

**Course Name : Data Structure using C**

**Topic: Sorting**



## Sorting-Introduction

- Sorting means **arranging** the elements of an array so that they are placed in either **ascending or descending order**.
- If A is an array, then the elements of A are arranged in a sorted order (ascending order) in such a way that  $A[0] < A[1] < A[2] < \dots < A[N]$ .
- A **sorting algorithm** is defined as an algorithm that puts the elements of a list in a **certain order**, which can be either **numerical** order, **lexicographical** order, or any **user-defined** order.
- Efficient sorting algorithms are widely used to **optimize** the use of other algorithms like **search and merge algorithms** which require sorted lists to work correctly.

## Sorting-Types

- **Two types :**
  - **Internal sorting** which deals with sorting the data stored in the computer's memory
  - **External sorting** which deals with sorting the data stored in files. External sorting is applied when there is voluminous data that cannot be stored in the memory.

## Sorting-Methods

- **Bubble Sort**
- **Insertion Sort**
- **Selection Sort**
- **Quick Sort**
- **Merge Sort**

## Bubble Sort

- Most simple method
- Sorts the array elements by repeatedly moving the largest element to the highest index position of the array segment (for ascending order)
- Consecutive adjacent pairs of elements in the array are compared with each other
- If the element at the lower index is greater than the element at the higher index, the two elements are interchanged so that the element is placed before the bigger one
- This process will continue till the list of unsorted elements exhausts

## Bubble Sort - Technique

- The basic methodology of the working of bubble sort is given as follows:
  - (a) In **Pass 1**, **A[0]** and **A[1]** are compared, then **A[1]** is compared with **A[2]**, **A[2]** is compared with **A[3]**, and so on. Finally, **A[N-2]** is compared with **A[N-1]**. **Pass 1** involves **n-1** comparisons and places the **biggest element** at the **highest index** of the array.
  - (b) In **Pass 2**, **A[0]** and **A[1]** are compared, then **A[1]** is compared with **A[2]**, **A[2]** is compared with **A[3]**, and so on. Finally, **A[N-3]** is compared with **A[N-2]**. **Pass 2** involves **n-2** comparisons and places the **second biggest element** at the **second highest index** of the array.
  - (c) In **Pass 3**, **A[0]** and **A[1]** are compared, then **A[1]** is compared with **A[2]**, **A[2]** is compared with **A[3]**, and so on. Finally, **A[N-4]** is compared with **A[N-3]**. **Pass 3** involves **n-3** comparisons and places the **third biggest element** at the **third highest index** of the array.
  - (d) In **Pass n-1**, **A[0]** and **A[1]** are compared so that **A[0] < A[1]**. After this step, **all the elements of the array are arranged in ascending order**.



## Bubble Sort - Example

- Consider an array  $A[]$  that has the following elements  $A[] = \{30, 52, 29, 87, 63, 27, 19, 54\}$
- Pass 1:**
  - (a) Compare **30** and **52**. Since  **$30 < 52$** , no swapping is done.
  - (b) Compare **52** and **29**. Since  **$52 > 29$** , swapping is done.  
**30, 29, 52, 87, 63, 27, 19, 54**
  - (c) Compare **52** and **87**. Since  **$52 < 87$** , no swapping is done.
  - (d) Compare **87** and **63**. Since  **$87 > 63$** , swapping is done.  
**30, 29, 52, 63, 87, 27, 19, 54**
  - (e) Compare **87** and **27**. Since  **$87 > 27$** , swapping is done.  
**30, 29, 52, 63, 27, 87, 19, 54**
  - (f) Compare **87** and **19**. Since  **$87 > 19$** , swapping is done.  
**30, 29, 52, 63, 27, 19, 87, 54**
  - (g) Compare **87** and **54**. Since  **$87 > 54$** , swapping is done.  
**30, 29, 52, 63, 27, 19, 54, 87**
- After end of the **first pass**, the **largest element** is placed at the **highest index of the array**. All the other elements are still unsorted.
- This is continued in **next few passes** until **all the elements are sorted in ascending order**.

