Experiment - 4 Date - 15/2/2024

Aim :- Estimate signal spectra using Discrete Fourier Transform(DFT) and Fast Fourier Transfor(FFT) .

Laboratory Exercises

A) Write a MATLAB Program to compute and plot the L-point DFT X[k] of a sequence x[n] of length N with L>= N and then to compute and plot as dftuser() and idftuser() for DFT ad IDFT, respectively.

```
clc ; clear all ; close all ;
xn = [1 2 3 4 5 6] ; L = 8 ; [X , k]= dftuser(xn,L) ;
disp(X) ;
```

21.0000 + 0.0000i -9.6569 - 3.0000i 3.0000 - 4.0000i 1.6569 + 3.0000i -3.0000 - 0.0000i 1.6569 - 3.0000i

```
clc ; clear all ; close all ;
X = [
      0.0000 + 0.0000i
                          0.0000 + 0.0000i
                                             0.0000 + 0.0000i
                                                                0.0000 + 0.0000i
0.0000 + 0.0000i
                  0.0000 + 0.0000i
                                     0.0000 + 0.0000i
                                                        0.0000 + 0.0000i
   0.0000 + 0.0000i
                     0.0000 + 0.0000i
                                        0.0000 + 0.0000i
                                                           0.0000 + 0.0000i
0.0000 + 0.0000i
                 0.0000 + 0.0000i
                                     0.0000 + 0.0000i
                                                        0.0000 + 0.0000i
   0.0000 + 0.0000i
                     0.0000 + 0.0000i
                                        0.0000 + 0.0000i
                                                           0.0000 + 0.0000i
0.0000 + 0.0000i
                  0.0000 + 0.0000i
                                     0.0000 + 0.0000i
                                                        0.0000 + 0.0000i
  0.0000 + 0.0000i
                     0.0000 + 0.0000i
                                        0.0000 + 0.0000i
                                                           0.0000 + 0.0000i
0.0000 + 0.0000i
                  0.0000 + 0.0000i
                                     0.0000 + 0.0000i
                                                        0.0000 + 0.0000i
   0.0000 + 0.0000i
                     0.0000 + 0.0000i
                                        0.0000 + 0.0000i
                                                           0.0000 + 0.0000i
0.0000 + 0.0000i 0.0000 + 0.0000i
                                     0.0000 + 0.0000i
                                                        0.0000 + 0.0000i
   0.0000 + 0.0000i
                     0.0000 + 0.0000i
                                        0.0000 + 0.0000i
                                                           0.0000 + 0.0000i
0.0000 + 0.0000i
                  0.0000 + 0.0000i
                                     0.0000 + 0.0000i
                                                        0.0000 + 0.0000i
  0.0000 + 0.0000i
                     0.0000 + 0.0000i
                                        0.0000 + 0.0000i
                                                           0.0000 + 0.0000i
0.0000 + 0.0000i
                  0.0000 + 0.0000i
                                     0.0000 + 0.0000i
                                                        0.0000 + 0.0000i
  -9.6569 + 3.0000i
                     0.0000 + 0.0000i
                                        0.0000 + 0.0000i
                                                           0.0000 + 0.0000i
0.0000 + 0.0000i
                  0.0000 + 0.0000i
                                     0.0000 + 0.0000i
                                                        0.0000 + 0.0000i;
N = 8; [xn, n] = idftuser(X, N);
disp(xn);
```

 $-1.2071 + 0.3750 i \quad -0.5884 + 1.1187 i \quad 0.3750 + 1.2071 i \quad 1.1187 + 0.5884 i \quad 1.2071 - 0.3750 i \quad 0.5884 - 1.1187 i \quad 0.5884 i \quad$

```
% function [X , k] = dftuser(xn,L)
%
      N = length(xn);
%
      X = [zeros(1,L)];
%
      for k = 1:L
%
          for n = 1:N
%
              X(k) = X(k) + xn(n) * exp(-1i * (2*pi/L) * (k-1) * (n-1));
%
          end
%
      end
%
      k = 0 : L-1 ;
% end
```

```
% function [xn, n] = idftuser(X , N)
%
      L = length(X);
%
      xn = [zeros(1,N)];
%
      for k = 1:N
%
          for n = 1:L
%
              xn(n) = xn(n) + X(k) * exp(1i * (2*pi/L) * (k-1) * (n-1));
%
%
      end
     xn = xn/L ; n = 0 : N-1 ;
%
% end
```

Inference: - The above functions computes DFT and IDFT for any given sequence. These functions help us to analyse Frequency Component of the input sequence.

