

Untitled38

July 5, 2020

1 ETS Models

```
In [72]: ## Load the libraries  
import numpy as np  
import pandas as pd  
import matplotlib.pyplot as plt  
%matplotlib inline
```

```
In [2]: ## import the data  
df = pd.read_csv("/Users/snigdhaheekoty/Desktop/prac/airline_passengers.csv", index_col=0,  
                 parse_dates = True)
```

```
In [3]: df.head(10)
```

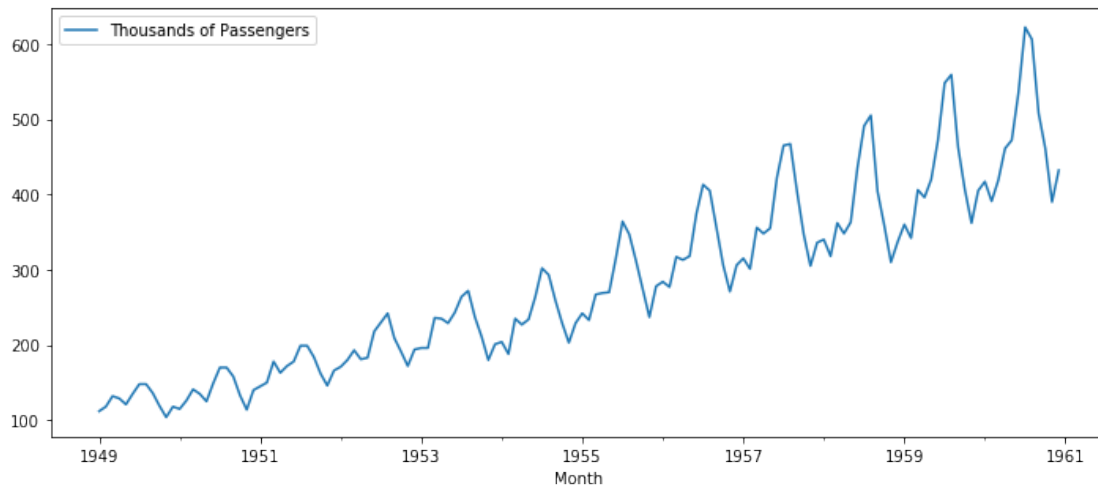
```
Out [3]:
```

| Month | Thousands of Passengers |
|------------|-------------------------|
| 1949-01-01 | 112 |
| 1949-02-01 | 118 |
| 1949-03-01 | 132 |
| 1949-04-01 | 129 |
| 1949-05-01 | 121 |
| 1949-06-01 | 135 |
| 1949-07-01 | 148 |
| 1949-08-01 | 148 |
| 1949-09-01 | 136 |
| 1949-10-01 | 119 |

```
In [9]: ### there are no missing values
```

```
In [11]: ## plotting the observations  
df.plot(figsize = (12,5))
```

```
Out [11]: <matplotlib.axes._subplots.AxesSubplot at 0x116c3de48>
```



```
In [12]: ## The trend look exponential than linear
         ## SO we apply the multiplicative ETS Model
         from statsmodels.tsa.seasonal import seasonal_decompose
         result = seasonal_decompose(df["Thousands of Passengers"], model = "multiplicative")
         type(result)
```

/anaconda3/lib/python3.6/site-packages/statsmodels/compat/pandas.py:56: FutureWarning: The pandas.core import datetools

Out[12]: statsmodels.tsa.seasonal.DecomposeResult

```
In [14]: result.trend.head(15) # observations of trend component
```

```
Out[14]: Month
1949-01-01      NaN
1949-02-01      NaN
1949-03-01      NaN
1949-04-01      NaN
1949-05-01      NaN
1949-06-01      NaN
1949-07-01    126.791667
1949-08-01    127.250000
1949-09-01    127.958333
1949-10-01    128.583333
1949-11-01    129.000000
1949-12-01    129.750000
1950-01-01    131.250000
1950-02-01    133.083333
1950-03-01    134.916667
Name: Thousands of Passengers, dtype: float64
```

```
In [15]: result.seasonal.head(15) # observations of seasonal component
```

```
Out[15]: Month
1949-01-01    0.910230
1949-02-01    0.883625
1949-03-01    1.007366
1949-04-01    0.975906
1949-05-01    0.981378
1949-06-01    1.112776
1949-07-01    1.226556
1949-08-01    1.219911
1949-09-01    1.060492
1949-10-01    0.921757
1949-11-01    0.801178
1949-12-01    0.898824
1950-01-01    0.910230
1950-02-01    0.883625
1950-03-01    1.007366
Name: Thousands of Passengers, dtype: float64
```

```
In [17]: result.resid.head(15) # observations of residual component
```

```
Out[17]: Month
1949-01-01    NaN
1949-02-01    NaN
1949-03-01    NaN
1949-04-01    NaN
1949-05-01    NaN
1949-06-01    NaN
1949-07-01    0.951664
1949-08-01    0.953401
1949-09-01    1.002220
1949-10-01    1.004028
1949-11-01    1.006270
1949-12-01    1.011812
1950-01-01    0.962603
1950-02-01    1.071467
1950-03-01    1.037447
Name: Thousands of Passengers, dtype: float64
```

```
In [19]: ## Plotting the trend, seasonality and residual components
result.plot(figsize = (12,5)) ## This doesn't work because there are MULTIPLE PLOTS
```

```
-----

TypeError                                Traceback (most recent call last)

<ipython-input-19-b6e5abd2a7a5> in <module>()
```

```

1 ## Plotting the trend, seasonality and residual components
----> 2 result.plot(figsize = (12,5))

