

## Batch Gradient Descent

- □ Stochastic Gradient Descent is computationally expensive
- □ There is a possibility that it can make a noisy gradient descent where values are jumping around uncontrollably
  - It was so noisy in some cases that we needed to tweak a bit in our implementation
- So we changed, it to batch gradient descent which performs model updates at the end of each training epoch

## **Epoch**

Dictionary: "A long period of time, especially one in which there are new developments and great change"

ML: One cycle through the entire training dataset

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## **Batch Gradient Descent**

□ Vanilla gradient descent, computes the gradient of the cost function w. r. t. for the entire training dataset:

$$\frac{\partial J}{\partial W} = \frac{1}{m} * \left( \sum \frac{\partial \ell(\mathsf{a}, \mathsf{y})}{\partial w^1} \right) \text{ and } \mathsf{W} = \mathsf{W} - \alpha . \frac{\partial J}{\partial W}$$

- ☐ Gradients for the whole dataset to perform one update, batch gradient
- Most deep learning libraries provide automatic differentiation that efficiently computes the gradient
- □ Update our parameters in the direction of the gradients with the learning rate
- □ For non–convex surfaces, it converges to local minima
- □ We have coded in recent examples

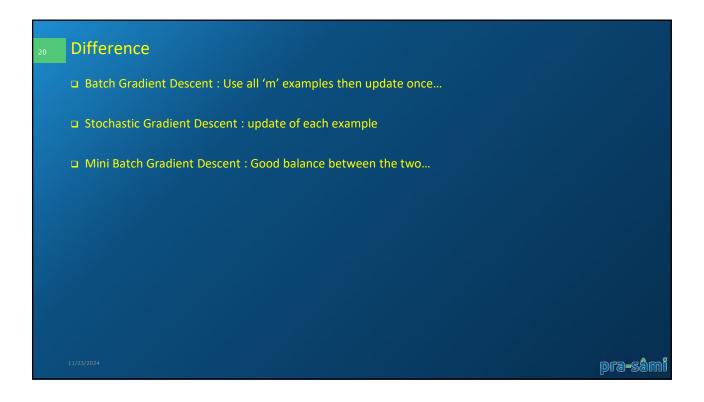
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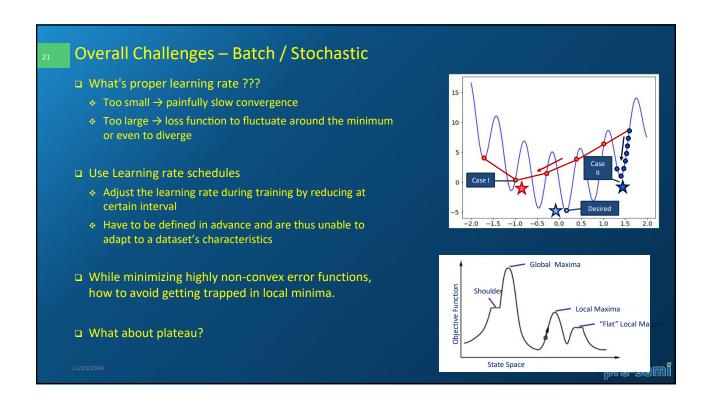




