

## AC Assignment (1)

Q.1. A carrier signal with an RMS voltage amplitude of 2V & a frequency of 1.5 MHz is amplitude modulated by a modulating sine wave with a frequency of 500 Hz & RMS amplitude level of 1V.

- Write an exp<sup>n</sup> for the resulting AM signal.
- Calculate amplitude modulation,  $m_a$  & percent  $M_a$
- Rewrite the exp<sup>n</sup> for AM wave by considering value of  $m_a$  as 0.5

Sol: Given:  $V_c = 2V$ ,  $f_m = 500 \text{ Hz}$ , frequency of modulating signal  
frequency of carrier signal = 1.5 MHz or  $1.5 \times 10^6 \text{ Hz}$   
 $V_m = 1V$ ,  $V_c = 2 \times \sqrt{2} V = 2.8V$

$$a) V_{AM}(t) = [V_c + V_m \sin(2\pi f_m t)] \sin(2\pi f_c t) \\ = [2.82 + 1.41 \sin(2\pi 500t)] \sin 2\pi(1.5 \times 10^6 t) \text{ volt}$$

b) AM modulation index,

$$m_a = \frac{V_m}{V_c} = \frac{1.41}{2.82} = \boxed{0.5}$$

$$M_a = m_a \times 100 = 0.5 \times 100 = \boxed{50\%}$$

c) Consider  $m_a = 0.5$

$$V_{AM}(t) = 2.82 [(1 + 0.5 \sin(2\pi \times 500t)) \sin(2\pi \times 1.5 \times 10^6 t)]$$

Q.2)

Sol: The modulation index of AM signal is,

$$m_r = \sqrt{m_a^2 + m_f^2 + m_p^2}$$

$$= \sqrt{(0.2)^2 + (0.4)^2 + (0.5)^2} = \sqrt{0.04 + 0.16 + 0.25}$$

$$\boxed{m_r = 0.67}$$

Q 3)

Sol: Given: unmodulated carrier power ( $P_c$ ) = 10 kWMax. percentage modulation,  $M_a = 40\%$ .

We know,

$$\text{modulation index, } m_a = \frac{M_a}{100} = \frac{40}{100} = 0.4$$

$$\therefore \text{The total modulated power, } P_t = P_c \left[ 1 + \frac{m_a^2}{2} \right]$$

$$i.e. = 10 \left[ 1 + \frac{(0.4)^2}{2} \right]$$

$$= 10 [1 + 0.08]$$

$$\boxed{P_t = 10.8 \text{ kW}}$$

$$\text{When } m_a = 0.3 \text{ (reduced modulation index) } = \frac{M_a}{100} = \frac{30}{100}$$

& max unmodulated carrier power =  $P'_c$ 

So,

$$P_t = P'_c \left[ 1 + \frac{m_a^2}{2} \right]$$

$$P'_c = \frac{P_t}{\left[ 1 + \frac{m_a^2}{2} \right]} = \frac{10.8}{\left[ 1 + \frac{(0.3)^2}{2} \right]} = \frac{10.8}{1.045}$$

$$\boxed{P'_c = 10.335 \text{ kW}}$$

Q 4)

