Section VI	Big O								
	Asymptotic notations								
	O(Big O)	Describes an upper bound on time	for example: algo that prints all the values in an array: could have Big O time as O (n), O(n^2), O(n^3) or O(2^n) and many other Big O's	Upper bounds on the runtime; similar to a less- than-or-equal-to relationship	then we also say that X<=	In industry, O and theta have been put together and we have to give the tightest description of runtime			
	Omega(n)	Describes the lower bound	for example: printing the values in an array is Omega (n) as well as Omega(logn) as well as Omega(1)						
	Theta(n)	Describes the tight bound on runtime	Theta here means both O and Omega; in this example, it would be Theta(n)						
	Best Case, Worst Case and Expected Case								
	Best Case:	For example, in Quick Sort, if all the elements are equal, then quick sort will, on average, just traverse through the array once - O(N) time	Quick Sort as we know picks random element as a pivot and then swaps values in the array such that the elements less than pivot appear before elements greater than pivot this gives partial sort. then it recursively sorts the left and right sides uing same process						
	Worst Case:	The pivot could be repeatedly the biggest element in the array. If pivot is the first element in a reversely sorted array. In this cae, our recursion does not divide the array in half and recurse on other half. Instead, it justs shrinks the subarray by 1 element.	Time taken would O(N^2)						
	Expected Case:	both the above best and worst conditions would rarely happen; thus we can expect a runtime of O(nlogn)							
		etween Asymptotic notations Worst Case and Expected							

There is no particular relationship between the two concepts										
	st Case and Expected Case act	vally describe the big O or big	Thata tima for nor	tioular acception	ubarasa thasa sa	motatia natatiana	describe the upp	ar lawar and tight	haunda far tha ri	ntima
Best Case, wors	st Case and Expected Case acti	lally describe the big O or big	Theta time for par	ticular scenarios v	vnereas tnese asy	mptotic notations	describe the upp	er, lower and tign	bounds for the ru	intime
Space complexity										
Memory or space required	to create an array - if it is unidimensional, O(N) space complexity; for a 2-D array, O (N^2)									
counts too.	However, just because you have N calls does not mean it will take O(N) time: check the example on Page 41 for more details									
Drop the constants										
O(2N) is actually O(N)										
Drop the non- dominant terms										
O(N^2 + N) becomes O (N^2)										
O(N + logN) becomes O(N)										
O(5*2^N + 1000N^100) becomes O (2^N)										
$O(x!) > O(2^x) >$	$O(x^2) > O(xlogx) > O(x)$									
Multi-Parts algorithms: add versus mutiply										
Add:	Non-nested chunk of work A and B	O(A + B)	"DO THIS THEN WHEN YOU ARE ALL DONE, DO THAT"							

Multiply	Nested A and B	O(AB)	"DO THIS FOR EACH TIME YOU DO THAT"				
Amortized tim	е						
arrayList addin actually takes copying N elements in a filled array in a new array with double capacit	,	But, this copying of elements into a new array does not happen quite often infact once in every some time	Amortized time a that the worst ca every once in a happens it won't	allows to describe ase can happen while but once it thappen again for cost is amortized			
Adding X more space to an array takes additional O(X) time; thus the amortized time for each adding is O(1)							
La abl as ablas and							
logN runtimes							
Example: Binary search. We are looking for an element in a sorted array. We first compare to the midpoint. If x = middle, then w return else if x middle, we search on the left side of arra else on the righ side.	we are down to N/2 elements x and in another step to N/4 elements and so on.	The total runtime is then a matter of how many steps we can take before it becomes 1	2 <sup>k</sup> = N => k = logN with base 2	Basically, when you see a problem with logN runtime, the problem space gets halved in each step			
Recursive runtimes							
Program:	int f(int n){						
	if(n <= 1){						
	return 1}						
	return f(n -1) + f(n -1);}						
How many call in the tree?	S						
Do not count and say 2							

rec wii an at	will have ccursive calls ith a depth N and 2^N nodes the bottom lost level	More genrically, 2^0 + 2^1 + 2^2 +2^n-1 = 2^n - 1 nodes		The space complexity would still be O (n) - even though we have O(2^n) nodes in tree total, only O(n) exists at a time				
Ex	xamples and E	Exercises						
	xample 1	O(n) time as we iterate						
		through array once in each loop which are non-nested						
Ex	xample 2	O(N^2) time as we have two nested loops						
Ex	xample 3	j basically runs for N-1 steps in first iteration, N-2 steps in second iteration and so on.	1 + 2 + 3 ++ N-1 = N(N - 1)/2 ~ N^2	O(N^2)				
Ex	xample 4	For each element of array A, the inner loop goes through b iterations where b is the length of array B. Thus, time complexity is O(ab)						
Ex	xample 5	Similar to example 4, 100,000 units of work is still constant; so the run time is O(ab)						
Ex	xample 6	O(N) time as the array is iterated even if half of it (constant 1/2 can be ignored)						
Ex	xample 7	There is no established relationship between N and M , thus all but the last one are equivalent to O(N)						
Ex	xample 8	s = length of the longest string Sorting each string would take elements of the array; thus O(a array would take O(s * aloga) a would take O(s) time in additio take O(aloga); thus adding the aloga) = O(a *s (log a + log s)	O(slogs) and we do this for a a * slogs). Now, sorting the as each string comparison in to array sorting that would					
Ex	xample 9	Approach 1: for summing up the nodes in a BST, each node is exactly traversed once, thus O(N) time complexity						
		Approach 2: The number of recursive calls is 2 and the depth is logN in a BST> O (branches ^ depth) = O(2 ^ logN) where the base of logN is also 2 => time complexity = O(N) after simpllifying						

