

B. TECH (CSE) & B. TECH (CSE) + MBA

**FOURTH SEMESTER END TERM EXAMINATION :
APRIL – 2013**

THEORY OF AUTOMATA & COMPUTATION

Time : 3 Hrs.

Maximum Marks : 70

Note: Attempt questions from all sections as directed.

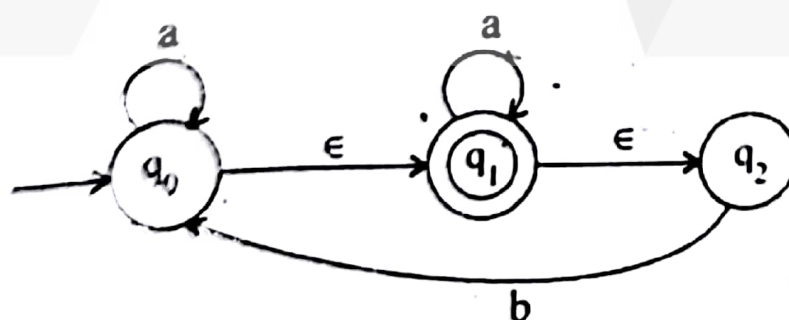
SECTION – A (30 Marks)

Attempt any 5 questions.

Each question carries 6 marks.

(a) Define Automata and it's applications.
Differentiate Finite Automata and Cellular
Automata. (2)

(b) Can NFA simulate a DFA ? Construct a DFA
from the following C-NFA and also compute C-
Closure of each state. (1+2+1)



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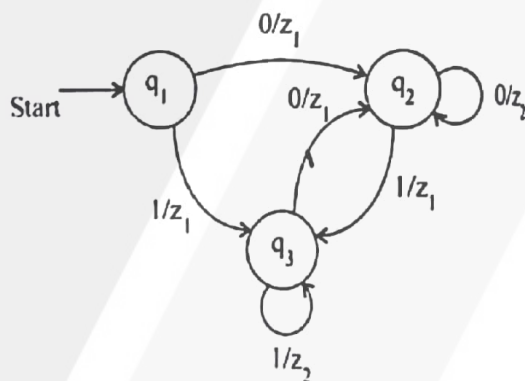
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2. (a) Differentiate 2 DFA and DFA. Write down Crossing Sequences for the string 101001 and DFA given below

| | 0 | 1 |
|-------------------|------------|------------|
| $\rightarrow q_1$ | (q_1, R) | (q_2, R) |
| $* q_2$ | (q_2, R) | (q_3, L) |
| q_3 | (q_1, R) | (q_3, L) |

- (b) Can Moore Machine simulate a Mealy Machine or vice versa? Give justification in support of your answer and also construct Moore Machine for the given Mealy Machine.

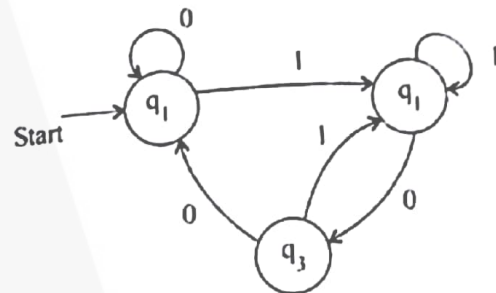


3. (a) What is Linear Bounded Automata (LBA)? Explain its importance in context of Context Sensitive Languages.

- (b) State and Prove Arden's Theorem. Construct Regular Expression corresponding to the following

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- (a) Prove or Disprove the following:

- (i) $C + 0(0+1)^* + (0+1)^* 00(0+1)^* = [(1^*0)^* 01^*]^*$
(ii) $L = \{a^n b^n c^n : n \geq 1\}$ is not regular (2+2)

- (b) What is ambiguous Grammar? Check the ambiguity of the following grammar

$$S \longrightarrow a S / a S b S / C \quad (1+1)$$

5. (a) Differentiate Context Free Grammars and Regular Grammars. Construct Left Linear and Right Linear Grammar for the following:

$$a(ba)^* \quad (2)$$

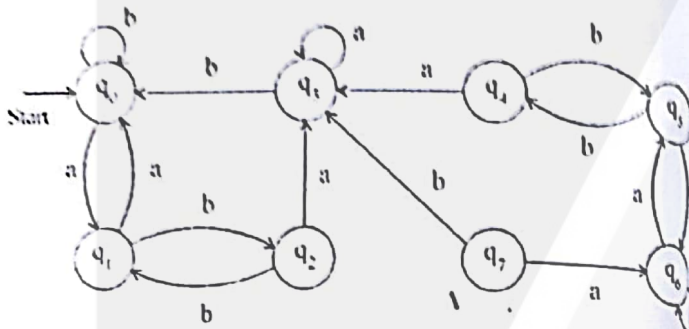
- (b) State the Myhill Nerode Theorem and its use. Also apply the Myhill Nerode Theorem on the following DFA.

