

# *Data and Signals*

By

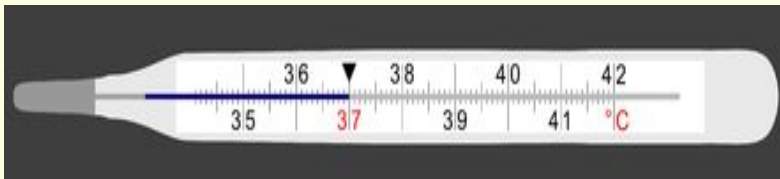
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# Data and Signal : Analog and Digital

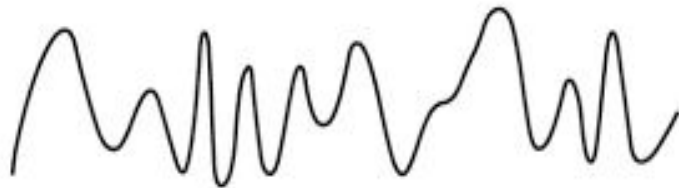
Analog Data



Digital Data



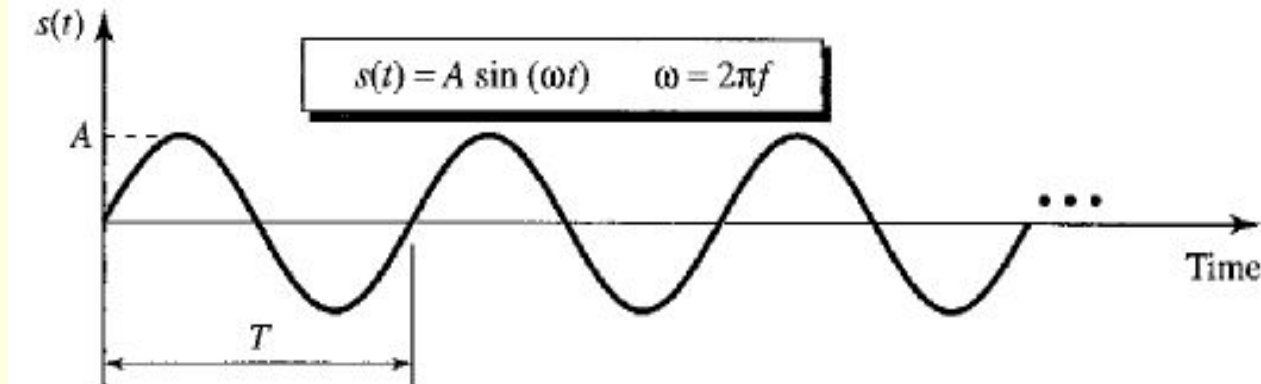
Analog Signal



Digital Signal



# Simple Periodic Signal



$s(t)$  □ Instantaneous Amplitude

$A$  □ Peak Amplitude

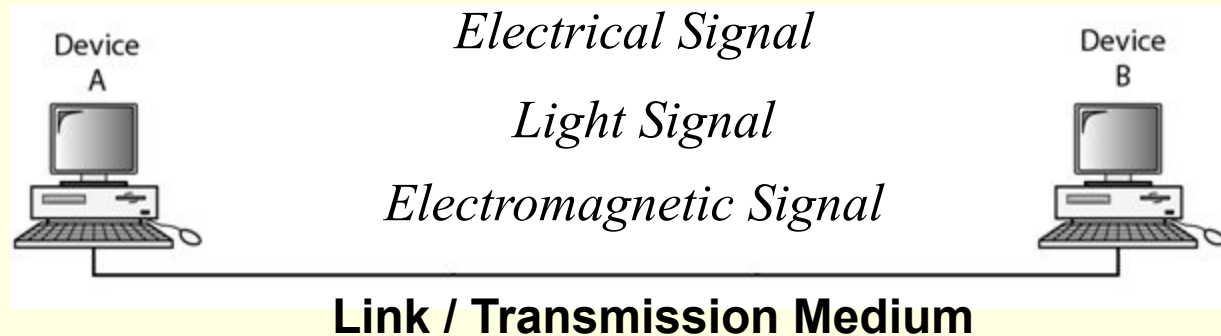
$T$  □ Period (time needed to complete 1 cycle)