```

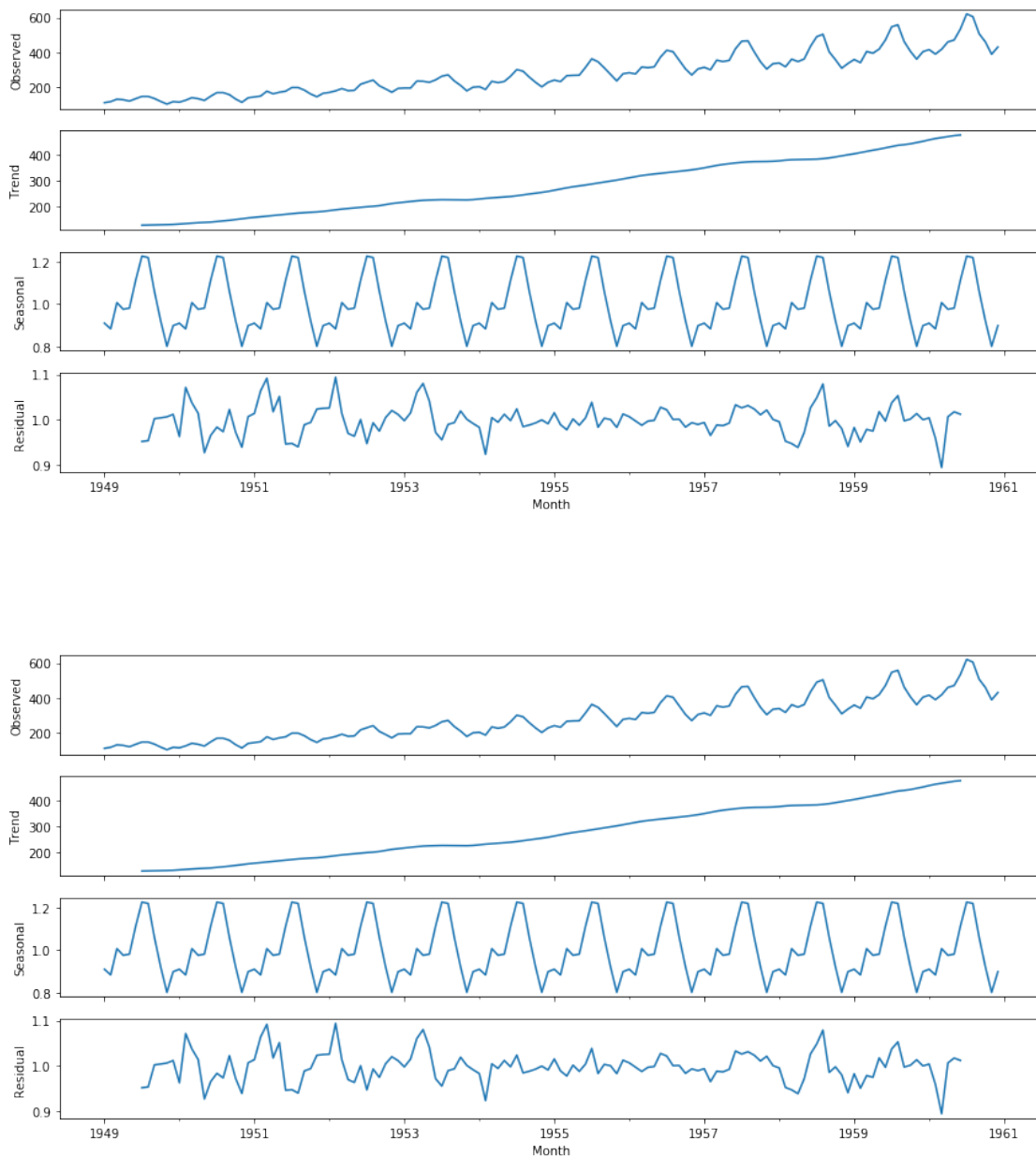
TypeError: plot() got an unexpected keyword argument 'figsize'

```

In [22]: ## Plotting the trend, seasonality and residual components
from pylab import rcParams
rcParams["figure.figsize"] = 12,6
result.plot()

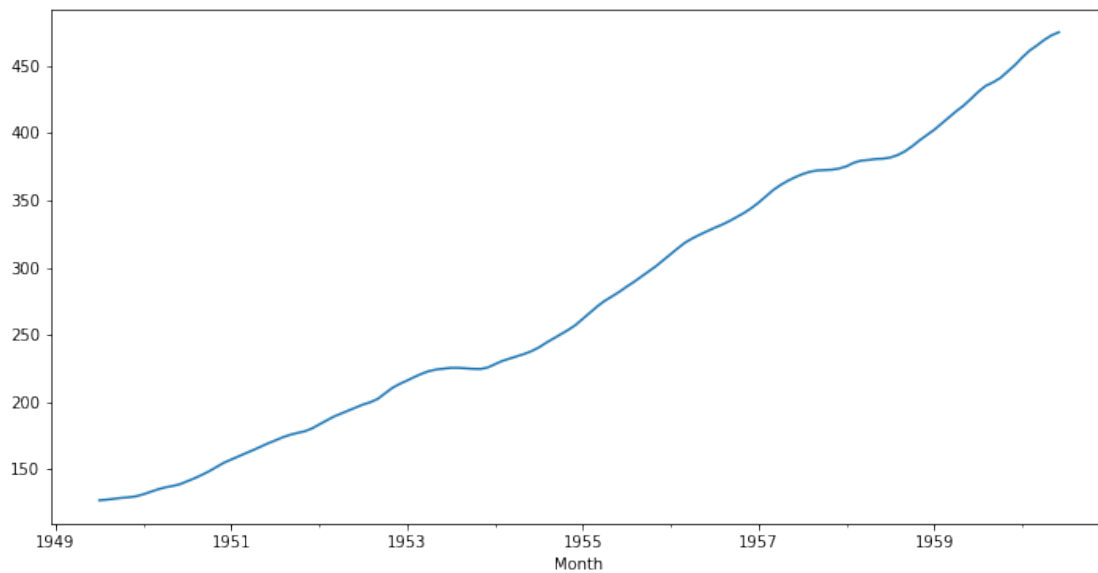
```