B) This exercise is aimed to identify how fast fft() is compared to regular DFT. For that reason, create a sinusoid that has the three spectral components of 50, 100 and 250 Hz, and sample this signal at 1000Hz. The duration of the signal so that you end up with 1024 points. You will test various implementations of DFT(dftuser() vs. fft()) on this three frequency test signal. Use tic and toc for timing comparison.

```
clc ; clear all ; close all ;
%Declaring Original Signal
freq1 = 50 ; samp1 = 1000 ; dur = 1.023 ;

t1 = 0 : (1/samp1) : dur ; x1 = sin(2*pi*freq1*t1) ;

freq2 = 100 ; x2 = sin(2*pi*freq2*t1) ;
freq3 = 250 ; x3 = sin(2*pi*freq3*t1) ;

x = x1 + x2 + x3 ; L = 1024 ;
tic ; X = dftuser(x , L) ; A = idftuser(x , L) ; toc ;
```

Elapsed time is 0.574104 seconds.

```
tic ; Z = fft(x , L) ; toc ;
```

Elapsed time is 0.000206 seconds.

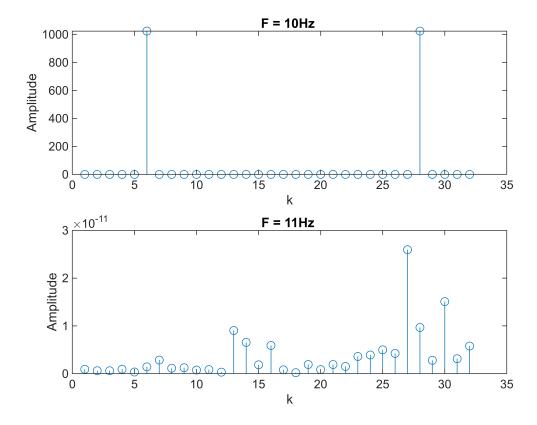
Inference : - Clearly , FFT has better computing speed than DFT and due to this it is widely used in Digital Signal Processing . Here , time increases with increase in the value of N .

C) A continuous time signal $x(t) = \sin(20pit)$ is sampled at 64Hz to obtain x[n]. If we denote X[k] as a 32 point DFT of x[n], then identify the peak amplitude and their respective indices k in MATLAB. Repeat the problem for a signal with analog frequency of 11 Hz. You need to use dftuser() as implemented in the previous exercise.

```
clc ; clear all ; close all ;
fs = 64 ; L = 32 ; t = 0 : 1/fs : (L-1/fs) ;
x15 = sin(20*pi*t) ;
[X1] = dftuser(x15 , L) ;
```

```
x23 = sin(22*pi*t);
[X2] = dftuser(x23 , L);

subplot(2,1,1); stem(abs(X1)); xlabel("k"); ylabel("Amplitude"); title('F = 10Hz ');
subplot(2,1,2); stem(abs(X2)); xlabel("k"); ylabel("Amplitude"); title('F = 11Hz ');
```



Inference: The peak amplitude when Frequency = 10 Hz is obtained two symmetric points whereas the peak amplitude when Frequency = 11 Hz is to be obtained at two symmetric points along with the nearby points having some amplitude.

From the peak amplitude we can find the major frequency component and its corresponding index in the Frequency Domain .

D)This exercise illustrates methods to compute linear convolution along with its timing requirements . Create a sinusoid with the three spectral components of 50, 100 and 200 Hz, and sample this signal at 1000 Hz. Determine the duration of the signal so that you end up with 1024 points. The LTI system is described with the difference equation same as Experiment 3, eq(1). Determine the convoluted output using three methods, direct linear convolution, using circular convolution and via DFT and IDFT, and compare timing requirements.

```
clc ; clear all ; close all ;
%Declaring Original Signal
freq1 = 50 ; freq2 = 100 ; freq3 = 200 ; samp1 = 1000 ; dur = 1.023 ;
```

```
t1 = 0 : (1/samp1) : dur ;
x1 = sin(2*pi*freq1*t1) + sin(2*pi*freq2*t1) + sin(2*pi*freq3*t1) ; n = length(x1) ;
%plot(t1,x1) ; xlabel("Time") ; ylabel("Amplitude") ; title("Original Signal") ;
grid on ;

h1n = [0.25 0.5 0.25] ; m = length(h1n) ;
x2 = [x1,zeros(1,m-1)] ; h2n = [h1n,zeros(1,n-1)] ;

tic
yn = conv(x1,h1n) ;
toc
```

Elapsed time is 0.961888 seconds.

```
tic
ync = cconv(x2,h2n);
toc
```

Elapsed time is 1.693031 seconds.

```
tic
xnl = fft(x2,n+m-1); hnl = fft(h2n,n+m-1); ynl = xnl .*hnl; ynd =
ifft(ynl,n+m-1);
toc
```

Elapsed time is 0.024024 seconds.

Inference: The above code is a comparison between different methods to find linear convolution. From this we determine that Convolution via DFT/IDFT Method take the least time to compute the Linear Convolution and overall requires less amount of Hardware (ADD and MUL).

Conclusion: In this experiment, we learnt to compute DFT and IDFT using UDF and also applied the FFT function to compare the timing requirements. We further compared the different methods to find Linear Convolution and measured their computational time. This experiment help us to learn about the importance of DFT / IDFT has in real life applications and hardware used for Digital Signal Processing.