Section VI	Big O					
	Asymptotic notations					
	O(Big O)	Describes an upper bound on time	for example: algo that prints all the values in an array: could have Big O time as O (n), O(n^2), O(n^3) or O(2^n) and many other Big O's	Upper bounds on the runtime; similar to a less- than-or-equal-to relationship	In industry, O and theta have been put together and we have to give the tightest description of runtime	
	Omega(n)	Describes the lower bound	for example: printing the values in an array is Omega (n) as well as Omega(logn) as well as Omega(1)			
	Theta(n)	Describes the tight bound on runtime	Theta here means both O and Omega; in this example, it would be Theta(n)			
	Best Case, Worst Case and Expected Case					
	Best Case:	For example, in Quick Sort, if all the elements are equal, then quick sort will, on average, just traverse through the array once - O(N) time	Quick Sort as we know picks random element as a pivot and then swaps values in the array such that the elements less than pivot appear before elements greater than pivot - this gives partial sort. then it recursively sorts the left and right sides uing same process			

	The pivot could be repeatedly the biggest element in the array. If pivot is the first element in a reversely sorted array. In this cae, our recursion does not divide the array in half and recurse on other half. Instead, it justs shrinks the subarray by 1 element.	Time taken would O(N^2)		
·	both the above best and worst conditions would rarely happen; thus we can expect a runtime of O(nlogn)			
Relationship ber and Best Case, Case Concepts	tween Asymptotic notations Worst Case and Expected			
There is no particular relationship between the two concepts				
Best Case, Worst Case and Expected Case actually describe the big O or big Theta time for particular scenarios whereas these asymptotic notations describe the upper, lower and tight bounds for the runtime				

Space complexity				
Memory or space required by an algorithm	to create an array - if it is unidimensional, O(N) space complexity; for a 2-D array, O (N^2)			
Stack space in recursive calls counts too. Each call adds a level tot he stack and takes up actual memory.	However, just because you have N calls does not mean it will take O(N) time: check the example on Page 41 for more details			
Dron the				
Drop the constants				
O(2N) is actually O(N)				
Drop the non- dominant terms				
O(N^2 + N) becomes O (N^2)				
O(N + logN) becomes O(N)				
O(5*2^N + 1000N^100) becomes O (2^N)				
$O(x!) > O(2^x) >$	$O(x^2) > O(x \log x) > O(x)$			

Multi-Parts algorithms: add versus mutiply					
	Non-nested chunk of work A and B	O(A + B)	"DO THIS THEN WHEN YOU ARE ALL DONE, DO THAT"		
Multiply	Nested A and B	O(AB)	"DO THIS FOR EACH TIME YOU DO THAT"		
Amortized time					
actually takes copying N elements in a	That copying might take additional O(N) time after accounting for initial O(N) time of adding the elements to the array	But, this copying of elements into a new array does not happen quite often infact once in every some time	Amortized time allows to describe that the worst case can happen every once in a while but once it happens it won't happen again for so long, that the cost is amortized		
	X + X/2 + X/4 + X/8 = 2X				
logN runtimes					

	We basically start off with N elements, after a single step, we are down to N/2 elements and in another step to N/4 elements and so on.	The total runtime is then a matter of how many steps we can take before it becomes 1	2 <sup>k</sup> = N => k = logN with base 2	Basically, when you see a problem with logN runtime, the problem space gets halved in each step	
Recursive					
runtimes					
Program:	int f(int n){				
	if(n <= 1){				
	return 1}				
	return f(n -1) + f(n -1);}				
How many calls in the tree?					
Do not count and say 2					
It will have recursive calls with a depth N and 2^N nodes at the bottom most level	More genrically, 2^0 + 2^1 + 2^2 +2^n-1 = 2^n - 1 nodes	O(branches^depth) where branches is the number of times each recursive call branches	The space complexity would still be O (n) - even though we have O(2^n) nodes in tree total, only O(n) exists at a time		
 	• •				
Examples and E	xercises				