$f$  □ Frequency (no. of cycles per second(Hz))

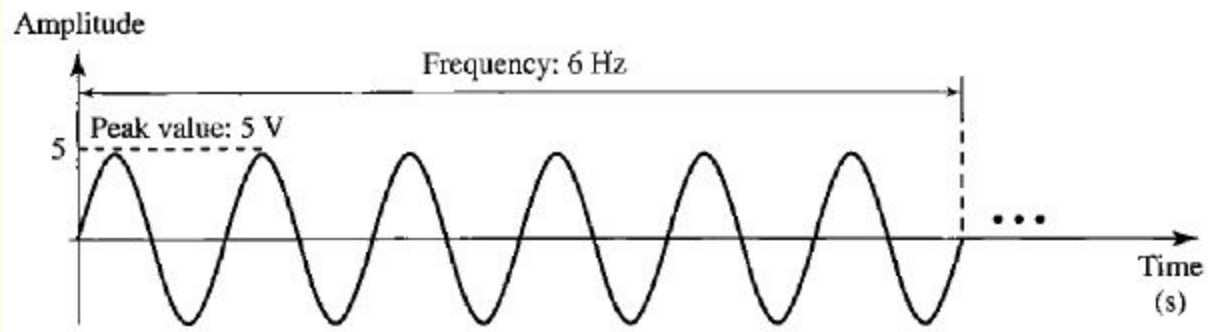
$\omega = 2\pi f$  □ Angular/Radian Frequency

# Types of Signal

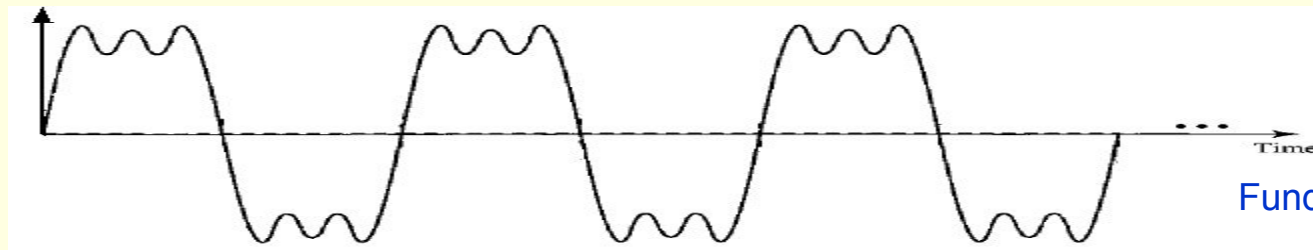
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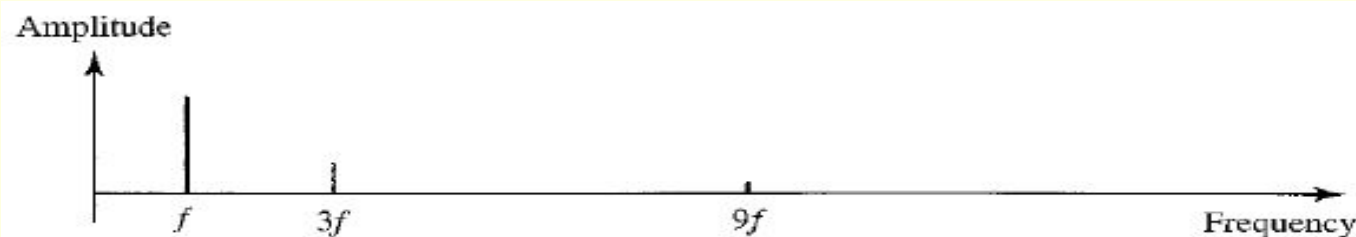
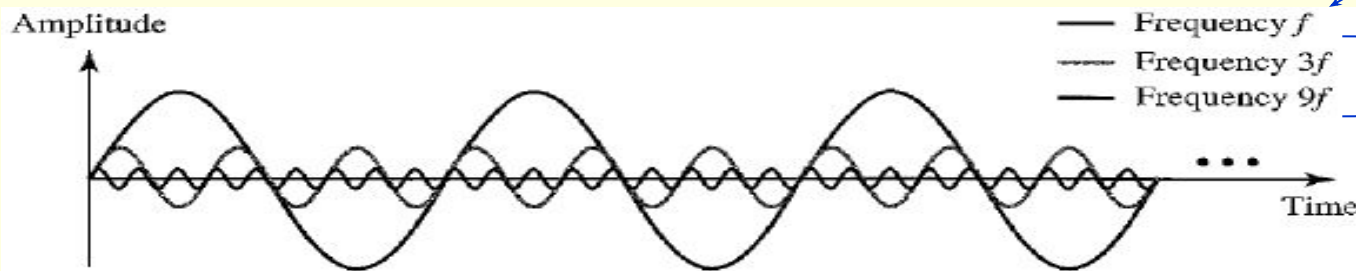
# Time Domain vs Frequency Domain



