

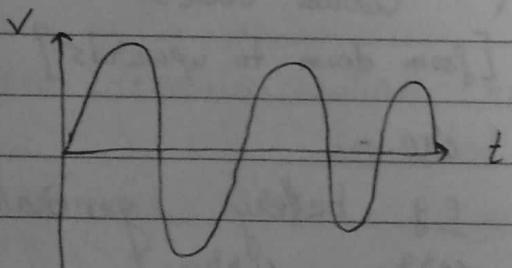
# Basics of Electrical Engineering

DC → Electronics [ devices, appliances ]  
 AC → Electrics [ work ]

## Introduction to DC Circuits -

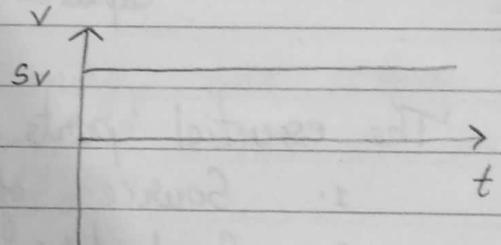
AC [ to stabilize the fluctuation, so we need stabilizers ]

⇒ AC



220 - 270 V

DC [ Mobile Battery ]



Constant

## DC Voltage

Constant voltage value

## DC Circuits

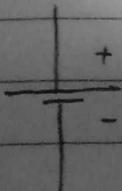
3 types of components  
 Closed path supplies current

is called Circuit

- Source
- Conductors
- Output

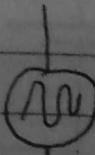
## DC Source

Positive & -ve terminal

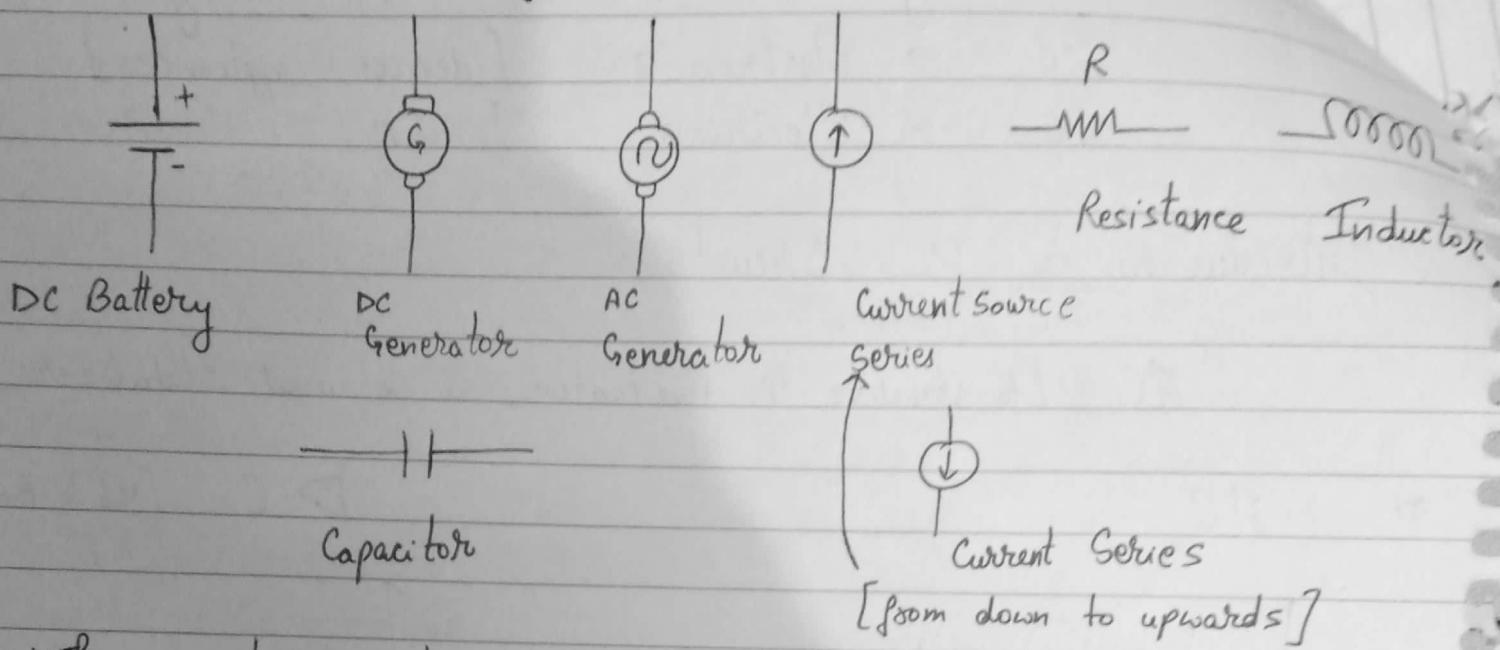


## AC Source

Sine Wave



# DC Terminology - [Components]

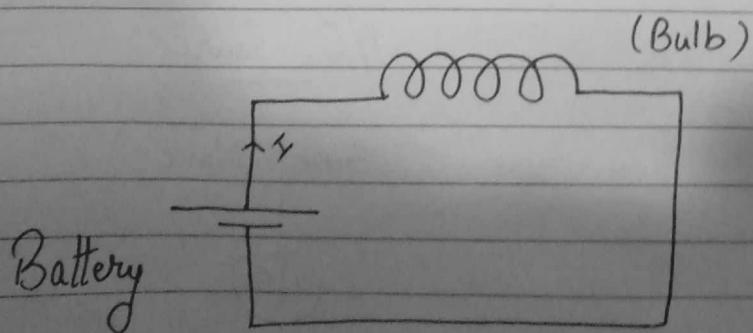


The essential parts of DC circuits are -

1. Source of Power      e.g. battery, generator
2. Conductors      - used to carry current
3. Load      - e.g. bulb, resistance

→ The Source supplies electrical energy to the load which converts it into heat or other form of energy. does conversion of electrical energy into another form of energy is possible only with the help of circuits.

→ The closed path followed by direct current is called DC Circuits.



In a DC circuit, load may be connected in series, parallel and their combination.

DC circuit can be classified as series ckt, parallel ckt and series parallel

\* Terminology of DC Circuit are Active and Passive:

Active Elements which supplies electrical energy to the circuit  
 $V_1$  and  $V_2$  are examples.

Passive Elements which receives electrical energy and either converted into heat energy or stores in  $\vec{E}$  and  $\vec{B}$ . e.g.  $R_1$ ,  $R_2$ ,  $R_3$

\* Parameters - Various elements of electric ckt.

Node : is a junction where two or more elements connecting together. e.g. A, B, C, D

Junction : is a point where three or more elements connecting only B and D

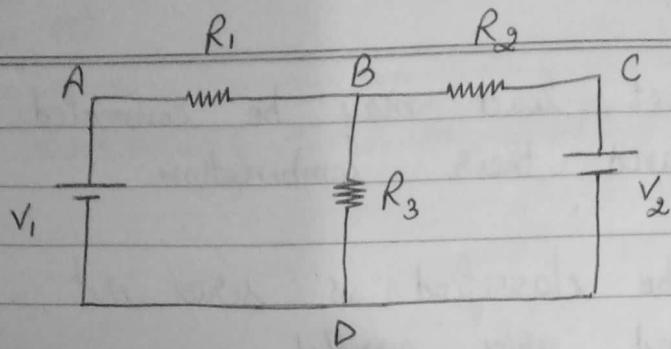
Branch : that part of a circuit which lies b/w two junction point or node.

BCD, BD, ABD

Loop : any closed path of circuit.

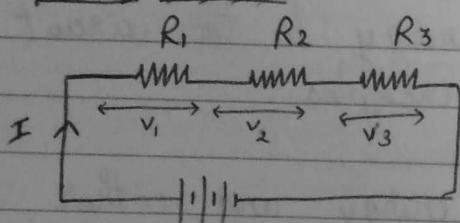
Mesh : Elementary form of loop and can not be further divided but loop in a loop is not a mesh.

Junction  $\rightarrow$  Major Node



## DC Circuit & its Terminology :

DC Circuits Types  $\rightarrow$



① Series Circuit - The circuit in which resistances are connected end to end so that there is only one path for current to flow is called a series circuit.

Consider three resistance  $R_1$ ,  $R_2$ ,  $R_3$  connect in series across a battery of  $V$  volts and there is only one path for current ( $I$ ) is same throughout the circuit.

By using Ohm's Law, the voltage drops across  $R_1$  is  $V_1$ , across  $R_2$  is  $V_2$  and across  $R_3$  is  $V_3$ .

$$\text{So } V_1 = IR_1$$

$$V_2 = IR_2$$

$$V_3 = IR_3$$

For a Series Circuit, sum of voltage drop is equals to applied voltage

$$V = V_1 + V_2 + V_3$$

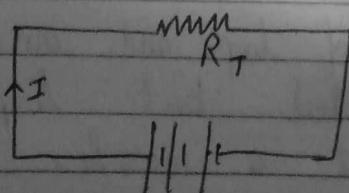
$$V = IR_1 + IR_2 + IR_3$$

$$V = I(R_1 + R_2 + R_3)$$

$$\frac{V}{I} = R_1 + R_2 + R_3$$

$$\therefore R_T = R_1 + R_2 + R_3$$

Hence when no. of resistances are connected in series then total  $R$  is the sum of individual resistances.



- Following Points :
- Current flowing through each resistance is same.
  - The applied voltage is equals to sum of the voltage drop differently.
  - The total path consumed in the circuit is equal to sum of path consumed by individual resistances.
  - Each resistance has its own ~~volt~~ voltage drop.

Voltage Divide Rule →

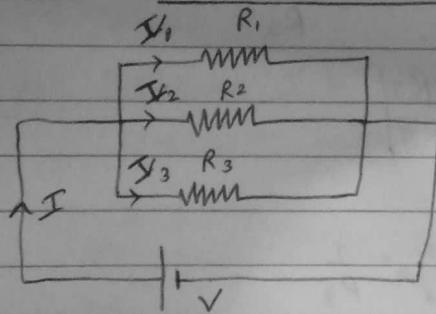
$$I = \frac{V}{R_T} \quad [ \text{Total one} ]$$

$$V_1 = IR_1 = \frac{VR_1}{R_T}$$

$$V_2 = \frac{VR_2}{R_T}$$

$$V_3 = \frac{VR_3}{R_T}$$

## ② Parallel Circuit -



The circuit in which one end of each resistance is joined to a common point and other end of each resistance is joined to another common point so there are as many paths for current flow as no. of resistances is called parallel circuit.

The current flowing through  $R_1$  is  $I_1$ , across  $R_2$  is  $I_2$  . . .

$$\text{So } I_1 = \frac{V}{R_1} \quad I_2 = \frac{V}{R_2} \quad I_3 = \frac{V}{R_3}$$

For a parallel circuit sum of branch current is equal to total current.

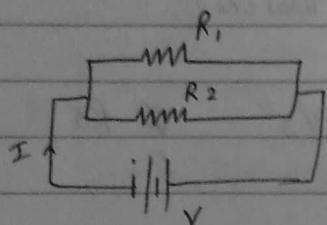
$$\begin{aligned} I &= I_1 + I_2 + I_3 \\ &= \frac{V}{R_1} + \frac{V}{R_2} + \frac{V}{R_3} \end{aligned}$$

$$\begin{aligned} \frac{I}{V} &= \frac{1}{R_1} + \frac{1}{R_2} + \frac{1}{R_3} \\ \frac{1}{R_T} &= \frac{1}{R_1} + \frac{1}{R_2} + \frac{1}{R_3} \end{aligned}$$

- Following Points :
- Voltage is same across the circuit.
  - Total current is equal to the sum of the individual currents.

- The total path consumed in the circuit is equal to the sum of path consumed by individual resistances.
- Each resistance has its own current.

Current Divide Rule -  $\checkmark \quad I = IRT$  [for total]



$$\frac{1}{R_T} = \frac{1}{R_1} + \frac{1}{R_2}$$

$$R_T = \frac{R_1 R_2}{R_1 + R_2}$$

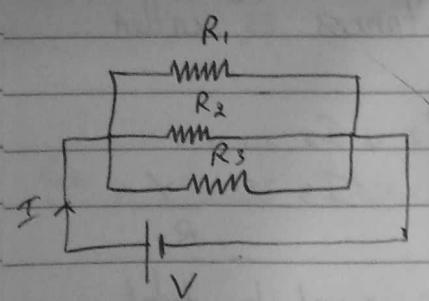
$$I_1 = \frac{V}{R_2} = \frac{IR_T}{R_1}$$

$$I_2 = \frac{V}{R_2} = \frac{IR_T}{R_2}$$

Put value  
of  $R_T$  to  
solve

$$I_3 = \frac{V}{R_3} = \frac{IR_T}{R_3}$$

Current Divide Rule for three resistances.



$$\frac{1}{R_T} = \frac{1}{R_1} + \frac{1}{R_2} + \frac{1}{R_3}$$

$$= \frac{R_2 R_3 + R_1 R_3 + R_1 R_2}{R_1 R_2 R_3}$$

$$V = IRT$$

$$R_T = \frac{R_1 R_2 R_3}{R_2 R_3 + R_1 R_3 + R_1 R_2}$$

$$I_1 = \frac{V}{R_1} = \frac{IR_T}{R_1} = \frac{I}{R_1} \left[ \frac{R_1 R_2 R_3}{R_2 R_3 + R_1 R_3 + R_1 R_2} \right] = \frac{I R_2 R_3}{R_1 R_2 + R_2 R_3 + R_1 R_3}$$

$$I_2 = \frac{V}{R_2} = \frac{IR_T}{R_2} = \frac{I R_1 R_3}{R_1 R_2 + R_2 R_3 + R_1 R_3}$$

$$I_3 = \frac{V}{R_3} = \frac{IR_T}{R_3} = \frac{I R_1 R_2}{R_1 R_2 + R_2 R_3 + R_1 R_3}$$

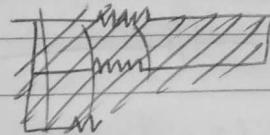
## Numericals :

Que: Determine current through and voltage in each resistance load.  
 $5, 7, 8 \Omega$  are connected in Series across a 100 V source.

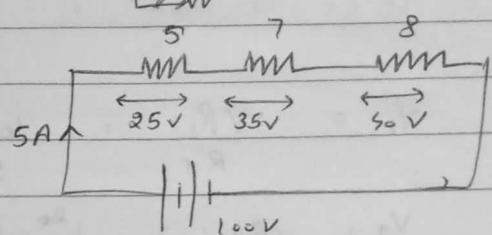
$$R_T = 5 + 7 + 8 = 20 \Omega$$

$$V = I R_T$$

$$I = \frac{V}{R_T} = \frac{100}{20} = 5 A$$



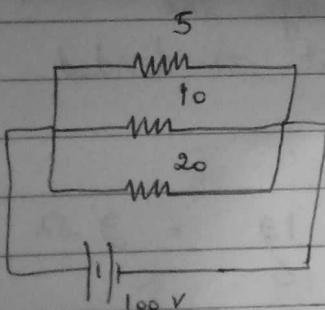
$$V_1 = \frac{V R_L}{R_T} = \frac{100 \times 5}{20} = 25 V$$



$$V_2 = \frac{V R_2}{R_T} = \frac{100 \times 7}{20} = 35 V$$

$$V_3 = \frac{V R_3}{R_T} = \frac{100 \times 8}{20} = 40 V$$

Que: Determine I & voltage through 3 resistance of  $5, 10, 20 \Omega$  in Parallel across 100 V battery also find the current drawn and Power from source?



$$I = \frac{V}{R_T} = \frac{V}{\frac{1}{5} + \frac{1}{10} + \frac{1}{20}} = \frac{V}{\frac{4+2+1}{20}} = \frac{V}{20}$$

$$R_T = \frac{20}{7} \Omega$$

$$V = I R_T$$

$$I = \frac{100 \times 7}{20} = 35 A$$

$$100 = I \times \frac{20}{7}$$

$$I_1 = \frac{35 \times 200}{50 + 200 + 100} = \frac{7000}{350} = 20 A$$

$$I_2 = \frac{35 \times 100}{350} = 10 A$$

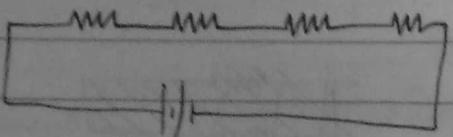
$$P = VI$$

$$= 100 \times 35$$

$$I_3 = \frac{35 \times 50}{350} = 5 A$$

$$= 3500 W$$

Ques: 4 resistances of ohmic value 5Ω, 10, 15, 20 are in series across 100V source. How voltage is divided & also find the power?



$$R_T = 5 + 10 + 15 + 20 \\ = 50 \Omega$$

$$V = IR_T$$

$$\therefore I = \frac{100}{50} = 2A$$

$$V_1 = \frac{VR_1}{R_T} = \frac{100 \times 5}{50} = 10V$$

$$V_2 = \frac{VR_2}{R_T} = \frac{100 \times 10}{50} = 20V$$

$$V_3 = \frac{VR_3}{R_T} = \frac{100 \times 15}{50} = 30V$$

$$P = VI$$

$$= 100 \times 2$$

$$V_4 = 100 - 60 = 40V$$

$$= 200 JW$$

Ques: 3 resistance 4, 12, 6 are connected in parallel if the total current is 12A. How is current is divided into the loads?

$$R_T = \frac{1}{\frac{1}{4} + \frac{1}{12} + \frac{1}{6}} = \frac{4+12+6}{12} = \frac{12}{6} = 2 \Omega$$

$$V = IR_T = 12 \times 2 = 24V$$

$$\therefore I_1 = \frac{IR_2R_3}{R_1R_2 + R_2R_3 + R_3R_1} = \frac{12 \times 12 \times 6}{12+12+6} = 6A$$

$$I_2 = \frac{12 \times 4 \times 6}{12+12+6} = 2A$$

$$I_3 = \frac{12 \times 4 \times 12}{12+12+6} = 4A$$

Ques 3 resistors of  $4, 12, 6 \Omega$  with voltage of 24 V. Find current across each?

$$\frac{1}{R_T} = \frac{1}{4} + \frac{1}{12} + \frac{1}{6} = \frac{3+1+2}{12}$$

$$R_T = 2 \Omega$$

$$V = 24 V$$

$$V = I R_T \quad I = \frac{V}{R_T} = \frac{24}{2} = 12 A$$

$$I_1 = \frac{V}{R_1} = \frac{24}{4} = 6 A$$

$$I_2 = \frac{V}{R_2} = \frac{24}{12} = 2 A$$

$$I_3 = \frac{V}{R_3} = \frac{24}{6} = 4 A$$

Ques 2 resistors  $R_1, R_2$  connected in Parallel to a certain supply the current taken from supply  $I = 5 A$ . Calculate the value of  $R_1$  if  $R_2 = 6 \Omega$  and current through  $R_1$  is 2A. Also find the total power absorbed by the circuit?

$$I_T = 5 A$$

$$I_1 = 2 A$$

$$I_2 = 3 A$$

$$I_1 = \frac{V}{R_1}$$

$$I_2 = \frac{V}{R_2}$$

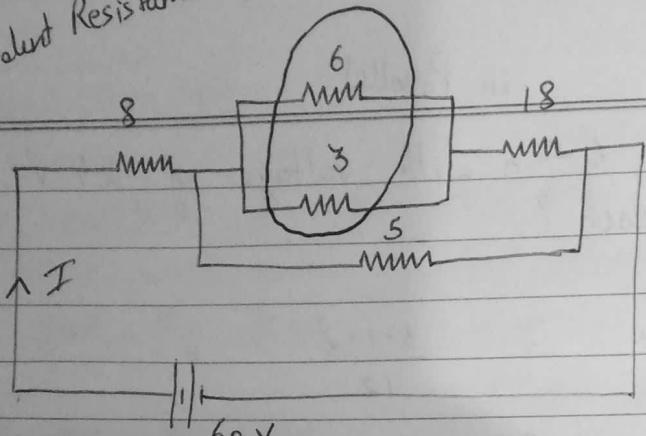
$$V = I_2 R_2 = 3(6) = 18 V$$

$$\therefore R_1 = \frac{V}{I_1} = \frac{18}{2} = 9 \Omega$$

$$\text{Power} = VI = 5 \times 18 = 90 W$$

Find equivalent Resistance?

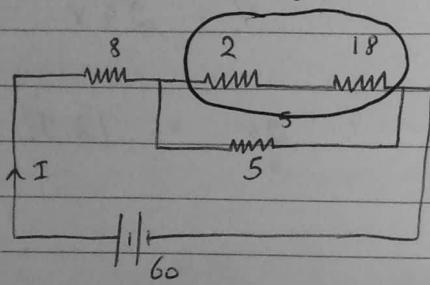
Ques



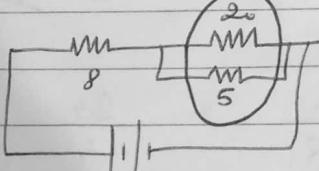
$$\frac{1}{R_p} = \frac{1}{6} + \frac{1}{3}$$

$$= \frac{1+2}{6}$$

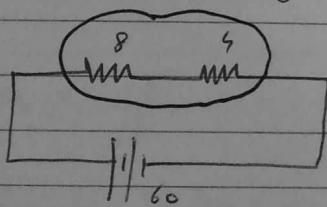
$$R_p = 6/3 = 2$$



$$R_s = 2 + 18 = 20$$



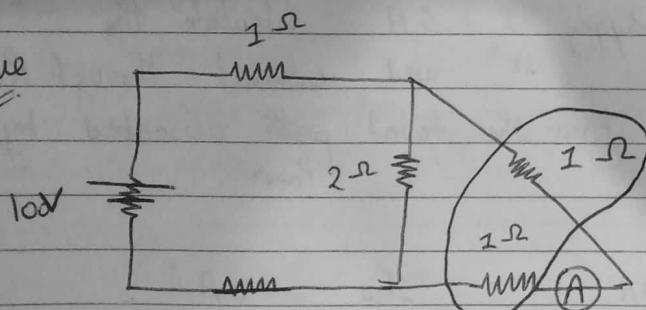
$$R_p = \frac{1}{20} + \frac{1}{5} = \frac{1+4}{20} = \frac{20}{5} = 4$$



$$R_T = 8 + 4 = 12 \Omega$$

$$I_T = \frac{V}{R} = \frac{60}{12} = 5A$$

Ques



Find current  
through ammeter ?

$$R_s = 1 + 1 = 2 \Omega$$

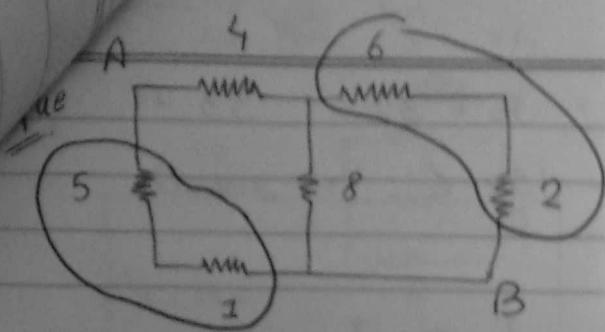
$$R_p = \frac{1}{2} + \frac{1}{2} = 1 \Omega$$

$$R_T = 1 + 1 = 2 \Omega$$

$$I = \frac{V}{R_T} = \frac{100}{2} = 50A$$

$$I_2 = \frac{IR_1}{R_T} = \frac{50 \times 2}{2}$$

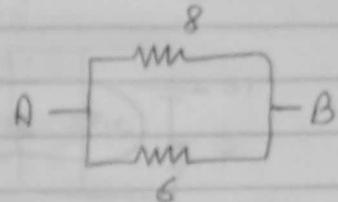
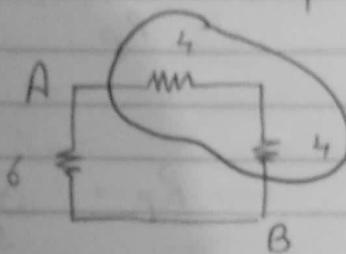
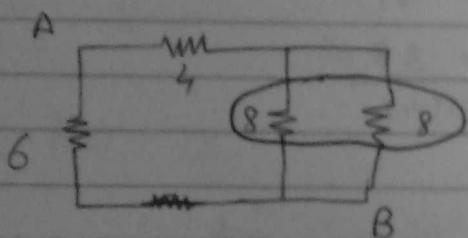
$$I_2 = 50A$$



$$R_S = 6 + 2 = 8 \Omega$$

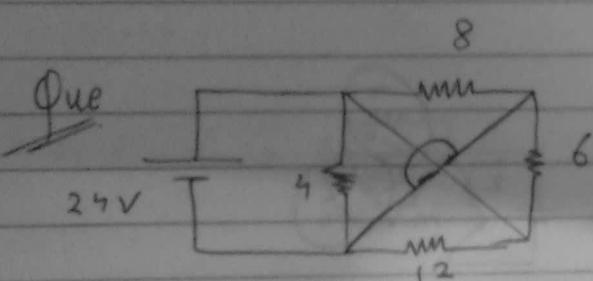
$$R_P = \frac{1}{8} + \frac{1}{8} = \frac{2}{8}$$

$$R_P = 4 \Omega$$



$$R_P = \frac{1}{8} + \frac{1}{6} = \frac{6+8}{48} = \frac{48}{144} = \frac{1}{3}$$

$$R_P = 3.42 \Omega$$



Ques

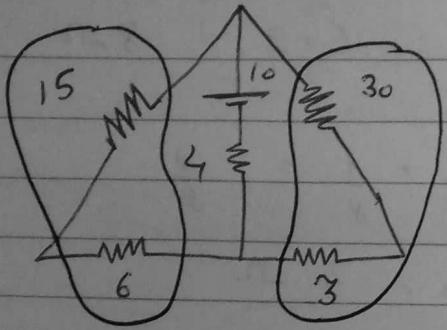
- Due to:
- Due to the diagonal wire, the all four become parallel combination

$$\therefore R_P = \frac{1}{\frac{1}{8} + \frac{1}{6} + \frac{1}{4} + \frac{1}{12}} = \frac{3+4+6+2}{24} = \frac{15}{24} = \frac{5}{8} \Omega$$

$$V = IR_P \quad I = \frac{V}{R_P}$$

$$I_T = \frac{24 \times 20}{24} = 20 A$$

Ques Find the equivalent resistance of the given circuit?



$$R_p = 30 + 3 = 33 \Omega$$

$$R_p = 15 + 6 = 21 \Omega$$

$$\frac{1}{R_p} = \frac{1}{33} + \frac{1}{21}$$

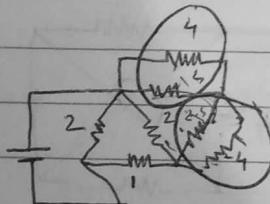
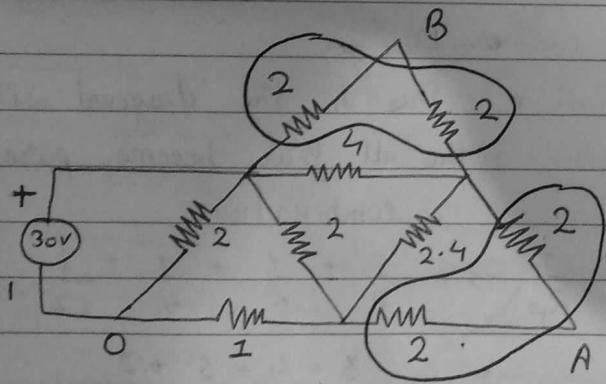
$$= \frac{21 + 33}{(33)(21)}$$

$$R_p = \frac{(33)(21)}{54}$$

$$(R_g) R_T = \frac{(33)(21)}{54} + 4(54) = 16.8 \Omega$$

$$I = \frac{10}{16.8} = 0.59 A$$

que.



