

```

# Let the three system of linear equations be:
# 1.  $3x_1 - x_2 + x_3 = 2$ 
# 2.  $-5x_1 + 4x_2 + 2x_3 = 4$ 
# 3.  $3x_1 - 2x_2 + 6x_3 = -7$ 

# As per Gauss-Seidel iterative method, let's assume initial values of
 $[x_1, x_2, x_3] = [0, 0, 0]$ 
# As per the theorem,  $x^{(k+1)} = \text{inv}(L)[b - Ux^{(k)}]$  for a given
equation  $Ax = b$ ,  $L$  = strictly Lower triangular matrix  $U$  = strictly
upper triangular matrix

```

```

from numpy import array, dot
import numpy as np
from numpy.linalg import inv

```

```

# Number of iterations to be considered
n=8

```

```

A = array([[3.0, -1.0, 1.0], [-5.0, 4.0, 2.0], [3.0, -2.0, 6.0]])
B = array([2.0, 4.0, -7.0])
initial = array([0.0, 0.0, 0.0])

```

```

U = np.triu(A,1)
L = np.tril(A,0)
inverse_L = inv(L)

```

```

# $x^{(k+1)} = \text{inv}(L)[b - Ux^{(k)}]$ 

```

```

for i in range(n):
    Neg_Ux_plusB = -dot(U,initial)+B
    initial = dot(inverse_L, Neg_Ux_plusB)
    print(i+1,np.round(initial,7))

```

```

1 [ 0.6666667  1.8333333 -0.8888889]
2 [ 1.5740741  3.412037  -0.816358 ]
3 [ 2.0761317  4.0033436 -0.8702846]
4 [ 2.2912094  4.2991541 -0.87922  ]
5 [ 2.3927914  4.4305992 -0.8861959]
6 [ 2.4389317  4.4917626 -0.8888783]
7 [ 2.4602136  4.5197062 -0.8902048]
8 [ 2.4699703  4.5325653 -0.8907967]

```

```

# Second method of solving the above set of equations using
numpy.linalg.solve

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```

import numpy as np
from scipy.linalg import solve

```

```

def gauss_seidel(A, B, initial2, n2):

```

```

L = np.tril(A)
U = A - L
for i in range(n):
    initial2 = np.dot(np.linalg.inv(L), B - np.dot(U, initial2))
    print(str(i+1))
    print(initial2)
return initial2

# Number of iterations to be considered
n2 = 8

A = np.array([[3.0, -1.0, 1.0], [-5.0, 4.0, 2.0], [3.0, -2.0, 6.0]])
B = [2.0, 4.0, -7.0]
initial2 = [0.0, 0.0, 0.0]

print(gauss_seidel(A, B, initial2, n2))
print(solve(A, B))

1
[ 0.66666667  1.83333333 -0.88888889]
2
[ 1.57407407  3.41203704 -0.81635802]
3
[ 2.07613169  4.00334362 -0.87028464]
4
[ 2.29120942  4.29915409 -0.87922001]
5
[ 2.39279137  4.43059922 -0.88619595]
6
[ 2.43893172  4.49176262 -0.88887832]
7
[ 2.46021365  4.51970622 -0.89020475]
8
[ 2.46997032  4.53256528 -0.89079674]
[ 2.46997032  4.53256528 -0.89079674]
[ 2.47826087  4.54347826 -0.89130435]

```

By comparing the above two methods, we can conclude that the values of [x1, x2, x3] are close in both the cases.