Out[22]:



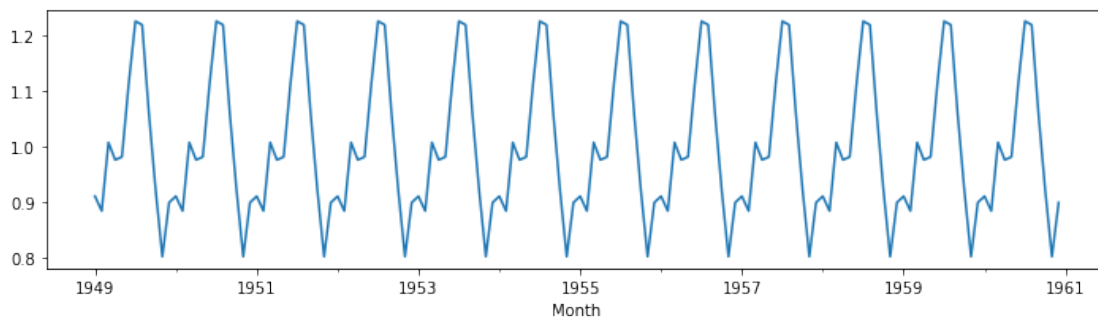
```
In [23]: ## Plotting the components individually  
result.trend.plot()
```

```
Out[23]: <matplotlib.axes._subplots.AxesSubplot at 0x1c19c6b390>
```