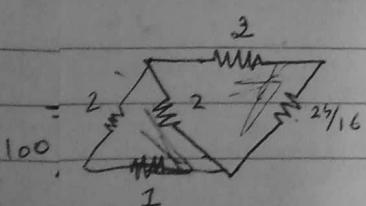
$$\frac{I}{R_p} = \frac{1}{5} + \frac{1}{5} = \frac{2}{5} = 0.4$$

$$R_S = \frac{6+12}{5+16} = \frac{3+3}{2} = 3 \Omega$$

$$\frac{1}{4} + \frac{10}{24} = \frac{6+10}{24} = \frac{16}{24} = \frac{2}{3}$$

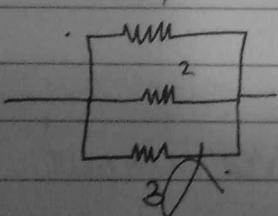
$$R_S = 2 + 1 = 3$$

$$R_S = \frac{2+24}{16} = \frac{32+24}{16} = \frac{56}{16} = 3.5 \Omega$$



$$\frac{I}{R_T} = \frac{1}{2} + \frac{1}{3} + \frac{7}{2} = \frac{3+2+21}{6}$$

$$R_T = \frac{6}{26} \times$$

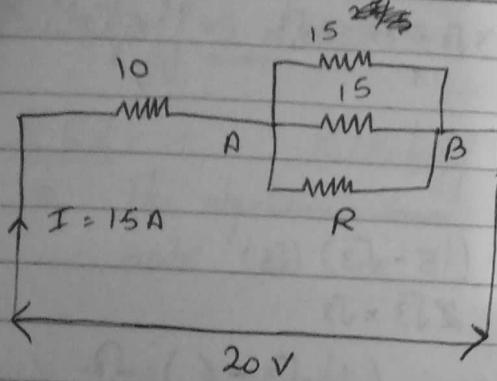


$$20 = V_1 + V_2$$

$$\begin{aligned}V_1 &= IR_1 & V_2 &= IR_2 \\&\approx 1.5(10) & 20 - 15 &= \\&= 15 & 5 &= IR_2\end{aligned}$$

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$$I = 1.5 \text{ A}$$

$$\frac{1}{R_T} = \frac{1}{15} + \frac{1}{15} + \frac{1}{R}$$

$$\frac{1}{R_T} = \frac{R + R + 15}{15R}$$

$$R_T = \frac{15R}{2R + 15}$$

$$R_{net} = \frac{V}{I}$$

$$= \frac{20}{10 + 15 + 15} = \frac{40}{45} = \frac{4}{3}$$

$$R_{net} = 10 + \frac{15R}{2R + 15}$$

$$\frac{10 + 15R}{2R + 15} = \frac{40}{3}$$

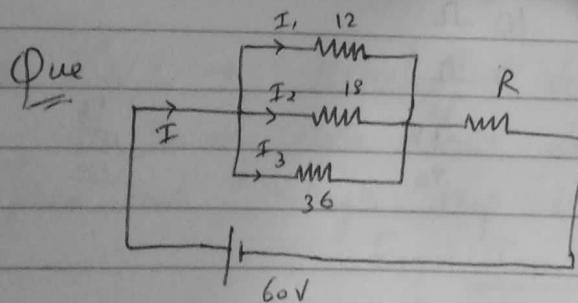
$$\frac{15R}{2R + 15} = \frac{40 - 30}{3} = \frac{10}{3}$$

$$4R + 30 = 9R$$

$$\frac{30}{R} = 5R$$

$$R = 6 \Omega$$

$$I_1 = \frac{V}{R_1} = \frac{20}{10} = 2 \text{ A} \quad I_2 = \frac{20}{15} = \frac{4}{3} \text{ A} \quad I_3 = \frac{20}{15} = \frac{4}{3} \text{ A}$$



$$\text{Power Consumed} = 36 \text{ W}$$

through 12  $\Omega$

In Parallel

In Series

$$P = I_1^2 R$$

$$V = I_1 R_1$$

$$V = V_1 + V_2$$

$$36 = I_1^2 (12)$$

$$= \sqrt{3} (12)$$

$$60 = 12\sqrt{3} + V_2$$

$$I_1^2 = 3$$

$$= 12\sqrt{3}$$

$$I_1 = \sqrt{3}$$

$$V_2 = 60 - 12\sqrt{3}$$

$$I_2 = \frac{V}{R} = \frac{12\sqrt{3}}{18 + 18} = \frac{2\sqrt{3}}{3}$$

$$R = \frac{V_2}{I} = \frac{60 - 12\sqrt{3}}{\sqrt{3} + \frac{2\sqrt{3}}{3} + \frac{\sqrt{3}}{3}}$$

$$I_3 = \frac{V}{R} = \frac{12\sqrt{3}}{36} = \frac{\sqrt{3}}{3}$$

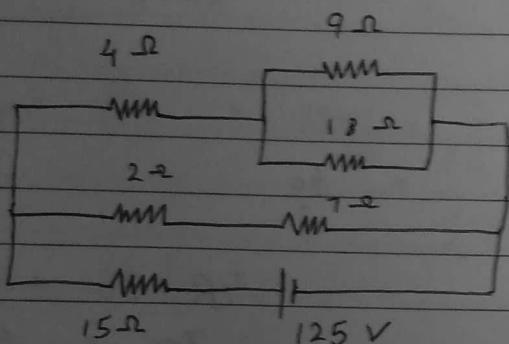
Kirchoff's

KCL →  
The al  
Node

$$\text{Total } I = \frac{\sqrt{3} + \frac{\sqrt{3}}{3} + \frac{2\sqrt{3}}{3}}{3} = \frac{3\sqrt{3} + \sqrt{3} + 2\sqrt{3}}{3} = \frac{6\sqrt{3}}{3} = 2\sqrt{3}$$

$$\therefore R = \frac{60 - 12\sqrt{3}}{2\sqrt{3}} = \frac{6(5 - \sqrt{3})}{2\sqrt{3} \times \sqrt{3}} = \frac{2(5\sqrt{3} - 3)}{3} = \frac{(10\sqrt{3} - 6)}{11} \Omega$$

Que



Find

- Current in 15
- Voltage across 18
- Power dissipated in 7Ω ?

$$\frac{I}{R_p} = \frac{1}{9} + \frac{1}{18} = \frac{2+1}{18} \quad R_p = \frac{18}{3} = 6 \Omega$$

$$R_{S_1} = 4 + 6 = 10 \Omega$$

$$R_{S_2} = 2 + 7 = 9 \Omega$$

$$\frac{I}{R_p} = \frac{1}{10} + \frac{1}{9} = \frac{9+10}{90} = \frac{19}{90}$$

$$R_p = \frac{90}{19} \Omega$$

$$R_T = 15 + \frac{90}{19} = \frac{15(19) + 90}{19}$$

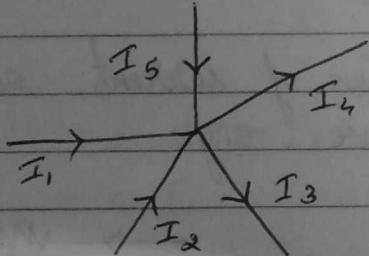
$$= \frac{285 + 90}{19} = \frac{375}{19}$$

$$I = \frac{V}{R} = \frac{25}{\frac{375}{19}} = \frac{25 \times 19}{375} = 6.3 A$$

## Kirchoff's Law :

- \* KCL → Kirchoff's Circuital Law [Current]
  - ⇒ The algebraic sum of current meeting at a junction or node in an electric Circuit is zero.

Consider five conductors carrying current meeting at a node A and algebraic sum is I in which the sign of quantity is taken into account if we take sign of current towards the node is positive and when we take sign of current flowing away from node A is negative. Thus apply KCL and we get.



$$I_1 + I_2 - I_3 + I_4 + I_5 = 0$$

- ⇒ Sum of currents flowing towards any junction in an electric Circuit is equal to sum of currents flowing away from that junction.

## \* KVL → Kirchoff's Voltage Law

In any close circuit or mesh, the algebraic sum of the electromotive force and voltage drop is equal to zero

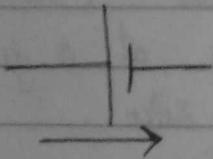
Sign Convention → Positive terminal → Rising Potential  
Negative terminal → Falling Potential

- While applying KVL to a close circuit, the algebraic sum are Consider therefore it is very important to assign proper sign to the emf and voltage drop to the circuit.

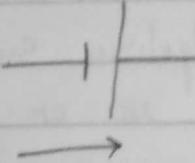
Rise in Potential is positive & fall in potential is negative

1. If we go from +ve terminal to -ve terminal of battery and there is fall in potential, so we get -ve sign.

2. If we go from -ve terminal to +ve terminal of battery there is rise in potential and sign of emf is positive.



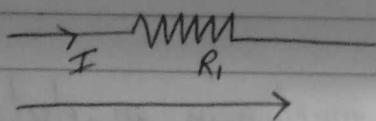
Emf is -ve



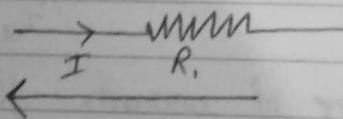
Emf is +ve

- When a current flows through resistor there is a voltage drop across it, if we go through the resistance in the same direction as the current, so there is fall in potential, the sign is negative.

If we go opposite to the direction of current, so here is rise in potential with positive sign.

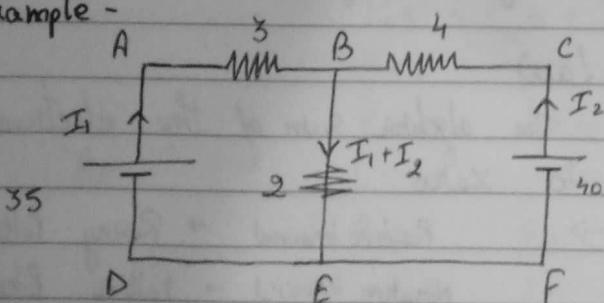


Emf is  $-IR_1$



Emf is  $+IR_1$

Example -



Apply KVL in ABEDA

$$-3I_1 - 2(I_1 + I_2) + 35 = 0$$

$$-3I_1 - 2I_1 - 2I_2 + 35 = 0$$

Apply KVL in EFEBC

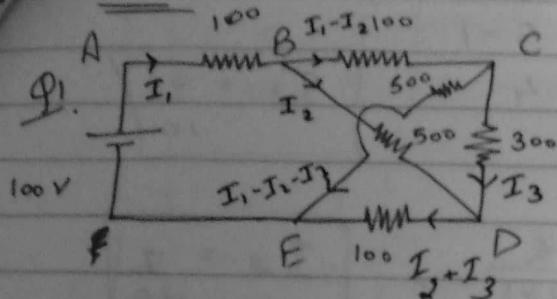
$$-2I_2 - 5I_1 + 35 = 0$$

$$-4_0 + 2(I_1 + I_2) + 4I_2 = 0 \quad \text{①}$$

$$-4_0 + 2I_1 + 2I_2 + 4I_2 = 0$$

$$2I_1 + 6I_2 - 4_0 = 0$$

$$- \text{②}$$

Numericals :

Find current across each branch?

Loop ABCDEA

$$-100I_1 - 100(I_1 - I_2) - 300I_3$$

$$-100(I_2 + I_3) + 100 = 0$$

$$-100I_1 - 100I_1 + 100I_2 - 300I_3 - 100I_2 - 100I_3 + 100 = 0$$

$$-200I_1 - 400I_3 = -100$$

$$2I_1 + 4I_3 = 1$$

$$I_1 = \frac{1 - 4I_3}{2}$$

Loop BCDB

$$-100(I_1 - I_2) - I_3 300 + 500I_2 = 0$$

$$-100I_1 + 100I_2 - 300I_3 + 500I_2 = 0$$

$$-100I_1 + 600I_2 - 300I_3 = 0$$

$$I_1 + 3I_3 = 6I_2 \quad \text{--- (2)}$$

Loop CEDC

$$-500(I_1 - I_2 - I_3) + 100(I_2 + I_3) + 300I_3 = 0$$

$$-500I_1 + 500I_2 + 500I_3 + 100I_2 + 100I_3 + 300I_3 = 0$$

$$-500I_1 + 600I_2 + 900I_3 = 0$$

$$6I_2 + 9I_3 = 5I_1 \quad \text{--- (3)}$$

Put  $I_1$  in (2)

$$\frac{1 - 4I_3 + 3I_3}{2} = 6I_2$$

$$1 - 4I_3 + 6I_3 = 12I_2$$

$$1 + 2I_3 = 12I_2$$

$$\frac{1 + 2I_3}{12} = I_2$$

Put in (3)

$$\frac{1 + 2I_3 + 9I_3}{2} = \frac{5 - 20I_3}{2}$$

$$1 + 2I_3 + 18I_3 = 5 - 20I_3$$

$$20I_3 + 20I_3 = 5 - 1$$

$$40I_3 = 4$$

$$I_3 = \frac{1}{10}$$

$$I_2 = \frac{1 + \frac{1}{5}}{12} = \frac{\frac{6}{5}}{\frac{12}{1}} = \frac{6}{12 \times 5} = \frac{1}{10}$$

$$I_1 = \frac{1 - \frac{4}{10}}{2} = \frac{\frac{6}{10}}{\frac{2}{1}} = \frac{6 \times 1}{2 \times 10} = \frac{3}{10}$$

$$I_1 = \frac{3}{10}$$

\*\* Apply Cramer's Rule to find value of current [Short Cut]

\* Make matrix of coefficient of variables

$$\begin{vmatrix} 2 & 0 & 4 \\ 1 & -6 & 3 \\ -5 & 6 & 9 \end{vmatrix} \begin{vmatrix} I_1 \\ I_2 \\ I_3 \end{vmatrix} = \begin{vmatrix} 1 \\ 0 \\ 0 \end{vmatrix}$$

\* Find determinant as  $\Delta$

$$\Delta = 2[-54 - 18] + 4[6 - 30]$$

$$= -2[72] + 4[-24]$$

$$= -240$$

\* Find  $\Delta_1$  using first column interchange with the equivalent Column

$$\begin{vmatrix} 1 & 0 & 4 \\ 0 & -6 & 3 \\ 0 & 6 & 9 \end{vmatrix} \quad \Delta_1 = -54 - 18 = -72$$

Exams, Apply Cramer's Rule for  
more than 3 equations...

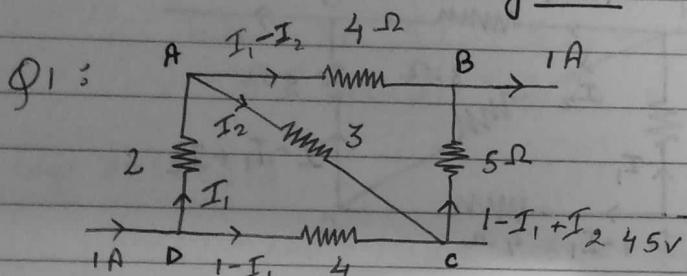
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$$\begin{vmatrix} 2 & 1 & 4 \\ 1 & 0 & 3 \\ -5 & 0 & 9 \end{vmatrix} \quad \Delta_2 = 1(9+15) = 24$$

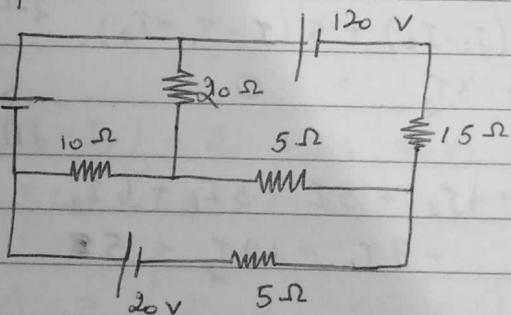
$$\begin{vmatrix} 2 & 0 & 1 \\ 1 & -6 & 0 \\ -5 & -6 & 0 \end{vmatrix} \quad \Delta_3 = -24 = 6-30$$

Then find values by  $I_1 = \frac{\Delta_1}{\Delta}$   $I_2 = \frac{\Delta_2}{\Delta}$   $I_3 = \frac{\Delta_3}{\Delta}$

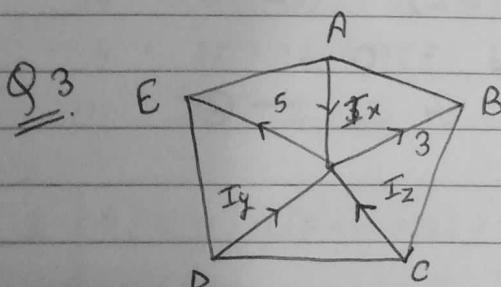
### Assignment :



Q2 Find Current across 20 Ω ?



Find current in each branch ?



(i)  $I_x = ?$  if  $I_y = 2A$   $I_z = 0A$

(ii)  $I_z = ?$  if  $I_x = 2$   $I_y = I_z$

(iii)  $I_y = ?$  if  $I_x = I_y$   $I_z = I_y$

Using KCL

Algebraic Sum of incoming = Algebraic Sum of outgoing  
 $I_y + I_z + I_n = 5 + 3$

$$I_n + I_y + I_z = 8$$

$$(i) \quad I_x + I_y + I_z = 8$$

$$I_x + 2 + 0 = 8 \quad I_x = 6A$$

$$(ii) \quad I_x + I_y + I_z = 8$$

$$2 + 2I_y + 2I_z = 8$$

$$2I_z = 8 - 2 \quad I_z = 3A$$

$$(iii) \quad I_x + I_y + I_z = 8$$

$$3I_y = 8 \quad I_y = 8/3 A$$

Ques! loop ABCA

$$-4(I_1 - I_2) + 5(I - I_1 + I_2) + 3I_2 = 0$$

$$-4I_1 + 4I_2 + 5I - 5I_1 + 5I_2 + 3I_2 = 0$$

$$-9I_1 + 12I_2 + 5I = 0 \quad \text{--- } ①$$

loop ADCA

$$2I_1 - 4(I - I_1) + 3I_2 = 0$$

$$2I_1 = 4 + 4I_1 + 3I_2 = 0$$

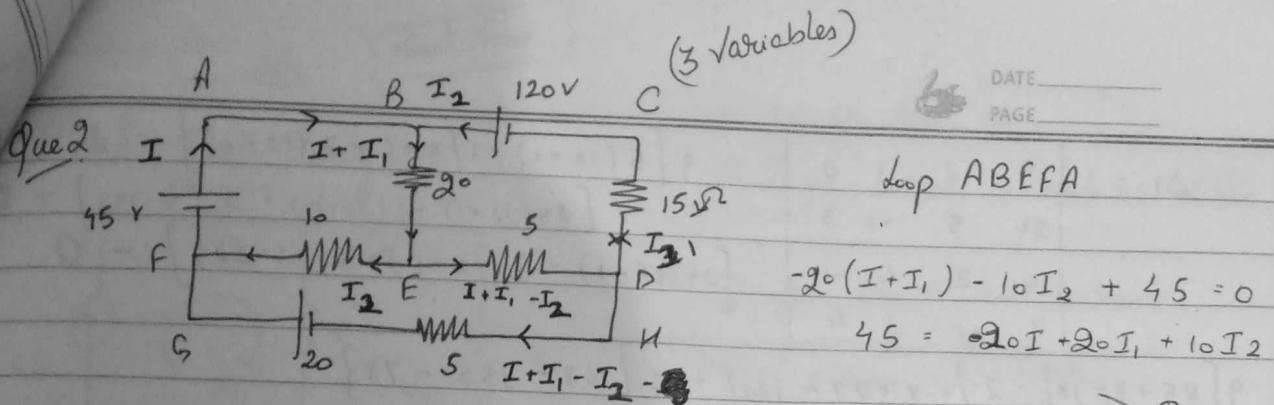
$$6I_1 + 3I_2 = 4 \quad \text{--- } ②$$

$$\Delta = \begin{vmatrix} 9 & -12 \\ 6 & 3 \end{vmatrix} = 27 + 72 = 99$$

$$\Delta_1 = \begin{vmatrix} 5 & -12 \\ 4 & 3 \end{vmatrix} = 15 + 48 = 63$$

$$\Delta_2 = \begin{vmatrix} 9 & 5 \\ 6 & 7 \end{vmatrix} = 36 - 30 = 6$$

$$I_1 = \frac{63}{99} = \frac{21}{33} = \frac{7}{11} \quad I_2 = \frac{16}{99} = \frac{52}{33}$$



Loop BCDEFB

$$-120 + 15I_3 + 5(I + I_1 - I_2) + 20(I + I_1) = 0$$

$$15I_3 + 5I + 5I_1 + -5I_2 + 20I_1 + 20I = 120$$

$$25I + 25I_1 - 5I_2 + 15I_3 = 120 \quad \text{--- (2)}$$

Loop FDHGF

$$+10I_2 - 5(I + I_1 - I_2) - 5(I + I_1 - I_2 - I_3) + 20 = 0$$

$$10I_2 - 5I - 5I_1 + 5I_2 - 5I - 5I_1 + 5I_2 + 5I_3 + 20 = 0$$

$$-10I - 10I_1 + 20I_2 + 5I_3 = -20 \quad \text{--- (3)}$$

Loop ABCDHF

$$-120 + 15I_3 - 5(I + I_1 - I_2 - I_3) + 20 + 45 = 0$$

$$15I_3 - 5I - 5I_1 + 5I_2 + 5I_3 = 120 - 65 = 55 \quad \text{--- (4)}$$

E.R.  $9 = 2I + 2I_1 + 2I_2$

$$24 = 5I + 5I_1 - I_2 + 3I_3$$

$$4 = 2I + 2I_1 - 4I_2 - I_3$$

$$11 = 3I_3 - I - I_1 + I_2$$

$$\Delta = \begin{vmatrix} 2 & 2 & 1 & 0 \\ 5 & 5 & -1 & 3 \\ 2 & 2 & -4 & -1 \\ -1 & -1 & 1 & 4 \end{vmatrix}$$

$$2 \left| 5(-16+1) + 1(8-1) + 3(2-4) \right| - 2 \left| 5(8-1) + 1(8-1) + 3(2-4) \right|$$

$$+ 1 \left| 5(20+3) - 5(8-1) + 3(-2+2) \right| + 0 \mid - \rangle$$

$$\Rightarrow 2[-75+7-6] - 2[85+7-6] + [115-35]$$

$$2[-74] - 2[36] + [80] = -148 - 72 + 80$$

$$= -140$$

Mesh And Thru

$$\Delta_1 = \begin{vmatrix} 9 & 2 & 1 & 0 \\ 24 & 5 & -1 & 3 \\ 4 & 2 & 4 & -1 \\ 11 & -1 & 1 & 4 \end{vmatrix} \quad 9 \left[ 5(16+1) + 1(8-1) + 3(2+4) \right] - 2 \left[ 24(16+1) + 1(16+11) + 3(4-35) \right] + \left[ 24(8-1) - 5(16+11) + 3(-4-22) \right] - 0$$

$$9[85+7+18] - 2[408+27-120] + 1[168-135-78] \\ 990 - 630 - 45 = 315$$

$$\Delta_2 = \begin{vmatrix} 2 & 9 & 1 & 0 \\ 5 & 24 & -1 & 3 \\ 2 & 4 & 4 & -1 \\ -1 & 11 & 1 & 4 \end{vmatrix} \quad 2 \left[ 24(16+1) + 1(16+11) + 3(4-35) \right] - 9 \left[ \dots \right]$$

$\Phi_2$

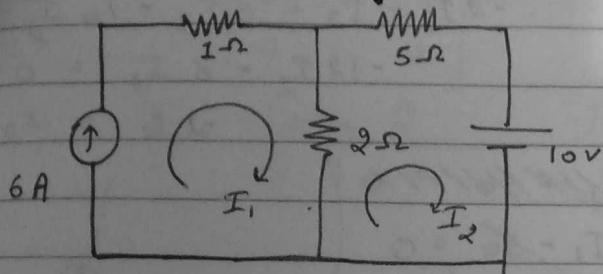
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## Mesh And Analysis :

① Identify Mesh

② Assign current in clockwise direction



If first branch has current source then it is equal to First Current.

$$\therefore I_1 = 6 \text{ A}$$

Apply KVL to 2nd loop

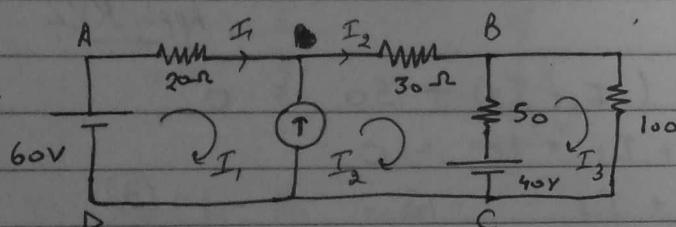
Mesh Current  
Loop

$$5I_2 - 10 - 2(I_1 - I_2) = 0$$

$$5I_2 - 10 - 2I_1 + 2I_2 = 0$$

$$7I_2 = 22$$

$$I_2 = \frac{22}{7} = 3.1 \text{ A}$$



If here is current source then first solve current source.