Example 1	O(n) time as we iterate through array once in each loop which are non-nested				
Example 2	O(N^2) time as we have two nested loops				
Example 3	j basically runs for N-1 steps in first iteration, N-2 steps in second iteration and so on.	1 + 2 + 3 ++ N-1 = N(N - 1)/2 ~ N^2	O(N^2)		
Example 4	For each element of array A, the inner loop goes through b iterations where b is the length of array B. Thus, time complexity is O(ab)				
Example 5	Similar to example 4, 100,000 units of work is still constant; so the run time is O(ab)				
Example 6	O(N) time as the array is iterated even if half of it (constant 1/2 can be ignored)				
Example 7	There is no established relationship between N and M , thus all but the last one are equivalent to O(N)				
Example 8	s = length of the longest string; a = length of the array; Sorting each string would take O(slogs) and we do this for a elements of the array; thus O(a * slogs). Now, sorting the array would take O(s * aloga) as each string comparison would take O(s) time in addition to array sorting that would take O(aloga); thus adding the two parts: O(a * slogs + s * aloga) = O(a *s (log a + log s)				
Example 9	Approach 1: for summing up the nodes in a BST, each node is exactly traversed once, thus O(N) time complexity				

	Approach 2: The number of recursive calls is 2 and the depth is logN in a BST> O (branches ^ depth) = O(2 ^ logN) where the base of logN is also 2 => time complexity = O(N) after simpllifying				
Example 10	O(root(N)) as the for loop does constant time and runs in O(root(N)) time				
Example 11	O(N) as the recursive process calls from N to N-1 to N-2 and so on until 1				
Example 12	Approach 1: We make a tree for that we branch 4 times at the retime. this gives us 4*3*2*1 leaf string. So, total nodes would be path with n nodes. Also, string the final time complexity in wor	oot, then 3 times, then 2 times nodes. We could say n! leaf no e n * n! as each leaf node is a concatenation will also take O	s, and then 1 odes for n length ttached to a (n) time. Thus,		
	Approach 2: At level 6, we have nodes; at level 4 we have 6!/2! total nodes in the tree in terms 1/n!). Now, the term in the brace n! * e whose value is around 2. Thus, the time complexity would thus, time complexity: O((n+1)!	nodesat level 0, we have 6!/ of n can be : n!(1/0! + 1/1! + 1/0) cket can be defined in terms of .718. The constant e can be dr ld be O(n! * n) where n is due for	6! nodes. so, the /2! + 1/3!+ f Euler's number: opped further.		
Example 13	(branches^depth) = O(2^N).	We can also get tighter runtime as O(1.6^N) if we consider that there might be just one call instead of 2 at the bottom of call stack sometimes.			
Example 14	From previous example, we de time. And, we have fib(1) + fib( $2^2 + 2^3 \dots + 2^n = 2^n + 2^n$ run time is approx. $2^n$	2) + $fib(3)$ + $fib(n)$ = 2^1 +			

Example 15	Now, here in this program we are doing memoization due to which the amount of work reduces to looking up fib(i - 1) and fib(i - 2) values in memo array at each call fib(i). Thus, we are doing a constant amount of work n times in n calls, hence time complexity: O(n)			
Example 16	The runtime is the number of times we can divide n by 2 until we get down to the base case 1. As, we know the number of times we can halve n until we get 1 is O (logN)			
Additional Prob	lems			
	The for loop iterates through b, thus time complexity is O (b)			
2	The recursive call iterates through b calls as it subtracts 1 in each iteration, thus time complexity is O(b)			
3	It does constant amount of work, thus time complexity is O(1)			
4	The variable count will eventually equal a/b. The while loop iterates through count times. Thus time complexity is O(a/b)			
5	The algorithm is actually doing a binary search to find the square root. Thus the runtime is O(logN)			

6	This is straightforward loop that stops when guess*guess > n or guess> sqrt(n); hence time complexity is O(sqrt(n))			
7	Ifa binary tree is not balanced, the max time to find an element would be the depth of the tree. The tree since it is imbalanced could be a straight list downwards and ave depth n. Thus, runtime is O(n)			
8	Without any ordering or sorting in a binary tree, we might need to traverse through all the nodes in the tree, thus the time complexity is O(n) where n is the number of nodes in the tree.			
9	The first call to appendToNew takes 1 copy. The second call takes 2 copies. The third call takes 3 copies. And so on. The total time will be sum through 1 to n, which is O(n^2)			
10	The runtime would be O(d) where d is the number of digits in the given number. A number with d digits can have a value upto 10^d. If n = 10^d, then d = log n. Thus, time complexity is O(log n) where the log is with base 10.			