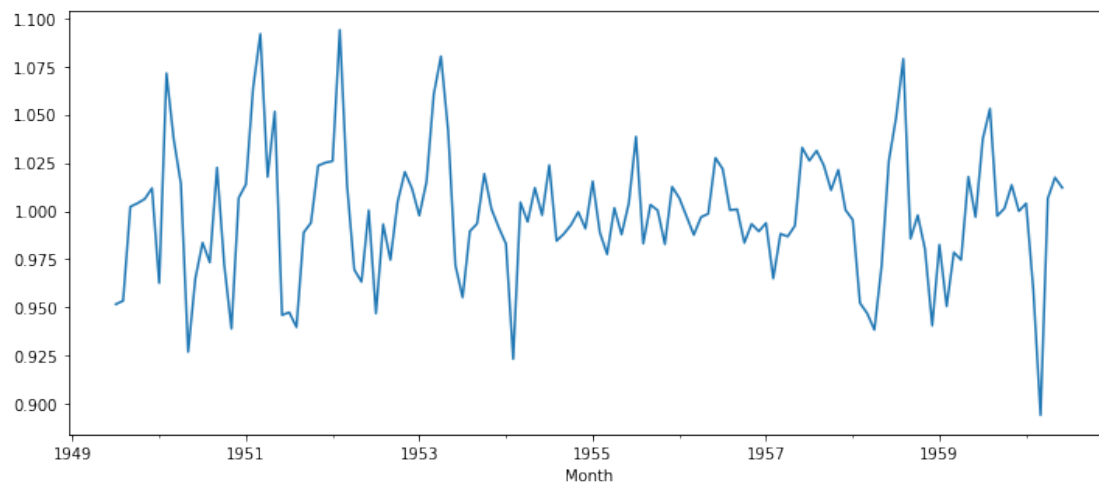
```
In [26]: result.seasonal.plot(figsize = (12,3))
```

```
Out[26]: <matplotlib.axes._subplots.AxesSubplot at 0x1c19e7e550>
```



```
In [28]: result.resid.plot(figsize = (12,5))
```

```
Out[28]: <matplotlib.axes._subplots.AxesSubplot at 0x1c1a256c50>
```



2 EWMA Model

```
In [29]: ### "EWMA" - Exponentially Weighted Moving Average Model
### More sophisticated model for analysing the time series trends
## It's a simple exponential smoothing method
## libraries required: numpy, pandas, matplotlib
```

```
In [31]: df.head(10)
```

```
Out [31]:
```

| Month | Thousands of Passengers |
|------------|-------------------------|
| 1949-01-01 | 112 |
| 1949-02-01 | 118 |
| 1949-03-01 | 132 |
| 1949-04-01 | 129 |
| 1949-05-01 | 121 |
| 1949-06-01 | 135 |
| 1949-07-01 | 148 |
| 1949-08-01 | 148 |
| 1949-09-01 | 136 |
| 1949-10-01 | 119 |

```
In [32]: df.index
```

```
Out [32]: DatetimeIndex(['1949-01-01', '1949-02-01', '1949-03-01', '1949-04-01',
                          '1949-05-01', '1949-06-01', '1949-07-01', '1949-08-01',
                          '1949-09-01', '1949-10-01',
                          ...,
                          '1960-03-01', '1960-04-01', '1960-05-01', '1960-06-01',
                          '1960-07-01', '1960-08-01', '1960-09-01', '1960-10-01',
```

```

        '1960-11-01', '1960-12-01'],
        dtype='datetime64[ns]', name='Month', length=144, freq=None)

```

```

In [34]: ## Applying SMA - Simple Moving Average
         df["6-month avg"] = df["Thousands of Passengers"].rolling(window = 6).mean()

In [35]: df["12-month avg"] = df["Thousands of Passengers"].rolling(window = 12).mean()

In [37]: df.head(20)

```

```

Out[37]:

```

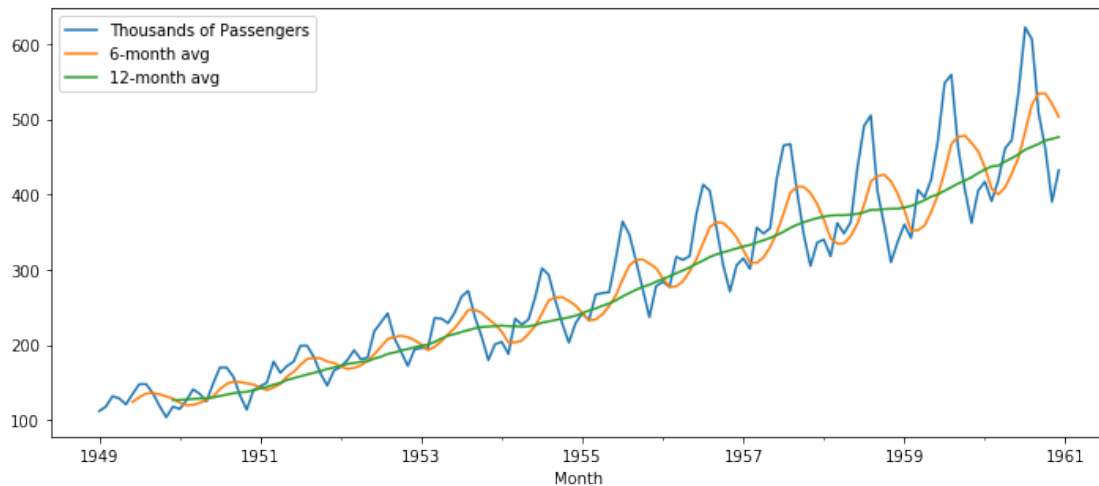
| Month | Thousands of Passengers | 6-month avg | 12-month avg |
|------------|-------------------------|-------------|--------------|
| 1949-01-01 | 112 | NaN | NaN |
| 1949-02-01 | 118 | NaN | NaN |
| 1949-03-01 | 132 | NaN | NaN |
| 1949-04-01 | 129 | NaN | NaN |
| 1949-05-01 | 121 | NaN | NaN |
| 1949-06-01 | 135 | 124.500000 | NaN |
| 1949-07-01 | 148 | 130.500000 | NaN |
| 1949-08-01 | 148 | 135.500000 | NaN |
| 1949-09-01 | 136 | 136.166667 | NaN |
| 1949-10-01 | 119 | 134.500000 | NaN |
| 1949-11-01 | 104 | 131.666667 | NaN |
| 1949-12-01 | 118 | 128.833333 | 126.666667 |
| 1950-01-01 | 115 | 123.333333 | 126.916667 |
| 1950-02-01 | 126 | 119.666667 | 127.583333 |
| 1950-03-01 | 141 | 120.500000 | 128.333333 |
| 1950-04-01 | 135 | 123.166667 | 128.833333 |
| 1950-05-01 | 125 | 126.666667 | 129.166667 |
| 1950-06-01 | 149 | 131.833333 | 130.333333 |
| 1950-07-01 | 170 | 141.000000 | 132.166667 |
| 1950-08-01 | 170 | 148.333333 | 134.000000 |

```

In [38]: ## Plotting SMA
         df.plot(figsize = (12,5))

Out[38]: <matplotlib.axes._subplots.AxesSubplot at 0x1c1a5829b0>

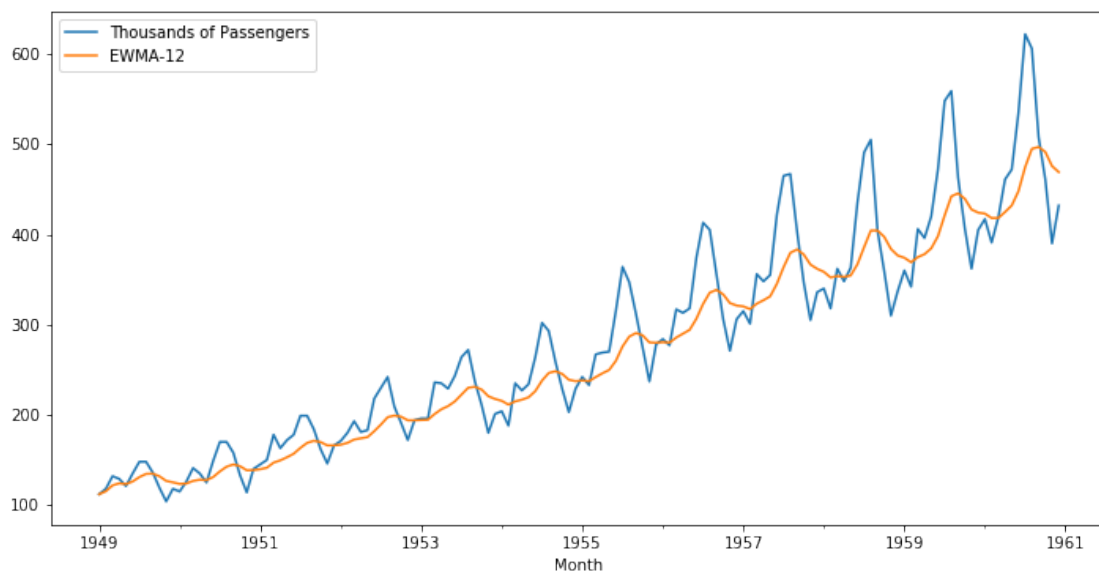
```



```
In [39]: ## Applying EWMA
         df["EWMA-12"] = df["Thousands of Passengers"].ewm(span = 12).mean()

In [40]: df[["Thousands of Passengers", "EWMA-12"]].plot()

Out[40]: <matplotlib.axes._subplots.AxesSubplot at 0x1c1a85c710>
```