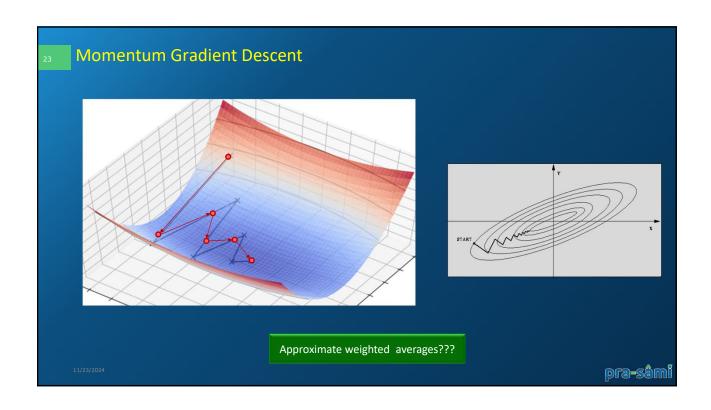


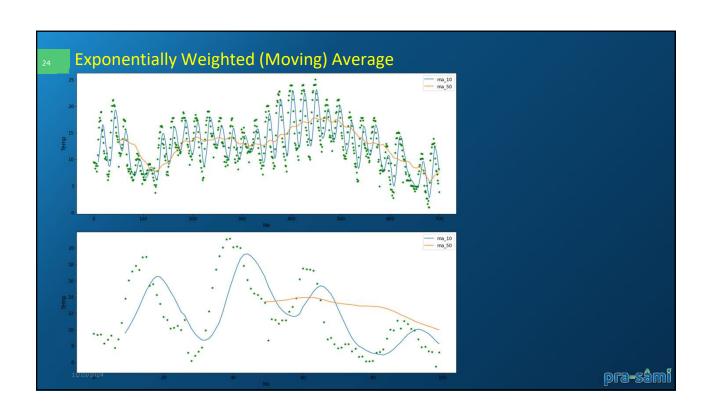


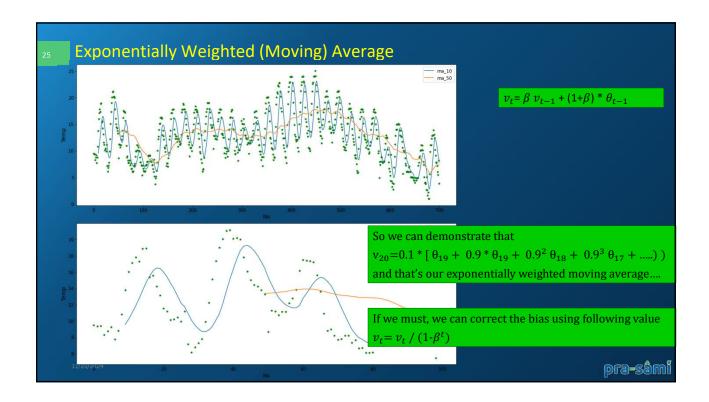


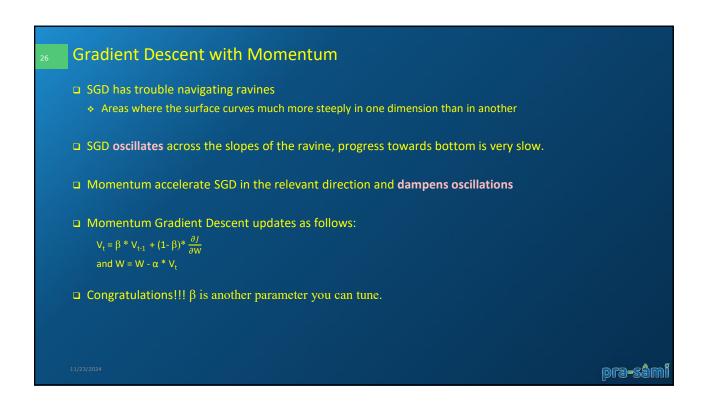


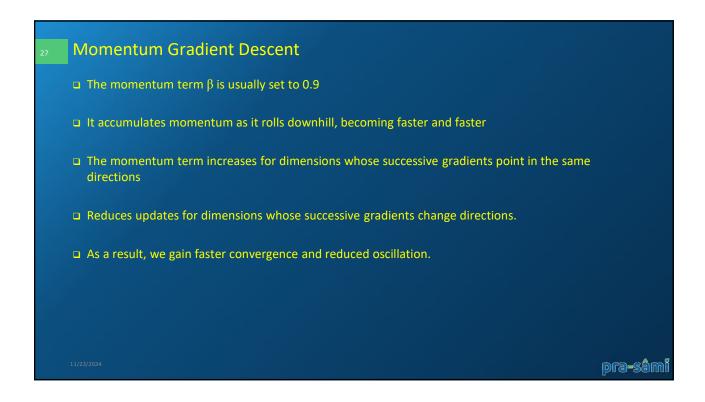


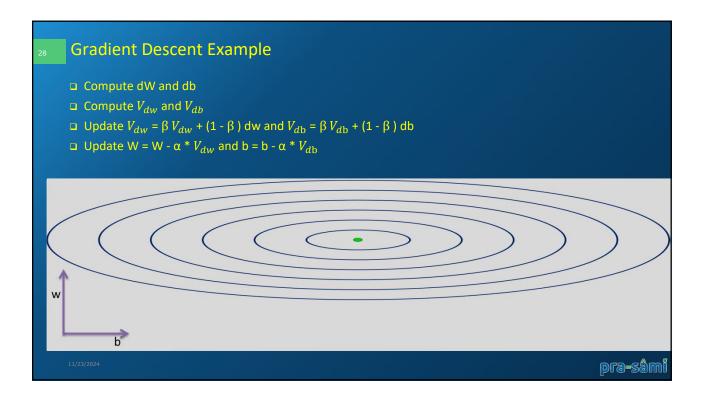


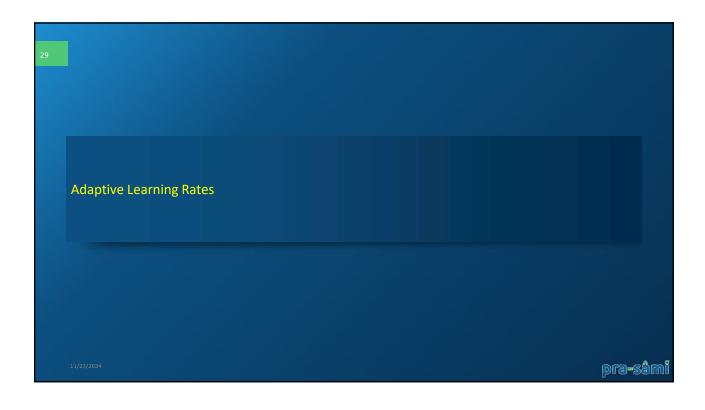


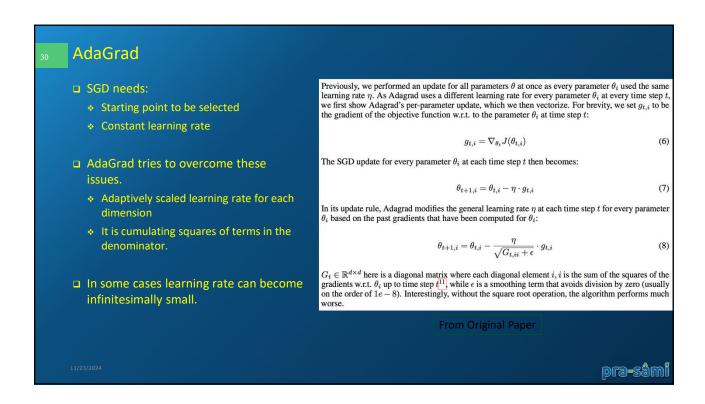


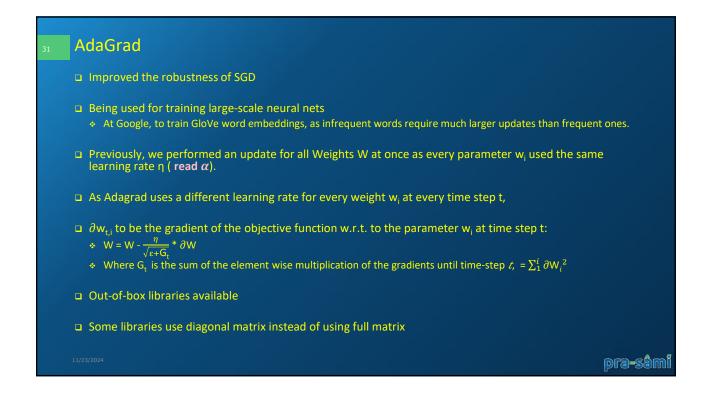


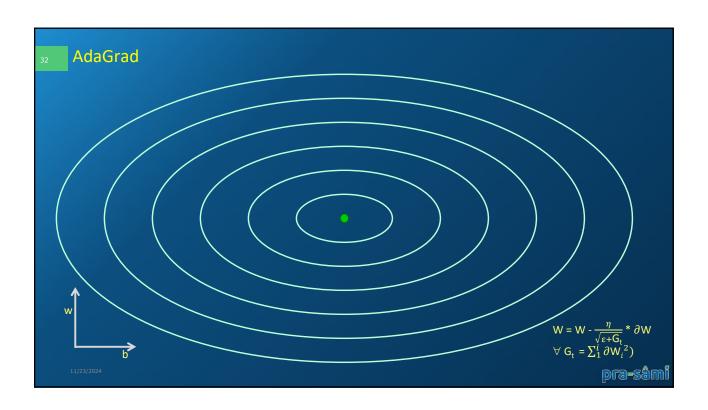


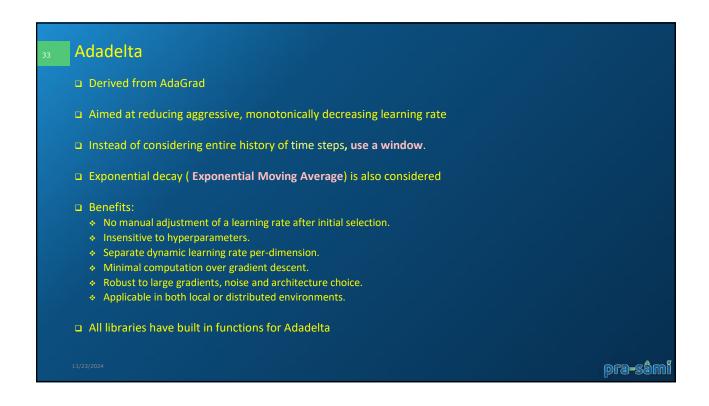


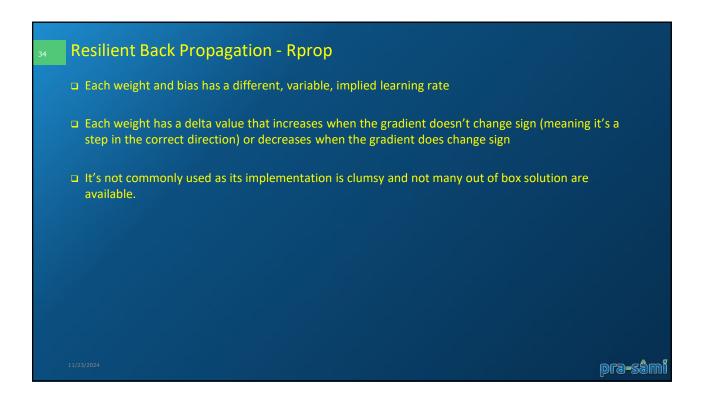














RMSprop is an unpublished, adaptive learning rate method proposed by Geoff Hinton in Lecture 6e of his Coursera Class [12].

