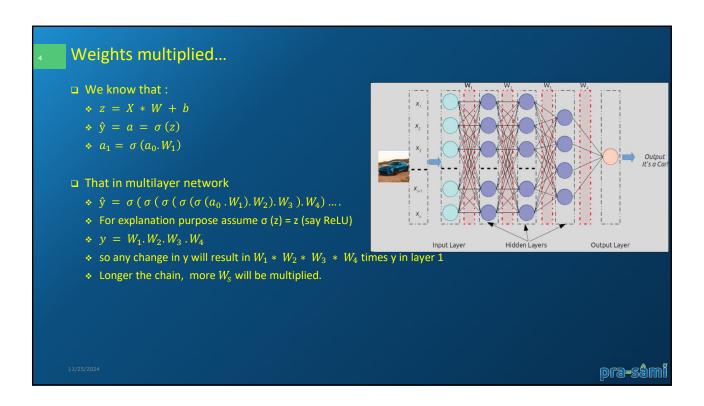


Deeper the network more are the chances of the gradients becoming smaller and smaller or keep growing...



```
More Layers... More problems

Assume we have 150 layers

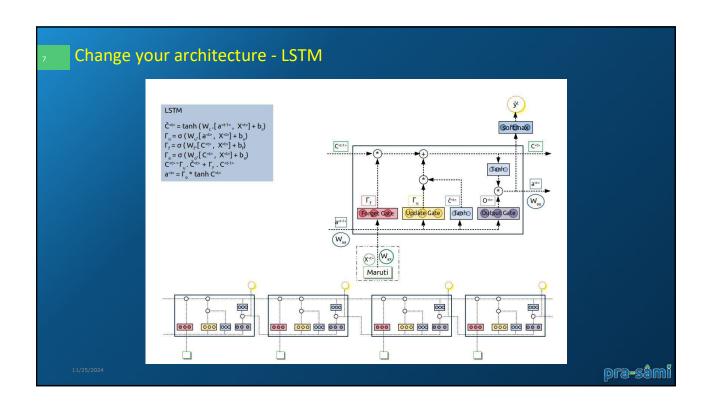
Also assume our weight is say 1.1

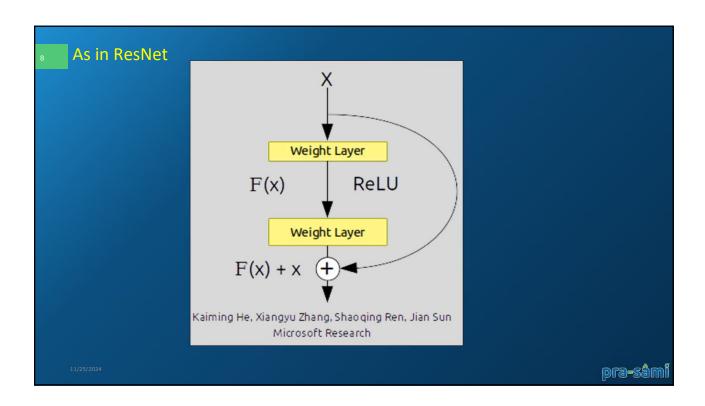
=> 1.1<sup>150</sup> = 1.6 million

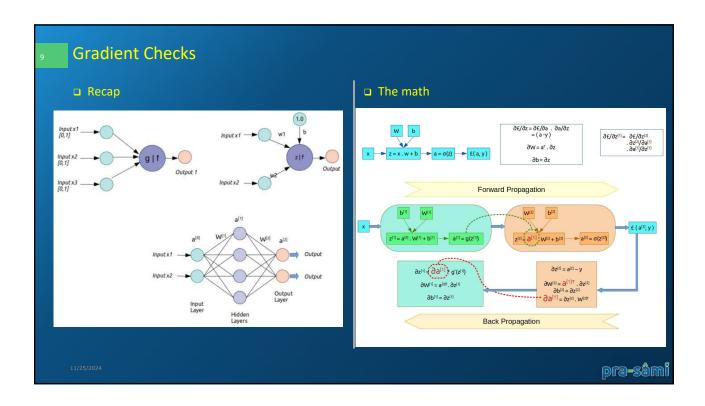
On the other hand assume our weight is 0.9

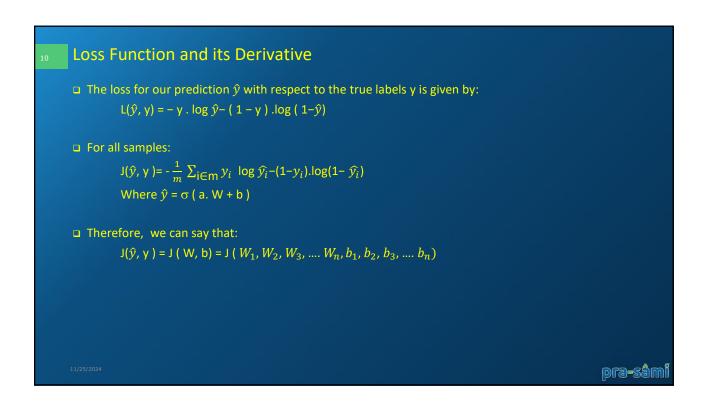
=> 0.9<sup>150</sup> = 1.4 e<sup>-7</sup>
```