## Bubble Sort - Algorithm

### BUBBLE\_SORT(A, N)

**Step 1:** Repeat **Step 2** For  $I = 0$  to  $N-1$

**Step 2:** Repeat For  $J = 0$  to  $N - I - 1$

**Step 3:** IF  $A[J] > A[J + 1]$   
SWAP  $A[J]$  and  $A[J+1]$

[END OF INNER LOOP]

[END OF OUTER LOOP]

**Step 4:** EXIT



## Bubble Sort - Optimization

- What if the array is **already sorted**?
- **No swapping is done**, still to continue **n-1 passes** unnecessarily.
- **Optimize** the bubble sort once the array is found to be sorted (**using a flag**)
- Set a variable flag to **TRUE** before every pass, change the status to **FALSE** if any swapping is performed

## Bubble Sort – Optimization Code

```
void bubble_sort(int *arr, int n)
{
    int i, j, temp, flag = 0;
    for(i=0; i<n; i++)
    {
        flag=0;
        for(j=0; j<n-i-1; j++)
        {
            if(arr[j]>arr[j+1])
            {
                flag = 1;
                temp = arr[j+1];
                arr[j+1] = arr[j];
                arr[j] = temp;
            }
        }
        if(flag == 0) // array is sorted
            break;
    }
}
```

12,15,23,34,45,56,68,89,90

## Insertion Sort

- This algorithm **inserts** each item into its **proper place** in the **final list**.
- To move the **current data element** past the **already sorted values** and **repeatedly interchanging it** with the **preceding value** until it is in its **correct place**.

## Insertion Sort-Technique

- Insertion sort works as follows:
- The array of values to be sorted is divided into two sets. One that stores sorted values and another that contains unsorted values.
- The sorting algorithm will proceed until there are elements in the unsorted set.
- Suppose there are  $n$  elements in the array. Initially, the element with index  $0$  (assuming  $LB = 0$ ) is in the sorted set. Rest of the elements are in the unsorted set.
- The first element of the unsorted partition has array index  $1$  (if  $LB = 0$ ).
- During each iteration of the algorithm, the first element in the unsorted set is picked up and inserted into the correct position in the sorted set.

## Insertion Sort-Explanation

- Sort the values in the array using insertion sort:

39	9	45	63	18	81	108	54	72	36	Pass 1	39	9	45	63	18	81	108	54	72	36	
Pass 2	9	39	45	63	18	81	108	54	72	36	Pass 3	9	39	45	63	18	81	108	54	72	36
Pass 4	9	39	45	63	18	81	108	54	72	36	Pass 5	9	18	39	45	63	81	108	54	72	36
Pass 6	9	18	39	45	63	81	108	54	72	36	Pass 7	9	18	39	45	63	81	108	54	72	36
Pass 8	9	18	39	45	54	63	81	108	72	36	Pass 9	9	18	39	45	54	63	72	81	108	36
Pass 10	9	18	36	39	45	54	63	72	81	108											
Unsorted											Sorted										

- Explanation:**

- Initially, **A[0]** is the only element in the sorted set. In **Pass 1**, **A[1]** will be placed either before or after **A[0]**, so that the array A is sorted. In **Pass 2**, **A[2]** will be placed either before **A[0]**, in between **A[0]** and **A[1]**, or after **A[1]**. In **Pass 3**, **A[3]** will be placed in its proper place. In **Pass N-1**, **A[N-1]** will be placed in its proper place to keep the array sorted.

