Large-scale structure of complex networks (Part 2)

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2017-12-27

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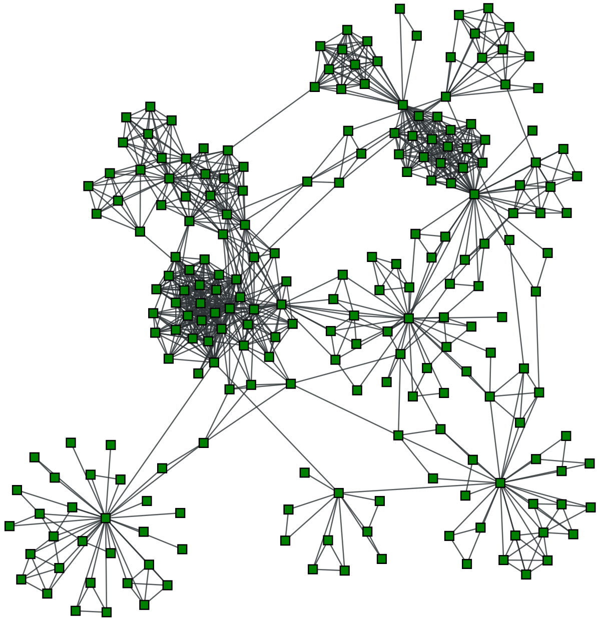
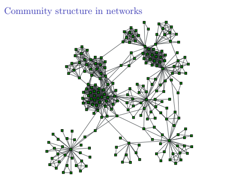
Hello

Community structure in networks





Network of coauthorships in a university department

Community structure in networks

What are communities?

- **Traditional definition**: Groups of nodes with a high internal link density
- **Modern definition**: Nodes with similar connection probabilities to the rest of the network

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Communities in the real-world networks

- **Social networks**:
  - Friend-circles
  - Research communities
  - Co-workers
- **World Wide Web**:
  - Pages with similar contents
  - Webpages under the same domain (e.g. Wikipedia)
- **Biological network**:
  - Proteins with similar roles in protein interaction networks
  - Chemicals together taking part in chemical reactions in metabolic networks
  - Communities in neuronal networks

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Community detection

Detecting communities is important!

- Communities are building blocks of networks
- Communities allow us to see “the big picture”
- Functional/Autonomous units
- Non-trivial effects on the processes on networks

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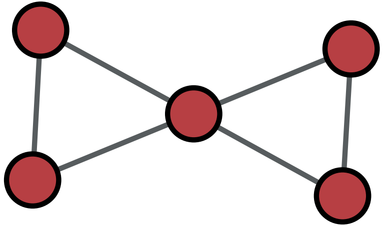
Graph partitioning

Problem of dividing a graph in a given number of groups of given sizes such that the number of links between the groups is minimized



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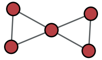

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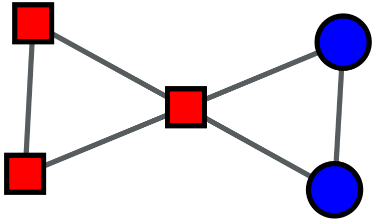

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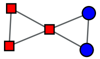

Partitioning is hard!

- Graph with n vertices
- Find two groups with sizes n_1 and n_2 such that the cut size is minimum
- Number of ways: $\frac{n!}{n_1!n_2!} \approx \frac{2^{n+1}}{\sqrt{n}}$

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Community detection is harder!

- **Graph partitioning**
  - well defined
  - Number of groups is fixed
  - Sizes of the groups are fixed
  - Divide even if no good division exists
- **Community detection**
  - ill-defined
  - Number of groups depends on the structure of the network
  - Sizes of the groups depend on the structure of the network
  - Discover natural fault lines

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Too many algorithms

- Girvan-Newman algorithm
- Modularity maximization
- Spectral decomposition
- Clique-percolation
- Radom walk methods
- Statistical inference
- Label propagation
- Hierarchical clustering

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I can go on

“The” simplest community detection problem

- Bisecting a graph with n nodes
- Group sizes are not fixed
- Minimum cut size?

Empty group

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A different measure of the quality of division is required..

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Different measure

Quantification of community structure

- Fewer than expected edges between the groups

Quantification of community structure

- Fewer than expected edges between the groups

few edges = expected edges = not a good division

Quantification of community structure

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- Equivalently, more than expected edges inside the groups

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Remember assortativity

Quantification of community structure

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- Assortativity mixing and modularity

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Divide network using modularity

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- Look for divisions with high modularity

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Heuristics are needed

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- Modularity maximization is hard

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Heuristic algorithms for modularity maximization

- **Agglomerative algorithms:**
  - Hierarchical clustering
  - Louvain method
  - CNM algorithm
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Newman-Girvan algorithm

- Look for edges between the communities
- Edge betweenness

Newman-Girvan algorithm

- Look for edges between the communities
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Let's have a look at the edge betweenness

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