Form a ~~mesh~~ Super mesh which proves that the current source is in 2<sup>nd</sup>.

Super Mesh: ABCDA

$$-20I_1 - 30I_2 - 50(I_2 - I_3) - 40 + 60 = 0 \quad \text{--- (1)}$$

$$20I_1 + 80I_2 - 50I_3 = -20$$

~~Current Source~~  $I_2 - I_1 = 1 \quad \text{--- (2)}$  (Simple Mesh)

~~Loop 3~~  $-100I_3 + 40 - 50(I_2 + I_3) = 0$

$$40 = 150I_3 + 50I_2 \quad \text{--- (3)}$$

$$I_2 = 1 + I_1 \quad 40 = 150I_3 + 50 + 50I_1 \quad (150I_3 + 50I_1 = -10) \times 2$$

$$20I_1 + 80 + 80I_1 - 50I_2 = -20 \quad -50I_2 + 100I_1 = -100$$

~~$300I_3 + 100I_1 = -20$~~

$$30 \left( \frac{150}{35} \right) + 20 = -50I_1$$

~~$-50I_3 + 100I_1 = -200$~~

$$+ \quad - \quad +$$

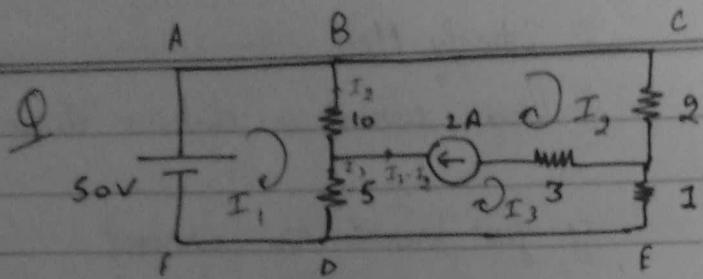
$$350I_3 = 80$$

$$\frac{240 + 140}{7} = \frac{380}{7 \times 50} = -I_1$$

$$I_1 = \frac{-38}{35} \text{ A}$$

$$I_3 = \frac{8}{35} \text{ A}$$

$$I_2 = \frac{-3}{35} \text{ A}$$



Super Mesh B.C.E.

$$\begin{aligned} -2I_1 - I_3 - 5I_3 - 10I_2 \\ -12I_2 - 6I_3 = 0 \\ -2I_2 = I_3 \end{aligned}$$

MESH ALGEBRA

Mesh ABDFEA

$$+10I_1 + 5I_3 + 50 = 0$$

$$10I_2 + 5I_3 + -50$$

$$10I_2 + 5(-2I_2) = -50$$

$$10I_2 - 10I_2 = -50$$

Mesh

$$r 3(I_3 - I_2) - I_3 - 5I_3 = 0$$

$$3I_3 - 3I_2$$

①

Apply KVL

Mesh ABDFEA

$$10(I_1 + I_2) + 5(I_1 + I_3) + 50 = 0$$

$$2I_1 + 2I_2 + I_1 + I_3 + 10 = 0$$

$$3I_1 + 2I_2 + I_3 = -10$$

— ③

$E_g$  of Current Source

$$I_2 - I_3 = 2$$

— ②

$$-2I_2 - 3I_3 - 5(I_3 + I_1)$$

$$\Delta = \begin{vmatrix} 0 & -2 & -1 \\ 3 & 2 & 1 \\ 0 & 1 & -1 \end{vmatrix} \quad 3[2+1] = 3 \times 3$$

$$\Delta_1 = \begin{vmatrix} 0 & -2 & -1 \\ -10 & 2 & 1 \\ 2 & 1 & -1 \end{vmatrix} \quad 2[10-2] - 1[-10-4] = 16 + 14$$

$$\Delta_2 = \begin{vmatrix} 0 & 0 & -1 \\ 3 & -10 & 1 \\ 0 & 2 & -1 \end{vmatrix} \quad 3[2] = 6$$

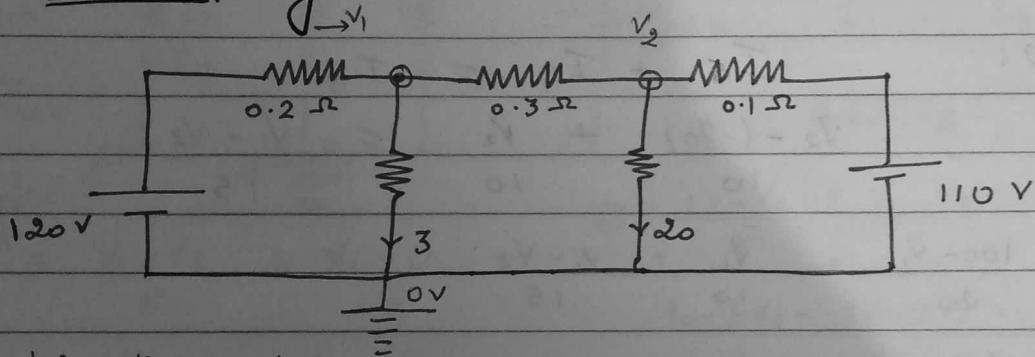
Mesh  $\rightarrow$  KVL  
Nodal  $\rightarrow$  KCL

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$$\Delta_3 = \begin{vmatrix} 0 & -2 & 0 \\ 3 & 2 & -10 \\ 0 & 1 & 2 \end{vmatrix} = -3 [-4] = 12$$

$$\therefore I_1 = \frac{10}{3} A \quad I_2 = \frac{2}{3} A \quad I_3 = \frac{4}{3} A$$

## Nodal Analysis :

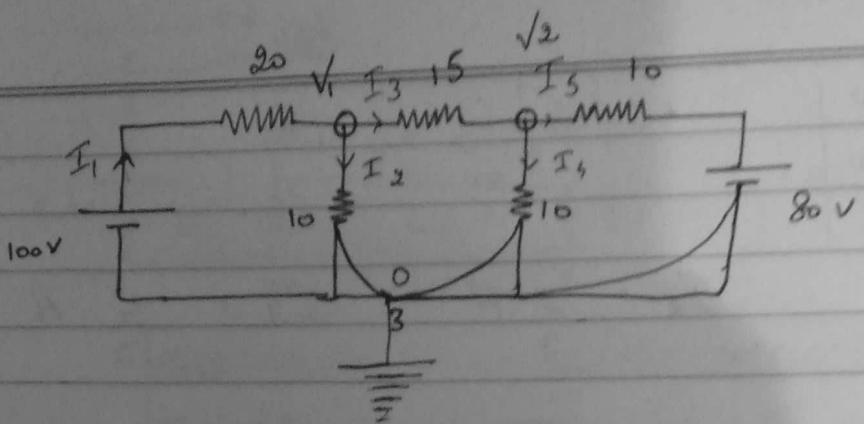


1. Identify the node.
2. Apply KCL in each and every node.
3. Select node as Reference node and give it as 0 V attached with ground potential.
4. Apply KCL
5. Voltage at node, we have to find.

STEPS:

- Mark all the nodes.
- Select one of the node as Reference Node.
- Assign the unknown potential (find) of all the nodes with respect to the reference node.
- At each node, assume the unknown current and mark the direction. Apply KCL at each node and the equation in terms of node voltage by solving the equation determining the node voltage.

$$I_1 = I_2 + 3$$



$$I = \frac{V}{R}$$

2 Poles

$$\text{At Node 1: } I_1 = I_2 + I_3$$

$$\frac{100 - V_1}{20} = \frac{(V_1 - 0)}{10} + \frac{V_1 - V_2}{15}$$

At Node 2:

$$I_5 + I_4 = I_3$$

$$\frac{V_2 - (-80)}{10} + \frac{V_2}{10} = \frac{V_1 - V_2}{15}$$

Now Solve:

$$\frac{100 - V_1}{20} = \frac{V_1}{10} + \frac{V_1 - V_2}{15}$$

$$\frac{300 - 3V_1}{20} = 6V_1 + 4V_1 - 4V_2$$

$$13V_1 - 4V_2 = 300 \quad \text{---(1)}$$

$$\frac{V_2 + 80}{10} + \frac{V_2}{10} = \frac{V_1 - V_2}{15}$$

$$\frac{3V_2 + 240 + 3V_2}{30} = 2V_1 - 2V_2$$

$$2V_1 - 8V_2 = 240 \quad \text{---(2)}$$

$$\frac{-300 + 13V_1}{4} = V_2 \quad \text{Put in (2)}$$

$$2V_1 - 8 \left[ \frac{13V_1 - 300}{4} \right] = 240$$

$$2V_1 - 26V_1 + 600 = 240$$

$$\frac{-300 + 13(15)}{4} = V_2$$

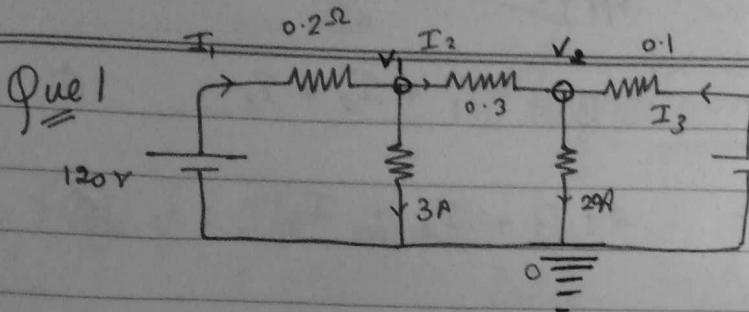
$$-24V_1 = -600 + 240$$

$$V_1 = \frac{360}{24} = 15 \text{ V}$$

$$\frac{-300 + 195}{4} = -\frac{105}{4} V_2$$

$$V_2 = \frac{105}{4} \text{ V}$$

$$V_1 = 15 \text{ V}$$

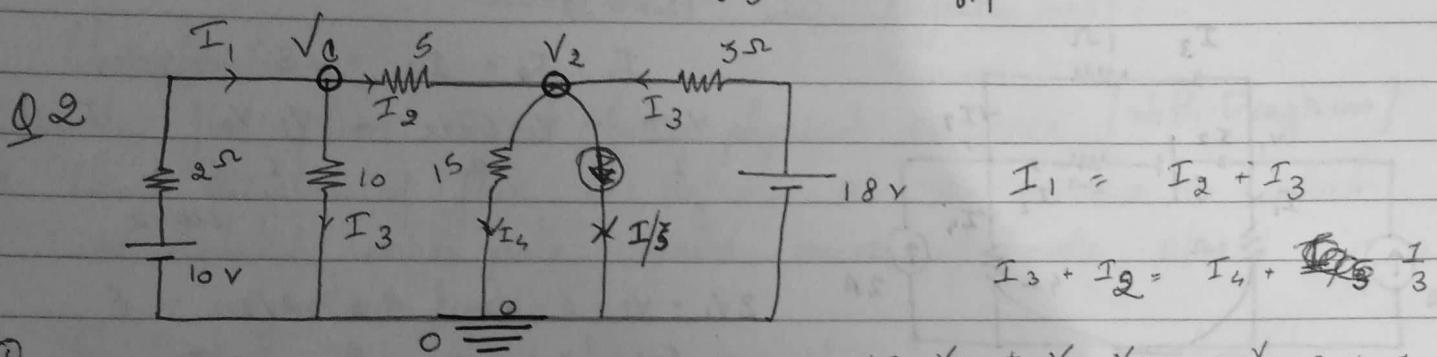


$$I_1 = I_2 + I_3$$

$$\frac{120 - V_1}{0.2} = \frac{V_1 - Q}{0.3} + 3$$

$$I_2 + I_3 = 20$$

$$\frac{V_1 - V_2}{0.3} + \frac{110 - V_2}{0.1} = 20$$



$$I_1 = I_2 + I_3$$

$$I_3 + I_2 = I_4 + \frac{1}{3}$$

$$\frac{10 - V_1}{2} = \frac{V_1 - V_2}{5} + \frac{V_1 - 0}{10}$$

$$\frac{18 - V_2}{3} + \frac{V_1 - V_2}{5} = \frac{V_2 - 0}{15} + \frac{1}{3}$$

$$50 - 5V_1 = 2V_1 - 2V_2 + V_1$$

$$85 = 2V_1 + 4V_2$$

$$8V_1 - 2V_2 = 50$$

$$4V_1 - V_2 = 25 \quad \text{--- (1)}$$

$$2V_1 + 4V_2 = 85 \quad \text{--- (2)}$$

$$4V_1 - 25 = V_2$$

$$2V_1 + 4[4V_1 - 25] = 85$$

$$2V_1 + 16V_1 - 100 = 85$$

$$V_2 = \frac{4(185)}{18} - 25$$

$$18V_1 = 185$$

$$= \frac{740 - 450}{18} = \frac{290}{18}$$

$$V_1 = \frac{185}{18}$$

$$V_2 = \frac{290}{18}$$

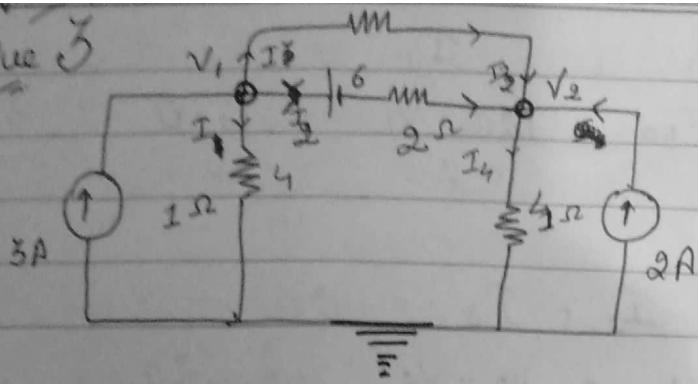
$$I_1 = \frac{10 - V_1}{2} = \frac{180 - 185}{36} = \frac{-5}{36}$$

$$I_2 = \frac{21}{18}$$

$$I_3 = \frac{V_1}{10} = \frac{185}{180}$$

$$I_4 = \frac{V_2}{15} = \frac{290}{15 \times 18} = \frac{+19}{27} = \frac{29}{27}$$

Que 3



$$I = I_1 + I_2 + I_3 \quad \text{①}$$

$$2 + I_3 + I_2 = I_4 \quad \text{②}$$

From ① equation.

$$I_1 + I_2 + I_3 = 3$$

$$\frac{V_1 - 0}{1} + \frac{V_1 - 6 - V_2}{2} + \frac{V_1 - V_2}{1} = 3$$

$$2V_1 - 6 - V_2 + 2V_1 - 2V_2 = 6$$

$$5V_1 - 3V_2 = 12 \quad -\text{①}$$

From ②

$$2 + I_3 + I_2 = I_4$$

$$\frac{2 + V_2 - V_1}{1} + \frac{V_1 - 6 - V_2}{2} = \frac{V_2 - 0}{4}$$

$$8 + 4V_2 - 4V_1 + 2V_1 - 12 - 2V_2 = V_2$$

$$-8 = 2V_1 - V_2 \quad -\text{②}$$

$$2V_1 + 4 = V_2$$

$$5V_1 - 3(2V_1 + 4) = 12$$

$$5V_1 - 6V_1 - 12 = 12$$

$$-V_1 = 24$$

$$V_2 = -38 + 4$$

$$V_1 = -24$$

$$V_2 = -38 + 4$$

$$I_1 = V_1 = -24 \text{ A}$$

$$I_2 = \frac{V_1 - 6 - V_2}{2} = \frac{-24 - 6 + 38}{2} = \frac{44 - 38}{2} = \frac{6}{2} = 3 \text{ A}$$

$$I_3 = V_1 - V_2 = -24 + 38 = 14 \text{ A}$$

$$I_4 = \frac{V_2}{4} = -9 \text{ A}$$

## Magnetic Circuits

Flux  $\phi$ : The magnetic lines of force produced by magnet is called Magnetic Flux.  
Its unit is Weber or Wb

$$1 \text{ Wb} = 10^8 \text{ Magnetic Lines}$$

Characteristic -

- Magnetic flux lines do not have physical existence [With Diagram]
- The direction of flux is defined as the direction in which an isolated north pole would move if it were placed in a magnetic field.
- Each line of flux form a close loop by itself.
- The flux lines never intersect
- The line of flux closer to each other and having same direction repel each other.
- The line of flux closer to each other and having opposite direction attract each other.

Definition of Magnetic Quantity:

Flux Density  $\rightarrow$  It is denoted by  $B$  and it is flux per unit area at a right angle to the flux.  
It's units are  $\text{Wb/m}^2$  or Tesla

Magneto Motive Force  $\rightarrow$  MMF is the cause for producing flux in a magnetic circuit.

It is obtain as the product of current flowing through a coil of  $n$ -turns, its units is A.

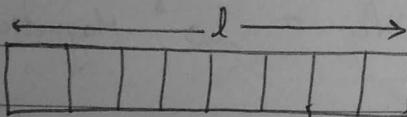
$$\text{MMF} = NI = \text{Amp}$$

Magnetic Field Intensity  $\rightarrow$  [Magnetising Force]

It is denoted by  $H$

It is defined as MMF per unit length of magnetic flux.

Power. It is a major of the ability of magnetising object to produce magnetic induction in another magnetic substance.



$$H = \frac{MMF}{l} = \boxed{\frac{NI}{L} = H}$$

Its Units  $A/m$

Permeability  $\rightarrow$  It is the property of magnetic medium.

Flux Density  $\propto$  Magnetising force which produces its

$$B \propto H$$

$$B = \mu H \quad \mu = B/H$$

$\mu$  is Constant of Proportionality called permeability

Relative Permeability  $\rightarrow$  It is defined as the ratio of flux density produced in that medium to the flux density produced in vacuum.

$$\mu_r = \frac{\mu}{\mu_0} \quad \mu_0 = 4\pi \times 10^{-7}$$

Reluctance  $\rightarrow$  It is def denoted by  $S$

It is defined as ratio of MMF to the flux

$$S = \frac{MMF}{\Phi} = \frac{NI}{\Phi} \text{ or } S = \frac{l}{\mu_0 \rho a}$$

Units -  $A/Wb$

Permeance  $\rightarrow$  It is the reciprocal of reluctance.

Units  $\text{WB} / \text{A}$

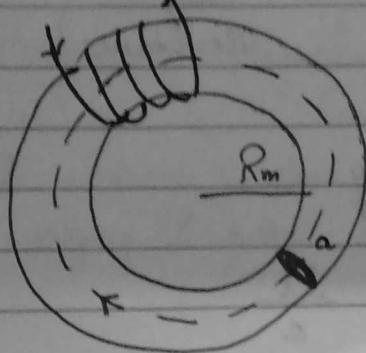
It is readiness with which magnetic flux is developed.

### Magnetic Circuits

Simple

Composite

### Analysis of Magnetic Circuit



$$\text{MMF} = NI$$

$$H = M = \frac{NI}{l} = \frac{NI}{2\pi R_m}$$

$$B = \mu_0 \mu_r H = \frac{\mu_0 \mu_r NI}{l}$$

$$\text{We know that } B = \frac{\phi}{a}$$

$$\phi = Ba$$

$$\phi = \frac{\mu_0 \mu_r NI}{l} a$$

Note  $S = \frac{l}{\mu_0 \mu_r a}$

or

$$\phi = \frac{NI}{\frac{l}{\mu_0 \mu_r a}} = \frac{NI}{S}$$

$$\boxed{\phi = \frac{NI}{S}}$$

$$\text{Flux} = \frac{\text{MMF}}{\text{Reluctance}} \quad \text{by} \quad \text{Current} = \frac{\text{emf}}{\text{Reluctance}}$$

$$B = \frac{\phi}{a} \quad H = \frac{B}{\mu_0 \mu_r}$$

$$\text{MMF} = NI$$

$$H = \frac{NI}{l}$$

$$H = \frac{NI}{\text{Reluctance}}$$

## Magnetic Circuit



- The closed path followed by magnetic flux is known as magnetic circuit.

$$\text{Flux} = \frac{\text{MMF}}{\text{Reluctance}}$$

- MMF
- Reluctivity
- Reluctance

$$S = \frac{l}{\mu_0 \mu_r a}$$

$$\text{Permeance} = \frac{1}{\text{Reluctance}}$$

$$\text{Flux Density } B = \frac{\phi}{a} \text{ Wb/m}^2$$

$$\text{Magnetising force } H = \frac{NI}{A/m}$$

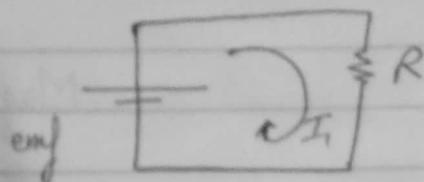
Mag Flux does not actually flow in magnetic circuit

The reluctance of mag circuit is not constant

In a mag circuit, the energy is req to date flux ht to maintain it

In a mag ckt, there is no insulation

## Electric Circuit



- The closed path followed by alternating current is known as electric circuit.

$$\text{Current} = \frac{\text{emf}}{\text{Resistance}}$$

- emf
- Resistivity
- Resistance

$$R = \frac{\rho l}{a}$$

$$\text{Conductance} = \frac{1}{\text{Resistance}}$$

$$\text{Current density } J = \frac{I}{a} \text{ A/m}^2$$

$$\text{Electric field intensity} = \frac{V}{d} \text{ Volt/m}$$

distance

Electric current actually flows in electric circuit

The resistance of electric circuit is Const

In an electric ckt, the energy is required as long as the current flowing through the circuit

These are many insulators.

Magnetic Circuit The closed path followed by magnetic flux.

Magnetic flux follows the complete loop or a circuit coming back to its starting point.

They are classified into 2 types

- ① Simple
- ② Composite

Simple which is made up of single magnetic materials.

Composite have 2 different specimen offering different magnetic properties. Both of them may be magnetic or one of them is non-magnetic.

Analysis of Magnetic Circuit - circular

Consider a ~~solid~~ solenoid having a magnetic path of  $l$ -meters, area of cross section  $A \text{ m}^2$  and coils of current carrying  $I$  current with  $N$  loops.

(Done notes in previous page)

[Assignment Tutorial 2 Q 8, 9] are v.v.v.v. & np

Electromagnetic Induction : The link between electricity and magnetism was discovered by Faraday in 1824. Later in 1831, Faraday discovered that magnetic field can create an electric current in a conductor. When the magnetic flux linking a conductor changes and emf is induced in a conductor. This phenomenon is known as Electromagnetic Induction.

Magnetic effect of electric current : When electric current flows through a conductor, magnetic field is set up along conductors length, The magnetic lines of forces are in the form of concentric circles, around the conductor. The direction of

of lines of forces depends upon direction of current. It can be determined by using 2 rules.

### Rule 1 Right Hand Gripping Rule

Hold the conductor in the right hand with outstretched thumb pointing in the direction of  $I$ . Then the other finger point in the direction of magnetic field around the conductor.

### Rule 2 Right Hand Corkscrew Rule

The direction of magnetic field is in the direction of rotation of a rotation of right hand cork screw turned as to advance along the wire in the current direction.

