Printed Pages: 02   **Sub Code: RCS403**
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B TECH
(SEM-IV) THEORY EXAMINATION 2018-19
THEORY OF AUTOMATA AND FORMAL LANGUAGES

Time: 3 Hours   *Total Marks: 70*
Note: Attempt all Sections. If require any missing data; then choose suitably.

SECTION A

1.   **Attempt *all* questions in brief.**   **2 x 7 = 14**

   a.   For the given language $L_1 = \varepsilon$, $L_2 = \{a\}$, $L_3 = \emptyset$. Compute $L_1 L_2^* \cup L_3^*$.
   b.   Design a FA to accept the string that always ends with 101.
   c.   Write regular expression for set of all strings such that number of a's divisible by 3 over $\Sigma = \{a,b\}$
   d.   Construct the CFG for the Language $L = \{a^{2n}b^n \mid n>=3\}$.
   e.   What do you mean by ε-Closure in FA?
   f.   Explain Universal TM.
   g.   Explain Two Stack PDA.

SECTION B

2.   **Attempt any *three* of the following:**   **7 x 3 = 21**

   a.   Construct a minimum state DFA from given FA
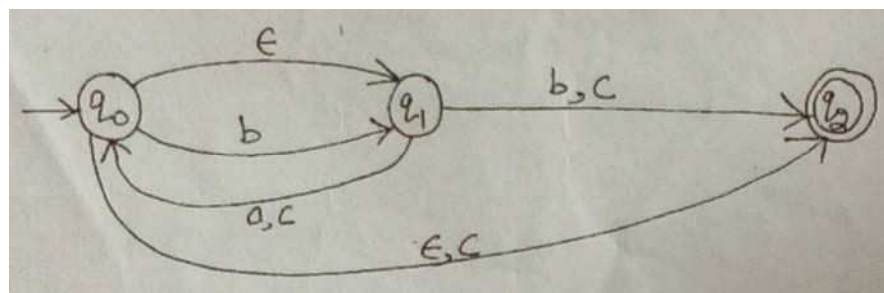

Fig. 1

   b.   Find the regular expression corresponding to the finite automata given bellow:
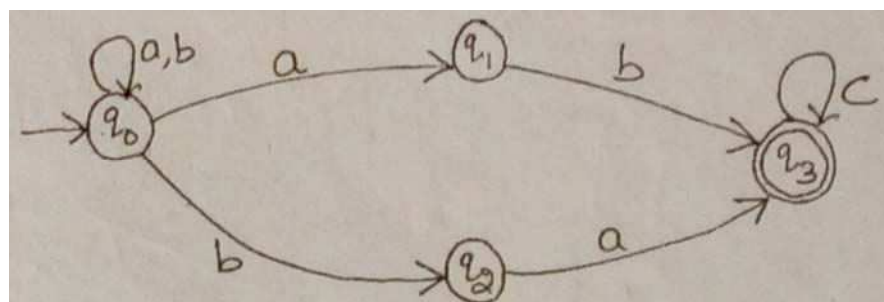

Fig. 2

    c.   Convert the following CFG to its equivalent GNF:
                $S \rightarrow AA \mid a$, $A \rightarrow SS \mid b$.

    d.   Design a PDA for the following language:
                $L = \{a^i b^j c^k \mid i = j \text{ or } j = k\}$

    e.   Design a TM for the following language:
                $L = \{ a^{n+2} b^n \mid n > 0 \}$

SECTION C

3.   **Attempt any *one* part of the following:**   **7 x 1 = 7**

    (a)   Design FA for ternary number divisible by 5.

    (b)   Explain Myhill-Nerode Theorem using suitable example.

4.   **Attempt any *one* part of the following:**   **7 x 1 = 7**

    (a)   Prove that the following Language $L = \{a^n b^n\}$ is not regular

    (b)   Explain the Closure properties of regular expression.

5.   **Attempt any *one* part of the following:**   **7 x 1 = 7**

    (a)   Design the CFG for the following language:
            i) $L = \{0^m 1^n \mid m \neq n \ \& \ m,n \geq 1\}$
            ii) $L = \{a^l b^m c^n \mid l + m = n \ \& \ l,m \geq 1\}$

    (b)   Prove that the following Language $L = \{a^n b^n c^n\}$ is not Context Free.

6.   **Attempt any *one* part of the following:**   **7 x 1 = 7**

    (a)   Design a PDA for the Language $L = \{WW^R \mid W = \{a,b\}^*\}$

    (b)   Generate CFG for the given PDA M is defined as
            $M = (\{q_0, q_1\}, \{0,1\} \ \{x, z_0\}, \delta, q_0, z_0, q_1)$ where δ is given as follows:
            $\delta (q_0,1, z_0) = (q_0, xz_0)$
            $\delta (q_0,1, x) = (q_0, xx)$
            $\delta (q_0,0, x) = (q_0, x)$
            $\delta (q_0, \varepsilon, x) = (q_1, \varepsilon)$
            $\delta (q_1, \varepsilon, x) = (q_1, \varepsilon)$
            $\delta (q_1,0, x) = (q_1, xx)$
            $\delta (q_1,0, z_0) = (q_1, \varepsilon)$

7.   **Attempt any *one* part of the following:**   **7 x 1 = 7**

    (a)   Design a TM for the following language:
            $L = \{ a^n b^n c^n \mid n \geq 1\}$

    (b)   Write short note on:
            i)   Recursive Language and Recursively Enumerable Language.
            ii) PCP problem and Modified PCP Problem