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(72)

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6. (a) Explain the term Computability in context Automata and also differentiate the following Partial functions, Total functions and Primitive recursive functions (1)

- (b) Design a Push down Automata for the following Language

$$L = \{a^n b^n : n > 0\}$$

SECTION - B

(20 Marks)

Attempt any two questions.

Each question carries 10 marks.

7. (a) State Decision Algorithms for Context free language. Explain the CYK algorithm and check the membership and also construct matrix of input string baaba for the grammar

$$S \longrightarrow AB / BC$$

$$A \longrightarrow BA / a$$

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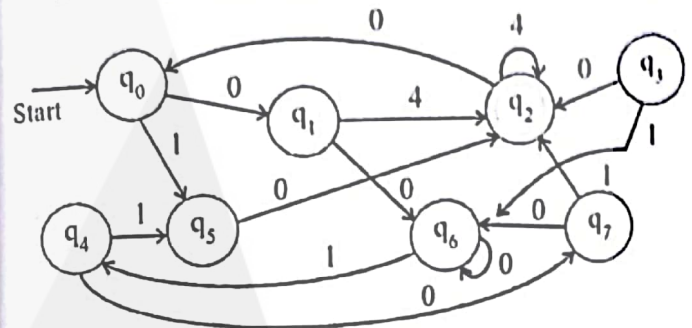
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$$B \longrightarrow CC / b$$

$$C \longrightarrow AB / a$$

(1+2+3)

- (b) Construct Minimum State Automata from the following Automata. (4)



8. (a) State the Pumping Lemma for Context Free Languages. Also Prove or disprove that

$$L = \{a^n b^m c^p : n < m < p\} \text{ is not CFL} \quad (2+2)$$

- (b) What are CNF and GNF of context free grammar? Explain with examples. Convert the following Grammar into GNF form

$$G = (\{S_1, S_2, S_3\}, \{a, b\}, P, S_1)$$

P consist of the following:

$$S_1 \longrightarrow S_2 S_3$$

$$S_2 \longrightarrow S_3 S_1 / b$$

$$S_3 \longrightarrow S_1 S_2 / a$$

(2+4)

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9. (a) (i) Construct a PDA for the following:

$$L = \{a^m b^n c^m d^n : m, n \geq 1\}$$

- (ii) Construct CFG from the following PDA

$$A = (\{q_0, q_1\}, \{a, b\}, \{a, z_0\}, \hat{\delta}, q_0, z_0)$$

$\hat{\delta}$ is given as

$$\hat{\delta}(q_0, a, z_0) = \{(q_0, a z_0)\}$$

$$\hat{\delta}(q_0, a, a) = \{(q_0, aa)\}$$

$$\hat{\delta}(q_0, b, a) = \{(q_1, a)\}$$

$$\hat{\delta}(q_1, b, a) = \{(q_1, a)\}$$

$$\hat{\delta}(q_1, a, a) = \{(q_1, C)\}$$

$$\hat{\delta}(q_1, C, z_0) = \{(q_1, C)\}$$

- (b) State Chomsky Hierarchy and also differentiate the Recursive Languages and Recursive Enumerable Languages.

SECTION - C

(20 Marks)

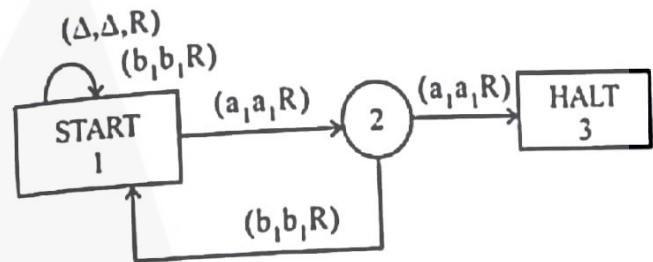
(Compulsory)

10. (a) What do you mean by Undecidability? Explain the Halting Problem of Turing Machine and explain whether it is Solvable or not. Write down the Language accepted by the following Turing Machine

(72)

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- (b) (i) What do you mean by Post Correspondence Problem (PCP)? Whether PCP is decidable or not Explain the application of PCP.

(2+1+1)

- (ii) Does the PCP with the following lists

$$X = (b, bab^3, ba) \text{ and } Y = (b^3, ba, a)$$

Has a solution? If so then write all the possible solutions.

(2)

- (c) (i) Design the Turing Machine which accepts the Language which contains the strings of PALINDROME over alphabet $\Sigma = \{a, b\}$.

(4)

- (ii) Design the Turing Machine for the Language

$$L = \{a^n b^{2n} : n \geq 1\}$$

(4)