$\Rightarrow$  The following facts can be noted about the magnetic effect of electric currents:

1. Greater the current through the conductor, stronger the magnetic field.
2. Magnetic field is stronger near the conductor and becomes weaker when we move away from the conductor.
3. The shape of conductor determine pattern of magnetic field.
4. When two conductors carrying the same amount of current in opposition directions are kept side by side then there is no magnetic effect.
5. When two conductors carrying same  $I$  in same direction are kept side by side then the magnetic effect product is twice the effect caused due to one such conductor.

## Current Carrying Conductors in magnetic field

Consider a current carrying conductor or placed at right angle to the magnetic field.

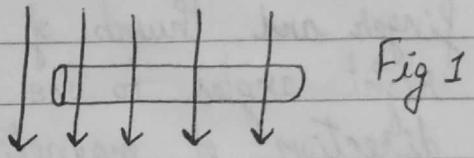


Fig 1

Let  $I$  be current through the conductor in Amperes. and it is the effective length of the conductor in meters.  $B$  is the flux density of magnetic field ( $\text{wb/m}$ ).

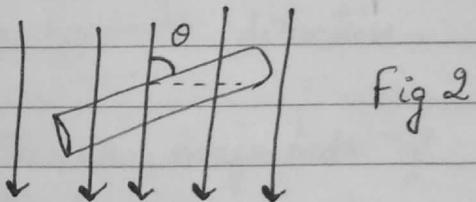


Fig 2

By the law of interaction, the conductor experiences the force which is  $\perp$  to both field and current.

The force,  $F$  acting on the conductor is  $BlI$

$$F = BlI \quad \text{--- ①}$$

This relation is true only when the conductor and the magnetic field are at right angles to each other. If the conductor is inclined at an angle  $\theta$  to the magnetic field (Fig 2), then length of conductor will be

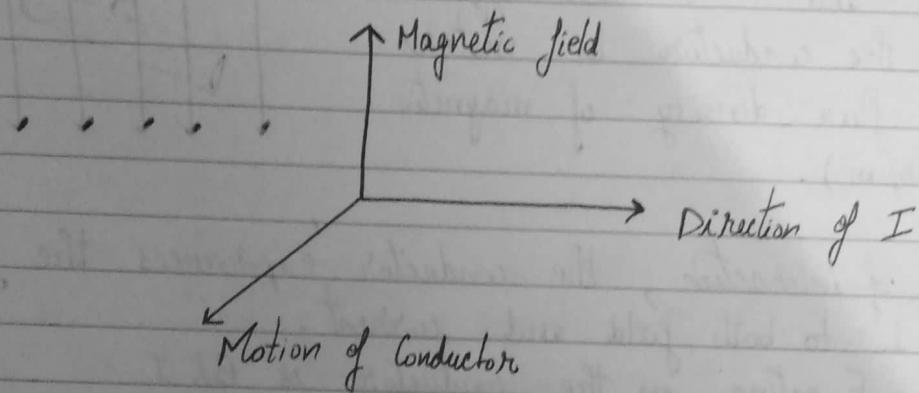
$$l = l \sin \theta \quad \text{--- ②}$$

$$F = Bl \sin \theta \quad \text{--- ③}$$

The direction of force can be calculated by applying Flemings left hand Rule.

## Flemings left Hand Rule :

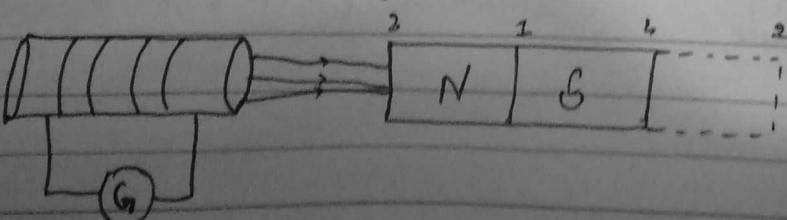
Stretch out the forefinger, middle finger and thumb of the left hand so that they are at right angles to one another. If the forefinger points in the direction of magnetic field ( $N \rightarrow S$ ) and the middle finger points towards the direction of current, then thumb will point in the direction of motion of conductor.



## Laws of Electromagnetic Induction :

- \* Faraday's Law  $\rightarrow$  Whenever the magnetic flux linking a circuit changes and emf is always induced in it. The magnitude of such an emf is proportional to the rate of change of flux linkages.
- \* Lenz Law  $\rightarrow$  This law states that any induced emf will circulate a current in such a direction so as to oppose the cause producing it.

### Illustration of Lenz law :



Case 1 → When bar magnet is stationary (1, 2)  
 [The flux is linking] No deflection

Case 2 → When bar magnet is near coil, flux increased (3, 4)  
 deflection takes place

Case 3 → bar magnet is moved away, flux decreases and  
 deflection in galvanometer but in opposite direction.

It can be noted that amt. of deflection in galvanometer i.e. magnitude of induced emf depends upon the quickness of bar magnet or coils movement.

Hence, we can conclude that whenever the magnetic flux linking a conductor changes an emf is always induced in it.  
 And its magnitude depends on the rate of change of the flux linking with coil.

### Mathematical Explanation :

$N$  → number of turns

$\phi_1$  → flux linked in coil Initially

$\phi_2$  → Final flux linked with coil

$t$  → time taken for creating change in flux

$$\text{Initial Flux linkage} = N\phi_1$$

$$\text{Final Flux linkage} = N\phi_2$$

$$\text{Magnitude of avg induced emf } E = \frac{N\phi_2 - N\phi_1}{t} \quad \checkmark$$

$$= \frac{N(\phi_2 - \phi_1)}{t} \quad \text{--- ①}$$

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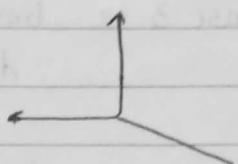
$$= \frac{N(\phi_2 - \phi_1)}{t} \quad \text{--- ①}$$

Calculating differential form of eq ① we get induced emf at any instant

$$E = \frac{N\phi_2 - N\phi_1}{t} = \frac{N(\phi_2 - \phi_1)}{t} \text{ volts}$$

Using lenz law, eq ② can be written as

$$\boxed{E = \frac{Nd\phi}{dt} \text{ volts}}$$



### Flemings Right hand Rule :

The direction of induced emf can be calculated by using Flemings right hand rule

→ Hold the thumb, forefinger and middle finger of the right hand at right angles to one another. If the thumb points to the direction of motion and the forefinger to the direction of magnetic field then the middle finger points towards the direction of induced emf.

Induced Emf : Two types of emf

- ① Dynamically induced emf
- ② Statically induced emf

Self induced emf

mutually induced emf

\* An emf is induced in a coil or conductor whenever there is change in flux linkages. It can be categorised into two ways.

Dynamically induced emf - The Conductor is moved in stationary magnetic field such that there is a mag changed in flux linkages. This kind of emf is called dynamically induced emf.

e.g generators

Statically induced emf The conductor is stationary and magnetic field is moving, this kind of induced emf is known as statically induced emf.

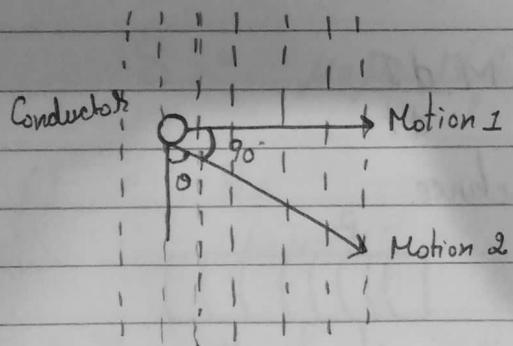
e.g transformer

Dynamically induced emf [Derivation]

Consider a stationary mag. field of flux density ( $B$ ). Let the direction of mag. field is as shown in fig. In this field, a conductor is circular cross section is placed.

Let  $l$  be the effective length of the conductor. Let the conductor is moving at right angles to the field.

In time  $dt$  seconds, the distance moved is  $dx$  m



The area  $a$  enclosed by conductor  $a = l dx$  and flux linked by conductor  $\phi = Ba = Bl dx$  — ①

Acc to Faraday's law

$$\text{induced emf} = E = \frac{\phi}{dt} = \frac{Bl dx}{dt}$$

$$\left[ \frac{dx}{dt} = v \right]$$

$$\therefore \boxed{E = Blv} \text{ volts}$$

Let the conductor  $B$  be moved with same velocity in an inclined direction making an angle  $\theta$  to the direction of field then

$$\text{induced emf } \boxed{E = Blv \sin \theta}$$

## Statistically induced emf

- Self Induced emf : The emf induced in a circuit when the mag flux linking it changes the flux <sup>produced</sup> by current in same circuit.

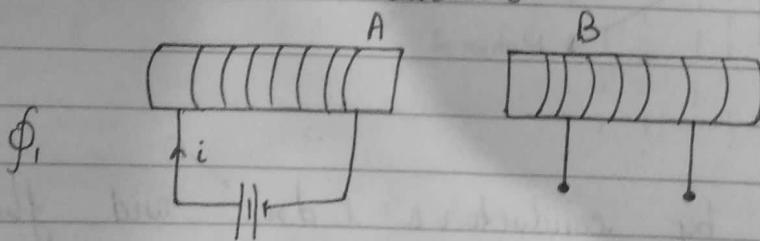
$$E = N \frac{d\phi}{dt} \quad \text{or} \quad E = L \frac{dI}{dt}$$

where  $L$  is coefficient of self inductance

- Mutually Induced emf The emf induced in one circuit due to change of flux linking it, the flux being produced by current in another circuit.

$$E_m = M \frac{dI}{dt}$$

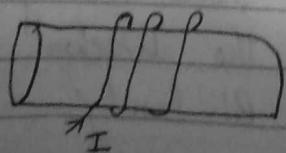
where  $M$  is mutual inductance



## ★ Self Inductance :

Self inductance of a circuit is the flux linkages per unit current.

Denoted by  $L = \frac{N\Phi}{I}$  Henry



## Equation for Self Inductance :

Consider a circuit with no. of turns in magnetising winding  
 $I$  is magnetising Current ,  $l \rightarrow$  length of magnetic Ckt.  
 $a$  is area of cross section  
 $\mu_r$  is the relative Permeability

$$\text{Magnetising force } (H) = \frac{\text{Magnetomotive Force}}{\text{length}} = \frac{NI}{l} \quad \text{--- (1)}$$

MMF  $\rightarrow$  The force which setup magnetic flux in a magnetic circuit.

$$\text{Magnetic Flux Density } (B) = \mu_0 \mu_r H \quad \text{--- (2)} \quad \boxed{B \propto H}$$

Use eq (1) in eq (2)

$$B = \frac{\mu_0 \mu_r N I}{l} \text{ Tesla}$$

$$\begin{aligned} \text{Magnetic flux } (\phi) &= Ba \\ &= \frac{\mu_0 \mu_r N I a}{l} \text{ Weber} \end{aligned}$$

$$\boxed{B = \Phi/a}$$

$$\text{Flux linkage of the circuit is } N\phi = \frac{\mu_0 \mu_r N^2 I a}{l}$$

$$\text{Self Inductance } = \frac{N\phi}{I} = \frac{\mu_0 \mu_r N^2 a}{l}$$

$$L = \frac{N^2}{S}$$

$$\boxed{S = \frac{l}{\mu_0 \mu_r a}}$$

where

$S$  is Reluctance  $\rightarrow$  The opposition offered to magnetic flux by a magnetic circuit

## \* Relationship Self Inductance & Self Induced emf :

We know that induced emf is  $-N \frac{d\phi}{dt}$

and we know that self inductance is  $\frac{N\phi}{I} = L$

For a small increment of current  $dI$ , let the instant flux is  $d\phi$

$$L dI = N d\phi$$

$$L = N \frac{d\phi}{dI}$$

$$L \frac{dI}{dt} = N \frac{d\phi}{dt}$$

$$-L \frac{dI}{dt} = -N \frac{d\phi}{dt} \quad \text{--- } \textcircled{3}$$

$$\boxed{e = -N \frac{d\phi}{dt}}$$

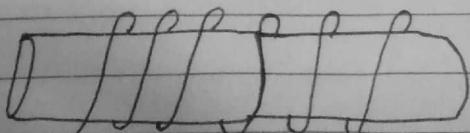
$$\text{where } L = \frac{N^2}{S}$$

The self induced emf in a circuit is directly proportional to the rate of change of current in the same circuit.

## \* Mutual Inductance : Denoted by M

Mutual Inductance b/w 2 circuits is defined as the flux linkages <sup>in 1 sec</sup> per unit current in the other circuit.

Units are Henry



$$M = \frac{N_2 \phi_1}{I_1}$$

$$\& M = \frac{N_1 \phi_2}{I_2}$$

$N_1$  is no. of turns in Coil 1

$a$ : area of cross section

$N_2$  is no. of turns in Coil 2

$I_1$ : Magnetising current in Coil 1

$l$  is length of circuit

$\phi_1$ : Mag flux produced by Current

$\mu_r$  is relative Permeability

Reluctance of the magnetic circuit ( $S$ ) is  $\frac{l}{a\mu_0\mu_r}$

$$\phi_1 \text{ is } \frac{\text{MMF}}{S} = \frac{N_1 I_1}{S}$$

Assume that all the flux ( $\phi_1$ ) links the entire coil 2.

$$\text{So flux linkage of circuit 2 } \psi_{21} = \frac{N_2 N_1 I}{S}$$

$$\psi_{21} = N_2 \phi_1 \quad \boxed{MI = N_2 \phi_1}$$

$$\psi_{21} = MI$$

$$\boxed{M = \frac{\phi_{21}}{I_1}}$$

Relationship b/w Mutual Inductance

$$\text{Mutually induced emf in Coil 2 is } EM_2 = \frac{\phi_{21}}{t} = \frac{N_2 \phi_1}{t}$$

$$\text{At any instance } EM_2 = -N_2 \frac{d\phi_1}{dt} \quad \text{--- ①}$$

$$\text{Mutual inductance b/w 2 circuits can be } \frac{N_2 \phi_1}{I_1}$$

$$MI_1 = N_2 \phi_1$$

$$N_2 \frac{d\phi}{dt} = M \frac{dI_1}{dt}$$

$$-N_2 \frac{d\phi}{dt} = -M \frac{dI_1}{dt} \quad - \textcircled{2}$$

From \textcircled{1} &amp; \textcircled{2}

$$\text{EMF}_2 = -M \frac{dI_1}{dt}$$

Hence

$$\text{EMF}_1 = -M \frac{dI_2}{dt}$$

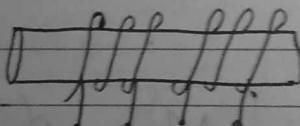
Thus the mutually induced emf in a circuit is directly proportional to the rate of change of current in another circuit.

$\Rightarrow$  Coupling Coefficient b/w two magnetically coupled circuits

$I_2 \rightarrow$  magnetising Current in  $L_2$

$\phi_2$  is flux caused by current  $I_2$

There will be mutual flux linkages when both the coils are energised simultaneously.



Let a fraction of flux  $\phi_1$  is linked in coil 2 is  $K_1 \phi_1$ .

Flux linkages of coil 2  $\Phi_{21} = N_2 K_1 \phi_1$

$$\Phi_{21} = N_2 \phi_1$$

Mutual Inductance  $M = \frac{\Phi_{21}}{I_1} = \frac{N_2 K_1 \phi_1}{I_1}$

$$= \frac{N_2 K_1 (N_1 I_1)}{I_1 S} \quad \phi = \frac{N^2}{S}$$

$$= \frac{N_1 N_2 K_1}{S} \quad - \textcircled{1}$$

Let a fraction of flux  $\phi_2$  is  $K_2 \phi_2$

$$\text{flux linkage of } \psi_{12} = N_1 K_2 \phi_2$$

$$M = \frac{\psi_{12}}{I_2} = \frac{N_1 K_2 \phi_2}{I_2}$$

$$= \frac{N_1 K_2}{I_2} \left( \frac{N_2 F_2}{S} \right)$$

$$= \frac{N_1 N_2 K_2}{S} \quad - \textcircled{2}$$

From  $\textcircled{1}$  &  $\textcircled{2}$

$$M^2 \Rightarrow (M_1 M_2) = \frac{N_1^2 N_2^2 K_1 K_2}{S^2}$$

$$M^2 = \frac{K^2 N_1^2}{S} \cdot \frac{N_2^2}{S} \quad | K_1 = K_2 = K$$

$$M^2 = K^2 L_1 L_2$$

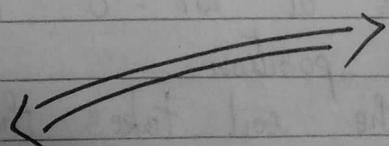
$$\therefore M = K \sqrt{L_1 L_2}$$

where  $L_1$  &  $L_2$  are self inductance of coil 1 and 2.

So,

$$K^2 = \frac{M^2}{L_1 L_2}$$

$$K = \frac{M}{\sqrt{L_1 L_2}}$$



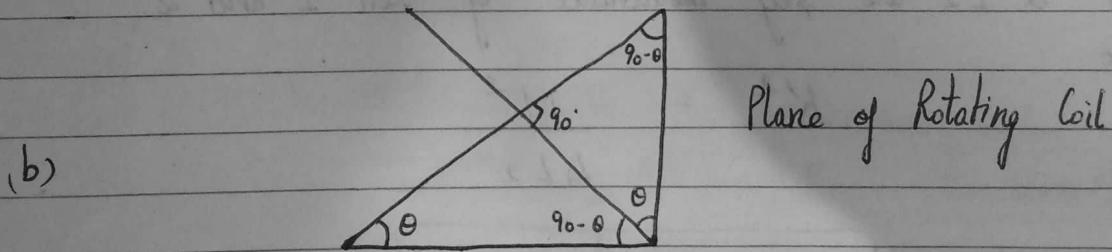
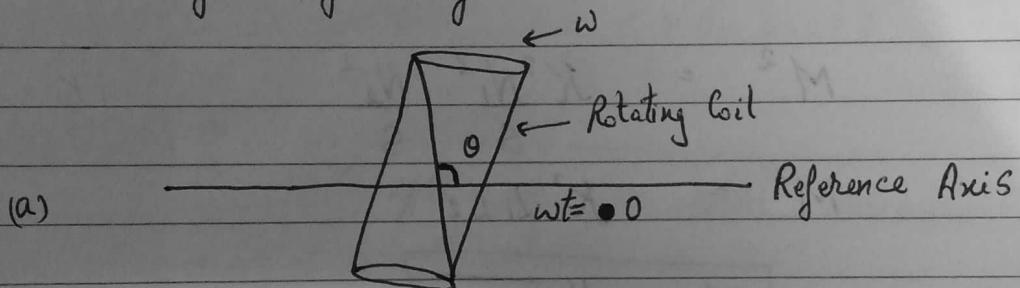
## \* AC Fundamentals :

Alternating quantity is one which is having ~~not~~ varying magnitude and angle with respect to x-axis.  
Since it is time varying in nature. So, we will represent it in three ways:

1. By its effective value
2. By its average value
3. By its peak value

Generation of alternating emf :

Consider a coil having  $n$  turns placed in a magnetic field of ~~Bmax~~ maximum value ' $\phi$ '<sub>m</sub>



The coil is initially along reference axis. Here field is up

When the coil is along reference axis at  $wt = 0$ , it is called zero emf position

at any instant ( $t$ ) sec, the coil takes the position as shown in fig (b). Here coil makes an angle

$\theta = \omega t$  with the reference axis.

In this position, the normal component of mag flux wrt plane of coil  
is  $\phi = \phi_m \cos \theta$

$$\theta = \omega t$$

$$\therefore \phi = \phi_m \cos \omega t$$

Flux linkage at this instant =  $N\phi = N\phi_m \cos \omega t$

The emf induced in this coil at this instant  $e = -\frac{d\phi}{dt}$

$$e = -\frac{(N\phi_m \cos \omega t)}{dt}$$

$$e = -\frac{d}{dt}(N\phi_m \cos \omega t) = \boxed{e = \omega N \phi_m \sin \omega t} \quad \text{--- (1)}$$

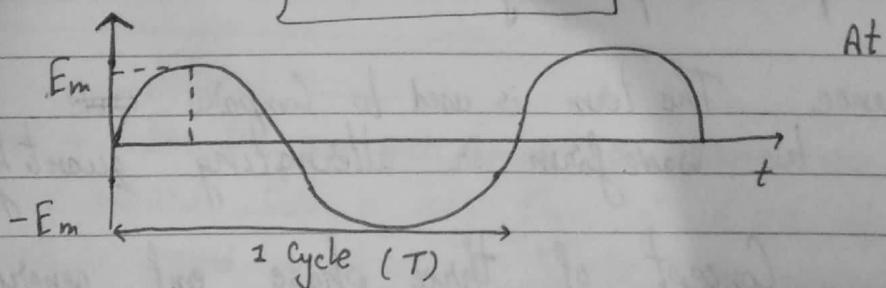
With eq(1) we can ~~do~~ calculate emf at any instant differently

- at  $\omega t = 0$  or  $180^\circ$   $e = 0$

- at  $\omega t = 90^\circ$   $e = \omega N \phi_m$  (Max)

- at  $\omega t = 270^\circ$   $e = -\omega N \phi_m$

Let  $N\phi_m$  denotes the maximum value of induced emf. So  
we can write it as  $\boxed{e = E_m \sin \omega t}$

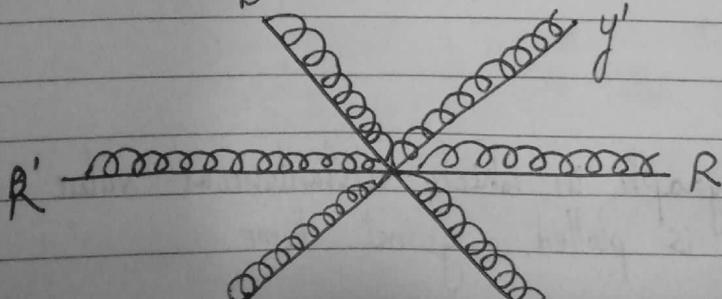


Important Terms :

- Waveform  $\rightarrow$  It is a graph in which instantaneous value of any quantity is plotted against time

- Alternating Waveform It reverses its direction at regularly recurring intervals.
- Periodic Waveform It repeats itself after definite time interval.
- Cycle One Complete Set of positive and negative half combine to form a cycle
- Amplitude The maximum +ve or -ve value of an alternating quantity is known as amplitude
- Frequency The no. of cycles per second of an alternating quantity is known as frequency.
- Period Time period of an alternating quantity is the time taken to complete one cycle.
- Phase It is the time that has elapsed since the quantity has last past through O point of reference and passed positively.
- Phase Difference This term is used to compare the phase of two wave form or alternating quantity.

⇒ Concept of three phase emf generation



120° separation  
with anticlockwise

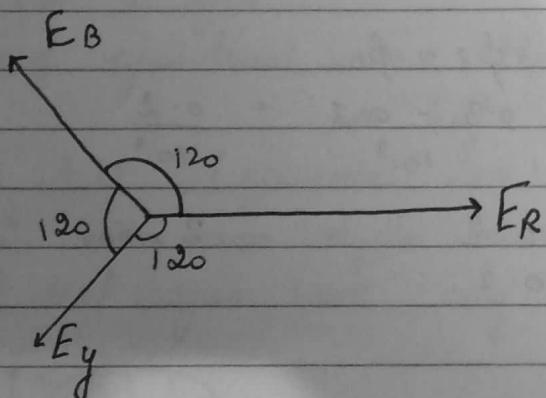
Consider three coils YY', RR', BB' placed in mag field of max value  $\phi_m$ . The coils are displaced by an angle of  $120^\circ$  in space b/w any two. Let all the coils rotate in anticlockwise direction with angular velocity  $\omega$

$$e_R = E_m \sin \omega t$$

$$e_Y = E_m \sin (\omega t - 120^\circ)$$

$$e_B = E_m \sin (\omega t - 240^\circ)$$

Phasor Diagram



The RYB indicates that R reaches at its maximum value first Y phase follows R and B follows Y reaching R.  
(RYB)

Hence, this sequence describes positive phase sequence.

Felts Poles

Ques The field coil of 4 pole DC gen each having 500 turns are Connec in Series. When field is excited, there is mag flux of  $0.02 \text{ Wb/P}$  if the field circuit is opened in  $0.02 \text{ S}$  & residual magnetism is  $0.002 \text{ Wb/Pole}$ , Calculate the avg voltage which is induced across the field terminals. In which direction, is voltage directed in the dir of current.

Que 2A

A Coil of resistance  $150\ \Omega$  placed in magnetic flux of  $0.1\ \text{Wb}$ . The Coil has 500 turns and a galvanometer  $450\ \Omega$  is Conn in Series with it. The Coil is moved  $0.1\text{s}$  from the given field to another field of  $0.3\text{ miliwb}$ . Find the avg induced emf & avg current through the coil?

$$R = 150 \quad \phi_1 = 0.1 \quad N = 500$$

$$e =$$
  
$$(IV)$$

$$\text{emf} = N \frac{d\phi}{dt}$$

$$i = \frac{V}{R}$$

$$d\phi = \phi_2 - \phi_1 \\ = \frac{0.3 - 0.1}{10^3} = \frac{0.2}{10^3}$$

$$= \frac{IV}{150 + 550}$$

$$= \frac{1}{600}$$

$$e = 500 \times \frac{0.2}{0.1} = 2 \times 500 = \frac{1000}{10^3} V = 0.0017$$

$$\boxed{e = IV}$$

\* Values of alternating quantity of Current :

Peak Value - The max value attained by an alt. quantity during one cycle is called peak value or max. value or crest or amplitude.