## Insertion Sort-Algorithm

### INSERTION-SORT (ARR, N)

**Step 1:** Repeat **Steps 2 to 5** for  $K = 1$  to  $N - 1$

**Step 2:** SET  $TEMP = ARR[K]$

**Step 3:** SET  $J = K - 1$

**Step 4:** Repeat while  $TEMP \leq ARR[J]$   
                SET  $ARR[J + 1] = ARR[J]$   
                SET  $J = J - 1$

[END OF INNER LOOP]

**Step 5:** SET  $ARR[J + 1] = TEMP$

[END OF LOOP]

**Step 6:** EXIT

39	9	45	63	18	81	108	54	72	36
----	---	----	----	----	----	-----	----	----	----

## Selection Sort

### Technique:

First find the **smallest value** in the array and place it in the first position. Then, find the **second smallest value** in the array and place it in the second position. Repeat this procedure until the **entire array is sorted**. Therefore,

In **Pass 1**, find the position **POS** of the **smallest value** in the array and then swap **ARR[POS]** and **ARR[0]**. Thus, **ARR[0]** is sorted.

In **Pass 2**, find the position **POS** of the **smallest value** in sub-array of  $N-1$  elements. Swap **ARR[POS]** with **ARR[1]**. Now, **ARR[0]** and **ARR[1]** is sorted.

In **Pass  $N-1$** , find the position **POS** of the **smaller of the elements** **ARR[ $N-2$ ]** and **ARR[ $N-1$ ]**. Swap **ARR[POS]** and **ARR[ $N-2$ ]** so that **ARR[0], ARR[1], ..., ARR[ $N-1$ ]** is sorted.



## Selection Sort-Example

**Sort the values in the array using Selection Sort:**

39	9	81	45	90	27	72	18
----	---	----	----	----	----	----	----

PASS	POS	ARR[0]	ARR[1]	ARR[2]	ARR[3]	ARR[4]	ARR[5]	ARR[6]	ARR[7]
1	1	9	39	81	45	90	27	72	18
2	7	9	18	81	45	90	27	72	39
3	5	9	18	27	45	90	81	72	39
4	7	9	18	27	39	90	81	72	45
5	7	9	18	27	39	45	81	72	90
6	6	9	18	27	39	45	72	81	90
7	6	9	18	27	39	45	72	81	90

## Selection Sort-Algorithm

### SELECTION SORT(ARR, N)

**Step 1:** Repeat **Steps 2 and 3** for  $K = 0$  to  $N-1$   
**Step 2:** CALL **SMALLEST**(ARR, K, N, POS)  
**Step 3:** SWAP  $A[K]$  with  $ARR[POS]$   
[END OF LOOP]  
**Step 4:** EXIT

### SMALLEST (ARR, K, N, POS)

**Step 1:** [INITIALIZE] SET  $SMALL = ARR[K]$   
**Step 2:** [INITIALIZE] SET  $POS = K$   
**Step 3:** Repeat for  $J = K+1$  to  $N-1$   
    IF  $SMALL > ARR[J]$   
        SET  $SMALL = ARR[J]$   
        SET  $POS = J$   
[END OF IF]  
[END OF LOOP]  
**Step 4:** RETURN POS

## Selection Sort-Algorithm Explanation

In the algorithm, during the **K<sup>th</sup>** pass, find the position **POS** of the **smallest elements** from **ARR[K], ARR[K+1], ..., ARR[N]**.

To find the **smallest element**, use a variable **SMALL** to hold the smallest value in the sub-array ranging from **ARR[K]** to **ARR[N]**.

Then, swap **ARR[K]** with **ARR[POS]**. This procedure is repeated until all the elements in the array are sorted.

## Merge Sort

This algorithm works by using a **divide-and-conquer** strategy - **divide**, **conquer** and **combine** algorithmic paradigm.

The merge sort algorithm works as follows:

- **Divide** means **partitioning** the  $n$ -element array to be sorted into **two sub-arrays of  $n/2$  elements**. If **A** is an array containing **zero or one element**, then it is already **sorted**. However, if there are **more elements** in the array, divide **A** into two sub-arrays, **A1** and **A2**, each containing about **half of the elements** of **A**.
- **Conquer** means **sorting** the two sub-arrays **recursively** using merge sort.
- **Combine** means **merging** the **two sorted sub-arrays** of size  $n/2$  to produce the sorted array of  **$n$  elements**.

