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CT-032

Question No 1:

Construct a combinational circuit with three inputs x , y and z and three outputs A , B , and C . When the binary input is 0, 1, 2 and 3, the binary output is one greater than the input. When the binary input is 4, 5, 6 or 7, the binary output is two less than the input.

x	y	z	A	B	C
0	0	0	0	0	1
0	0	1	0	1	0
0	1	0	0	1	1
0	1	1	1	0	0
1	0	0	0	1	0
1	0	1	0	1	1
1	1	0	1	0	0
1	1	1	1	0	1

A

xy	$z=0$	$z=1$
00		
01		1
11	1	1
10		

B

xy	$z=0$	$z=1$
00		1
01	1	
11		
10	1	1

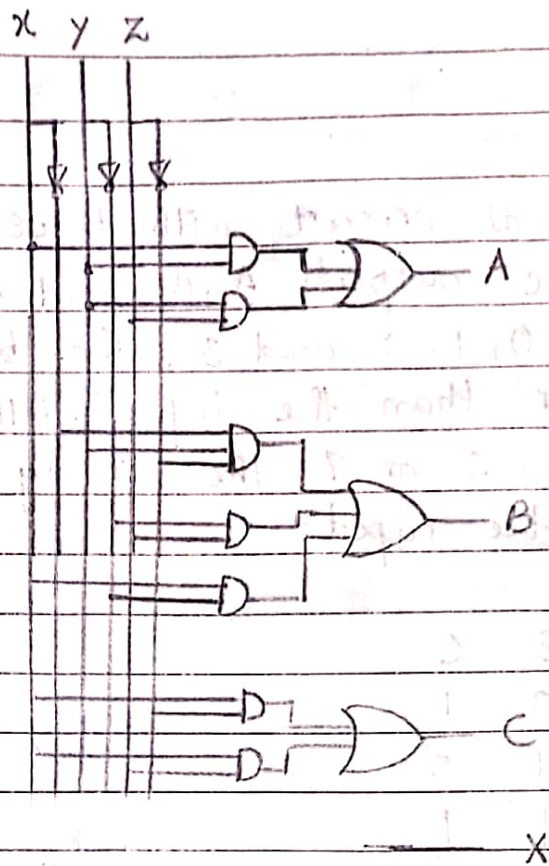
C

xy	$z=0$	$z=1$
00	1	
01	1	
11		1
10		1

$$A = xy + yz$$

$$B = \bar{x}y\bar{z} + \bar{y}z + x\bar{y}$$

$$C = \bar{x}z + xz$$



Question Number 2:

Construct a full-subtractor circuit with three inputs x, y, B_{in} and two outputs $Diff$ and B_{out} . The circuit subtracts $x - y - B_{in}$, where B_{in} is the input borrow, B_{out} is the output borrow, and $Diff$ is the difference.

x	y	B_{in}	$Diff$	B_{out}
0	0	0	0	0
0	0	1	1	1
0	1	0	1	1
0	1	1	0	1
1	0	0	1	0
1	0	1	0	0
1	1	0	0	0
1	1	1	1	1

(Diff)

xy	B _{in} 0	1
00		1
01	1	
11		1
10	1	

$$\text{Diff} = \bar{x}\bar{y}B_{in} + \bar{x}y\bar{B}_{in} + x\bar{y}B_{in} + x\bar{y}\bar{B}_{in}$$

$$\text{Diff} = \bar{x}(\bar{y}B_{in} + y\bar{B}_{in}) + x(yB_{in} + \bar{y}\bar{B}_{in})$$

$$\text{Diff} = \bar{x}(y \oplus B_{in}) + x(\bar{y} \oplus B_{in})$$

$$\boxed{\text{Diff} = x \oplus (y \oplus B_{in})}$$

(B_{out})

xy	B _{in} 0	1
00		1
01	1	1
11		1
10		

From K-map:

$$B_{out} = \bar{x}yB_{in} + \bar{x}y + yB_{in}$$

$$\boxed{B_{out} = \bar{x}y + B_{in}(\bar{x} + y)}$$

Simplified From Truth Table:

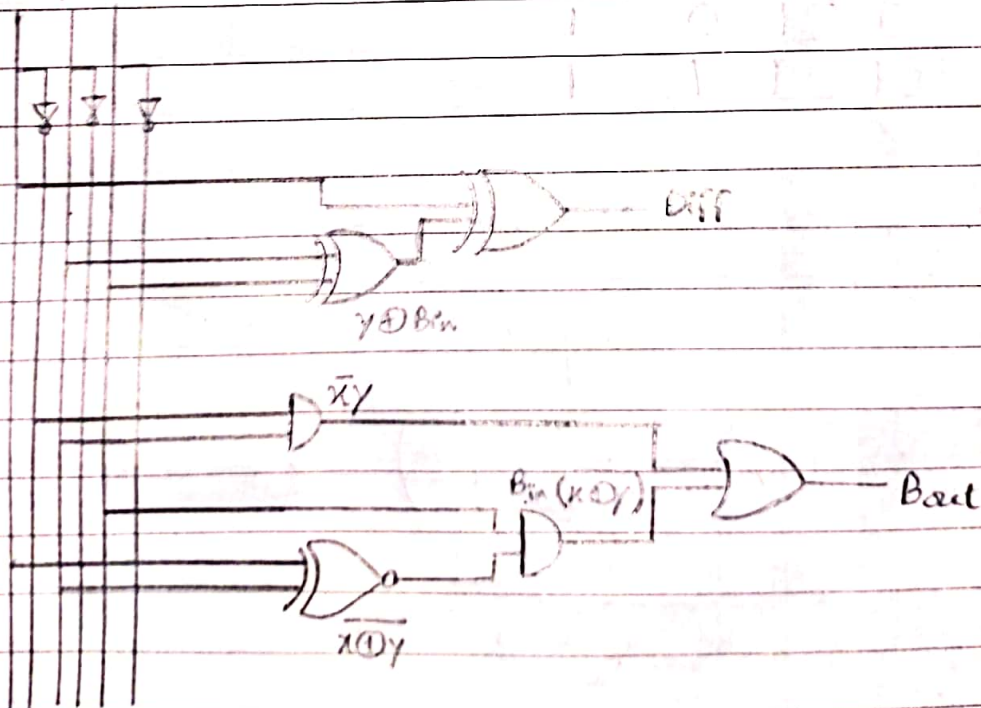
$$B_{out} = \bar{x}yB_{in} + \bar{x}y\bar{B}_{in} + \bar{x}yB_{in} + xyB_{in}$$

$$B_{out} = \bar{x}yB_{in} + xyB_{in} + \bar{x}y\bar{B}_{in} + \bar{x}yB_{in}$$

$$B_{out} = B_{in}(\bar{x}y + xy) + \bar{x}y(\bar{B}_{in} + B_{in})$$

$$B_{out} = B_{in}(x \oplus y) + \bar{x}y(1)$$

$$\boxed{B_{out} = \bar{x}y + B_{in}(x \oplus y)}$$

x y B_{in}

X

Question Number 3:

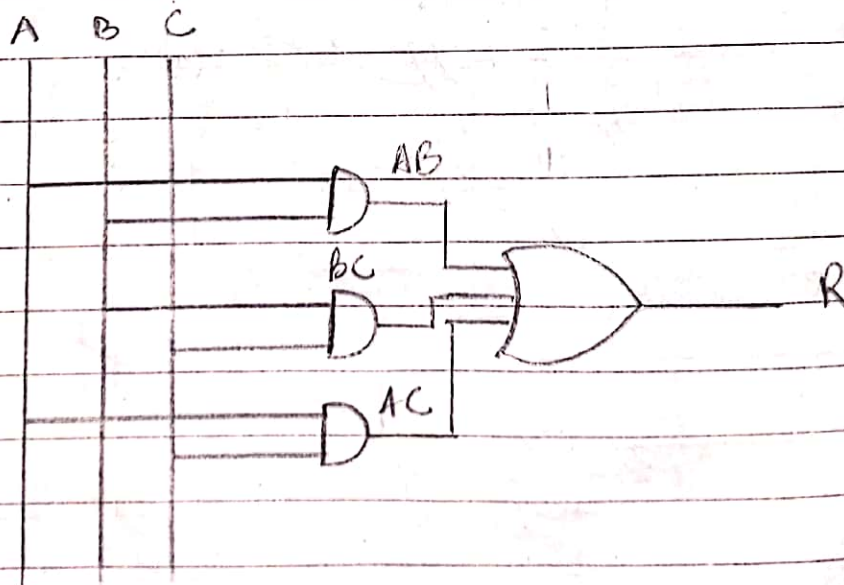
A committee of three individuals decides issues for an organization. Each individual votes either yes or no for each proposal that arises. A proposal is passed if it receives at least two yes votes. Construct a circuit that determines whether a proposal passes.