RMSprop and Adadelta have both been developed independently around the same time stemming from the need to resolve Adagrad's radically diminishing learning rates. RMSprop in fact is identical to the first update vector of Adadelta that we derived above:

Added exponential moving average on AdaGrad

$$E[g^{2}]_{t} = 0.9E[g^{2}]_{t-1} + 0.1g_{t}^{2}$$

$$\theta_{t+1} = \theta_{t} - \frac{\eta}{\sqrt{E[g^{2}]_{t} + \epsilon}}g_{t}$$
(18)

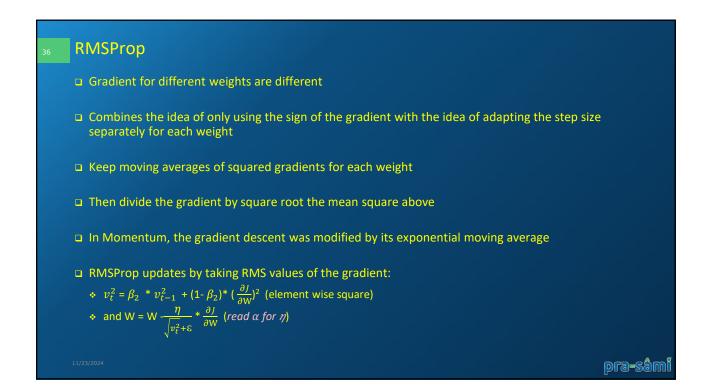
RMSprop as well divides the learning rate by an exponentially decaying average of squared gradients. Hinton suggests  $\gamma$  to be set to 0.9, while a good default value for the learning rate  $\eta$  is 0.001.

Read  $\beta$ 

Read  $\alpha$ 

11/23/202





## Adaptive Moment Estimation (Adam) Adam is another method that computes adaptive learning rates for each parameter. SGD was too simplistic, Adam is an improvement Adam was presented by Diederik Kingma (OpenAl) and Jimmy Ba (University of Toronto) in their 2015 ICLR paper (poster) titled "Adam: A Method for Stochastic Optimization" Its name Adam is derived from Adaptive Moment Estimation Stochastic gradient descent maintains a single learning rate (termed alpha) for all weight updates and the learning rate does not change during training. Adam is adopted from two other methods Adaptive Gradient Algorithm (AdaGrad): works well with sparse gradients Root Mean Square Propagation (RMSProp): works well in on-line and non-stationary settings Also storing an exponentially decaying average of past squared gradients v<sub>t</sub>