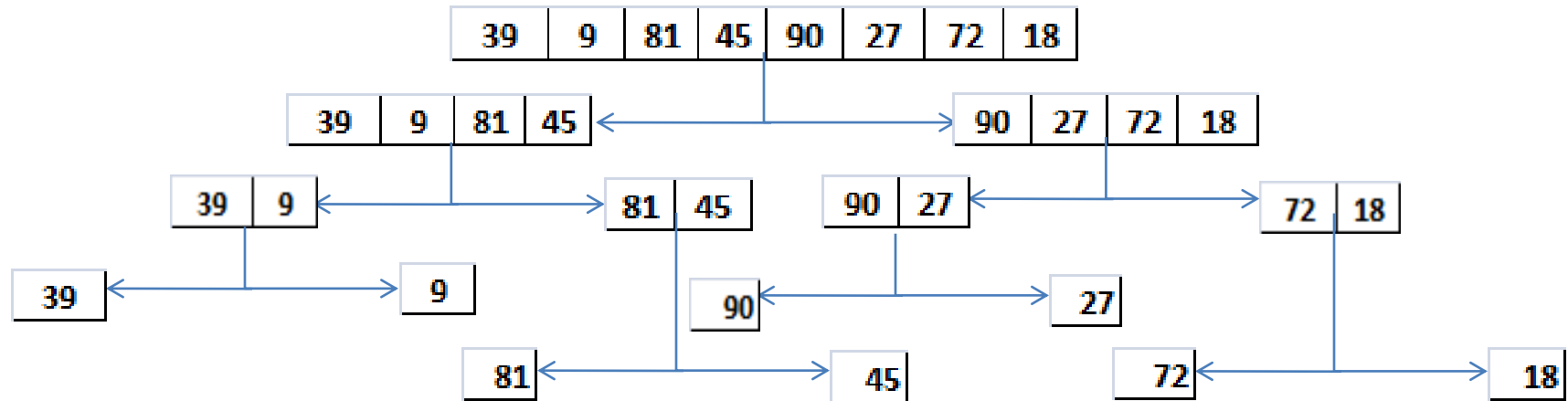
## Merge Sort-Technique

Merge sort works as follows:

- If the array is of length **0 or 1**, then it is already **sorted**.
- Otherwise, **divide the unsorted array into two sub-arrays** of about **half the size**.
- Use **merge sort algorithm recursively** to **sort** each sub-array.
- **Merge the two sub-arrays** to form a **single sorted list**.