3 HOLT WINTERS METHOD

```
In [42]: # EWMA - SIMPLE Exponential Smoothing
         # Holt Winters- DOUBLE Exponential Smoothing and TRIPLE Exponential Smoothing
         # Parameters - 'alpha' for Level, 'beta' for trend, 'gamma' for seasonality
```



```
In [44]: ## libraries - numpy , pandas , matplotlib
```

```
df.index
```

```
Out [44]: DatetimeIndex(['1949-01-01', '1949-02-01', '1949-03-01', '1949-04-01',
                        '1949-05-01', '1949-06-01', '1949-07-01', '1949-08-01',
                        '1949-09-01', '1949-10-01',
                        ...,
                        '1960-03-01', '1960-04-01', '1960-05-01', '1960-06-01',
                        '1960-07-01', '1960-08-01', '1960-09-01', '1960-10-01',
                        '1960-11-01', '1960-12-01'],
                        dtype='datetime64[ns]', name='Month', length=144, freq=None)
```

```
In [53]: ## As you see above, freq = None. This needs to be changed to fit the model using Sta
## Because: Data has frequency and Statsmodels needs to know it
```

```
## Hence, Setting the frequency to index
```

```
df.index.freq = 'MS'
```

```
## MS - Because the observations start at the starting of each month
```

```
In [54]: df.head()
```

```
Out [54]:
```

| | Thousands of Passengers | 6-month avg | 12-month avg | EWMA-12 |
|------------|-------------------------|-------------|--------------|------------|
| Month | | | | |
| 1949-01-01 | 112 | NaN | NaN | 112.000000 |
| 1949-02-01 | 118 | NaN | NaN | 115.250000 |
| 1949-03-01 | 132 | NaN | NaN | 121.787529 |
| 1949-04-01 | 129 | NaN | NaN | 124.064224 |
| 1949-05-01 | 121 | NaN | NaN | 123.231685 |

```
In [60]: ## Simple Exponential Smoothing using EWM
```

```
import pandas as pd
```

```
span = 12 # 12 months in a year
```

```
alpha = 2/(span+1) # alpha - formula
```

```
df["EWMA12"] = df["Thousands of Passengers"].ewm(alpha = alpha, adjust = False).mean()
```

```
In [61]: df.head(10)
```

```
Out [61]:
```

| | Thousands of Passengers | 6-month avg | 12-month avg | EWMA-12 | \ |
|------------|-------------------------|-------------|--------------|------------|---|
| Month | | | | | |
| 1949-01-01 | 112 | NaN | NaN | 112.000000 | |
| 1949-02-01 | 118 | NaN | NaN | 115.250000 | |
| 1949-03-01 | 132 | NaN | NaN | 121.787529 | |
| 1949-04-01 | 129 | NaN | NaN | 124.064224 | |
| 1949-05-01 | 121 | NaN | NaN | 123.231685 | |
| 1949-06-01 | 135 | 124.500000 | NaN | 126.092005 | |
| 1949-07-01 | 148 | 130.500000 | NaN | 130.980697 | |

| | | | | |
|------------|-----|------------|-----|------------|
| 1949-08-01 | 148 | 135.500000 | NaN | 134.532364 |
| 1949-09-01 | 136 | 136.166667 | NaN | 134.822714 |
| 1949-10-01 | 119 | 134.500000 | NaN | 131.824316 |

EWMA12

| Month | |
|------------|------------|
| 1949-01-01 | 112.000000 |
| 1949-02-01 | 112.923077 |
| 1949-03-01 | 115.857988 |
| 1949-04-01 | 117.879836 |
| 1949-05-01 | 118.359861 |
| 1949-06-01 | 120.919883 |
| 1949-07-01 | 125.086055 |
| 1949-08-01 | 128.611277 |
| 1949-09-01 | 129.748004 |
| 1949-10-01 | 128.094465 |

```
In [98]: ## Simple Exponential Smoothing using HoltWinters model
         from statsmodels.tsa.holtwinters import SimpleExpSmoothing
```

```
In [110]: fit = SimpleExpSmoothing(df["Thousands of Passengers"]).fit(smoothing_level= alpha, c
```

```
In [116]: ## Double Exponential Smoothing using HoltWinters model
         from statsmodels.tsa.holtwinters import ExponentialSmoothing
         df["DES_add_12"] = ExponentialSmoothing(df["Thousands of Passengers"],trend="add").f
```

```
In [117]: df.head()
```