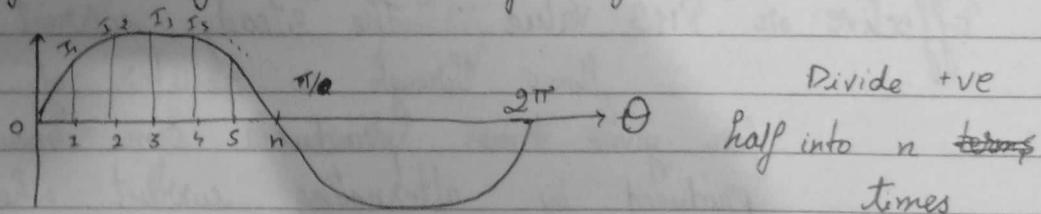
at  $90^\circ$  Max value is  $E_m$

Avg value or Mean Value - The arithmetic average of all the instantaneous value considered of an alternating quantity ( $i$  or  $v$ ) over a cycle.

e.g. in case of symmetrical waves, the +ve half is equal to -ve half cycle.

So net  $= 0$  (sine wave)  $\int_{-\pi}^{\pi}$  (1 cycle)

Therefore, avg value over one cycle is zero. So, to determine avg value of such symm wave, only half cycle is considered



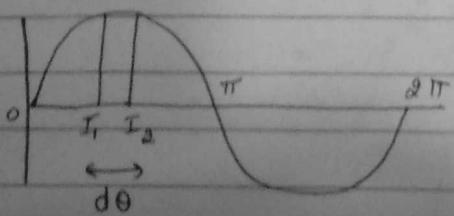
Mid Coordinates are  $i_1, i_2, \dots$

Formula

$I_{av} = \text{Mean value of mid ordinates}$

$$I_{av} = \frac{I_1 + I_2 + I_3 + I_4 + \dots + I_n}{n}$$

$$= \frac{\text{area of alternation}}{\text{Base}}$$



$$Im \sin \theta = i$$

Consider elementary strip of thickness  $d\theta$  in the +ve half cycle where  $i$  is the mid ordinate then area of strip  $= id\theta$

$$\text{Area of strip} = I_d \theta \pi$$

$$\text{Area of half cycle} = \int_0^{\pi} I_d \theta$$

$$= \int_0^{\pi} I_m \sin \theta \, d\theta$$

$$= -I_m \cos \theta \Big|_0^{\pi}$$

$$= -I_m [ \cos \pi - \cos 0 ]$$

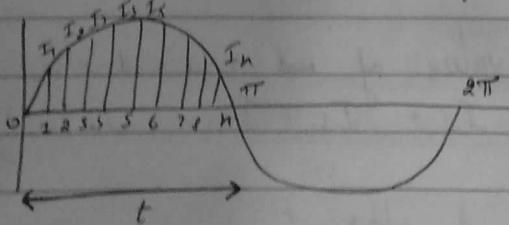
$$= -I_m [ -1 - 1 ]$$

$$= 2 I_m$$

Base =  $\pi$

$$\text{Avg value of Current} = \frac{2 I_m}{\pi} = 0.637 I_m$$

**Effective or RMS Value:** The steady current which when flows through a resistor of known resistance for given time produces same amount of heat as produced by alternating current when flows through the same current for the same time.



Let  $i$  be the alternating current flowing through resistor  
 $t \rightarrow$  time taken

$I_{eff} \rightarrow$  by dc

Each interval is having  $t/n$  (s) duration  
 Mid ordinates are  $i_1, i_2, i_3, \dots, i_n$

Then the heat produced

in 1st interval

$$H = i^2 R t$$

2nd interval

$$= i_1^2 R t/n$$

$n^{th}$

$$= i_n^2 R t/n$$

$$\text{Total heat produced} = \frac{i_1^2 R t}{n} + \frac{i_2^2 R t}{n} + \dots + \frac{i_n^2 R t}{n}$$

Since, Total heat produced is equal to heat produced by DC  
 $\therefore I_{\text{eff}}^2 R t = \text{Total heat produced}$

Comparing both Equations

$$I_{\text{eff}}^2 = \frac{i_1^2 + i_2^2 + i_3^2 + \dots + i_n^2}{n}$$

∴  $I_{\text{eff}}$  is equal to square root of mean of squares of instantaneous values.

or also called Root mean square value

Note. RMS is the actual value of alternating quantity which tells the energy transfer of alternating current source capability

RMS value of Sinosoidal wave :

To determine the RMS value, the squared wave of alternating current is drawn in which elementary strip of thickness  $d\theta$  in first half cycle ( $i^2$ ) is the mid ordinate

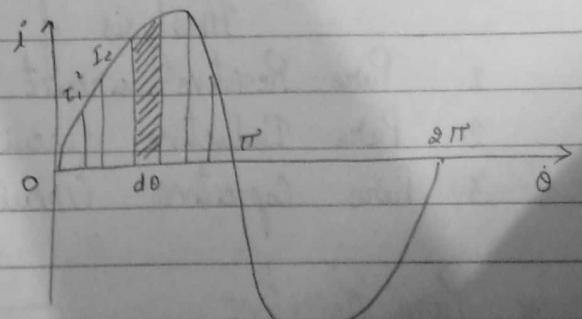
$$I = I_m \sin \theta$$

$$\text{Area of strip} = I^2 d\theta$$

$$\text{Area of +ve cycle} = \int_0^\pi I^2 d\theta$$

$$= \int_0^\pi I_m^2 \sin^2 \theta d\theta$$

$$= I_m^2 \int_0^\pi \frac{1 - \cos 2\theta}{2} d\theta$$



$$= \frac{I_m^2}{2} \left[ \theta - \frac{\sin 2\theta}{2} \right]_0^{\pi}$$

$$= \frac{I_m^2}{2} [\pi] = \frac{\pi I_m^2}{2}$$

$$\text{Base} = \pi$$

$$\text{Area of First half} = \frac{\pi}{2} I_m^2$$

$$I_{rms} = \frac{\sqrt{\text{Area of 1st half of sig}}}{\text{Base}} = \frac{I_m}{\sqrt{2\pi}}$$

$$I_{rms} = 0.707 I_m$$

- Forum Factor - It is the ratio of RMS value to ~~avg~~<sup>avg</sup> value of an instantaneous quantity

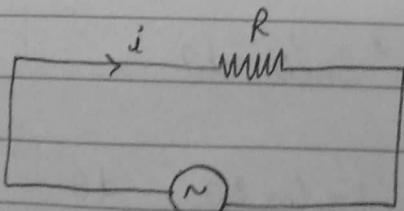
- Peak Factor - It is the ratio of peak value to the rms value of alternating voltage or current.

### \* Phasor Representation of Alternating Quantities :

Analysis of AC Circuits →

1. Pure Resistive circuit
2. Pure Inductive Circuit
3. Pure Capacitive Circuit

#### \* Pure Resistive



$$V = V_m \sin \omega t$$

We know that

$$V = V_m \sin \omega t$$

$$\text{&} \quad V = iR$$

$$i = \frac{V}{R} = \frac{V_m \sin \omega t}{R}$$

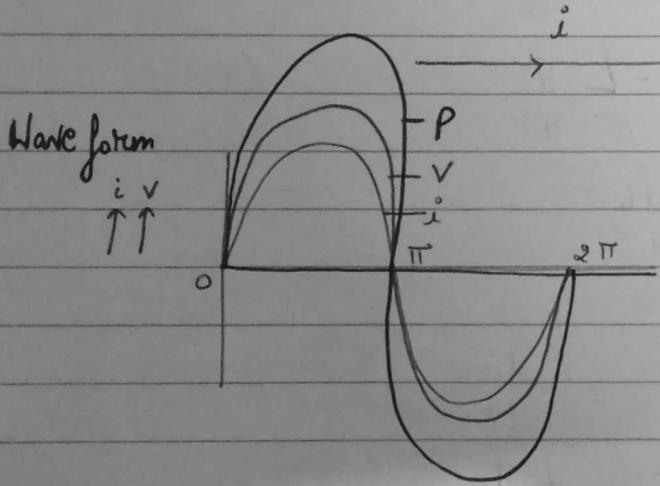
$$\text{So } i = I_m \sin \omega t$$

resulting

From ① & ② we find that applied voltage and current are in same phase with each other.

### Phasor Representation

Voltage and current are in same phase



Independence

$$Z = \frac{\text{Total voltage}}{\text{Total current}}$$

$$Z = \frac{V}{i} = \frac{V_m \sin \omega t}{I_m \sin \omega t}$$

$$= \frac{V_m}{I_m} = \frac{V_m}{\frac{V_m}{R}} \quad \boxed{Z = R}$$

Avg Power

$$P = VI$$

$$P = V_m \sin \omega t I_m \sin \omega t$$

$$= V_m I_m \sin^2 \omega t \quad (\omega t = 0)$$

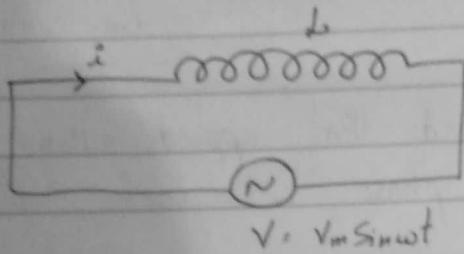
$$\text{Avg } P = \int_0^{\pi} V_m I_m \sin^2 \omega t \, d\theta = V_m I_m \int_0^{\pi} \frac{1 - \cos 2\theta}{2} \, d\theta$$

$$= \frac{V_m I_m}{2} \left[ \theta - \frac{\sin 2\theta}{2} \right]_0^{\pi} = \frac{V_m I_m \pi}{2} \therefore \frac{V_m I_m \pi}{2}$$

**Power Factor** It is the Cosine of the phase angle b/w voltage and current.

$$\cos \phi = \cos 0 = 1.$$

### \* Pure Inductive



We know that  
and

$$V = V_m \sin \omega t \quad \text{--- (1)}$$

Self induced emf always opposes the applied voltage

$$e = -L \frac{di}{dt} \quad (V = -e)$$

$$V = L \frac{di}{dt} \quad \text{--- (2)}$$

Use (1) in (2)

$$V_m \sin \omega t = L \frac{di}{dt}$$

$$V_m \sin \omega t dt = L di$$

$$\int di = \int \frac{V_m \sin \omega t}{L} dt$$

$$i = \frac{V_m}{L} \int \sin \omega t dt$$

$$X_L = \omega L$$

$$i = \frac{V_m}{\omega L} \left[ -\cos \omega t \right]$$

$$\therefore i_m = \frac{V_m}{X_L}$$

$$i = \frac{V_m}{\omega L} i_m \sin \left( \omega t - \frac{\pi}{2} \right) \quad \text{--- (3)}$$

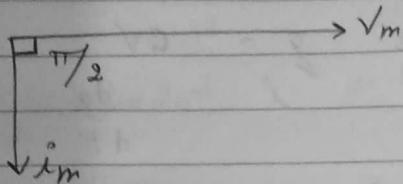
$$Z = \frac{V_m}{I_m} = \frac{\frac{V_m}{\sqrt{2}}}{\frac{I_m}{\omega L}}$$

$$Z = \underline{\omega L}$$

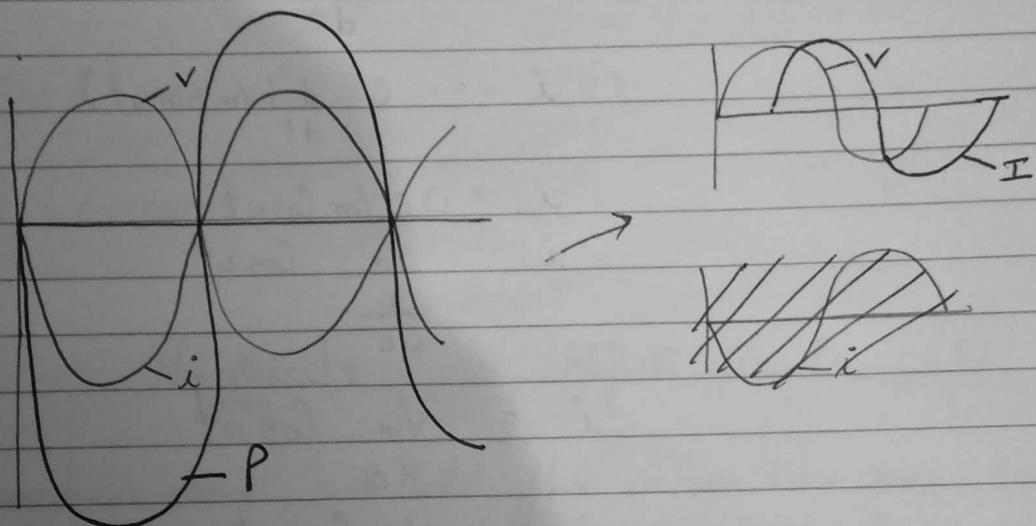
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From Q. 20  
③ The current through inductance lags behind the applied voltage by an angle of  $90^\circ$ .

Phasor :



Waveform



Avg Power

$$P = VI$$

$$P = -V_m \sin \omega t I_m \cos \omega t$$

$$P = -\frac{V_m I_m}{2} (\sin \omega t \cos \omega t)$$

$$\text{Avg } P = \int_0^{\pi} -\frac{V_m I_m}{2} \sin \omega t \cos \omega t dt = -\frac{V_m I_m}{2} \int_0^{\pi} \sin 2\omega t dt$$

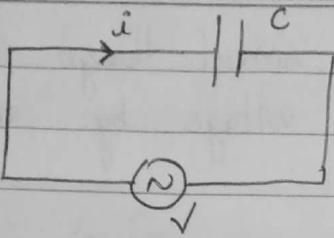
$$= -\frac{V_m I_m}{2} \left[ -\frac{\cos 2\omega t}{2\omega} \right]_0^{\pi}$$

$$= -\frac{V_m I_m}{2} \left[ -\cos \pi + \cos 0 \right] = 0$$

Power Factor

$$\cos \phi = \cos 90^\circ = 0$$

Pure Capacitive



$$V = V_m \sin \omega t \quad \text{--- (1)}$$

We know

$$\begin{aligned} \text{charge on capacitor } q &= CV \\ \text{current through circuit } i &= \frac{dq}{dt} \end{aligned}$$

$$\therefore i = \frac{d(CV)}{dt}$$

$$i = C \frac{d(V_m \sin \omega t)}{dt}$$

$$i = \omega C V_m \cos \omega t$$

$$i = \frac{V_m}{\omega C} \cos \omega t$$

$$i = \frac{V_m}{X_C} \cos \omega t$$

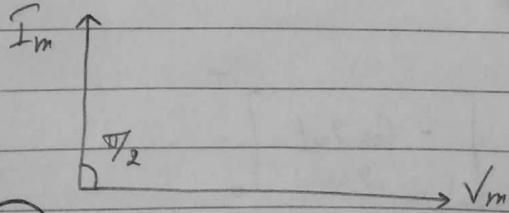
$$i = I_m \cos \omega t$$

$$i = I_m \sin \left( \omega t + \frac{\pi}{2} \right) \quad \text{--- (2)}$$

From (1) & (2)

In a pure Capacitive circuit, ~~capacitor leads~~ current leads the applied voltage by an angle of  $90^\circ$ .

Phasor



Waveform



Thy Power

$$P = VI$$

$$P = V_m \sin \omega t I_m \sin(\omega t + \frac{\pi}{2})$$

$$P = \frac{V_m I_m}{2} \sin 2\omega t$$

$$\text{Avg } P = \int_{-\pi}^{\pi} \frac{V_m I_m}{2} \sin 2\omega t = 0$$

Power Factor

$$\cos \phi = \cos 90^\circ = 0$$

No power is consumed....

### Numericals : Magnetic Circuits (5)

Q1: Find the exciting current and total flux in an iron ring 10 cm in mean diameter  $10 \text{ cm}^2$  in cross section and wound 150 turns of wire. The flux density is  $0.1 \text{ Wb/m}^2$  and permeability  $(\mu_r)$  is 800.

(2.083  
 $\times 10^3 \text{ A}$ )

$$\begin{aligned} \phi &= BA \\ &= 0.1 \times (10 \times 10^{-4}) \\ &= 1 \times 10 \times 10^{-4} = 10^{-4} \end{aligned}$$

$$\text{Total Flux} = 0.1 \text{ mWb}$$

$$\frac{\phi L}{A \mu_0 \mu_r} = NI \quad (\text{Resistance})$$

$$L = \pi D$$

$$\begin{aligned} L &= 3.14 \times 10 \times 10^{-2} \\ &= 3.14 \times 10^{-2} \end{aligned}$$

$$\frac{\frac{4\pi \times 10^{-7}}{10 \times 10^{-4}} \times 0.1 \times 3.14 \times 10^{-1}}{800 \times 150} = I$$

(l)

Q2 An air core solenoid has length 30 cm and D of 1.5 cm.  
 Calculate its reluctance if it has 900 turns.

(s)

(N)

(1350939

 $\times 10^3 \text{ A/Wb})$ 

$$S = l$$

$$\alpha \mu_0 \mu_r$$

$$a = \frac{\pi D^2}{4} \frac{\mu_0 \mu_r}{\delta}$$

$$\mu_r = 1 \text{ (Default)}$$

$$S = \frac{30 \times 10^{-2} \times \pi \times 1.5 \times 10^{-2}}{\pi \times (1.5 \times 10^{-2})^2 \times 1} = 400 \quad \cancel{813.33}$$

x

(l)

(II)

Que 3 A Conductor 10 cm long carrying current of 60 A lies  $\perp$  to a field of strength 1000. Calculate ① Force acting on the Conductor  
 (II) ② Mechanical Power to move this Conductor  
 against this force a speed of 1 m/s<sup>(v)</sup>  
 ③ Emf induced in the conductor.

$$\text{Force} = BIl = \mu_0 H Il = 4\pi \times 10^{-7} \times 1000 \times 60 \times 1 \text{ N}$$

1 PP

$$= 24\pi \times 10^{-4} \text{ N} \quad (7.5 \times 10^{-3} \text{ N})$$

$$\text{Power} = F \times v$$

$$= 7.5 \times 10^{-3} \times 1 = 7.5 \times 10^{-3} \text{ W}$$

$$\text{Emf} = Blv = \mu_0 H l v = 4\pi \times 10^{-7} \times 1000 \times 1 \times 1 \text{ V}$$

19

$$= 4\pi \times 10^{-5} \text{ V}$$

Que 4 The no. of turns in two coupled coils are  $N_1$  &  $N_2$ . When a current of 6A flows in second coil. The total mag flux produced in Coil is 0.8 mWb ( $\phi_2$ ) and the flux linked with the first coil is 0.5 ( $\phi_1$ ). Calculate  $I_1$ ,  $I_2$  and  $K_M$ .

(0.228)

(0.226)

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$$l_1 = \frac{N_1 \phi_1}{I_1}$$

$$l_2 = \frac{N_2 \phi_2}{I_2}$$

**M** =  $K \sqrt{l_1 l_2}$

(0.05)



(0.625)

$$M = \frac{N_1 N_2 K}{S}$$

$$K = \frac{\phi_{21}}{\phi_2}$$

Q5 A Conductor of length 1m moves at right to a uniform Mag field of density 1.5 wb/m with a velocity of 50 m/s Calculate the emf used in it. also find the value of induced emf when Conductor moves at  $30^\circ$  to the direction of field ?

$$\text{emf} = Blv$$

$$= 1.5 \times 1 \times 50$$

$$= 75$$

$$\text{ind emf} = Blv \sin \theta$$

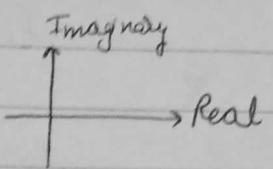
$$= 75 \sin 30$$

$$= 75 \cdot \frac{1}{2} = 37.5$$

# Single Phase AC Circuits :

Phasors :

- Magnitude
- Angle



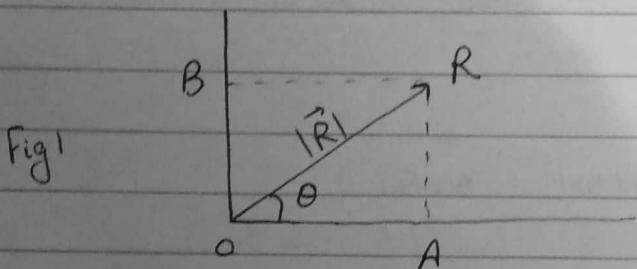
$$a \pm ib$$

$$\text{Mag} = \sqrt{a^2 + b^2}$$

$$\text{Angle} = \theta = \tan^{-1}\left(\frac{b}{a}\right)$$

The phasor of alternating quantities can be represented as

(a) Rectangular form



(b) Polar form

1. Rectangular In  $\triangle OAR$   $\cos \theta = \frac{OA}{OR}$

$$OA = OR \cos \theta = R \cos \theta \quad \text{--- (1)}$$

By  $\sin \theta = \frac{AR}{OR}$

$$RA = OR \sin \theta = R \sin \theta \quad \text{--- (2)}$$

X Component  $\Rightarrow R \cos \theta$

Y Component  $\Rightarrow R \sin \theta$

$$\therefore \vec{R} = R \cos \theta + i R \sin \theta \quad \text{--- (3)}$$

$$R = a + ib$$

2. Polar In fig (1) if vector  $|R|$  represent magnitude of the vector then  $\theta$  will represent angle.

Then expression R will be -

$$R = \sqrt{a^2 + b^2}$$

$$\text{and } \theta = \tan^{-1} \left( \frac{b}{a} \right)$$

$$|R| \text{ angle } \pm \theta$$

$$\text{or } R e^{\pm i\theta}$$

e.g. Express the Complex no. in polar form  $7 - 5j$

$$|\vec{R}| = \sqrt{(7)^2 + (5)^2} = \sqrt{58+25} = \sqrt{73}$$

$$= 8.602$$

$$\theta = \tan^{-1} \left( \frac{-5}{7} \right) = -0.62$$

$$= -35.54^\circ$$

ab.  $8.602 < -35.54$

$$\begin{array}{ll} ① & -9 + 6j \\ ② & -8 - 8j \end{array} \quad ] \text{ Practise}$$

Que Solve the expression in polar form  $10 \angle 60^\circ + 8 \angle -45^\circ$

$$\Rightarrow 10e^{60^\circ} + 8e^{-45^\circ}$$

$$\Rightarrow 10 \left[ \cos 60^\circ + i \sin 60^\circ \right] + 8 \left[ \cos (-45^\circ) + i \sin (-45^\circ) \right]$$

$$\Rightarrow 10 \cos 60^\circ + 10i \sin 60^\circ + 8 \cos (-45^\circ) + 8i \sin (-45^\circ)$$

$$= 10 \times \frac{1}{2} + i 10 \times \frac{\sqrt{3}}{2} + 8 \cos \left( -\frac{45}{\sqrt{2}} \right) + \left( -8i \frac{1}{\sqrt{2}} \right)$$

$$= 5 + i 5\sqrt{3} + \frac{8}{\sqrt{2}} - \frac{8i}{\sqrt{2}} \Rightarrow 10.656 + i 3.01$$

$$= 5 + 5.656 + i (8.66 - 5.656)$$

$$= 10.656 + i 3.01$$

$11.07 \angle 15.72^\circ$

$$\begin{aligned}
 \text{Magnitude} &= \sqrt{(10.66)^2 + (3.01)^2} \\
 &= \sqrt{113.63 + 9.06} \\
 &= \sqrt{122.69} = 10.61
 \end{aligned}$$

$$\begin{aligned}
 \text{Angle} &= \tan^{-1} \left( \frac{3.01}{10.66} \right) \\
 &= \tan^{-1} (0.282) \\
 &= 0.1274 \quad 15.74^\circ
 \end{aligned}$$

$$\begin{aligned}
 ① \quad (-2 - 5j) &\div (5 + 7j) \\
 ② \quad (5 + 4j) \times (-4 - 6j) &
 \end{aligned}
 \quad \left. \begin{array}{l} \text{Practise } 46.15 < -83.03^\circ \\ 5.39 < -111.8^\circ \\ 8.6 < 55.56^\circ \end{array} \right\}$$