Sol: Given:  $m_a = 0.5$ ,  $V_c = 10\text{V}$ ,  $R_L = 10\Omega$ 

a) The carrier power

$$P_c = \frac{V_c^2}{2R_L} = \frac{(10)^2}{2 \times 10} = \frac{100}{20} = 5$$

$$\therefore \boxed{P_c = 5 \text{ W}}$$



b) The lower side band & upper side band

$$P_{LSB} = P_{USB} = \frac{m_a^2 P_c}{4} = \frac{(0.5)^2 \times 5}{4}$$

$$= \frac{0.25 \times 5}{4} = \frac{0.125}{4}$$

$$\therefore P_{LSB} = P_{USB} = 0.3125 \text{ W}$$

c) Total side band power

$$P_{sb} = \frac{m_a^2}{2} \times P_c$$

$$= \frac{(0.5)^2 \times 5}{2}$$

$$= \frac{0.125}{2}$$

$$\therefore P_{sb} = 0.625 \text{ W}$$

d) Total AM Power.  $P_{AM} = P_c \left(1 + \frac{m_a^2}{2}\right)$

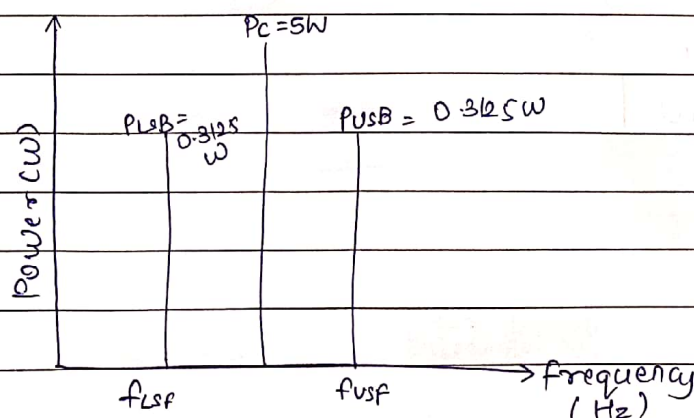
$$m_a = 0.5, P_c = 5$$

$$\therefore P_{AM} = 5 \left(1 + \frac{(0.5)^2}{2}\right) = 5 \times 1.125$$

$$= 56.25 \text{ W}$$

$$\therefore P_{AM} = 56.25 \text{ W}$$

e) Sketch the AM power spectrum.



AM Power Spectrum

0.5)

Sol: a)  $V_{AM}(t) = [10 (1 + 0.5 \sin(2\pi \times 10^3 t) + 0.2 \sin(4\pi \times 10^3 t))] \text{ V}$   
 Compare above eqn with,

$$V_{AM}(t) = [V_c \sin(2\pi f_c t) + m_{a1} \sin(2\pi f_c t) \sin(2\pi f_{m1} t) + m_{a2} \sin(2\pi f_c t) \sin(2\pi f_{m2} t)]$$

We get,  $m_{a1} = 0.5$  &  $m_{a2} = 0.2$

$$\therefore m_T = \sqrt{(0.5)^2 + (0.2)^2} = \underline{\underline{0.539}}$$

b) Unmodulated carrier power

$$P_c = \frac{V_c^2}{2} = \frac{(10)^2}{2} = \frac{100}{2} = 50 \text{ W}$$

$$\therefore \boxed{P_c = 50 \text{ W}}$$

c) Sideband power

$$P_{sb} = \frac{m_a^2}{2} \cdot P_c = \frac{(0.5)^2}{2} \times 50$$

$$= 0.125 \times 50$$

$$\boxed{P_{sb} = 7.25 \text{ W}}$$

d) Total power of AM signal

$$P_{AM} = P_c \left(1 + \frac{m_a^2}{2}\right)$$

$$= 50 \left[1 + \frac{(0.5)^2}{2}\right]$$

$$= 50 \times 1.125$$

$$\boxed{P_{AM} = 56.25 \text{ W}}$$



Q.1) A communication receiver has a noise power bandwidth of 10 kHz. A resistor that matches its i/p impedance is connected across its antenna terminals. Determine the noise power contributed by the external resistor in the receiver bandwidth. Assume the operating temperature of 27°C. ( $k = 1.38 \times 10^{-23} \text{ J/K}$ )

Sol: Given: BW = 10 KHz,  $k = 1.38 \times 10^{-23} \text{ J/K}$

$$T = 27^\circ\text{C} = 300 \text{ K}$$

Thermal Noise Power =  $N =$

$$\begin{aligned} & 10 \log(k) + 10 \log(T) + 10 \log(B) \text{ dBW} \\ &= 10 \log(1.38 \times 10^{-23}) + 10(\log 300) + 10 \log(10 \times 10^3) \text{ dBW} \\ &= -228.60 + 24.77 + 40 \\ &= -163.83 \text{ dBW} \end{aligned}$$

$\therefore$  Noise power contributed by external resistor is -163.83 dBW.

Q.2) An electronic ckt is perfectly noiseless & adds no extra noise to the signal. The SNR at the i/p is equal to the SNR at the o/p. What is the noise figure of the ckt?

Sol: Given:  $\text{SNR}_0 = \text{SNR}$

$$\text{We know, Noise Factor (F)} = \frac{\text{SNR i/p}}{\text{SNR o/p}} = 1$$

$$\begin{aligned} \text{Noise Figure (NF)} &= 10 \times \log_{10}(F) \\ &= 10 \times \log_{10}(1) \end{aligned}$$

$$\therefore \boxed{\text{NF} = 0 \text{ dB}}$$

Q.3) A practical amplifier ckt has i/p signal power of  $2 \times 10^{-10} \text{ W}$ , input noise power of  $2 \times 10^{-18} \text{ W}$ , available power gain of  $10^6$ . Determine i/p SNR (dB) & o/p signal power.