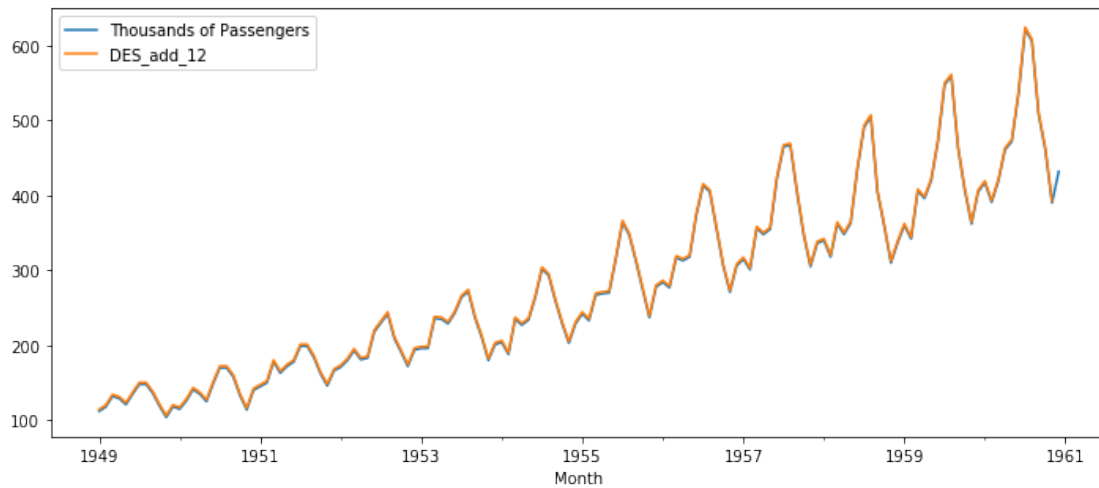
```
Out[117]:
```

| | Thousands of Passengers | 6-month avg | 12-month avg | EWMA-12 | \ |
|------------|-------------------------|-------------|--------------|------------|---|
| Month | | | | | |
| 1949-01-01 | 112 | NaN | NaN | 112.000000 | |
| 1949-02-01 | 118 | NaN | NaN | 115.250000 | |
| 1949-03-01 | 132 | NaN | NaN | 121.787529 | |
| 1949-04-01 | 129 | NaN | NaN | 124.064224 | |
| 1949-05-01 | 121 | NaN | NaN | 123.231685 | |

| | EWMA12 | DES_add_12 |
|------------|------------|------------|
| Month | | |
| 1949-01-01 | 112.000000 | 114.336734 |
| 1949-02-01 | 112.923077 | 120.336734 |
| 1949-03-01 | 115.857988 | 134.336734 |
| 1949-04-01 | 117.879836 | 131.336734 |
| 1949-05-01 | 118.359861 | 123.336734 |

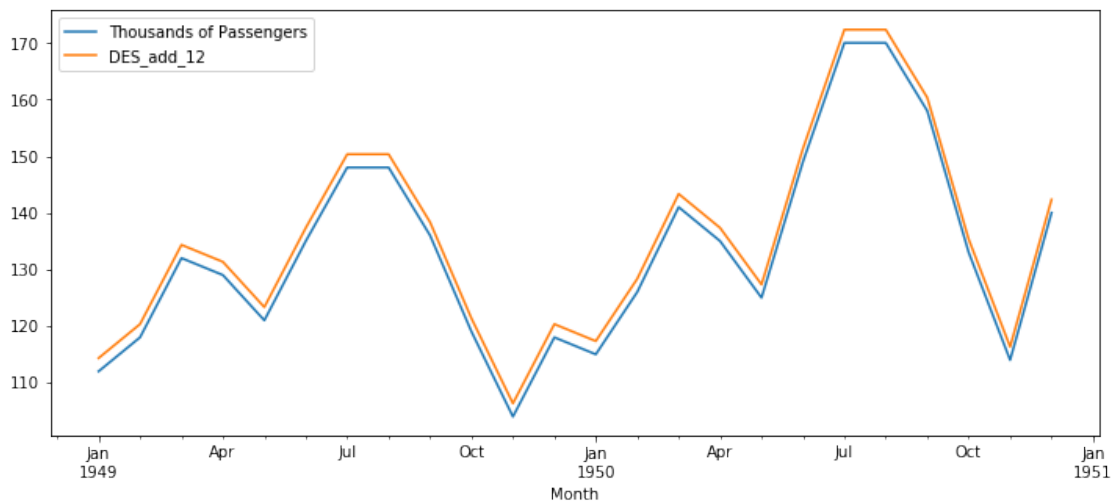
```
In [119]: ## Plotting the double exponential moving average
         df[["Thousands of Passengers", "DES_add_12"]].plot(figsize = (12,5))
```

```
Out[119]: <matplotlib.axes._subplots.AxesSubplot at 0x1c1c5f57f0>
```



```
In [120]: df[["Thousands of Passengers", "DES_add_12"]].iloc[:24].plot(figsize = (12,5))
```

```
Out[120]: <matplotlib.axes._subplots.AxesSubplot at 0x1c1c5235c0>
```



```
In [125]: ## Triple Exponential Smoothing
from statsmodels.tsa.holtwinters import ExponentialSmoothing
df["DES_mul_12"] = ExponentialSmoothing(df["Thousands of Passengers"], trend = "mul"
```

```
In [126]: df.head()
```

```
Out[126]:
```

