

## ② Huffman coding & decoding:

Why Huffman coding and decoding is needed??  
Let us take an example to understand.

Example:

Normal coding:

| Char   | Ascii value | frequency | code |
|--------|-------------|-----------|------|
| A      | 65          | 3         | 000  |
| B      | 66          | 5         | 001  |
| C      | 67          | 6         | 010  |
| D      | 68          | 4         | 011  |
| E      | 69          | 2         | 100  |
| Total: |             | 20        |      |

To store 20 alphabets we need  $(20 \times 3) = 60$  bits

Huffman coding

(i) sort according to frequency.



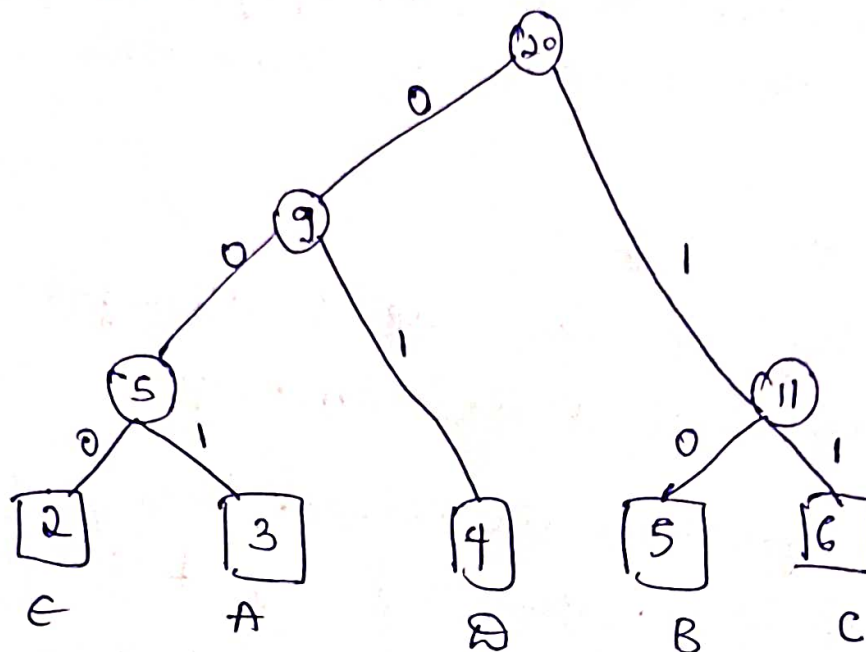
(ii) select the 2 smallest frequency and form a node.

(iii) Repeat the process untill all the nodes are covered.

EV

left path assign 0

Right path assign 1



|   | Huffman codes |
|---|---------------|
| A | 001           |
| B | 10            |
| C | 11            |
| D | 01            |
| E | 000           |

To store 20 alphabets we need =  $\overset{A}{\underset{\text{frequency}}{3 \times 3}} + \overset{B}{\underset{\text{no of bits}}{(5 \times 2)}} + \overset{C}{(6 \times 2)} + \overset{D}{(4 \times 2)} + \overset{E}{(2 \times 3)}$

$$= 35 \text{ bits}$$

$$\left\{ \begin{array}{l} \text{Difference} \\ \text{b/w normal} \\ \text{\& Huffman} \end{array} \right\} = 60 - 35 = 25 //$$

∴ we saved 25 bits using Huffman coding.

### Time complexity:

$$O(n \log n)$$

where  $n$  is the number of alphabets.

Since Huffman coding will use the min-heap. And min heap formation takes  $O(n \log n)$  time for its creation. This algorithm also takes the same time.

### Huffman decoding:

→ Given the character, its frequencies, we will be able to construct the min-heap.

→ Once you have the encoded string, travel left if '0' comes, travel right if '1' comes.

→ The decoded string will be found.

### Time complexity:

Since this will also use min-heap. It is  $O(n \log n)$

$$O(n \log n)$$

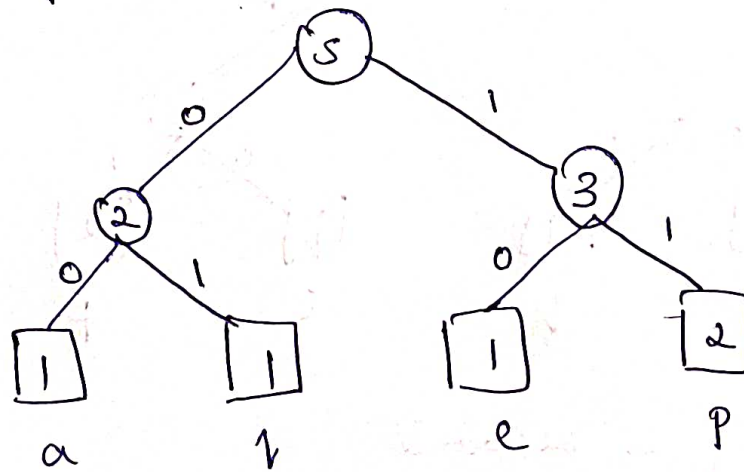
# Huffman encoding

Input:

Enter a word: apple

|   | frequency |
|---|-----------|
| a | 1         |
| p | 2         |
| t | 1         |
| e | 1         |

Output:



|   | Huffman codes |
|---|---------------|
| a | 00            |
| e | 10            |
| t | 01            |
| p | 11            |

Encoded string: a p p t e  
00 11 11 01 10

## Huffman decoding :-

Input:

Enter the frequency table.

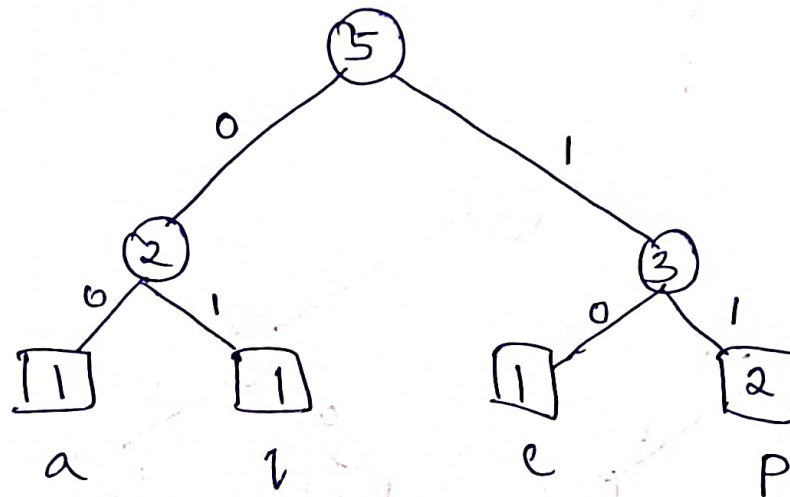
|   | frequency |
|---|-----------|
| a | 1         |
| p | 2         |
| t | 1         |
| e | 1         |

Enter the Encoded string :

001110110

Output :

create min-heap using frequency table.



Encoded string is decoded

|           |           |           |           |           |
|-----------|-----------|-----------|-----------|-----------|
| <u>00</u> | <u>11</u> | <u>11</u> | <u>01</u> | <u>10</u> |
| <hr/>     |           |           |           |           |
| a         | p         | p         | l         | e         |

∴ Decoded string: apple.

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