# Composite Periodic Signal



Fundamental Frequency



**Bandwidth** of a composite signal is the difference between the **highest frequency** and the **lowest frequency** contained in the composite signal

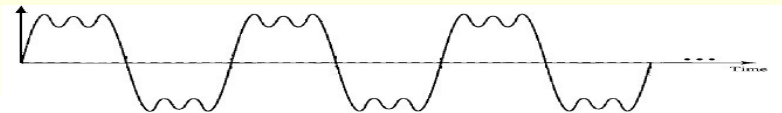
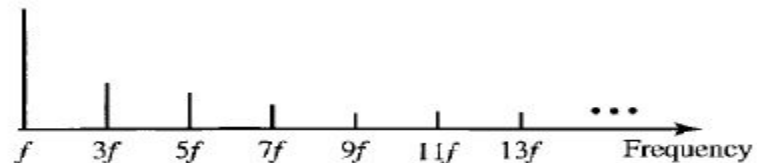
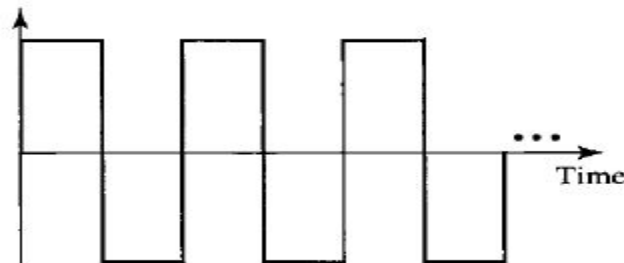
**Spectrum** of a composite signal is the **set of frequencies** contained in it.

