Cryptography

Assignment :05.

Elgamal encryption and decryption using elliptic curve cryptography.

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Algorithm :-

Library function which will be used often :

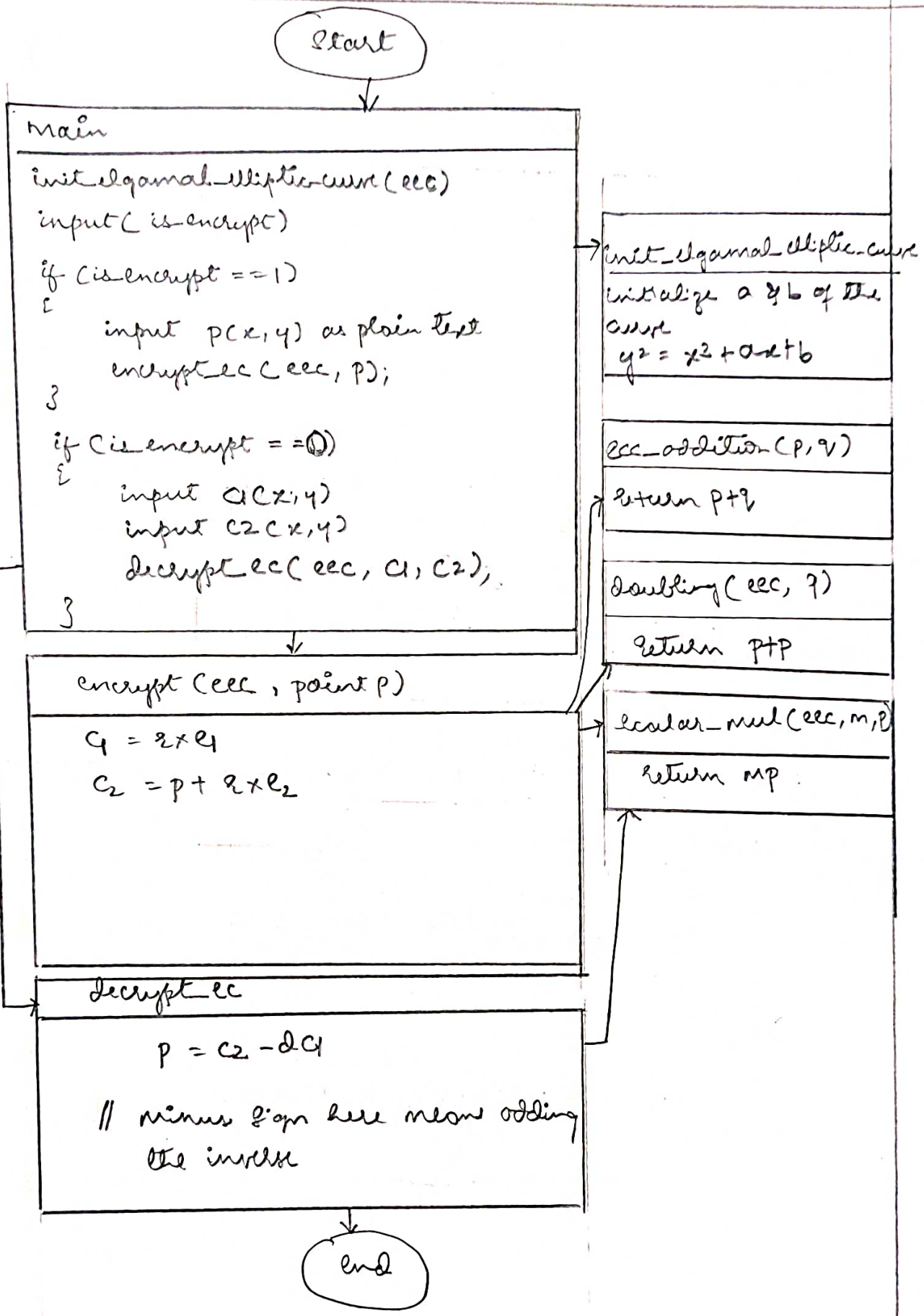
```
point ecc_addition ( elgamal_elliptic_curve, ecc , point p, point q)
{
    return p+q;
}

point doubling ( ecc, point p)
{
    return  p+p
}
point scalar_mul (ecc, int n, point p)
{
    return np
}

init_elgamal_elliptic_curve
{
    // y^2 =  x^3 + ax + b.
     initialize a, b
}
Void destroy_elgam_ec
  {
     free (ecc)
  }
```

```
Void encrypt_ec( eec, point p)
{
    c1 = r x g
    c2 = p + r x k2
}
Void decrypt_ec (eec, point c1, point c2)
{
    p = c2 - (d x c1)
    // minus sign here means adding with the inverse
}
int main()
{
    init_elgamal_elliptic_curve(eec);
    input is_encrypt;
    if (is_encrypt == 1)
    {
        input p(x,y) as plain text
        encrypt_ec(eec, p);
    }
    if (is_encrypt == 0)
    {
        input c1(x,y)
        input c2(x,y)
        decrypt_ec (eec, c1, c2);
    }
    destroy_elgamal_ec (eec
}
```

Flowchart :


Start
main
init_elgamal_elliptic_curve(ecc)
input(is_encrypt)
if (is_encrypt == 1)
{
input p(x,y) as plain text
encrypt_ecc(ecc, p);
}
if (is_encrypt == 0)
{
input c1(x,y)
input c2(x,y)
decrypt_ecc(ecc, c1, c2);
}
init_elgamal_elliptic_curve
initalize a & b of the curve
y² = x³ + ax + b
ecc_addition(p, q)
return p+q
doubling(ecc, p)
return p+p
scalar_mul(ecc, m, p)
return mp
encrypt(ecc, point p)
c1 = r × e1
c2 = p + r × e2
decrypt_ecc
p = c2 - dc1
// minus sign here means adding the inverse
end

Example:

$E_{67}(2,3)$ ---⇒ mod is over 67

$a = 2$

$b = 3$

Bob/Recipient:

$q = (2, 22)$

$d = 4$

$e_2 = d \times q = 4(2, 22) = (13, 45)$

Announce $[E, q, e_2]$

Alice/Sender:

Send $P(24, 26)$

$r = 2$

$c_1 = (35, 1)$ i.e., $c_1 = r \times q = 2 \times (2, 22) = (35, 1)$

$c_2 = P + r \times e_2 = (22, 26) + 2 \times (13, 35) = (21, 44)$

Send (c_1, c_2)

Bob:

$P = c_2 - dc_1$

$dc_1 = 2(35, 1) = (22, 25)$

dc_1 inverse $= (23, 25)$

$P = c_2 + (\text{Inverse of } dc_1)$

$= (21, 44) + (23, 25)$

$\boxed{P = (24, 26)}$

—— X ——