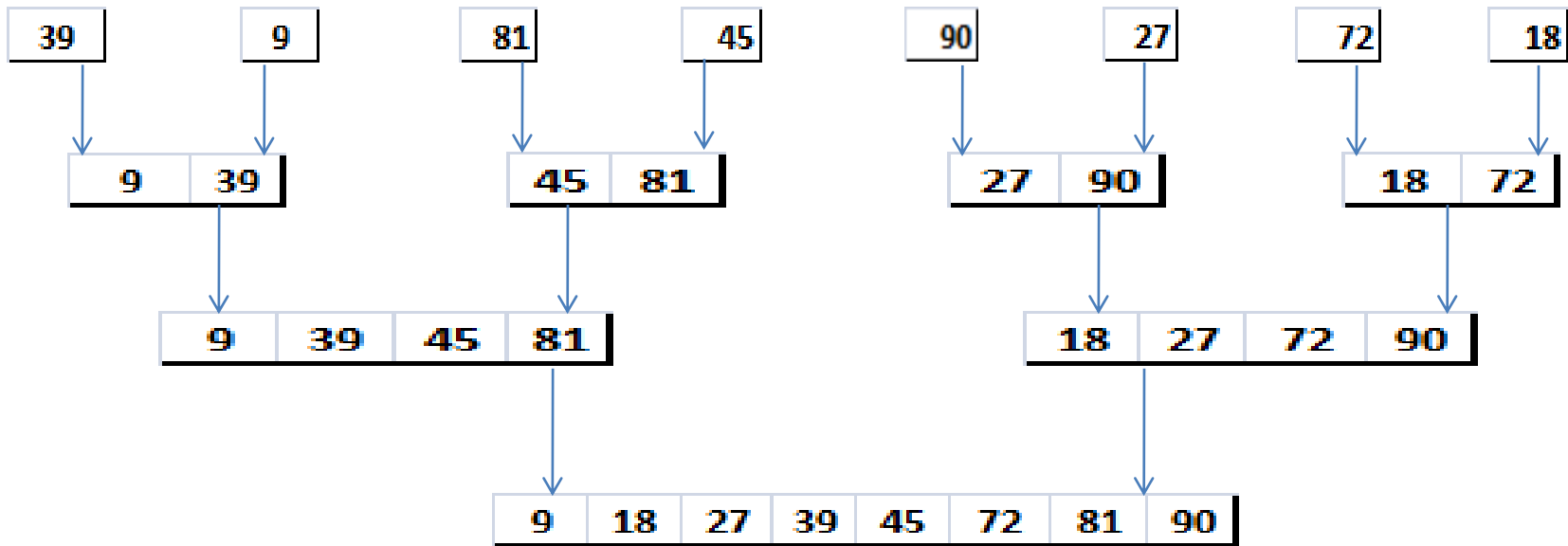
## Merge Sort-Example

Sort the values in the array using Merge sort:



Divide and Conquer the array

## Merge Sort-Example Continued



Combine the elements to form a sorted array



## Merge Sort-Example Continued

- The merge sort algorithm uses a **function merge** which **combines the sub-arrays** to form a **sorted array**.
- While the merge sort algorithm **recursively divides** the **list into smaller lists**, the **merge algorithm** conquers the list to **sort the elements in individual lists**.
- Finally, the **smaller lists** are **merged** to **form one list**.

## Merge Sort-Example Continued

- Compare  $ARR[I]$  and  $ARR[J]$ , the **smaller** of the two is placed in **TEMP** at the location specified by **INDEX** and subsequently the value **I** or **J** is incremented.

9	39	45	81	18	27	72	90	TEMP	9							
BEG, I			MID				J	END	INDEX							

9	39	45	81	18	27	72	90	TEMP	9	18						
BEG	I		MID	J			END		INDEX							

9	39	45	81	18	27	72	90	TEMP	9	18	27					
BEG	I		MID		J		END		INDEX							

9	39	45	81	18	27	72	90	TEMP	9	18	27	39				
BEG	I		MID			J	END		INDEX							

9	39	45	81	18	27	72	90	TEMP	9	18	27	39	45			
BEG		I	MID			J	END		INDEX							

9	39	45	81	18	27	72	90	TEMP	9	18	27	39	45	72		
BEG			I, MID			J	END		INDEX							

9	39	45	81	18	27	72	90	TEMP	9	18	27	39	45	72	81	
BEG			I, MID			J	END		INDEX							

- When **I** is greater than **MID**, copy the remaining elements of the **right sub-array** in **TEMP**.

9	39	45	81	18	27	72	90	TEMP	9	18	27	39	45	72	81	90
BEG			MID	I			J	END	INDEX							

## Merge Sort-Algorithm

**MERGE (ARR, BEG, MID, END)**

**Step 1:** [INITIALIZE] SET  $I = \text{BEG}$ ,  $J = \text{MID} + 1$ ,  $\text{INDEX} = 0$

**Step 2:** Repeat while  $(I \leq \text{MID})$  AND  $(J \leq \text{END})$

IF  $\text{ARR}[I] < \text{ARR}[J]$

SET  $\text{TEMP}[\text{INDEX}] = \text{ARR}[I]$

SET  $I = I + 1$

ELSE

SET  $\text{TEMP}[\text{INDEX}] = \text{ARR}[J]$

SET  $J = J + 1$

[END OF IF]

SET  $\text{INDEX} = \text{INDEX} + 1$

[END OF LOOP]