A 1 \Rightarrow Yes
0 \Rightarrow NO

A	B	C	R
0	0	0	0
0	0	1	0
0	1	0	0
0	1	1	1
1	0	0	0
1	0	1	1
1	1	0	1
1	1	1	1

R	C	0	1
AB	00		
01		1	1
10	1	1	1

$$R = AB + BC + AC$$



Question Number 4:

Construct a BCD-to-decimal decoder using the unused combinations of the BCD code as don't-care conditions.

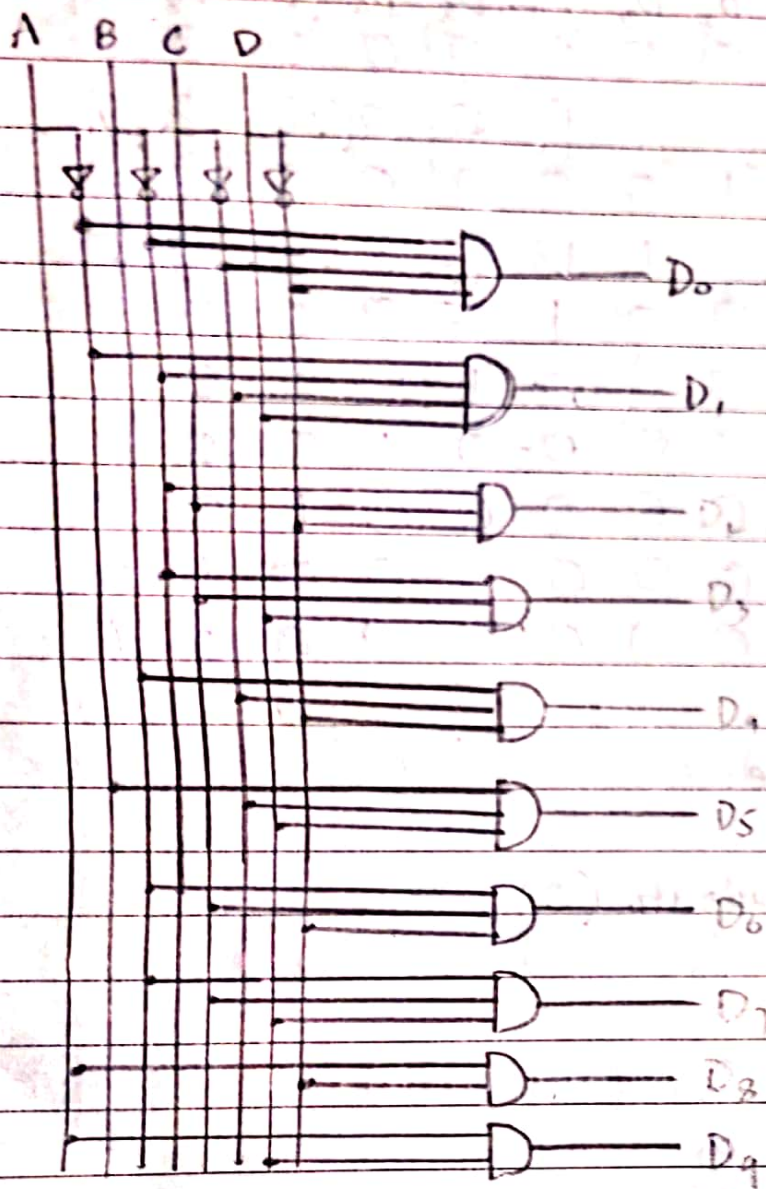
A	B	C	D	D ₀	D ₁	D ₂	D ₃	D ₄	D ₅	D ₆	D ₇	D ₈	D ₉
0	0	0	0	1	0	0	0	0	0	0	0	0	0
0	0	0	1	0	1	0	0	0	0	0	0	0	0
0	0	1	0	0	0	1	0	0	0	0	0	0	0
0	0	1	1	0	0	0	1	0	0	0	0	0	0
0	1	0	0	0	0	0	0	1	0	0	0	0	0
0	1	0	1	0	0	0	0	0	1	0	0	0	0
0	1	1	0	0	0	0	0	0	0	1	0	0	0
0	1	1	1	0	0	0	0	0	0	0	1	0	0
1	0	0	0	0	0	0	0	0	0	0	0	1	0
1	0	0	1	0	0	0	0	0	0	0	0	0	1