NOTE

Multiplication of two complex

$$A \angle \theta \times B \angle \phi = AB \angle \theta + \phi$$

Division of two Complex

$$A \angle \theta \div B \angle \phi = \frac{A}{B} \angle \theta - \phi$$

Practise

Q1. Express in polar @  $-9 + 6j$

$$\text{Mag} = \sqrt{81 + 36} = \sqrt{117} = 10.82$$

$$\theta = \tan^{-1} \left( \frac{-6}{-9} \right) = \tan^{-1} \left( \frac{2}{3} \right) = -33.69^\circ$$

$$10.82 \angle -33.69^\circ$$

$$b. -8 - 8j$$

$$|\vec{R}| = \sqrt{64 + 64} = \sqrt{128}$$

$$= 11.31$$

$$\theta = \tan^{-1}\left(\frac{-8}{8}\right) = \tan^{-1}(0) = 0^{\circ}$$

$$\therefore 11.31 \angle 0^{\circ}$$

$$11.31 e^{0^{\circ}}$$

Q Express in polar form (a)  $(-2 - 5j) \div (5 + 7j)$



$$(i) -2 - 5j$$

$$\text{Mag} = \sqrt{4+25} = \sqrt{29} = 5.38$$

$$\theta = \tan^{-1}\left(\frac{5}{2}\right) = \tan^{-1}\left(\frac{5}{2}\right) = 68.19^{\circ}$$

$$5.38 \angle 68.19^{\circ}$$

$$(ii) 5 + 7j \quad \text{Mag} = \sqrt{25+49} = \sqrt{74} = 8.6$$

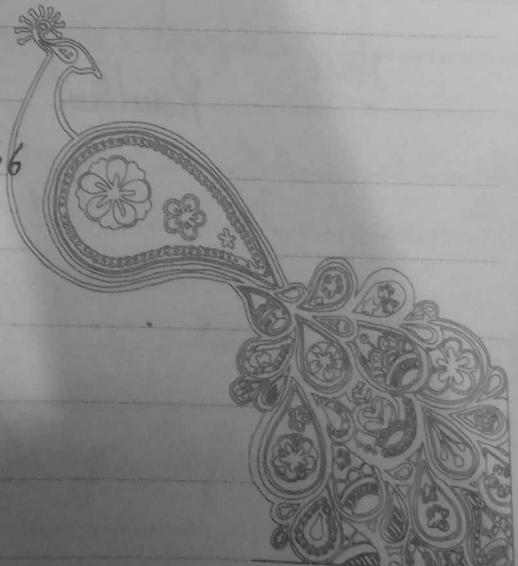
$$\theta = \tan^{-1}\left(\frac{7}{5}\right) = 54.46^{\circ}$$

$$8.6 \angle 54.46^{\circ}$$

Resultant:  $5.38 \angle 68.19 \div 8.6 \angle 54.46$

$$\Rightarrow \frac{5.38}{8.6} \angle 68.19 - 54.46$$

$$\Rightarrow 0.625 \angle 13.73^{\circ}$$



(b)  $(5+4j) \times (-4-6j)$

(i)  $5+4j$

$$\text{Mag} = \sqrt{25+16} = \sqrt{41}$$
$$= 6.40$$

$$\theta = \tan^{-1}\left(\frac{4}{5}\right) = 38.65^\circ$$

$$\therefore 6.40 \angle 38.65^\circ$$

(ii)  $-4-6j$

$$\text{Mag} = \sqrt{16+36} = \sqrt{52}$$
$$= 7.21$$

$$\theta = \tan^{-1}\left(\frac{6}{4}\right) = 56.30^\circ$$

$$\therefore 7.21 \angle 56.30^\circ$$

Hence

Resultant

$$6.40 \angle 38.65^\circ \times 7.21 \angle 56.30^\circ$$

$$\rightarrow (6.40)(7.21) \angle 38.65 + 56.30$$

$$= 46.144 \angle 94.95^\circ$$

\* RL, LC, RC Series Circuit Thd Power Calculations :

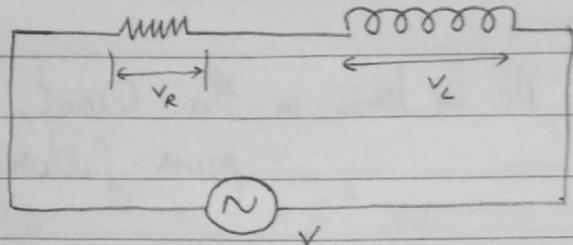
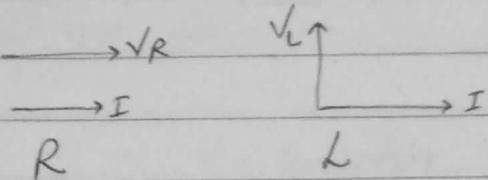
RL Circuit :

In Case of purely resistive circuit,

$\sqrt{V}$  &  $I$  in same phase

$$R = \sqrt{V_R} = IR$$

$$L = \sqrt{V_L} = IX_L$$



$$\text{Applied Voltage } V = V_R + V_L \quad - \textcircled{1}$$

$$V = IR + jIX_L - \textcircled{2} \quad I [R + jX_L]$$

$$\frac{V}{I} = R + jX_L$$

$$\text{Impedance } Z = R + jX_L$$

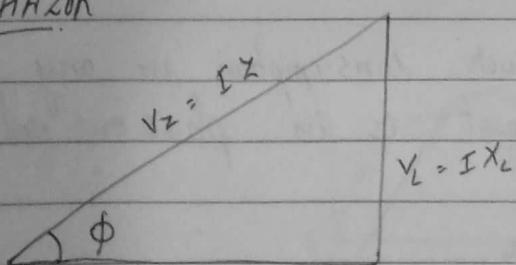
$$\text{So, } V = \sqrt{(V_R)^2 + (V_L)^2} = \sqrt{(IR)^2 + (IX_L)^2}$$

$$V = I \sqrt{R^2 + X_L^2} \quad - \textcircled{3}$$

$$I = \frac{V}{\sqrt{R^2 + X_L^2}} \quad \frac{V}{I} = \sqrt{R^2 + X_L^2}$$

$$|Z| = \sqrt{R^2 + X_L^2} \quad - \textcircled{4}$$

PHAZOR



$$V_R = IR$$

From the triangle ABC

$$\tan \phi = \frac{X_L}{R} = \frac{\omega L}{R}$$

$$\phi = \tan^{-1} \left( \frac{X_L}{R} \right) - \textcircled{5}$$

$\phi$  is called the phase angle and it is the voltage angle b/w voltage and angle.

Power Factor

$$\cos \phi = \text{Power Factor}$$

$$\cos \phi = \frac{R}{Z}$$

As we know in this Circuit, the current lags the voltage so the power factor is lagging.

$$\cos \phi = \cos \left( \tan^{-1} \left( \frac{x_L}{R} \right) \right) \quad - \textcircled{5}$$

Power Calculation

The Principle Current  $I$  can be written in two forms of current Component i.e.  $I_a$  and  $I_r$ .  
First one is a component  $I_a$  in phase with voltage  
this is called active or real or Wattfull Component.

$$\therefore I_a = I \cos \phi$$

Second, the component  $I_r$  at right angle to voltage  
this component is called Reactive or Quadrative  
or Watties Component

$$\therefore I = \sqrt{I_a^2 + I_r^2}$$

We will calculate three types of power, ① Actual Power, ② Reactive Power  
③ Complex Power.

Actual Power ( $P$ ) - There is a real power consumption in any (True) circuit when a current component is in phase with voltage

It is measured in Watt

$$P = VI_a$$

$$P = VI \cos \phi$$

$$P = V \frac{IR}{Z} = \frac{V \cdot IR}{Z}$$

$$P = I^2 R$$

It can be seen that the actual power consumption is dependent on power factor circuit.

### Reactive / Quadrature Power ( $Q$ )

$Q = \sqrt{V^2 - P^2}$  or  
 $Q = V \times \text{quadrature component of current}$

When  $90^\circ$  phase apart

$$Q = V I_r$$

$$Q = V I \sin \phi$$

$$Q = V I \frac{X_L}{Z} = I^2 X_L$$

Units of reactive power is VAR (Reactive Volt Ampere)

Complex or Apparent Power ( $S$ ) It is calculated as the product of voltage and current and measured in Volt Ampere

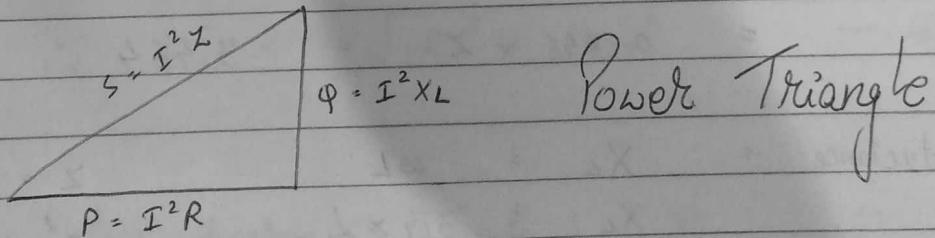
Resultant Power

$$S = V I \rightarrow \text{Total Current (Resultant)}$$

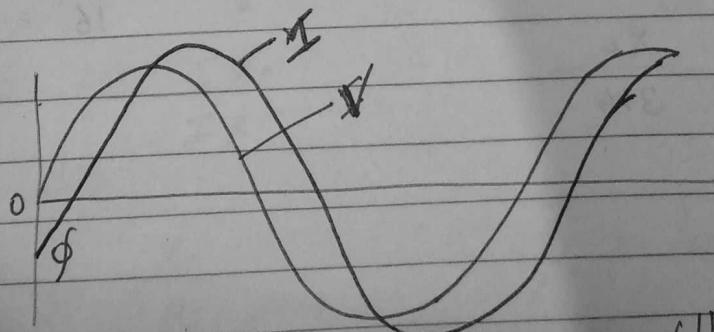
$$S = I^2 Z$$

$$S = \frac{V^2}{Z}$$

These three powers can be represented as



Waveform



Voltage leads Current

Q In a series circuit containing pure resistive & inductive, the current and voltage are expressed as  $i(t) = 5 \sin [314 + \frac{2\pi}{3}]$

$$v(t) = 20 \sin [314 + \frac{5\pi}{6}]$$

Find (i) impedance

(ii) resistance, inductance and power factor

$$\text{Phase Angle of } V = \frac{2\pi}{3} \times \frac{180}{\pi}^{\circ} = 120^{\circ}$$

$$\text{Phase Angle of } I = \frac{5\pi}{6} \times \frac{180}{\pi}^{\circ} = 150^{\circ}$$

Voltage leads by  $30^{\circ}$

$$\text{Power Factor} = \cos \phi = \cos 30 = \frac{\sqrt{3}}{2} = 0.8$$

$$\text{Impedance} = Z = \sqrt{R^2 + X_L^2} = \frac{20}{5} = 4$$

$$\text{Resistance} = R = \frac{Z \cos \phi}{Z}$$

$$= 0.866 \times Z = 3.464$$

$$\text{Inductance} = X_L = \omega L$$

$$X_L = 314 \times L$$

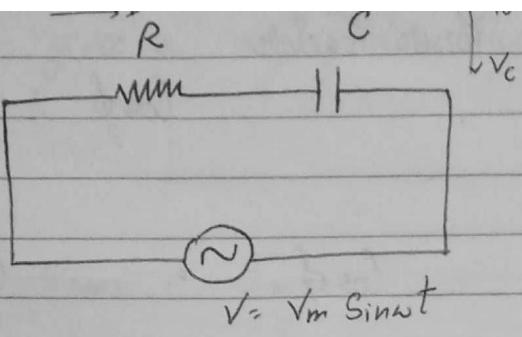
$$Z = \sqrt{R^2 + X_L^2}$$

$$Z^2 = R^2 + X_L^2$$

$$16 = (3.4)^2 + X_L^2$$

$$L = \frac{X_L}{314}$$

## RC Series Circuit -



In Case of purely Resistive Ckt

$V \propto I$  in same phase

$$R \Rightarrow V_R = IR$$

$$C \Rightarrow V_C = IX_C$$

$$V = V_m \sin \omega t$$

Magnitude

In  $\triangle AOB$

$$V = \sqrt{(V_R)^2 + (V_C)^2}$$

$$V = \sqrt{(IR)^2 + (IX_C)^2}$$

$$V = I \sqrt{R^2 + X_C^2} \quad \text{--- (1)}$$

$$I = \frac{V}{\sqrt{R^2 + X_C^2}}$$

$$I = \frac{V}{Z} \quad \text{where } Z \text{ is impedance}$$

$$\therefore |Z| = \sqrt{(R)^2 + (X_C)^2} \quad \text{--- (2)}$$

Phase Angle

$$\text{From phasor diagram} \quad \tan \phi = \frac{V_C}{V_R} \quad \text{--- (3)}$$

$$\therefore \tan \phi = \frac{I X_C}{I R}$$

$$\tan \phi = \frac{X_C}{R}$$

$$\phi = \tan^{-1} \left( \frac{X_C}{R} \right) \quad \text{--- (4)}$$

## Power Factor

$$\cos \phi = \frac{R}{Z}$$

$$\cos \phi = \cos \left( \tan^{-1} \left( \frac{x_c}{R} \right) \right) \quad \textcircled{1}$$

- Power Calculation
- Active Power
  - Reductive Power
  - Apparent Power

$$V = V_m \sin \omega t$$

$$i = I_m \sin(\omega t + \phi)$$

$$\begin{aligned} \text{Instantaneous power} &= p = Vi \\ &= I_m \sin(\omega t + \phi) V_m \sin \omega t \\ &= V_m I_m \sin \omega t \sin(\omega t + \phi) \\ &= \frac{V_m I_m}{2} 2 \sin \omega t \sin(\omega t + \phi) \\ &= \frac{V_m I_m}{2} [\cos(-\phi) - \cos(2\omega t + \phi)] \end{aligned}$$

$$\therefore p = \frac{\sqrt{m} I_m}{2} [\cos \phi - \cos(2\omega t + \phi)]$$

$$p = \frac{V_m I_m}{\sqrt{2} \sqrt{2}} [\cos \phi - \cos(2\omega t + \phi)]$$

- Avg Power consumed in the circuit over a complete cycle.

$$P = \text{avg } \frac{V_m I_m \cos \phi}{\sqrt{2} \sqrt{2}} - \text{avg } \frac{V_m I_m}{\sqrt{2} \sqrt{2}} \cos(2\omega t + \phi)$$

As the quantity  $\frac{\sqrt{m}}{\sqrt{2}} \frac{T_m}{\sqrt{2}} \cos(2\omega t + \phi)$  gives a negligible value

So we can ignore this term.

$$\text{As } V_{\text{rms}} = \frac{\sqrt{m}}{\sqrt{2}} \quad \& \quad T_{\text{rms}} = \frac{T_m}{\sqrt{2}}$$

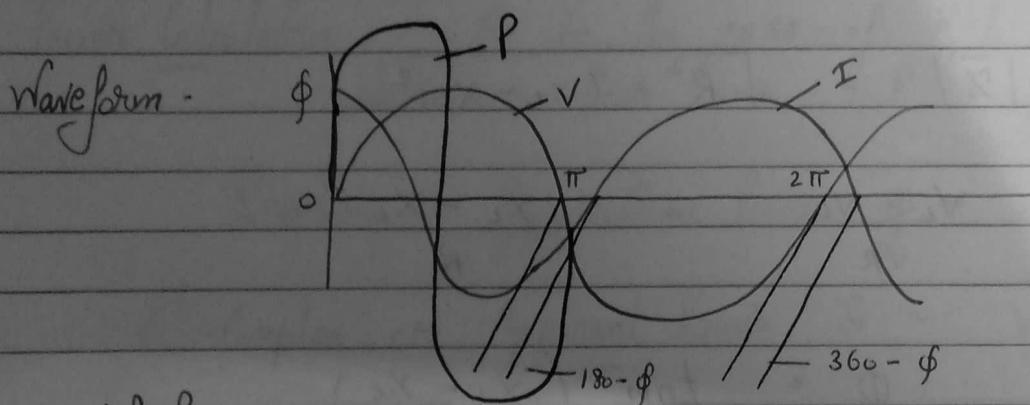
Hence,

$$P = V_{\text{rms}} T_{\text{rms}} \cos \phi$$

$$P = VI \cos \phi$$

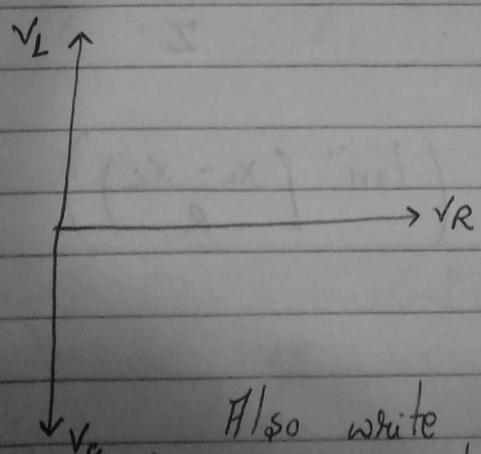
$$\phi = VI \sin \phi$$

$$S = VI$$

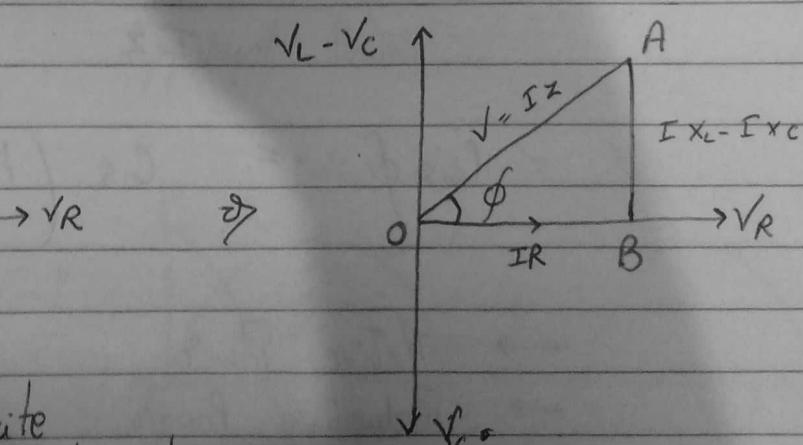


\*\*\*\* M. Imp.

## RLC Series Circuit :



Also write  
the theory of introduction



Magnitude

$$V = \sqrt{(VR)^2 + (VL - VC)^2}$$

$$V = \sqrt{(IR)^2 + (IX_L - IX_C)^2}$$

$$V = I \sqrt{R^2 + (X_L - X_C)^2}$$

$$\frac{V}{I} = \sqrt{R^2 + (X_L - X_C)^2}$$

$$I = \frac{V}{\sqrt{R^2 + (X_L - X_C)^2}} \quad \text{--- ①}$$

$$I = \frac{V}{Z} \quad \text{--- ②}$$

So.

$$|\vec{Z}| = \sqrt{R^2 + (X_L - X_C)^2}$$

$$\tan \phi = \frac{V_L - V_C}{VR} = \frac{X_L - X_C}{R}$$

$$\phi = \tan^{-1} \left( \frac{X_L - X_C}{R} \right)$$

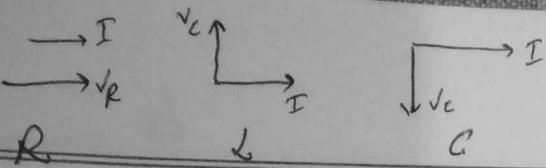
$$\cos \phi = \frac{IR}{IZ} = \frac{R}{Z}$$

$$\cos \phi = \cos \left( \tan^{-1} \left( \frac{X_L - X_C}{R} \right) \right)$$

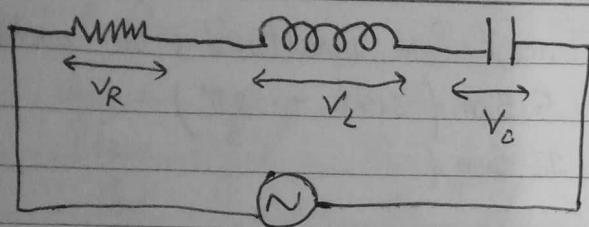
→ Active Power

→ Reductive Power

→ Apparent Power



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$$\text{Voltage across } R = V_R = RI$$

$$\begin{aligned}\text{Voltage across } L &= V_L \\ &= IXL\end{aligned}$$

$$\begin{aligned}\text{Voltage across } C &= V_C \\ &= IXC\end{aligned}$$

If  $X_L > X_C$ , circuit behave like R-L circuit

If  $X_C > X_L$ , circuit behave like R-C circuit

If  $X_L = X_C$ , circuit behave like pure resistive circuit  
 ↳ Resonance

Power Calculation: As in the case of R-L circuit  
 Actual or Real Power  $P = VI \cos \phi$  W

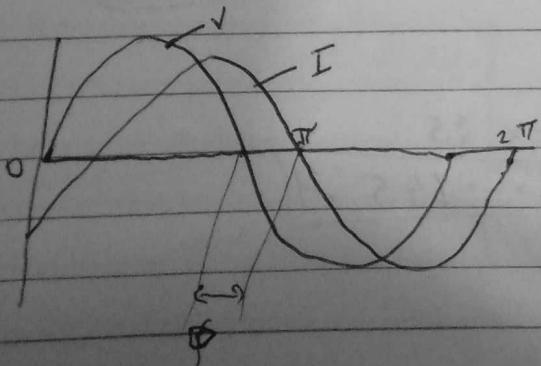
Reactive or Quadrative Power  $Q = VI \sin \phi$  VAR

Complex or Apparent Power  $S = VI$  Volt Ampere

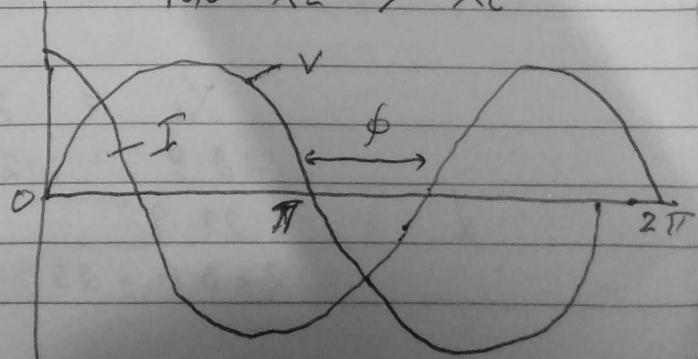
$$S = \sqrt{P^2 + Q^2}$$

Power Factor.  $\text{p.f.} = \cos \phi = \frac{\text{Real Power}}{\text{Apparent Power}}$

for  $X_C > X_L$



For  $X_L > X_C$



Q In a series circuit containing Pure Resistance, Pure Inductance, the current in pure resistive is  $i(t) = 5 \sin(314t + \frac{2\pi}{5})$   
 $v(t) = 20 \sin($

Que An inductive coil take 10 A & dissipates 1000 W when connected to a supply at 250 Volts, 25 Hz. Calculate impedance, reactance, effective resistance, Inductance & Power Factor.

$$P = VI \cos \phi$$

$$1000 = 250 \times 10 \times \cos \phi$$

$$\frac{1000}{250 \times 10} = \cos \phi$$

$$\boxed{\cos \phi = \frac{2}{5}}$$

$$P = I^2 R$$

$$1000 = 10 \times 10 R$$

$$\boxed{R = 10 \Omega}$$

$$Z = \frac{V}{R} = \frac{250}{10}$$

$$\boxed{Z = 25}$$

$$Z^2 = R^2 + (X_L)^2$$

$$(25)^2 = (10)^2 + (X_L)^2$$

$$X_L = \sqrt{625 - 100}$$

$$X_L = \sqrt{525}$$

$$\boxed{X_L = 22.91 \Omega}$$

$$X_L = 2\pi f L$$

$$22.9 = 2 \times 3.14 \times L \times 25$$

$$\therefore L = \frac{22.9}{2 \times 3.14 \times 25} = \boxed{L = 0.145 H}$$

Ques A Resistance of  $100\ \Omega$  is connected in series with  $50\text{ micro F}$  capacitor to a supply at  $200\text{ V}$ ,  $50\text{ Hz}$ . Find Impedance, Current, Phase Angle. Also find voltage across Resistance and Capacitor. And draw the phasor diagram.

$$X_C = \frac{1}{2\pi f C} = \frac{1}{2\pi \times 50 \times 50 \times 10^{-6}} = \frac{10^6}{2 \times 3.14 \times 2500} = \frac{10^6}{15700} = 63.69$$

$$Z = \sqrt{R^2 + (X_C)^2} = \sqrt{(100)^2 + (63.69)^2} = \sqrt{14056.4161} \\ = 118.56\ \Omega$$

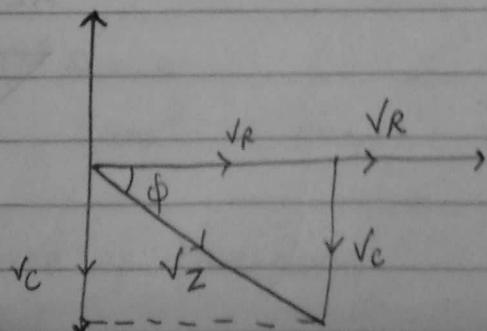
$$i = \frac{V}{Z} = \frac{200}{118.56} = 1.69\text{ A}$$

$$\text{Power} \quad \cos \phi = \frac{R}{Z} = \frac{100}{118.56} = 0.843$$

$$\phi = \cos^{-1}(0.843) = 32.486^\circ$$

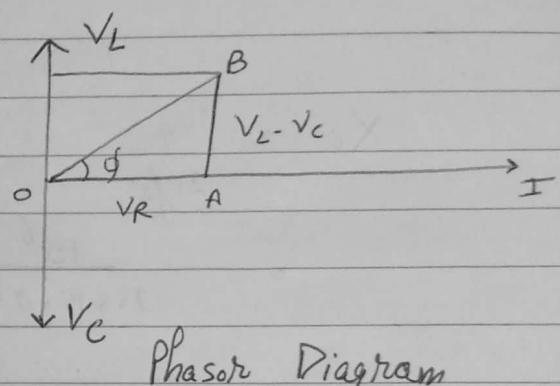
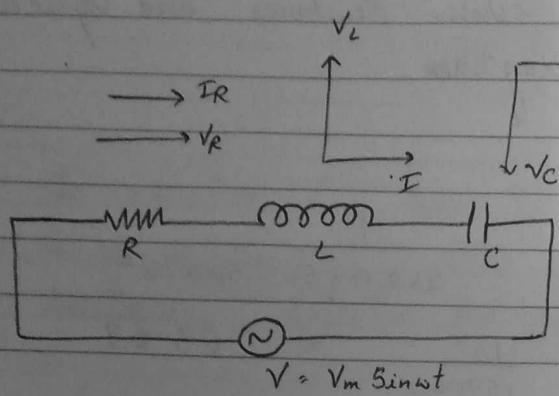
$$\sqrt{R} = IR = 1.69 \times 100 = 169\text{ V}$$

$$\sqrt{C} = IX_C = 1.69 \times 63.69 = 107.63\text{ V}$$



Continued

## R.L.C Circuit



if  $i = i_m \sin \omega t$        $v = v_m \sin \omega t$

then circuit current can be considered in three cases in RLC

Case 1:  $X_L > X_C$  Then the circuit is R-L Circuit

Current lags behind voltage at angle of  $90^\circ$

$$i = i_m \sin(\omega t - \phi)$$

Case 2:  $X_L < X_C$  Then the circuit is RC Circuit

Current leads the voltage by  $90^\circ$

$$i = i_m \sin(\omega t + \phi)$$

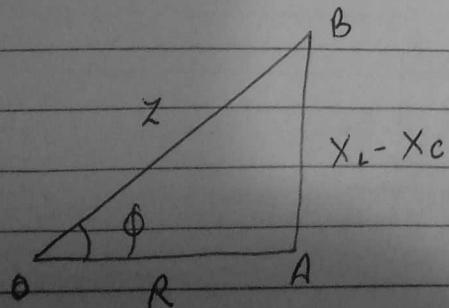
Case 3:  $X_L = X_C$  Then the circuit is purely R

$$Z = R$$

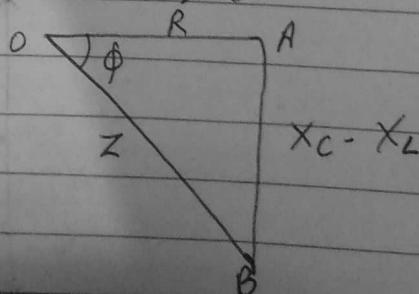
$$i = i_m \sin \omega t$$

$$\rightarrow \rightarrow Z$$

$$X_L > X_C$$



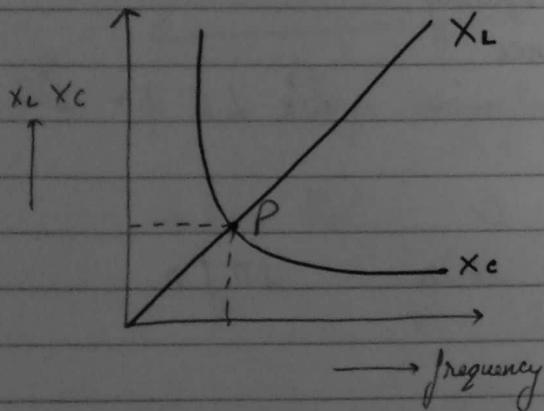
$$X_L < X_C$$



## \* Resonance :

When the circuit current is in phase with the applied voltage, the circuit is said to be in Resonance.