	11	If the length of the string is k, t inOrder or sorted, takes O(k) of the string is c characters. No characters and k length would wish to construct astring length and b, thus the number of string Similarly here, that runtime woruntime to get all the strings of and check if they are sorted we	time. Also, suppose the length ow, to get strings of c be O(c^k). for example, you a 3 with just two characters a gs possible would be 2^3. buld be O(c^k). Thus, overall k length with c characters			
	12	Print of all the runtime for mergethen, for each element in a, wb-runtime would be O(a * log (blog b + a log b).	ve are doing binary search of			
Section IX	Interview Ques	tions				
Chapter 1	Arrays and Str					
	Hash Table					
	A hash table is a data structure that maps keys to values for efficient lookup.					
	Hash Table Implementation					
	Approach 1	We use an array of Linked List	s and a hash code function.			
		To insert a key ( a string or any we follow the following steps:	other datatype) and value			
		or long. Two different keys cou	I. Compute the key's hashcode, which will usually be an itn or long. Two different keys could have the same hashcode, as there may be numerous keys but finite number of ints.			
		This could be done with some	2. Then, we map the hash code to an index in the array. This could be done with something like hash (key) % array_length. Two different hashcodes could of course map			
		3. At this index, there is a linked list of keys and values. Store the key and value in the index. We must use a Linked List to tackle collisions: you could have two different keys with same hashcode or two different hashcodes but same index				

		To retrieve the value pair by its key, we repeat the process. Compute the hash code by key, and then index by hashcode. Then, search through the Linked List for the value and its key.	If it is the worst case, collisions are very high, runtime would be O(N) where N is the number of keys. And, if it is the best case, collisions are minimum, look up time would be O(1)			
	Approach 2	We can implement a look up s search tree. This gives us O(l advantage of this approach is we no longer allocate a large a through keys in order.	ogN) lookup time. The potentially less space, since			
	ArrayList & Res	sizable Arrays				
	When you need an array-like datastructure with dynamic resizing, you should use an ArrayList.	that when the array is full, the	We can work backwards to comany elements we copied at eincrease to get an array of size N/8 ++ 2+ 1 = N. Therefore elements takes O(N) worktota insertion on an average takes though some insertions take Coworst case.	each capacity e N: N/2 + N/4 + , inserting N l. Thus, each O(1), even		
	StringBuilder					
	Normally, concatenating n strings of x characters each would take O (xn^2).					
		n reduce this complexity as it cre ing them to one string only if ne				
Oh amt = == 0	Limbort Links					
Chapter 2	Linked Lists		D. H. Palader C. C.			
	LinkedList is a datastructure representing a sequence of nodes.	Singly Linked List> there is a pointer to the next node	Doubly Linked List> there is a pointer to the next and previous nodes			

	,		Benefit of a Linked List is that one can add or remove items from the beginning of the list in constant time			
Chapter 3	Stacks and Queues					
			A stack does not offer constant-time access to the ith item. However, it allows constant time adds and removes as it does not require shifting elements around.	most useful case: recursive algorithms - one needs to push temporary data oto a stack as one recurses, but then remove them as one backtracks		
	Queue implements FIFO	Operations of a queue: add (item), remove(), peek(), isEmpty()	most useful case: breadth- first search and implementing a cache			
Chapter 4	Trees and Graphs					
	Searching a tree is more complicated than searching any linear data structure	The worst case and the average case time may vary wildly and we must evaluate both the aspects of any problem	Tree is actually a type of graph in which cycles / loops are not possible			
Trees	In programming, The root node ha	structure composed of nodes. each tree has a root node. as zero or more children. Each ero or more children and so	The nodes may be in any order and may have any data types as values and may or may not have links back to their parent nodes.	A node is called a leaf node if it has no children.		
Trees vs. binary trees	A binary tree is a tree in which each node has upto two children. Not all trees are binary trees.	For example, a 10-ary tree representing a bunch of phone numbers is not a binary tree.				
Binary Tree vs. Binary Search Tree	A binary search tree is a binary tree in which		This inequality condition must be true for all of a node's descendants, not just its immediate children.			