Abbreviated Truth Table:

A	B	C	D	Output (O)
0	0	0	0	D ₀
0	0	0	1	D ₁
0	0	1	0	D ₂
0	0	1	1	D ₃
0	1	0	0	D ₄
0	1	0	1	D ₅
0	1	1	0	D ₆
0	1	1	1	D ₇
1	0	0	0	D ₈
1	0	0	1	D ₉

	CD	00	01	11	10
AB	00	D_0	D_1	D_2	D_3
	01	D_4	D_5	D_7	D_6
	11	X	X	X	X
	10	D_8	D_9	X	X

$$\begin{aligned}
 D_0 &= \overline{A}BCD & D_6 &= BCD \\
 D_1 &= \overline{A}BC\overline{D} & D_7 &= BCD \\
 D_2 &= \overline{B}C\overline{D} & D_8 &= A\overline{D} \\
 D_3 &= \overline{B}CD & D_9 &= AD \\
 D_4 &= B\overline{C}\overline{D} & & \\
 D_5 &= B\overline{C}D & &
 \end{aligned}$$



— X —

Question Number 5:

Construct a 5-bit parity system.

Parity Generator:

A	B	C	D	P_{odd}	P_{even}
0	0	0	0	1	0
0	0	0	1	0	1
0	0	1	0	0	1
0	0	1	1	1	0
0	1	0	0	0	1
0	1	0	1	1	0
0	1	1	0	0	0
0	1	1	1	0	1
1	0	0	0	0	1
1	0	0	1	1	0
1	0	1	0	1	0
1	0	1	1	0	1
1	1	0	0	1	0
1	1	0	1	0	1
1	1	1	0	0	1
1	1	1	1	1	0

P_{odd} :

$$P_{\text{odd}} = \overline{A}BCD + \overline{A}\overline{B}CD + \overline{A}B\overline{C}D + \overline{A}B\overline{C}\overline{D} + A\overline{B}C\overline{D} + A\overline{B}C\overline{D} + A\overline{B}\overline{C}D + A\overline{B}\overline{C}\overline{D}$$

$$P_{\text{odd}} = \overline{A}\overline{B}(\overline{C}D + CD) + \overline{A}B(\overline{C}D + C\overline{D}) + AB(\overline{C}D + CD) + A\overline{B}(\overline{C}D + C\overline{D})$$

$$P_{\text{odd}} = \overline{A}\overline{B}(C \oplus D) + \overline{A}B(C \oplus D) + AB(\overline{C} \oplus \overline{D}) + A\overline{B}(C \oplus D)$$

$$P_{\text{odd}} = \overline{A}[\overline{B}(C \oplus D) + B(C \oplus D)] + A[B(\overline{C} \oplus \overline{D}) + \overline{B}(C \oplus D)]$$

$$P_{\text{odd}} = \overline{A}(B \oplus C \oplus D) + A(B \oplus C \oplus D)$$

$$P_{\text{odd}} = A \oplus (B \oplus C \oplus D)$$

Even:

$$P_{\text{even}} = \overline{A}BCD + \overline{A}BC\overline{D} + \overline{A}B\overline{C}D + \overline{A}B\overline{C}\overline{D} + A\overline{B}CD + A\overline{B}C\overline{D} + A\overline{B}\overline{C}D + A\overline{B}\overline{C}\overline{D}$$

$$P_{\text{even}} = \overline{A}B(\overline{C}D + C\overline{D}) + \overline{A}B(\overline{C}D + C\overline{D}) + AB(\overline{C}D + C\overline{D}) + A\overline{B}(\overline{C}D + C\overline{D})$$

$$P_{\text{even}} = \overline{A}B(C \oplus D) + \overline{A}B(\overline{C} \oplus D) + AB(\overline{C} \oplus D) + A\overline{B}(C \oplus D)$$

$$P_{\text{even}} = \overline{A}[\overline{B}(C \oplus D) + B(\overline{C} \oplus D)] + A[B(C \oplus D) + \overline{B}(\overline{C} \oplus D)]$$

$$P_{\text{even}} = \overline{A}(B \oplus C \oplus D) + A(\overline{B} \oplus C \oplus D)$$

$$P_{\text{even}} = A \oplus (B \oplus C \oplus D)$$

Parity Checker:

