

For each of the following pairs of functions, either  $f(n)$  is  $O(g(n))$ ,  $f(n)$  is  $\Omega(g(n))$ , or  $f(n) = \Theta(g(n))$ . Determine which relationship is correct and explain.

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|----|--------------------|-------------------|
| a. | $f(n) = n^{0.25};$ | $g(n) = n^{0.5}$  |
| b. | $f(n) = n;$        | $g(n) = \log^2 n$ |
| c. | $f(n) = \log n;$   | $g(n) = \lg n$    |
| d. | $f(n) = e^n;$      | $g(n) = 2^n$      |
| e. | $f(n) = 2^n;$      | $g(n) = 2^{n+1}$  |
| f. | $f(n) = 2^n;$      | $g(n) = 2^{2^n}$  |
| g. | $f(n) = 2^n;$      | $g(n) = n!$       |
| h. | $f(n) = (n+1)!;$   | $g(n) = n!$       |

4.) big O is the upper bound; omega is lower

- a.)  $O(g(n))$  ;
- b.)  $\Omega(g(n))$  ;  $N_0=1$
- c.)  $\Theta(g(n))$  ;  $N_0=1$
- d.)  $\Omega(g(n))$  ; for all  $N$
- e.)  $O(g(n))$  ;for all  $N$
- f.)  $O(g(n))$  ; for all  $N$
- g.)  $O(g(n))$  ;  $N_0=4$
- h.)  $\Omega(g(n))$  ; for all  $N$