Balanced vs. unbalanced tree	not neccessarily perfectly balanced but ensures O(log n) times for insert and find	Two common types of balanced trees: Red-black trees and AVL trees			
Complete binary trees	A complete binary tree is a binary tree in which every level of the tree is fully filled, except for the last level. To the extent the last level is filled, it is filled from left to right				
Full binary tree	each node has either 2 or zero children. There is no node having only one child				
Perfect binary tree	All interior nodes have two children and all leaf nodes are at the same level.		It must have exactly 2 <sup>k</sup> - 1 nodes where k is the number of levels.		
In-order traversal	"visit" the left branch, then the current node, and finally the right node	when performed on a binary search tree, it visits the nodes in ascending order.			
Pre-order traversal	"visits" the current node before its child nodes	The root is always the first node visited			
Post-order traversal	"visits" the current node after its child nodes	The root is always the last node visited			
Binary Heaps (min-heaps and max- heaps)	A min heap is a complete binary tree where each node is smaller than its children.	The root thus is the minimum element in the tree.	Two key operations: insert and extract-min		
Insert operation on min-heap	We start by inserting at the next available spot (looking left to right on the bottommost level). We fix the tree by swapping the new element with its parent, until we find an appropriate spot for the element. We essentially bubble up the minimum spot.		This takes O(logN) time, where N is the number of nodes in the heap.		

Extract-min operation on min-heap	The minimum element of a min-heap is always at the top.	for extracting the min element, we remove the minimum element and swap it with the last element in the heap (the bottommost, rightmost element). Then, we bubble down this element, swapping it with one of its children until the min-heap property is restored.	This takes O(logN) time, where N is the number of nodes in the heap.				
Tries (Prefix trees)	A trie is a variant of an n-ary tree in which characters are stored at each node. Each path down the tree may represent a word. The * nodes (sometimes called "null nodes") are often used to indicate complete words.		The actual implementation of these * nodes might be a special type of child (such as a TreminatingTrieNode, which inherits from Trie node). Or, we could use just a boolean flag that terminates within the parent node.	A node in a trie could have anywhere from 1 through ALPHABET_SIZE + 1 children (or, 0 through ALPHABET_SIZE if a boolean flag is used instead of * node)		A trie is usally used to store the entire (English) language for quick prefix lookups.	While a hashtable can quickly look up whether a string is a valid word or not, it cannot tell us if a string is a prefix of a any valid word. A trie can do this very quickly.
	A trie can check if a string is a valid string in O (k) time where k is the length of the string.  In situations, when we search to prefixes repeatedly, (e.g. looking then MANY), we might pass are current node in the tree. This work child of MAN, rather than starting.		ng up M, then MA, then MAN, round a reference to the will allow us to check if Y is a				
Graphs	A tree is actually a graph but not all graphs are trees. A tree is simply a connected graph without cycles.		A graph is simply a collection of nodes with edges between (some of ) them.	Graphs can either be directed or undirected.	An uncyclic graph is one without cycles.		

There are two common ways to represent a graph:	Adjacency list: This is the most common way to represent a graph. Every vertex or node stores a list of adjacent vertices. In an undirected graph, an edge like (a,b) would be stored twice: once in a's adjacent vertices, and once in b's vertices.	The graph class is used because, unlike in a tree, you can't necessarily reach all the nodes from a single node.	An array (or a hashtable) of lists (arrays, arraylists, linkedlists, etc.) can store the adjacency list.		
	Adjacency matrix: An adjacency matrix is a NXN boolean matrix where N is the number of nodes, a true value indicates the presence of an edge from node i to j. In an undirected graph, adjacency matrix would be symmetric whereas in a directed graph, it need not be symmetric.	All the algorithms used for adjacency lists can be used for adjacency matrices, but they would be less eficient. The reason is in adjacency list, the user can easily iterate through the neighbors of a node whereas in an adjacency matrix, the user will need to iterate through all the nodes to identify a node's neighbors.			