P/Po	A	B	C	D	C _{odd}	C _{even}	P/Po	A	B	C	D	C _{odd}	C _{even}
0	0	0	0	0	1	0	0	1	1	1	1	1	0
0	0	0	0	1	0	1	1	0	0	0	0	0	1
0	0	0	1	0	0	1	1	0	0	0	1	1	0
0	0	0	1	1	1	0	1	0	0	1	0	1	0
0	0	1	0	0	0	1	1	0	0	1	1	0	1
0	0	1	0	1	1	0	1	0	1	0	0	1	0
0	0	1	1	0	1	0	1	0	1	0	1	0	1
0	0	1	1	1	0	1	1	0	1	1	0	0	1
0	1	0	0	0	0	1	1	0	1	1	1	1	0
0	1	0	0	1	1	0	1	1	0	0	0	1	0
0	1	0	1	0	1	0	1	1	0	0	1	0	1
0	1	0	1	1	0	1	1	1	0	1	0	0	1
0	1	1	0	0	1	0	1	1	0	1	1	1	0
0	1	1	0	1	0	1	1	1	1	0	0	0	1
0	1	1	1	0	0	1	1	1	1	0	1	1	0

Code	BCD	000	001	010	011	100	101	110	111
P ₀ A	00	1		1		1		1	
	01		1		1		1		1
	11	1		1		1		1	
	10		1		1		1		1

$$C_{odd} = \overline{P_0} \overline{A} \overline{B} \overline{C} \overline{D} + \overline{P_0} \overline{A} \overline{B} \overline{C} D + \overline{P_0} \overline{A} \overline{B} C \overline{D} + \overline{P_0} \overline{A} \overline{B} C D + \overline{P_0} \overline{A} B \overline{C} \overline{D} + \overline{P_0} \overline{A} B \overline{C} D + \overline{P_0} \overline{A} B C \overline{D} + \overline{P_0} \overline{A} B C D + \overline{P_0} A \overline{B} \overline{C} \overline{D} + \overline{P_0} A \overline{B} \overline{C} D + \overline{P_0} A \overline{B} C \overline{D} + \overline{P_0} A \overline{B} C D + \overline{P_0} A B \overline{C} \overline{D} + \overline{P_0} A B \overline{C} D + \overline{P_0} A B C \overline{D} + \overline{P_0} A B C D$$

$$C_{odd} = \overline{P_0} (\overline{A} \overline{B} \overline{C} \overline{D} + \overline{A} \overline{B} \overline{C} D + \overline{A} \overline{B} C \overline{D} + \overline{A} \overline{B} C D + \overline{A} B \overline{C} \overline{D} + \overline{A} B \overline{C} D + \overline{A} B C \overline{D} + \overline{A} B C D) + P_0 (A \overline{B} \overline{C} \overline{D} + A \overline{B} \overline{C} D + A \overline{B} C \overline{D} + A \overline{B} C D + A B \overline{C} \overline{D} + A B \overline{C} D + A B C \overline{D} + A B C D)$$

$$C_{odd} = \overline{P_0} [\overline{A} \{ \overline{B} (\overline{C} \overline{D} + C \overline{D}) + B (\overline{C} \overline{D} + C \overline{D}) \} + A \{ \overline{B} (\overline{C} \overline{D} + C \overline{D}) + B (\overline{C} \overline{D} + C \overline{D}) \}] + P_0 [A \{ \overline{B} (\overline{C} \overline{D} + C \overline{D}) + B (\overline{C} \overline{D} + C \overline{D}) \} + \overline{A} \{ \overline{B} (\overline{C} \overline{D} + C \overline{D}) + B (\overline{C} \overline{D} + C \overline{D}) \}]$$