This condition can be achieved in RLC circuit



We know that, at resonance

$$X_L = X_C$$

$$X_L - X_C = 0 \quad \text{--- (1)}$$

$$Z_r = \sqrt{R^2 + (X_L - X_C)^2}$$

use eq. ①

$$\text{we get } Z_r = R$$

$$\text{We know that } I_r = \frac{V}{Z_r} = \frac{V}{R} \quad \therefore$$

$$I_r = \frac{V}{R}$$

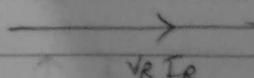
1. Current is Maximum, Resonance

2. Power Factor =  $\cos\phi = \cos 0 = 1$

when  $\cos\phi = 1 \rightarrow$  In Pure Resistive circuit

$\rightarrow$  In RLC circuit

3.  $V_R = I_R$  in phase



4. Impedance is Minimum

$\therefore$  Current is Max  $\rightarrow$  Power is also Max  
as  $P = I^2 R$

5. Power at Resonance is Maximum

~~Ques.~~ This circuit is called Resonance Circuit

and

Resonance Frequency Frequency at which resonance occurs is known as resonance frequency.

$$X_L = X_C \text{ at resonance}$$

$$\omega_{rL} = \frac{1}{\omega_{rC}} \Rightarrow \omega_{rL}^2 LC = 1$$

$$\omega_r = \frac{1}{\sqrt{LC}}$$

$$\omega_r = 2\pi f_r$$

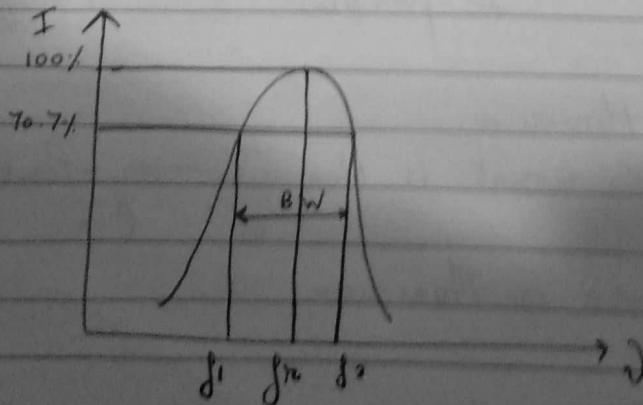
$$\therefore 2\pi f_r = \frac{1}{\sqrt{LC}}$$

$$\boxed{f_r = \frac{1}{2\pi\sqrt{LC}}}$$

Bandwidth The range of frequency at which circuit offers low impedance is called bandwidth circuit.

OR

The range of frequency at which current or voltage is equal to 70.7% of maximum value of is called bandwidth



Quality factor the factor of which different different factors like  
ratio to that of the applied voltage is called Quality factor

$$Q = \frac{\text{Voltage across shunt } \theta}{\text{Applied Voltage}}$$

or  $Q$  is voltage magnification at resonance

$$\text{we know that } V_h = T_0 X_L = Q$$

$$V_h = T_0 \times \frac{X_L}{R} = Q$$

$$\text{Voltage Magnification} = \frac{V_h}{V} \text{ or } \frac{V_h}{V}$$

$$Q = \frac{T_0 X_L}{R} = \frac{V_h}{T_0 R} = Q$$

$$Q = \frac{X_L}{R} = \frac{V_h}{R} = T_0 L$$

or

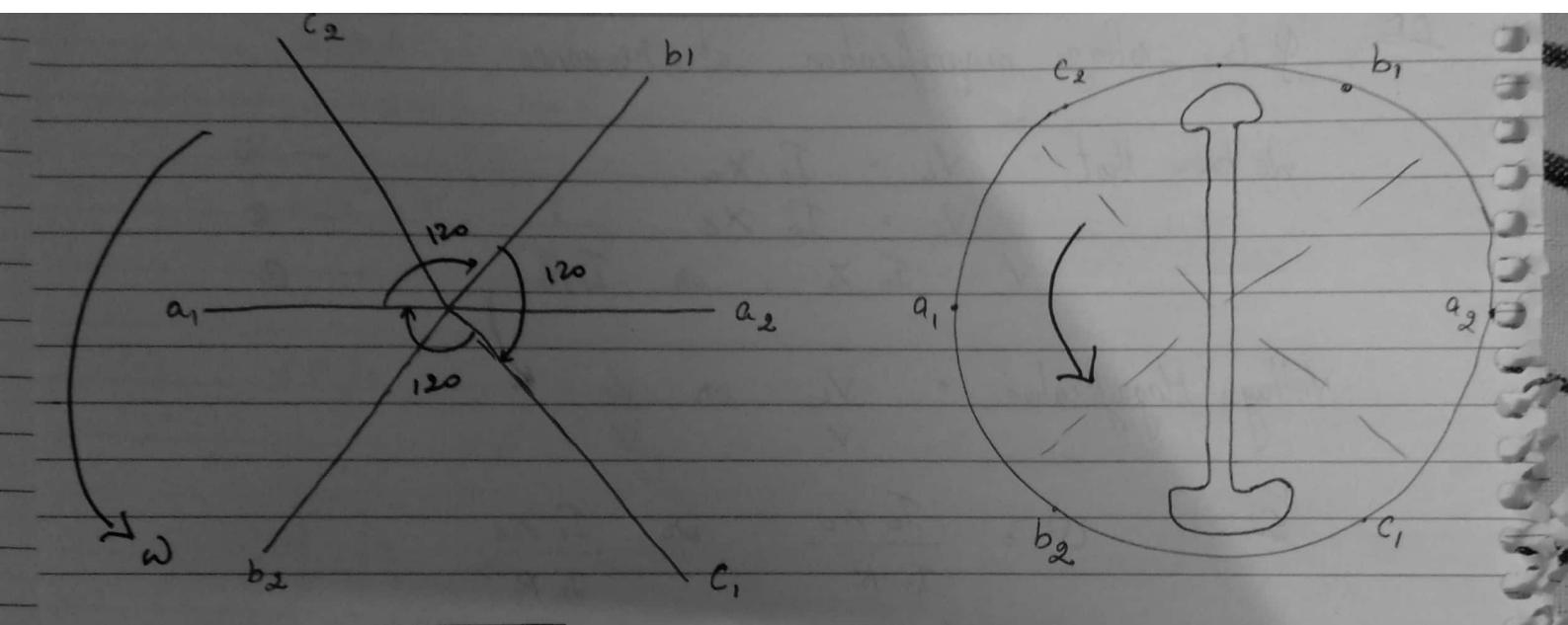
$$Q = \frac{X_L}{R} = \frac{I}{R} = \text{fig C}$$

Use anyone of

$$Q = \frac{2\pi f h L}{R} = \frac{2\pi f}{R} L$$

$$Q = \frac{L}{R \sqrt{C}}$$

$$Q = \frac{1}{R \sqrt{C}}$$



a<sub>2</sub> 2

4

6

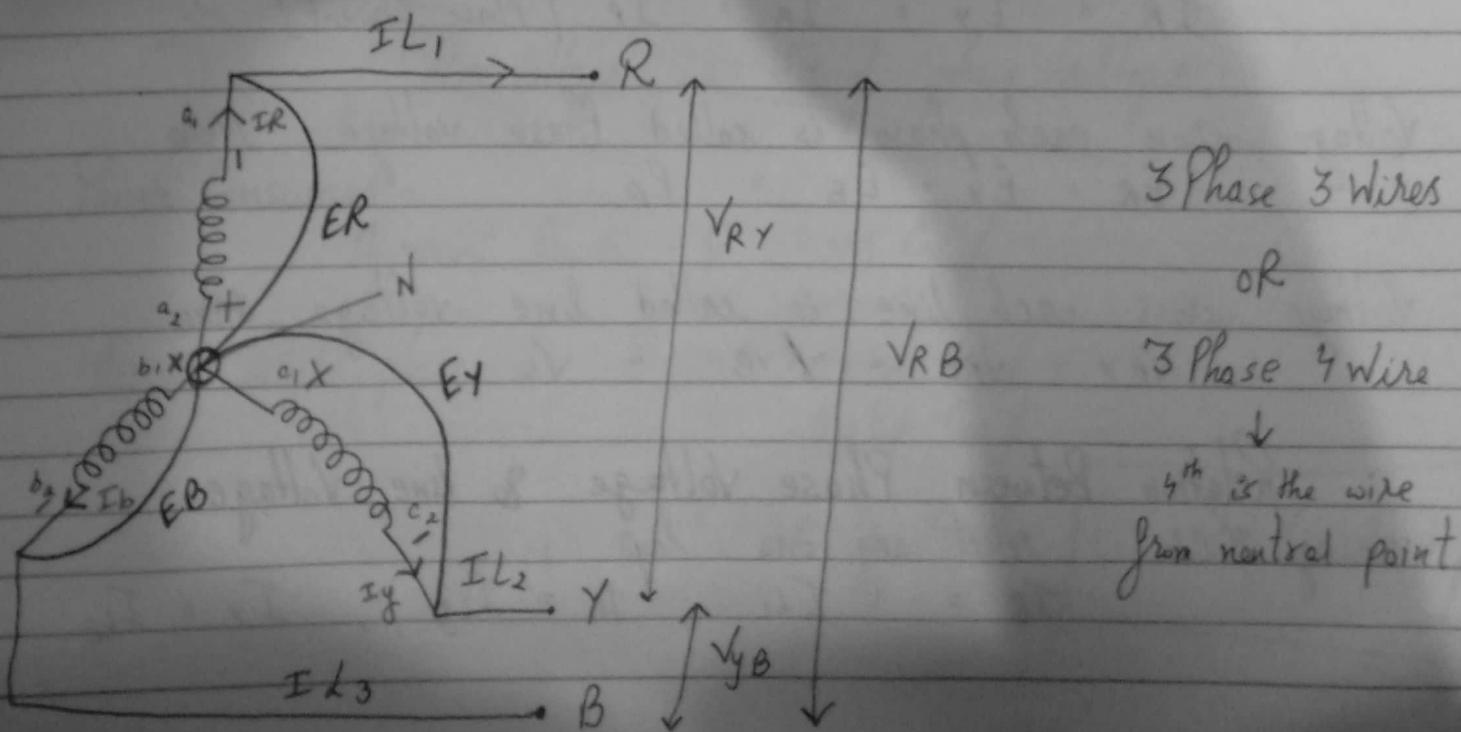
To connect coil with load, we need 2 wires and to connect 3 windings & 3 load, we need 6 wires.

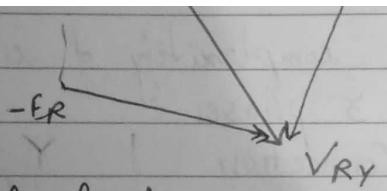
To decrease the complexity of circuit, or (no. of ~~wires~~) we use 3 phases

- Star Connection | Y
- Delta Connection or Mesh

## STAR Connection :

The point at which we connect similar point is called neutral.





Similar ends either start or finish of windings are connected at a common point called Common or neutral points.

The current in each line is called line current. Here  
 $I_{L1} = I_{L2} = I_{L3} = I_L$  [Line Current]

Incoming = Outgoing

$$I_P = I_L - \textcircled{1}$$

Hence, Phase Current = Line Current

Using KVL, select anyone loop

$$E_R + \sqrt{R_Y} - E_Y = 0$$

$$\sqrt{R_Y} = E_Y - E_R - \textcircled{2} \rightarrow \text{This helps us in making phasor}$$

\*\*\* Draw Directions carefully for phasor

Using law of parallelogram

$$|\vec{a} - \vec{b}| = \sqrt{|a|^2 + |b|^2 + 2|a||b|\cos\theta} - \textcircled{3}$$

Using  $\textcircled{2}$  in  $\textcircled{3}$

$$\sqrt{R_Y} = \sqrt{(E_R)^2 + (E_Y)^2 + 2E_R E_Y \cos\theta}$$

$$\sqrt{L} = \sqrt{3} E_P - \textcircled{4}$$

Similarly  $\sqrt{V_{RB}} = \sqrt{R_B} = \sqrt{L} = \sqrt{3} E_P$

So,

line voltage is  $\sqrt{3}$  of phase voltage

Power Consumed -

$$\text{Apparent Power } P = V I \cos\phi$$

Across 1 single phase

$$P = I R_E \cos\phi$$

$$= I_P E_P \cos\phi$$

$$= I_P \frac{\sqrt{L}}{\sqrt{3}} \cos\phi$$

$$P = \frac{I_L \sqrt{L} \cos\phi}{\sqrt{3}}$$

Total Apparent Power in 3 phase =  $3 \cdot V_L I_L \cos \phi$

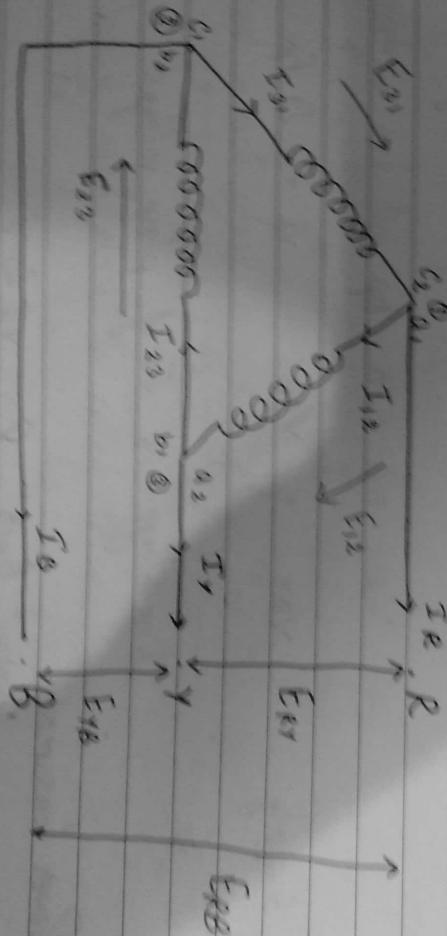
$$= \sqrt{3} V_L I_L \cos \phi \text{ watt}$$

$$\text{Positive Phase - } P_h = E_p I_p \sin \phi$$

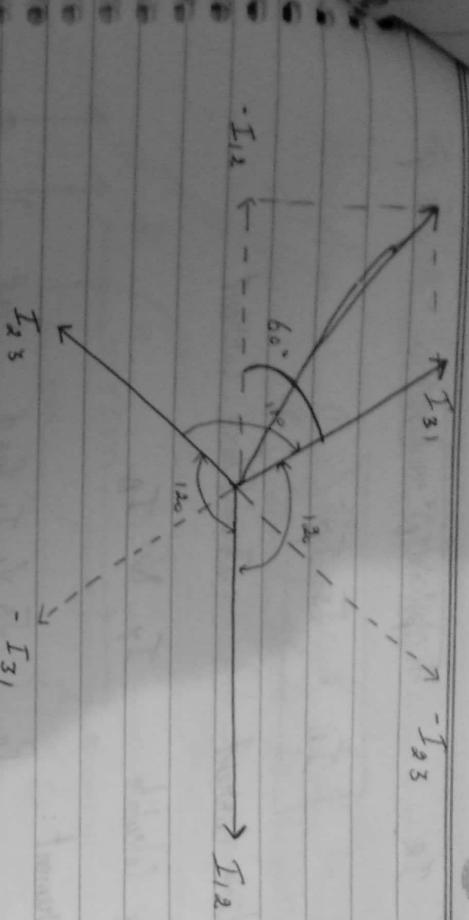
$$\boxed{P_h = \sqrt{3} V_L I_L \sin \phi \text{ W}}$$

### Delta Connection:

Dissimilar ends of 3 phase coil are connected together to form a mesh. It means finish of one winding to the start terminal of the other wind.



$$\begin{aligned}
 E_{PA} &= E_{PB} = E_{PC} = E_L \quad [\text{Line Voltage}] \\
 I_{1a} &= I_{2b} = I_{3c} = I_p \quad [\text{Phase Current}] \\
 I_L &= I_1 = I_2 = I_3 = I_L \quad [\text{Line Current}] \\
 E_{1a} &= E_{2b} = E_{3c} = E_p \quad [\text{Phase Voltage}]
 \end{aligned}$$



Voltage across Terminal 1, 2 is same as across RY

$$E_{12} = E_{RY}, \quad E_{23} = E_{RB}, \quad E_{31} = E_{BR}$$

$$\therefore \boxed{E_P = E_R} \quad \textcircled{1} \quad \text{Hence, } \boxed{\text{line Voltage} = \text{Phase Voltage}}$$

Relation b/w Phase Current and line Current -

Since, the system is balanced.

So,  $I_{12}$ ,  $I_{23}$ ,  $I_{31}$  are equal in magnitude but displaced from one another by  $120^\circ$ .

$$I_{12} = I_{23} = I_{31} = I_P \quad \textcircled{2}$$

Current is divided at every junction 1, 2 and 3

So, using KCL in junction 1.

$$\therefore I_R = I_{31} + I_{12}$$

$$I_R = \sqrt{(I_{31})^2 + (I_{12})^2 + 2(I_{31})(I_{12}) \cos 60^\circ}$$

$$I_R = \sqrt{(I_P)^2 + (I_P)^2 + (I_P)^2} = \sqrt{3} I_P$$

$$I_L = \sqrt{3} I_P$$

Hence, Line Current =  $\sqrt{3} \times$  Phase Current

Similarly calculate  $I_Y$  &  $I_B$

### Power Measurement:

$$\begin{aligned} P_A &= \sqrt{3} V_L I_L \cos \phi & \text{Watt} \\ P_R &= \sqrt{3} V_L I_L \sin \phi & \text{VAR} \end{aligned} \quad \left. \right\} \textcircled{3}$$

Hence. Total Power consumed is same in star and delta Connection.

### Measurement of Power in 3-Phase Circuits

OR. Explain the wattmeter method for Power ?

Power consumed in 3-Phase can be calculated by using 2 wattmeters.

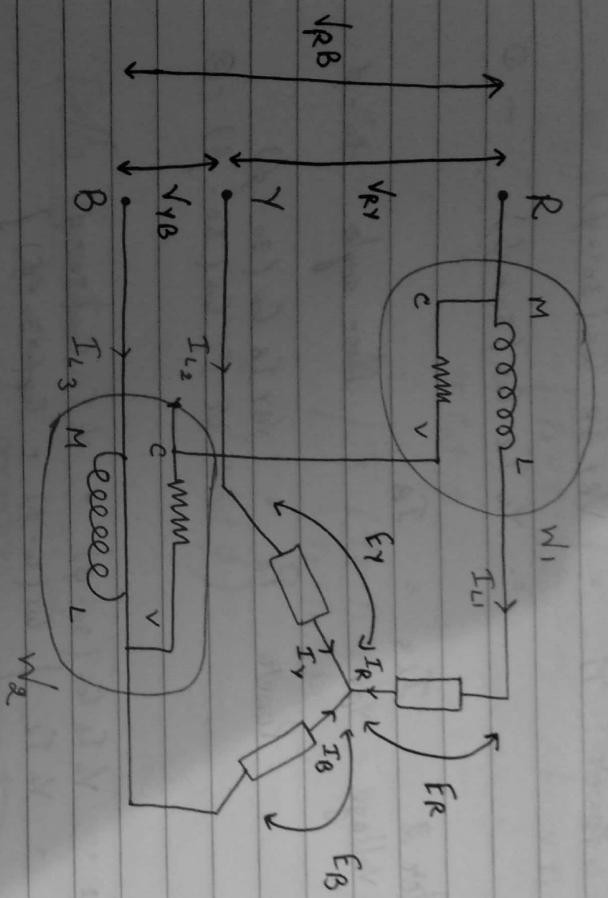
Wattmeter is an indicating instrument which will show deflection in the form of Power.

Two coils are used, one as current coil and other as voltage or pressure coil. The current coil is connected in series with the load and the pressure coil is connected across the load.

Deflection torque is produced with which is proportional to the power being measured.

## \* Star Connection load :

- Assumption -**
- The circuit should be  $RYB$ .
  - Circuit should be balanced.
  - Load is  $R_L$  in nature.