**Step 3:** [Copy the remaining elements of right sub-array, if any]

IF  $I > \text{MID}$

Repeat while  $J \leq \text{END}$

SET  $\text{TEMP}[\text{INDEX}] = \text{ARR}[J]$

SET  $\text{INDEX} = \text{INDEX} + 1$ , SET  $J = J + 1$

[END OF LOOP]

[Copy the remaining elements of left sub-array, if any]

ELSE

Repeat while  $I \leq \text{MID}$

SET  $\text{TEMP}[\text{INDEX}] = \text{ARR}[I]$

SET  $\text{INDEX} = \text{INDEX} + 1$ , SET  $I = I + 1$

[END OF LOOP]

[END OF IF]

**Step 4:** [Copy the contents of TEMP back to ARR] SET  $K = \text{INDEX}$

**Step 5:** Repeat while  $K < \text{INDEX}$

SET  $\text{ARR}[K] = \text{TEMP}[K]$

SET  $K = K + 1$

[END OF LOOP]

**Step 6:** END

## Merge Sort-Algorithm Continued

### **MERGE\_SORT(ARR, BEG, END)**

Step 1: IF BEG < END

SET MID = (BEG + END)/2

CALL MERGE\_SORT (ARR, BEG, MID)

CALL MERGE\_SORT (ARR, MID + 1, END)

MERGE (ARR, BEG, MID, END)

[END OF IF]

Step 2: END

## Quick Sort

- This algorithm (also known as **partition exchange sort**) works by using a **divide-and-conquer strategy** to divide a single unsorted array into **two smaller sub-arrays**. The quick sort algorithm works as follows:
  - Select an element **pivot** from the array elements.
  - Rearrange the elements in the array in such a way that **all elements that are less than the pivot appear before the pivot** and **all elements greater than the pivot element come after it** (equal values can go either way).
  - After such a partitioning, the pivot is placed in **its final position**. This is called the **partition operation**.
  - **Recursively sort** the two sub-arrays thus obtained. (One with sub-list of values **smaller than that of the pivot** element and the **other having higher value elements**.)
  - The base case of the recursion occurs when the array has zero or one element because in that case the array is already sorted.

## Quick Sort-Technique

Quick sort works as follows:

- 1. Set the index of the **first element** in the array to **loc** and **left variables**. Also, set the **index of the last element** of the **array to the right variable**.

That is, **loc = 0**, **left = 0**, and **right = n-1** (where n is the number of elements in the array)

- 2. Start from the element **pointed by right** and scan the array from **right to left**, comparing each element on the way with the element pointed by the variable **loc**.

That is, **a[loc]** should be **less than a[right]**.

(a) If that is the case, then simply continue comparing until **right becomes equal to loc**. Once **right = loc**, it means the pivot has been placed in its **correct position**.

(b) However, if at any point, we have **a[loc] > a[right]**, then **interchange the two values** and jump to Step 3.

(c) Set **loc = right**

## Quick Sort-Technique

- 3. Start from the element pointed by **left** and scan the array from **left to right**, comparing each element on the way with the element pointed by **loc**. That is,  $a[loc]$  should be greater than  $a[left]$ .
  - (a) If that is the case, then simply continue comparing until **left becomes equal to loc**. Once **left = loc**, it means the pivot has been placed in its correct position.
  - (b) However, if at any point, we have  $a[loc] < a[left]$ , then interchange the two values and jump to Step 2.
  - (c) Set **loc = left**.



## Quick Sort-Example

Sort the values in the array using Quick sort:

27	10	36	18	25	45
----	----	----	----	----	----

We choose the first element as the pivot.  
Set  $loc = 0$ ,  $left = 0$ , and  $right = 5$ .

27	10	36	18	25	45
$loc$					$right$
$left$					



Scan from right to left. Since  $a[loc] < a[right]$ , decrease the value of  $right$ .

27	10	36	18	25	45
$loc$					$right$
$left$					



Since  $a[loc] > a[right]$ , interchange the two values and set  $loc = right$ .

25	10	36	18	27	45
				$right$	$loc$
$left$					



Start scanning from left to right. Since  $a[loc] > a[left]$ , increment the value of  $left$ .