Sol<sup>n</sup> Given:

$$\text{i/p signal power} = 2 \times 10^{-10} \text{ W}$$

$$\text{i/p noise power} = 2 \times 10^{-18} \text{ W}$$

$$\text{Available power gain} = 10^6$$

$$\text{i/p SNR (dB)} = 10 \times \log \left( \frac{\text{i/p signal power}}{\text{i/p noise power}} \right)$$

$$= 10 \times \log_{10} \left( \frac{2 \times 10^{-10}}{2 \times 10^{-18}} \right)$$

$$= 10 \times \log(10^8)$$

$$\therefore \text{i/p SNR (dB)} = 80 \text{ dB}$$

Now,

$$\text{o/p signal} = \frac{\text{i/p signal power} \times \text{available power gain}}{\text{power}}$$

$$= 2 \times 10^{-10} \times 10^6$$

$$= 2 \times 10^{-4}$$

$$= 0.0002 \text{ W}$$

$$\therefore \text{o/p signal power} = 200 \mu\text{W}$$

Q.4) A practical amplifier ckt has i/p signal power  $2 \times 10^{-10} \text{ W}$ , i/p noise power of  $2 \times 10^{-18} \text{ W}$ , available power gain of  $10^6$  & internal noise of  $6 \times 10^{-12} \text{ W}$ . Determine o/p noise power & o/p SNR (dB).

Sol<sup>n</sup> Given:

$$\text{i/p signal power} = 2 \times 10^{-10} \text{ W}$$

$$\text{i/p noise power} = 2 \times 10^{-18} \text{ W}$$

$$\text{available power gain} = 10^6$$



$$\text{Internal noise} = 6 \times 10^{-12} \text{ W}$$

$$\begin{aligned} \text{O/p noise power} &= [\text{i/p noise power} \times \text{power gain}] + \text{internal noise} \\ &= (2 \times 10^{-18} \times 10^6) + 6 \times 10^{-12} \\ &= (2 \times 10^{-12}) + (6 \times 10^{-12}) \end{aligned}$$

$$\therefore \text{O/p noise power} = 8 \times 10^{-12} \text{ W}$$

Now,

$$\text{O/p SNR(dB)} = 10 \times \log \left( \frac{\text{O/p signal power}}{\text{O/p noise power}} \right)$$

$$\& \text{O/p signal power} = \text{i/p signal power} \times \text{power gain}$$

$$= 2 \times 10^{-10} \times 10^6$$

$$= 2 \times 10^{-4}$$

$$= 0.002 \text{ W}$$

$$\therefore \text{O/p SNR(dB)} = 10 \times \log \left( \frac{2 \times 10^{-4}}{8 \times 10^{-12}} \right)$$

$$= 10 \times \log \left( \frac{1}{4} \times 10^8 \right)$$

$$= 10 \times \log (0.25 \times 10^8)$$

$$\therefore \text{O/p SNR(dB)} = 73.97$$

$$\therefore \text{O/p SNR} = 73.97 \text{ dB}$$

Q.5) A practical amplifier ckt has i/p SNR of  $1 \times 10^8 \text{ W}$  & O/p SNR, of  $2.5 \times 10^7 \text{ W}$ . Determine noise factor (ratio) & noise figure (dB)

Sol: Given:

$$\text{i/p SNR} = 1 \times 10^8 \text{ W}$$

$$\text{O/p SNR} = 2.5 \times 10^7 \text{ W}$$

$$\begin{aligned} \text{Noise Factor (ratio)} &= \frac{\text{i/p SNR}}{\text{O/p SNR}} = \frac{1 \times 10^8 \text{ W}}{2.5 \times 10^7 \text{ W}} = 4 \end{aligned}$$

$$\begin{aligned} \& \text{ Noise Figure} &= 10 \log(NF) \\ (NF) &= 10 \log(4) \\ &= 6.02 \end{aligned}$$

$$\boxed{NF = 6 \text{ dB}}$$

Q.6) Determine equivalent noise temperature corresponding to noise figure of 6dB. Assume 290K for reference temperature

Sol: Given:

Reference temp ( $T$ ) = 290 K

Noise figure (NF) = 6dB

We know,

$$\begin{aligned} T_e &= T(NF - 1) \\ &= 290 \times (6 - 1) \end{aligned}$$

$$\boxed{T_e = 1450 \text{ K}}$$

$\therefore$  Equivalent noise temperature = 1450 K.