Example 10	O(root(N)) as the for loop does constant time and runs in O(root(N)) time						
Example 11	O(N) as the recursive process calls from N to N-1 to N-2 and so on until 1						
Example 12	Approach 1: We make a tree for that we branch 4 times at the root time. this gives us 4*3*2*1 leaf no string. So, total nodes would be repath with n nodes. Also, string couthe final time complexity in worst.	t, then 3 times, then 2 times des. We could say n! leaf no n * n! as each leaf node is at neatenation will also take O(	, and then 1 odes for n length tached to a n) time. Thus,				
	Approach 2: At level 6, we have nodes; at level 4 we have 6!/2! no total nodes in the tree in terms of 1/n!). Now, the term in the bracken! * e whose value is around 2.71 Thus, the time complexity would thus, time complexity: O((n+1)!)	desat level 0, we have 6!/ n can be : n!(1/0! + 1/1! + 1/ et can be defined in terms of 8. The constant e can be dr	6! nodes. so, the 2! + 1/3!+ Euler's number: opped further.				
Example 13	pattern for recursive calls: O (branches^depth) = O(2^N).	e can also get tighter ntime as O(1.6^N) if we nsider that there might be st one call instead of 2 at e bottom of call stack metimes.					
Example 14	From previous example, we dedu time. And, we have fib(1) + fib(2) 2^2 + 2^3+2^n = 2^(n+1) - 2, 1 run time is approx. 2^n	+ fib(3) +fib(n) = 2^1 +					
Example 15	Now, here in this program we are doing memoization due to which the amount of work reduces to looking up fib(i - 1) and fib(i - 2) values in memo array at each call fib(i). Thus, we are doing a constant amount of work n times in n calls, hence time complexity: O(n)						
Example 16	The runtime is the number of times we can divide n by 2 until we get down to the base case 1. As, we know the number of times we can halve n until we get 1 is O (logN)						
Additional Pro	blems						
	The for loop iterates through b, thus time complexity is O (b)						
	2 The recursive call iterates through b calls as it subtracts 1 in each iteration, thus time complexity is O(b)						

3 It does constant amount of work, thus time complexity is O(1)					
4 The variable count will eventually equal a/b. The while loop iterates through count times. Thus time complexity is O(a/b)					
5 The algorithm is actually doing a binary search to find the square root. Thus the runtime is O(logN)					
6 This is straightforward loop that stops when guess*guess > n or guess> sqrt(n); hence time complexity is O(sqrt(n))					
7 Ifa binary tree is not balanced, the max time to find an element would be the depth of the tree. The tree since it is imbalanced could be a straight list downwards and ave depth n. Thus, runtime is O(n)					
8 Without any ordering or sorting in a binary tree, we might need to traverse through all the nodes in the tree, thus the time complexity is O(n) where n is the number of nodes in the tree.					
9 The first call to appendToNew takes 1 copy. The second call takes 2 copies. The third call takes 3 copies. And so on. The total time will be sum through 1 to n, which is O(n^2)					
The runtime would be O(d) where d is the number of digits in the given number. A number with d digits can have a value upto 10^d. If n = 10^d, then d = log n. Thus, time complexity is O(log n) where the log is with base 10.					
If the length of the string is k, the inOrder or sorted, takes O(k) till of the string is c characters. Not characters and k length would be wish to construct astring length and b, thus the number of string Similarly here, that runtime wor runtime to get all the strings of k and check if they are sorted wor	ne. Also, suppose the length v, to get strings of c e O(c^k). for example, you a s with just two characters a s possible would be 2^3. Id be O(c^k). Thus, overall length with c characters				