$$= \overline{P_0} [\overline{A} \{ \overline{B} (C \oplus D) + B (C \oplus D) \} + A \{ \overline{B} (C \oplus D) + B (C \oplus D) \}] + P_0 [A \{ \overline{B} (C \oplus D) + B (C \oplus D) \} + \overline{A} \{ \overline{B} (C \oplus D) + B (C \oplus D) \}]$$

$$C_{odd} = \overline{P_0} [\overline{A} \{ B \oplus (C \oplus D) \} + A \{ B \oplus (C \oplus D) \}] + P_0 [A \{ B \oplus (C \oplus D) \} + \overline{A} \{ B \oplus (C \oplus D) \}]$$

$$C_{odd} = \overline{P_0} [A \oplus \{ B \oplus (C \oplus D) \}] + P_0 [A \oplus \{ B \oplus (C \oplus D) \}]$$

$$C_{odd} = P_0 \oplus (A \oplus B \oplus C \oplus D)$$

$$C_{even} = \overline{P_0} \overline{A} \overline{B} \overline{C} \overline{D} + \overline{P_0} \overline{A} \overline{B} \overline{C} D + \overline{P_0} \overline{A} \overline{B} C \overline{D} + \overline{P_0} \overline{A} \overline{B} C D + \overline{P_0} \overline{A} B \overline{C} \overline{D} + \overline{P_0} \overline{A} B \overline{C} D + \overline{P_0} \overline{A} B C \overline{D} + \overline{P_0} \overline{A} B C D + \overline{P_0} A \overline{B} \overline{C} \overline{D} + \overline{P_0} A \overline{B} \overline{C} D + \overline{P_0} A \overline{B} C \overline{D} + \overline{P_0} A \overline{B} C D + \overline{P_0} A B \overline{C} \overline{D} + \overline{P_0} A B \overline{C} D + \overline{P_0} A B C \overline{D} + \overline{P_0} A B C D$$

$$C_{even} = \overline{P_0} (\overline{A} \overline{B} \overline{C} \overline{D} + \overline{A} \overline{B} \overline{C} D + \overline{A} \overline{B} C \overline{D} + \overline{A} \overline{B} C D + \overline{A} B \overline{C} \overline{D} + \overline{A} B \overline{C} D + \overline{A} B C \overline{D} + \overline{A} B C D) + P_0 (A \overline{B} \overline{C} \overline{D} + A \overline{B} \overline{C} D + A \overline{B} C \overline{D} + A \overline{B} C D + A B \overline{C} \overline{D} + A B \overline{C} D + A B C \overline{D} + A B C D)$$

$$C_{even} = \overline{P_e} \left[\overline{A} \{ \overline{B} (\overline{C}D + C\overline{D}) + B(CD + C\overline{D}) \} + A \{ \overline{B} (\overline{C}D + C\overline{D}) + B(\overline{C}D + C\overline{D}) \} \right] + P_e \left[A \{ \overline{B} (\overline{C}D + C\overline{D}) + B(CD + C\overline{D}) \} + A \{ \overline{B} (\overline{C}D + C\overline{D}) + B(C\overline{D} + \overline{C}D) \} \right]$$

$$= \overline{P_e} \left[\overline{A} \{ \overline{B} (C \oplus D) + B(\overline{C \oplus D}) \} + A \{ \overline{B}(C \oplus D) + B(\overline{C \oplus D}) \} \right] + P_e \left[A \{ \overline{B} (C \oplus D) + B(\overline{C \oplus D}) \} + \overline{A} \{ \overline{B} (\overline{C \oplus D}) + B(C \oplus D) \} \right]$$

$$= \overline{P_e} \left[\overline{A} \{ B \oplus (\overline{C \oplus D}) \} + A \{ B \oplus (\overline{C \oplus D}) \} \right] + P_e \left[A \{ B \oplus (\overline{C \oplus D}) \} + \overline{A} \{ B \oplus (\overline{C \oplus D}) \} \right]$$

$$= \overline{P_e} \left[A \oplus \{ B \oplus (\overline{C \oplus D}) \} \right] + P_e \left[A \oplus \{ B \oplus (\overline{C \oplus D}) \} \right]$$

$$\boxed{C_{even} = P_e \oplus (A \oplus B \oplus C \oplus D)}$$

Date: _____