6	It's a Severe Problem	
	□ No silver bullet solution	
	□ There is multi-prong approach to it	
	□ First, Initialise your weights as close to 1 as possible ( not 1)	
	<ul> <li>□ It is found that for tanh activation function</li> <li>Divide by √number of nodes in the previous layer</li> <li>for Gaussian distribution it normalises the data with var =1</li> </ul>	
	$ \Box \text{ Some cases : } \frac{2}{\sqrt{number\ of\ nodes\ in\ the\ previous\ layer}} $	
	$ \  \   \square \   \text{In ReLU , :} \frac{2}{\sqrt{number\ of\ nodes\ in\ the\ previous\ layer+number\ of\ nodes\ in\ current\ layer}} $	
	Some literature, even $\frac{K}{\sqrt{number\ of\ nodes\ in\ the\ previous\ layer}}$ ; K is a another parameter to tune	
		pra-sâmi









## Calculation of derivative Use the centered formula The formula you may have seen for the finite difference approximation when evaluating the numerical gradient is not as good as centered formula Weights Weights

## Gradient Checking

- □ Also called "Grad Check"
- □ Do it to verify the model's math(Debug) only
  - \* Too heavy for training, switch off once the model is verified.
- □ For all values of Ws and Bs, we can calculate:

$$\delta\theta_{approx} = J(W_1, ..., W_i + \varepsilon, ..., W_n, b_1, b_2, b_3, ..., b_n) - J(W_1, ..., W_i - \varepsilon, ..., W_n, b_1, b_2, b_3, ..., b_n) / (2 * \varepsilon)$$

 $\Box$  To check if  $\delta\theta_{approx}$  and  $\delta$   $\theta$  are close

$$\frac{\|\delta\theta_{approx} - \delta\;\theta\|_2}{\|\delta\theta_{approx}\;\|_2 + \|\;\delta\;\theta\|_2}\;\text{is very small}$$

- $\Box$  For  $\varepsilon$  = 1e-7
  - ❖ Relative error > 1e-2 usually means the gradient is probably wrong
  - 1e-2 > relative error > 1e-4 should make you feel uncomfortable
  - 1e-4 > relative error is usually okay for objectives with kinks. But if there are no kinks (e.g. use of tanh nonlinearities and softmax), then 1e-4 is too high.
  - 1e-7 and less you should be happy

1/25/2024



## Grad Check Steps

- □ Recall: Our model has all weights and biases stored
  - \* Model ={ " $W_1$ ": ..., " $b_1$ ": ..., " $W_2$ ": ..., " $b_2$ ": ..., ... ... " $W_n$ ": ..., " $b_n$ ": ...}
  - We have implemented our forward prop and back prop
- $\hfill \square$  Step 1 : Pick model and convert all weights and biases into a vector  $\theta$
- $\hfill \Box$  Step 2: Similarly pick  $\delta W$  and  $\delta b$  and convert to a vector  $\delta \theta$
- $\Box$  Step 3: for each of the value in the vector  $\theta$ 
  - \* Make copy of  $\theta$  and  $\delta\theta$
  - \* Increase  $\theta_i$  to  $\theta_i$  + ε
  - \* Calculate J + (Cost with increased  $\theta$ )
  - \* Similarly calculate J- ( Cost with decreased  $\theta$ )
  - Use J+ and J- to calculate if  $\delta\theta_{approx}$
  - Calculate  $\delta\theta$  as usual
  - Find error

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## Remember to Turn off Dropout/Augmentations

- □ When performing gradient check, remember to turn off any non-deterministic effects in the network, such as dropout, random data augmentations, etc.
- Otherwise these can clearly introduce huge errors when estimating the numerical gradient
- ☐ The downside of turning off these effects is that you wouldn't be gradient checking them (e.g. it might be that dropout isn't backpropagated correctly)
- □ Therefore, a better solution might be to force a particular random seed before evaluating both f(x+h) and f(x-h), and when evaluating the analytic gradient.

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