25	10	36	18	27	45
				$right$	$loc$
	$left$				



Since  $a[loc] < a[left]$ , interchange the values and set  $loc = left$ .

25	10	27	18	36	45
		$left$		$right$	
	$loc$				



Scan from right to left. Since  $a[loc] < a[right]$ , decrement the value of  $right$ .

25	10	27	18	36	45
		$left$	$right$		
			$loc$		



Since  $a[loc] > a[right]$ , interchange the two values and set  $loc = right$ .

25	10	18	27	36	45
			$right$		
			$loc$		
			$left$		

## Quick Sort-Example Continued

- Now **left = loc**, so the procedure terminates, as the pivot element (the first element of the array, that is, 27) is placed in its correct position.
- All the elements smaller than 27 are placed before it and those greater than 27 are placed after it.
- The left sub-array containing 25, 10, 18 and the right sub-array containing 36 and 45 are sorted in the same manner.

## Quick Sort-Algorithm

### **PARTITION (ARR, BEG, END, LOC)**

**Step 1:** [INITIALIZE] SET  $LEFT = BEG$ ,  $RIGHT = END$ ,  $LOC = BEG$ ,  $FLAG = 0$

**Step 2:** Repeat Steps 3 to 6 while  $FLAG = 0$

**Step 3:** Repeat while  $ARR[LOC] \leq ARR[RIGHT]$  AND  $LOC \neq RIGHT$

SET  $RIGHT = RIGHT - 1$

[END OF LOOP]

**Step 4:** IF  $LOC = RIGHT$

SET  $FLAG = 1$

ELSE IF  $ARR[LOC] > ARR[RIGHT]$

SWAP  $ARR[LOC]$  with  $ARR[RIGHT]$

SET  $LOC = RIGHT$

[END OF IF]

**Step 5:** IF  $FLAG = 0$

Repeat while  $ARR[LOC] \geq ARR[LEFT]$  AND  $LOC \neq LEFT$

SET  $LEFT = LEFT + 1$

[END OF LOOP]

**Step 6:** IF  $LOC = LEFT$

SET  $FLAG = 1$

ELSE IF  $ARR[LOC] < ARR[LEFT]$

SWAP  $ARR[LOC]$  with  $ARR[LEFT]$

SET  $LOC = LEFT$

[END OF IF]

[END OF IF]

**Step 7:** [END OF LOOP]

**Step 8:** END

## Quick Sort-Algorithm Continued

**QUICK\_SORT (ARR, BEG, END)**

**Step 1: IF (BEG < END)**

CALL PARTITION (ARR, BEG, END, LOC)

CALL QUICKSORT(ARR, BEG, LOC - 1)

CALL QUICKSORT(ARR, LOC + 1, END)

[END OF IF]

**Step 2: END**

## Quick Sort-Pros & Cons

- It is faster than other algorithms such as bubble sort, selection sort, and insertion sort.
- Quick sort can be used to sort arrays of small size, medium size, or large size.
- On the flip side, quick sort is complex and massively recursive.

## Quick Sort-Comparison of Algorithms

Algorithm	Average Case	Worst Case
Bubble sort	$O(n^2)$	$O(n^2)$
Bucket sort	$O(n.k)$	$O(n^2.k)$
Selection sort	$O(n^2)$	$O(n^2)$
Insertion sort	$O(n^2)$	$O(n^2)$
Shell sort	–	$O(n \log^2 n)$
Merge sort	$O(n \log n)$	$O(n \log n)$
Heap sort	$O(n \log n)$	$O(n \log n)$
Quick sort	$O(n \log n)$	$O(n^2)$

## Sort-Assignments

- Write a program in C to sort an array using bubble sort algorithm.
- Write a program in C to sort an array using insertion sort algorithm.
- Write a program in C to sort an array using selection sort algorithm.
- Write a program in C to sort an array using quick sort algorithm.
- Write a program in C to sort an array using merge sort algorithm.



# Thank You

