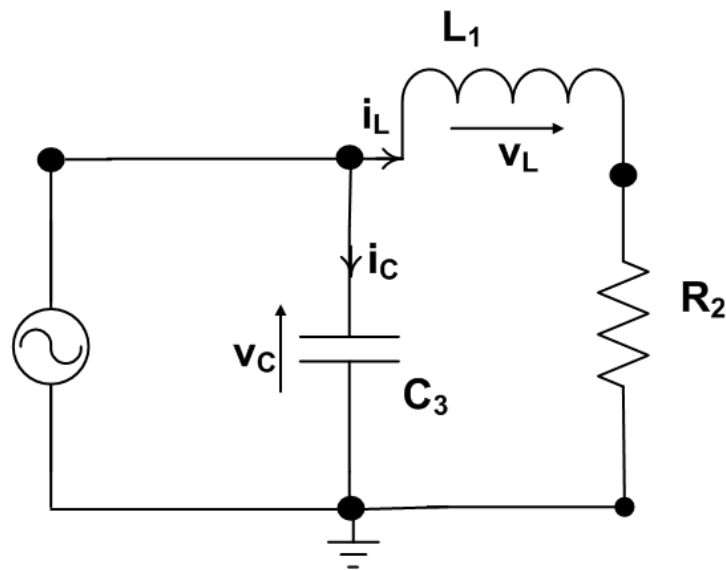


Figure 5: Circuit Schematic for Questions (25)-(26)

**Question 25.**

At a particular instant of time,  $V_C = -9\text{V}$ ,  $i_C = -600\text{mA}$ ,  $V_L = 3.6\text{V}$ ,  $i_L = 700\text{mA}$ . At that instant of time, how much energy is stored in the inductor?

- A. 1.42 J
- B. -1.42 J
- C. 53.9 mJ
- D. -53.9 mJ
- E. none of the above

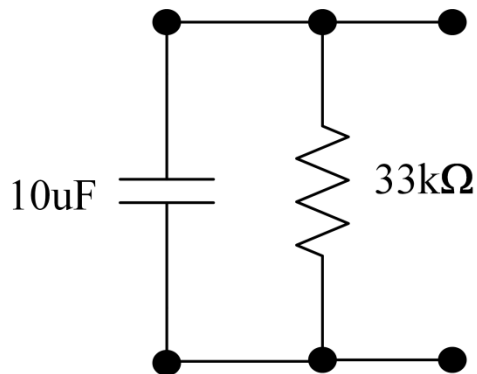
**Question 26.**

At a particular instant of time,  $V_C = -9\text{V}$ ,  $i_C = -600\text{mA}$ ,  $V_L = 3.6\text{V}$ ,  $i_L = 700\text{mA}$ . At that instant of time, how much energy is stored in the capacitor?

- A. 1.90 mJ
- B. -1.90 mJ
- C. 8.46  $\mu\text{J}$
- D. -8.46  $\mu\text{J}$
- E. None of the above

**Question 27.**

Consider the one-port network shown below.

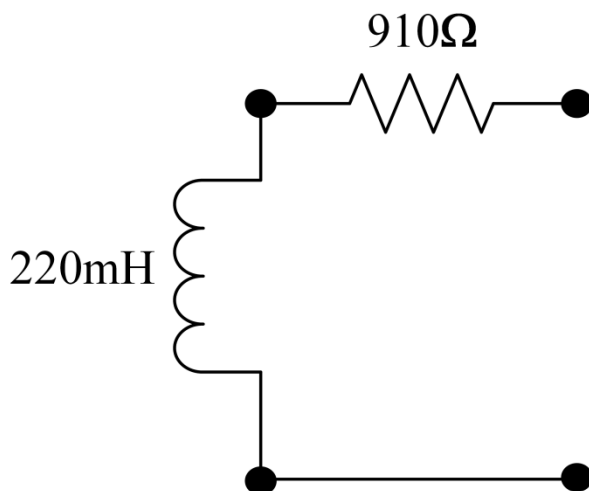


If the frequency of operation is 2Hz, what is the equivalent impedance of this network?

- A.  $33000 - j7957 \Omega$
- B.  $1769 - j7529 \Omega$
- C.  $2200 - j628.3 \Omega$
- D.  $33000 - j(10^{-5}) \Omega$
- E.  $33000 + j(10^{-5}) \Omega$

**Question 28.**

Consider the one-port network shown below.



If the frequency of operation is 700Hz, what is the equivalent impedance of this network?

- A.  $910e^{j2.42 \times 10^{-4}} \Omega$
- B.  $910e^{-j2.42 \times 10^{-4}} \Omega$
- C.  $910e^{-j1.14 \times 10^{-6}} \Omega$
- D.  $1328e^{j0.816} \Omega$
- E.  $1328e^{-j0.816} \Omega$



Questions (29)-(30) refer to the schematic in Figure 6 below, where:

- $\underline{V_S} = 6 e^{j0}$  volts,  $f = 120\text{Hz}$
- $R = 330\Omega$
- $C = 2.7 \mu\text{F}$
- $L = 160\text{mH}$

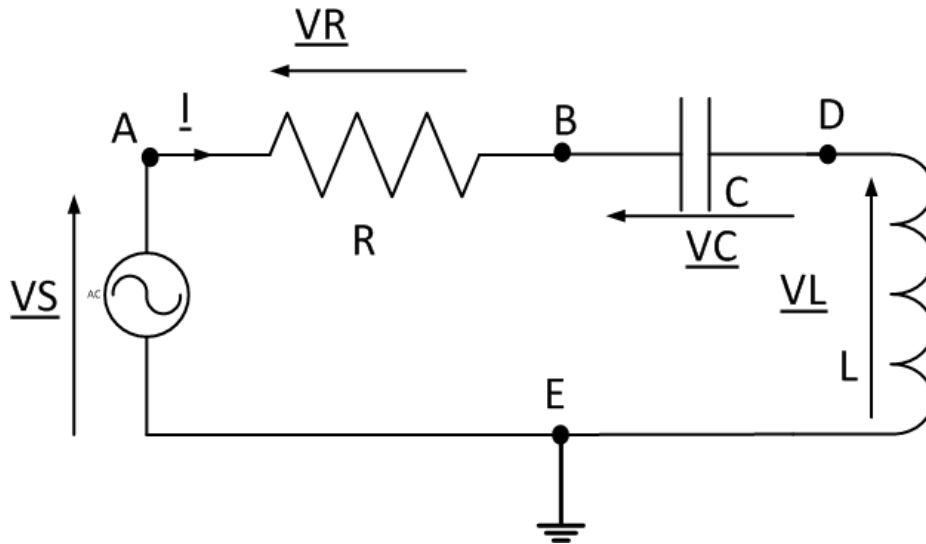


Figure 6: Circuit Schematic for Questions (29)-(30)

**Question 29.**

In the circuit shown in Figure 6 with the component values listed above, what is the value of the phasor current  $\underline{I}$ ?

- A. 18.2 mA
- B.  $7.61e^{-j0.91}\text{mA}$
- C.  $7.61e^{j0.91}\text{mA}$
- D.  $12.1e^{j0.84}\text{mA}$
- E. It is impossible to calculate the phasor current with the provided information.

**Question 30.**

In the circuit shown in Figure 6 with the component values listed above, what is the value of the phasor voltage across the inductor,  $\underline{V_L}$ ?

- A.  $1.46e^{-j2.41}\text{V}$
- B.  $1.46e^{j2.41}\text{V}$
- C. 0 V
- D.  $0.918e^{-2.48}\text{V}$
- E. It is impossible to calculate the phasor voltage across the inductor with the provided information.

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