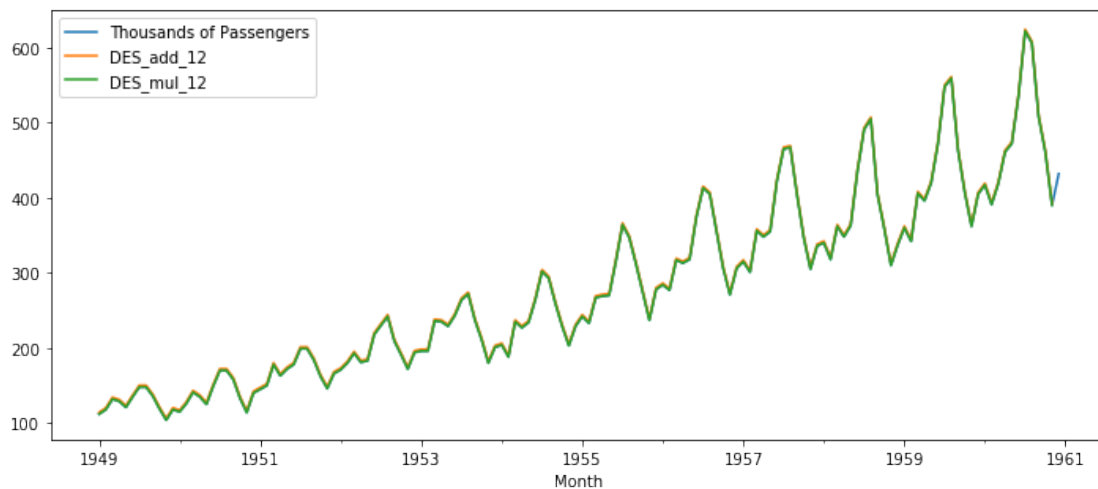
| Month | Thousands of Passengers | 6-month avg | 12-month avg | EWMA-12 | \ |
|-------|-------------------------|-------------|--------------|---------|---|
|-------|-------------------------|-------------|--------------|---------|---|

| | | | | |
|------------|-----|-----|-----|------------|
| 1949-01-01 | 112 | NaN | NaN | 112.000000 |
| 1949-02-01 | 118 | NaN | NaN | 115.250000 |
| 1949-03-01 | 132 | NaN | NaN | 121.787529 |
| 1949-04-01 | 129 | NaN | NaN | 124.064224 |
| 1949-05-01 | 121 | NaN | NaN | 123.231685 |

| | EWMA12 | DES_add_12 | DES_mul_12 |
|------------|------------|------------|------------|
| Month | | | |
| 1949-01-01 | 112.000000 | 114.336734 | 112.049247 |
| 1949-02-01 | 112.923077 | 120.336734 | 118.051885 |
| 1949-03-01 | 115.857988 | 134.336734 | 132.058041 |
| 1949-04-01 | 117.879836 | 131.336734 | 129.056722 |
| 1949-05-01 | 118.359861 | 123.336734 | 121.053204 |

```
In [131]: ## Plotting
df[["Thousands of Passengers", "DES_add_12", "DES_mul_12"]].plot(figsize = (12,5))
```

```
Out[131]: <matplotlib.axes._subplots.AxesSubplot at 0x1c1c570c50>
```



```
In [134]: df[["Thousands of Passengers", "DES_add_12", "DES_mul_12"]].iloc[:12].plot(figsize =
```

```
Out[134]: <matplotlib.axes._subplots.AxesSubplot at 0x1c1ca91668>
```



In []: *## We can see that multiplicative model models the data better*