# Fourier Analysis of a Composite Signal

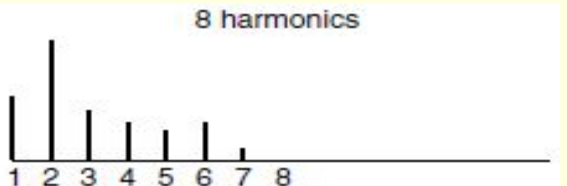
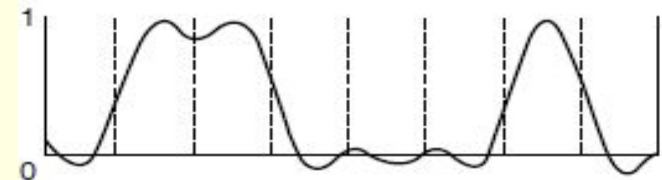
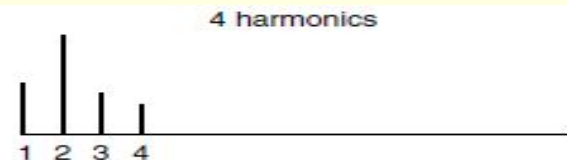
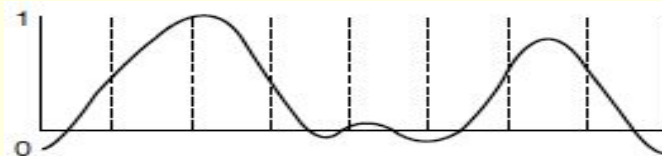
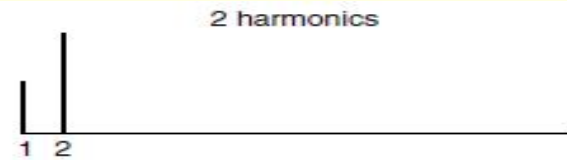
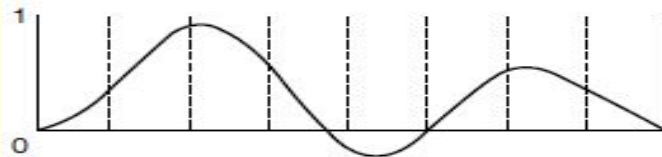
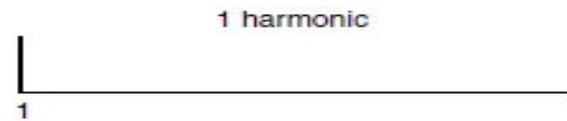
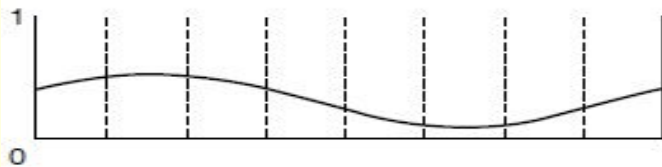
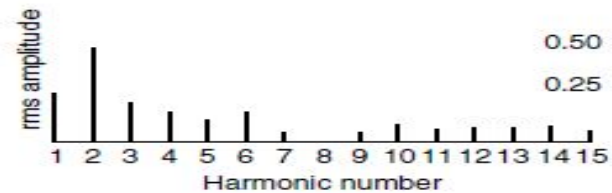
$$g(t) = \frac{1}{2}c + \sum_{n=1}^{\infty} a_n \sin(2\pi nft) + \sum_{n=1}^{\infty} b_n \cos(2\pi nft)$$

$$a_n = \frac{2}{T} \int_0^T g(t) \sin(2\pi nft) dt \quad b_n = \frac{2}{T} \int_0^T g(t) \cos(2\pi nft) dt \quad c = \frac{2}{T} \int_0^T g(t) dt$$

- A composite periodic signal with period T (frequency f) can be decomposed into an **infinite** series of **sine** and **cosine** functions in which each function is an integral harmonic of the fundamental frequency f.
- Fourier Analysis changes a **time-domain signal** to a **frequency-domain signal** and vice versa
- Digital Signal is a Composite Signal



# Transmission of Digital Signal





# Relation between Data Rate and No. of Harmonics

Given a Data Rate of  $b$  bits/second over a telephone line with  $f_c = 3000\text{Hz}$

$$T = 8/b \quad \text{and} \quad f = 1/T$$

$$n.f \leq f_c$$

Bps	T (msec)	First harmonic (Hz)	# Harmonics sent
300	26.67	37.5	80
600	13.33	75	40
1200	6.67	150	20
2400	3.33	300	10
4800	1.67	600	5
9600	0.83	1200	2
19200	0.42	2400	1
38400	0.21	4800	0