	12	Pirst of all the runtime for merg then , for each element in a , w b - runtime would be O(a * log ( b log b + a log b).	e are doing binary search of					
Section IX	Interview Ques	tions						
Chapter 1	Arrays and Str							
Griupter 1	Hash Table	iligo						
		a data structure that maps keys cient lookup.						
	Hash Table Imp	olementation						
	Approach 1	We use an array of Linked List	s and a hash code function.					
		To insert a key ( a string or any we follow the following steps:	other datatype) and value					
		Compute the key's hashcod or long. Two different keys cou as there may be numerous key	ld have the same hashcode,					
		2. Then, we map the hash cod This could be done with somet array_length. Two different has to the same index.	hing like hash (key) %					
		3. At this index, there is a linke Store the key and value in the List to tackle collisions: you column with same hashcode or two diffindex	index. We must use a Linked uld have two different keys					
		its key, we repeat the process. Compute the hash	If it is the worst case, collisions are very high, runtime would be O(N) where N is the number of keys. And, if it is the best case, collisions are minimum, look up time would be O(1)					
	Approach 2	We can implement a look up si search tree. This gives us O(lo advantage of this approach is we no longer allocate a large a through keys in order.	ogN) lookup time. The potentially less space, since					
	ArrayList & Re	sizable Arrays						
	When you need an array-like datastructure with dynamic resizing, you should use an ArrayList.	A typical implementation is that when the array is full, the array doubles in size (in Java, the size might instead increase by 50% or another value). Each resizing takes O (n) time, but happens rarely that its amortized insertion time is O(1) only.	increase to get an array of siz N/8 ++ 2+ 1 = N. Therefore elements takes O(N) worktota	each capacity e N: N/2 + N/4 + e, inserting N I. Thus, each O(1), even				
	StringBuilder							

	Normally, concatenating n strings of x characters each would take O							
	(xn^2).							
		n reduce this complexity as it cr ring them to one string only if ne						
Chapter 2	Linked Lists							
	LinkedList is a datastructure representing a sequence of nodes.	Singly Linked List> there is a pointer to the next node	Doubly Linked List> there is a pointer to the next and previous nodes					
	constant time ac	LinkedList does not provide cess to any element of the list. through K elements to get the	Benefit of a Linked List is that one can add or remove items from the beginning of the list in constant time					
Chapter 3	Stacks and Que	eues						
	Stack uses LIFO	Operations of a stack: pop(), push(item), peek(), isEmpty()	A stack does not offer constant-time access to the ith item. However, it allows constant time adds and removes as it does not require shifting elements around.	most useful case algorithms - one temporary data of one recurses, buthem as one bac	needs to push oto a stack as ut then remove			
	Queue implements FIFO	Operations of a queue: add (item), remove(), peek(), isEmpty()	most useful case: breadth- first search and implementing a cache					
Chapter 4	Trees and Grap		P Q					
	Searching a tree is more complicated than searching any linear data structure	The worst case and the average case time may vary wildly and we must evaluate both the aspects of any problem	Tree is actually a type of graph in which cycles / loops are not possible					
Trees	In programming, The root node ha	structure composed of nodes. each tree has a root node. as zero or more children. Each ero or more children and so	The nodes may be in any order and may have any data types as values and may or may not have links back to their parent nodes.	A node is called a leaf node if it has no children.				
Trees vs. binary trees	A binary tree is a tree in which each node has upto two children. Not all trees are binary trees.	For example, a 10-ary tree representing a bunch of phone numbers is not a binary tree.						
	evry node fits a sleft descendants	tree is a binary tree in which specific ordering property: all is <= n < all right descendants. e for each node n	This inequality condition must be true for all of a node's descendants, not just its immediate children.					

Balanced vs. unbalanced tree	not neccessarily perfectly balanced but ensures O(log n) times for insert and find	Two common types of balanced trees: Red-black trees and AVL trees					
Complete binary trees		ry tree is a binary tree in which of the last level. To the extent the					
Full binary tree	each node has e is no node havin	either 2 or zero children. There g only one child					
Perfect binary tree	All interior nodes nodes are at the	s have two children and all leaf same level.	It must have exactly 2 <sup>k</sup> - 1 nodes where k is the number of levels.				
In-order traversal	"visit" the left branch, then the current node, and finally the right node	when performed on a binary search tree, it visits the nodes in ascending order.					
Pre-order traversal	"visits" the current node before its child nodes	The root is always the first node visited					
Post-order traversal	"visits" the current node after its child nodes	The root is always the last node visited					
Binary Heaps (min-heaps and max- heaps)		The root thus is the minimum element in the tree.	Two key operations: insert and extract-min				
Insert operation on min-heap	(looking left to rig We fix the tree b with its parent, u	rting at the next available spot ght on the bottommost level). y swapping the new element ntil we find an appropriate spot We essentially bubble up the	This takes O(logN) time, where N is the number of nodes in the heap.				
Extract-min operation on min-heap	The minimum element of a min-heap is always at the top.	for extracting the min element, we remove the minimum element and swap it with the last element in the heap (the bottommost, rightmost element). Then, we bubble down this element, swapping it with one of its children until the min-heap property is restored.					