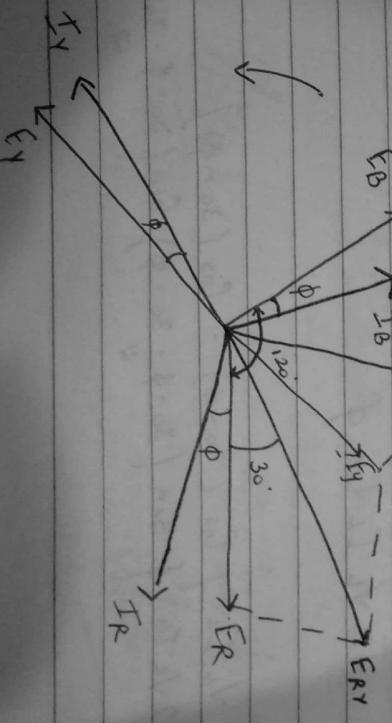


$$I_{L1} = I_{L2} = I_{L3} = I_L \quad [\text{line current}]$$

$$E_R = E_Y = E_B = E_p \quad [\text{phase voltage}]$$

$$V_{RY} = V_{RB} = V_{BY} = V_L \quad [\text{line voltage}]$$

$$I_R = I_Y = I_B = I_p \quad [\text{phase current}]$$



for meter 1  $I_{A1} = I_R$

voltage  $\sqrt{V_R}$

Phase angle  $= 30 + \phi$

$$\text{Power } P_1 = \sqrt{V_R} I_R \cos(30 + \phi)$$

$$= \sqrt{V_R} I_R \cos(30 + \phi) - \textcircled{1}$$

for meter 2  $I_{A2} = I_R$

voltage  $\sqrt{V_R}$

Phase angle  $= 30 - \phi$

$$\text{Power } P_2 = \sqrt{V_R} I_R \cos(30 - \phi)$$

$$= \sqrt{V_R} I_R \cos(30 - \phi) - \textcircled{2}$$

Add.

$$P_1 + P_2 = \sqrt{V_R} I_R \cos(30 - \phi) + \sqrt{V_R} I_R \cos(30 + \phi)$$

$$= \sqrt{V_R} I_R \left[ \cos(30 - \phi) + \cos(30 + \phi) \right]$$

$$= 2\sqrt{V_R} I_R \left[ \cos\left(\frac{30 - \phi + 30 + \phi}{2}\right) \cos\left(\frac{30 - \phi - 30 - \phi}{2}\right) \right]$$

$$= 2\sqrt{V_R} I_R \cos 30 \cos \phi$$

$$= 2 \times \sqrt{V_R} I_R \times \frac{\sqrt{3}}{2} \cos \phi$$

$$= \sqrt{3} \sqrt{V_R} I_R \cos \phi$$

Sub.

$$P_A - P_B = \sqrt{V_R} I_R \left[ \cos(30 - \phi) - \cos(30 + \phi) \right]$$

$$= -2\sqrt{V_R} I_R \left[ \sin\left(\frac{30 - \phi + 30 + \phi}{2}\right) \sin\left(\frac{30 - \phi - 30 - \phi}{2}\right) \right]$$

$$= 2V_L I_L \sin 30 \sin \phi$$

$$= V_L I_L \sin \phi$$

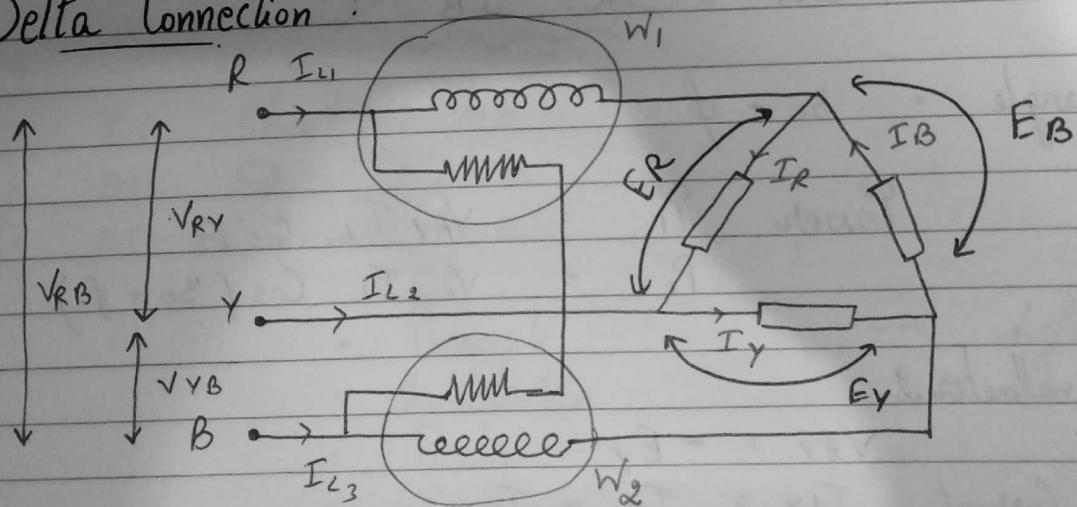
$$\tan \phi = \sqrt{3} \left[ \frac{P_2 - P_1}{P_2 + P_1} \right] = \sqrt{3} \left[ \frac{\sqrt{3} V_L I_L \cos \phi}{V_L I_L \sin \phi} \right]$$

$$= 3 \cot \phi$$

$$\cos \phi = \cos \left[ \sqrt{3} \left( \frac{P_2 - P_1}{P_2 + P_1} \right) \right] = \cos \left[ \sqrt{3} (\sqrt{3} \cot \phi) \right]$$

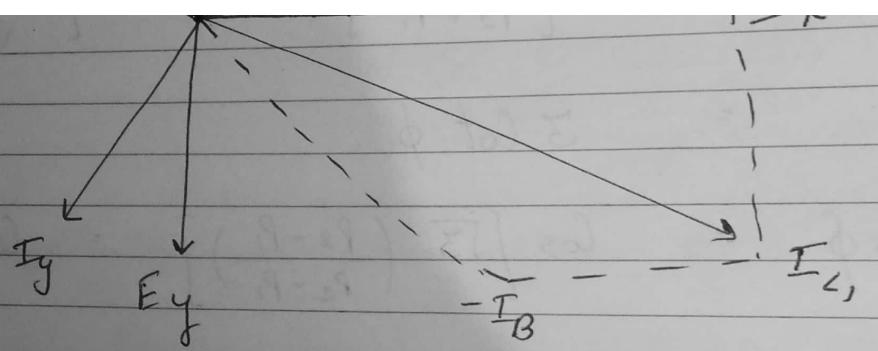
$$= \cos (3 \cot \phi)$$

Delta Connection:



Phasor

Similar to the  
Star Connection



Ferrari wattmeter 1

$$\tan \phi = \sqrt{3} \left[ \frac{P_2 - P_1}{P_2 + P_1} \right]$$

Power Factor

$$\cos \phi = \cos \left[ \tan^{-1} \sqrt{3} \left( \frac{P_2 - P_1}{P_2 + P_1} \right) \right]$$

## DC Motor

1. DC Shunt Motor
2. DC Series Motor
3. DC Composed Motor

- Principle → Left Hand Rule

- Construction
- Parts

- Working

- Definition
- Diagram

Resistance

$$E_b = V - I_a R_a$$

back emf  
Armature  
voltage

$$I_{sh} = \frac{V}{R_{sh}}$$

$$I_a = I_L - I_{sh}$$

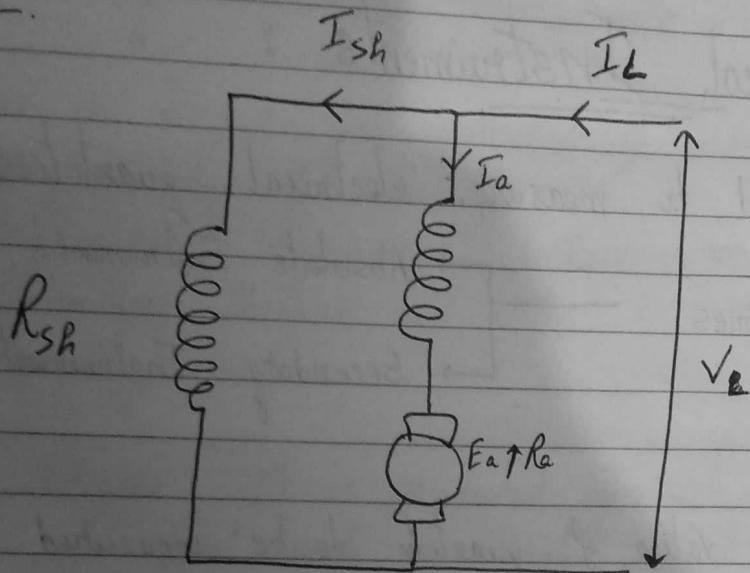
$$E_b = V - I_a R_a - 2 \sqrt{b}$$

Compound :



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$$I_{sh} = \frac{V}{R_{sh}}$$

$$I_a = I_L - I_{sh}$$

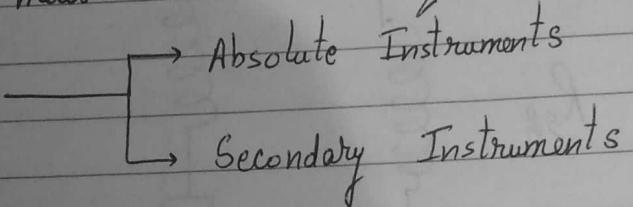
$$I_{se} = I_a$$

$$E_b = V - V_a (R_a + R_{se}) - 2V_b$$

# \* Electrical Instruments :

These are used to measure electrical quantities.

2 Broad Categories



Absolute : Give value of quantity to be measured in form of constant of instrument.

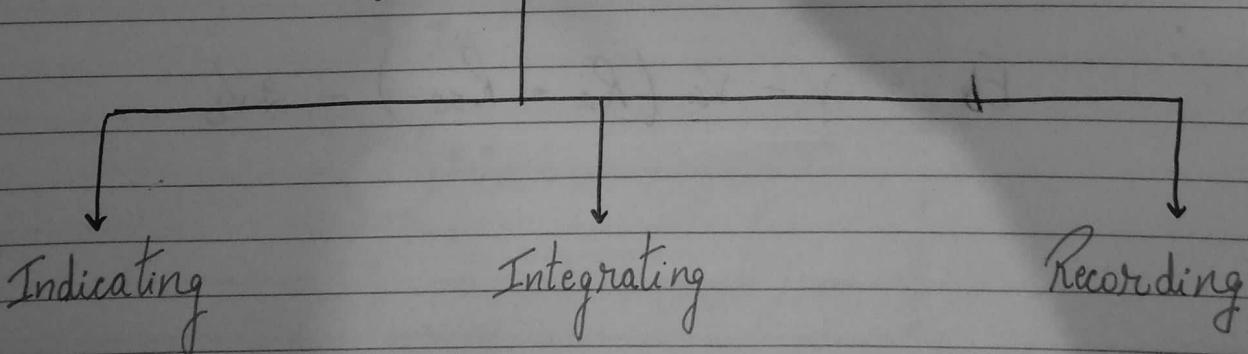
They don't require any prior Calibration.

↓  
changes in Reading to get correct Readings

e.g galvanometer

Secondary : Give value of quantity to be measured in the form of deflection.

It is further divided into 3 categories



- Indicate magnitude of electrical quantity being measured
- Pointer moves over the scale to indicate magnitude.

e.g ammeter, voltmeter etc.

- These are those which adds up electrical energy and measure the total energy in given time period.

e.g energymeter.

- Gives continuous record of variation of electrical quantity being measured.

## Essentials of Indicating Instruments :

- The force or torque for operation of indicating instruments are basically of 3 types :
  1. Deflection Torque ( $T_d$ )
  2. Controlling Torque ( $T_c$ )
  3. Damping Torque

Deflecting Torque It is produced by making of one of the effect such as magnetic effect, Dynamic effect.

It is required to move the moving system from zero position.

Controlling Torque It opposes the  $T_d$  and increases with deflection of moving system. The pointer is broad to rest at a position where  $T_c$  and  $T_d$  are equal.

Damping Torque When  $T_d$  is applied to moving system, it deflects the pointer whereas  $T_c$  controls the deflection and tries to stop the pointer at its final position ( $T_c = T_d$ ). But due to initial Problem, pointer oscillates before coming to rest position. These oscillations are undesirable, so move the pointer quickly to rest position we apply damping Torque.

## Transducers :

Which converts non-electrical quantity into electrical signals

→ Active

Passive

Active Which generally produce own power for operation

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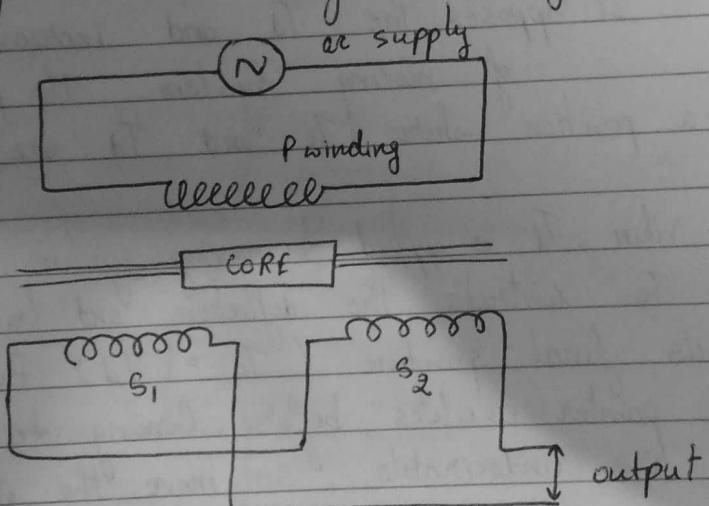
Passive which require external power for their operation.

### LVDT :

Linear Variable Differential Transducer

→ It consists of 1 primary winding to which ac source is connected and consists of two secondary windings  $S_1$  and  $S_2$  which are placed on either side of primary winding. Secondary having equal no. of turns but are connected in series opposition, so that emf induced in coils opposes each other.

The position of core determines flux linkage b/w primary and each of the secondary windings.



1 Case 1 of Core is in between

Both are having equal emf...  $\therefore E_{S_1} = E_{S_2}$

• In

• of e

• Poles

the

m

e.g

Case 2 Core is at left side

induced emf linking with  $S_1$  is more than  $S_2$

$$E_{S_1} > E_{S_2}$$

Voltage is in phase with  $S_1$ .

Case 3

Core is shifted towards right side

$$C_{S_2} > C_{S_1}$$

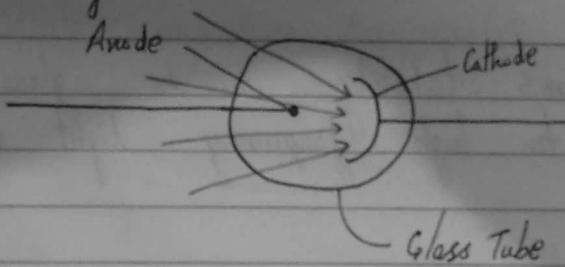
Hence.

Induced emf is varying linearly :  
Output voltage of LVDT is linear function of core  
Displacement.

### Photo Electric Transducers :

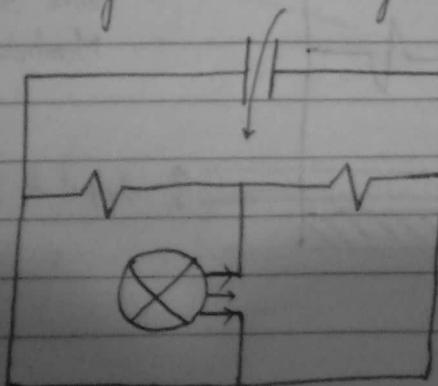
This transducer may use of photoelectric cells or phototubes's properties.

Incident light changes into voltage, induced emf.  
Phototube is a device and its electron emission is controlled by amount of incident light.



Principle:

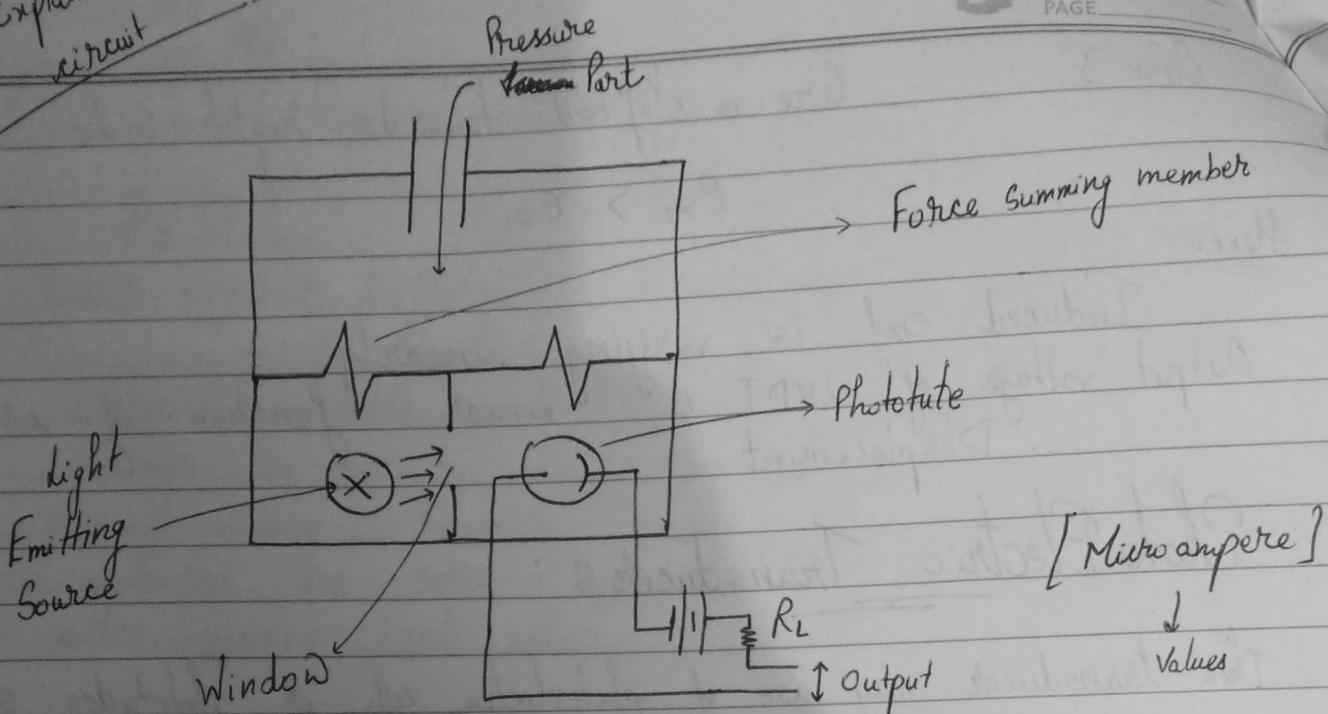
The current produced is directly proportional to the amount of incident light.



Explain this circuit

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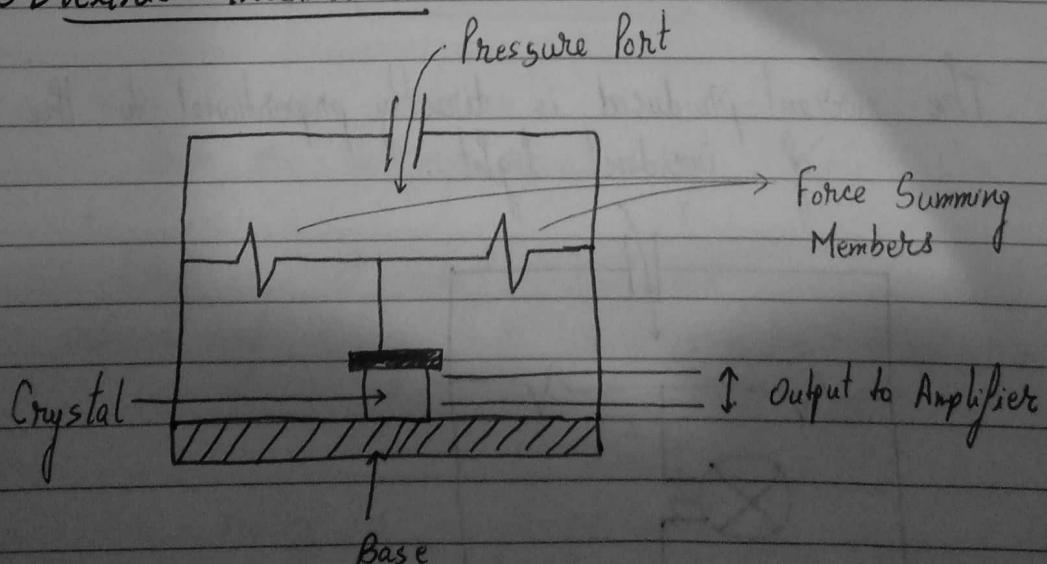
## ADVANTAGE

- High efficiency
- It can measure static & Dynamic phenomena

## DISADVANTAGE

- Poor long Terms Stability due to glass tube
- Poor Response to high frequency light variations.

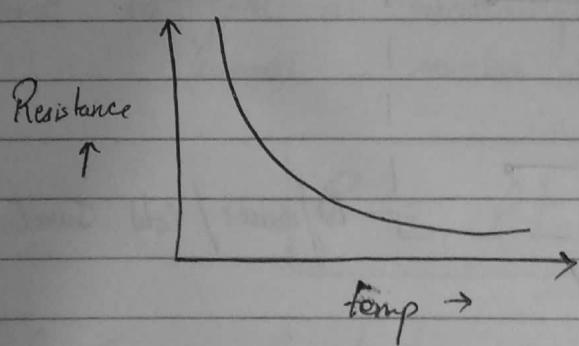
## Piezo Electric Transducers :



Thermist :  $\rightarrow$  Thermal + Resistor

Two terminal semi-conductor device.

It is having negative temperature Coefficient of Resistance  
( It is inversely proportional to resistance )

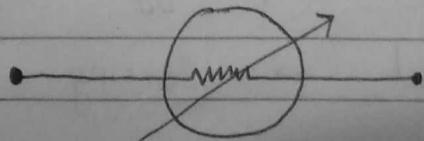


Normal Range of Thermister

-100 °C to 300 °C

Resistance Range of thermister  
0.5 Ω to 4.5 MΩ

Symbol



$$\text{Equation } R_{T_1} = R_{T_0} \exp \left[ \beta \left( \frac{1}{T_1} - \frac{1}{T_2} \right) \right]$$

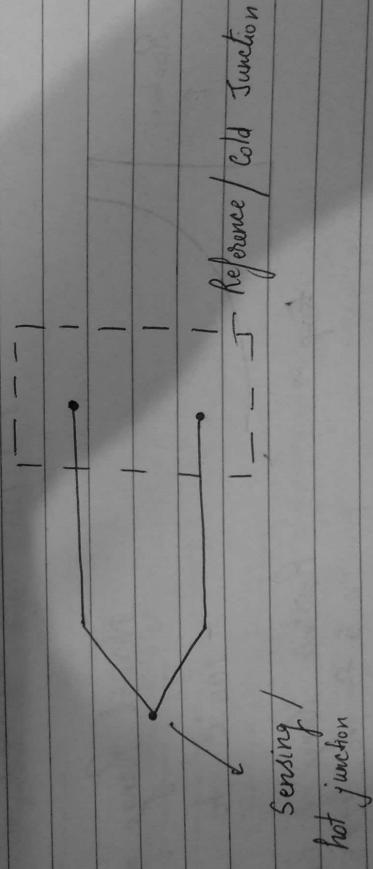
↓  
absolute temp

### Application :

It is used to measure thermal conductivity, Power at high temp. Time Delay in Circuit operation.

- \* It is composed of nickel, uranium and cobalt.

Thermo Couple : It consists of two metal [dissimilar] wires which is joined together at one end and terminated at another end.



Emf is induced when there is temp difference by two junction

Joined together Terminal → Sensing

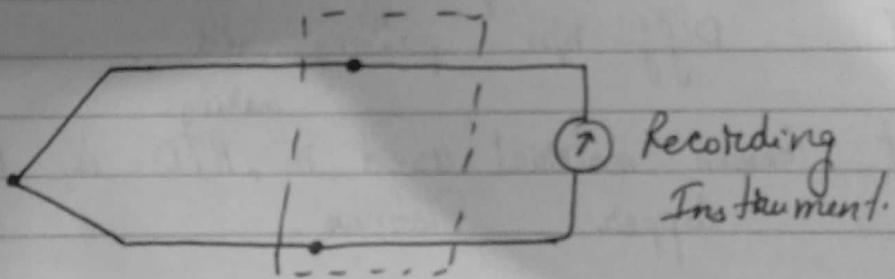
When a temp diff. exist b/w sensing and reference, junction, an emf is induced that causes flow of current in the circuit.

- \* Thermo electric effect caused by contact potential at a junction is called Seebeck effect.

↳ Thermocouple produces an emf when a temp difference exist between hot and cold junction.

Magnitude of produced emf is directly proportional to difference in temp b/w hot and cold junction.

#



To Measure the temp by using thermocouple, A simple method is used to join a recording instrument or (connect) sensitive milliamperes.

$$C = At + \frac{1}{2} Bt^2 + \frac{1}{3} Ct^3$$

If  $A, B, C$  are Constant &  $t$  is the temperature difference.

Resistor of a conductor changes when its temp changes.  
This property is used in RTD for temperature measurement.

$$R_t = R_{\text{reference}} [1 + \alpha \Delta T]$$

$R_t$  = resistance of conductor at  $t^{\circ}\text{C}$

$R_{\text{ref}}$  = resistance at Reference temp

$\alpha$  is the temp coefficient of resistance

$\Delta T$  Diff b/w operating and

making

The most common material used in RTD is Nickel,  
Copper, Platinum.

### The Properties of Conductor Material in RTD :

1. High temp coeff of Resistance ( $\alpha$ )
2. High Resistivity to Permit Construction of small sensor
3. Melting temperature should be high.

The Resistance temp Relationship of Platinum is

$$\left\{ T = \frac{100 [R_T - R_0]}{R_{100} - R_0} + \alpha \left( \frac{T - 1}{100} \right) \frac{T}{100} \right\}$$

Here.

$T$  : temp

$R_T$  : Resistance at temp  $T$

$R_0$  : Resistance at  $0^\circ\text{C}$  temp

$R_{100}$  : Resistance at  $100^\circ\text{C}$

$d$  : Callendar's Constant

Resistance Thermometer are generally of probe type for immersion in medium whose temp is to be measured. While measuring temp, the change in Resistance [ $\Delta R$ ] is measured using Wheat stone Bridge.

