Section VI	Big O					
	Asymptotic notations					
	O(Big O)	Describes an upper bound on time	for example: algo that prints all the values in an array: could have Big O time as O (n), O(n^2), O(n^3) or O(2^n) and many other Big O's	Upper bounds on the runtime; similar to a less- than-or-equal-to relationship	In industry, O and theta have been put together and we have to give the tightest description of runtime	
	Omega(n)	Describes the lower bound	for example: printing the values in an array is Omega (n) as well as Omega(logn) as well as Omega(1)			
	Theta(n)	Describes the tight bound on runtime	Theta here means both O and Omega; in this example, it would be Theta(n)			
	Best Case, Worst Case and Expected Case					
	Best Case:	For example, in Quick Sort, if all the elements are equal, then quick sort will, on average, just traverse through the array once - O(N) time	Quick Sort as we know picks random element as a pivot and then swaps values in the array such that the elements less than pivot appear before elements greater than pivot - this gives partial sort. then it recursively sorts the left and right sides uing same process			

	The pivot could be repeatedly the biggest element in the array. If pivot is the first element in a reversely sorted array. In this cae, our recursion does not divide the array in half and recurse on other half. Instead, it justs shrinks the subarray by 1 element.	Time taken would O(N^2)		
·	both the above best and worst conditions would rarely happen; thus we can expect a runtime of O(nlogn)			
Relationship ber and Best Case, Case Concepts	tween Asymptotic notations Worst Case and Expected			
There is no particular relationship between the two concepts				
Best Case, Worst Case and Expected Case actually describe the big O or big Theta time for particular scenarios whereas these asymptotic notations describe the upper, lower and tight bounds for the runtime				

Space complexity				
Memory or space required by an algorithm	to create an array - if it is unidimensional, O(N) space complexity; for a 2-D array, O (N^2)			
Stack space in recursive calls counts too. Each call adds a level tot he stack and takes up actual memory.	However, just because you have N calls does not mean it will take O(N) time: check the example on Page 41 for more details			
Dron the				
Drop the constants				
O(2N) is actually O(N)				
Drop the non- dominant terms				
O(N^2 + N) becomes O (N^2)				
O(N + logN) becomes O(N)				
O(5*2^N + 1000N^100) becomes O (2^N)				
$O(x!) > O(2^x) >$	$O(x^2) > O(x \log x) > O(x)$			

Multi-Parts algorithms: add versus mutiply					
	Non-nested chunk of work A and B	O(A + B)	"DO THIS THEN WHEN YOU ARE ALL DONE, DO THAT"		
Multiply	Nested A and B	O(AB)	"DO THIS FOR EACH TIME YOU DO THAT"		
Amortized time					
actually takes copying N elements in a	That copying might take additional O(N) time after accounting for initial O(N) time of adding the elements to the array	But, this copying of elements into a new array does not happen quite often infact once in every some time	Amortized time allows to describe that the worst case can happen every once in a while but once it happens it won't happen again for so long, that the cost is amortized		
	X + X/2 + X/4 + X/8 = 2X				
logN runtimes					

	We basically start off with N elements, after a single step, we are down to N/2 elements and in another step to N/4 elements and so on.	The total runtime is then a matter of how many steps we can take before it becomes 1	2 ^k = N => k = logN with base 2	Basically, when you see a problem with logN runtime, the problem space gets halved in each step	
Recursive					
runtimes					
Program:	int f(int n){				
	if(n <= 1){				
	return 1}				
	return f(n -1) + f(n -1);}				
How many calls in the tree?					
Do not count and say 2					
It will have recursive calls with a depth N and 2^N nodes at the bottom most level	More genrically, 2^0 + 2^1 + 2^2 +2^n-1 = 2^n - 1 nodes	O(branches^depth) where branches is the number of times each recursive call branches	The space complexity would still be O (n) - even though we have O(2^n) nodes in tree total, only O(n) exists at a time		
 	• •				
Examples and E	xercises				

Example 1	O(n) time as we iterate through array once in each loop which are non-nested				
Example 2	O(N^2) time as we have two nested loops				
Example 3	j basically runs for N-1 steps in first iteration, N-2 steps in second iteration and so on.	1 + 2 + 3 ++ N-1 = N(N - 1)/2 ~ N^2	O(N^2)		
Example 4	For each element of array A, the inner loop goes through b iterations where b is the length of array B. Thus, time complexity is O(ab)				
Example 5	Similar to example 4, 100,000 units of work is still constant; so the run time is O(ab)				
Example 6	O(N) time as the array is iterated even if half of it (constant 1/2 can be ignored)				
Example 7	There is no established relationship between N and M , thus all but the last one are equivalent to O(N)				
Example 8	s = length of the longest string; a = length of the array; Sorting each string would take O(slogs) and we do this for a elements of the array; thus O(a * slogs). Now, sorting the array would take O(s * aloga) as each string comparison would take O(s) time in addition to array sorting that would take O(aloga); thus adding the two parts: O(a * slogs + s * aloga) = O(a *s (log a + log s)				
Example 9	Approach 1: for summing up the nodes in a BST, each node is exactly traversed once, thus O(N) time complexity				

	Approach 2: The number of recursive calls is 2 and the depth is logN in a BST> O (branches ^ depth) = O(2 ^ logN) where the base of logN is also 2 => time complexity = O(N) after simpllifying				
Example 10	O(root(N)) as the for loop does constant time and runs in O(root(N)) time				
Example 11	O(N) as the recursive process calls from N to N-1 to N-2 and so on until 1				
Example 12	Approach 1: We make a tree for that we branch 4 times at the retime. this gives us 4*3*2*1 leaf string. So, total nodes would be path with n nodes. Also, string the final time complexity in wor	oot, then 3 times, then 2 times nodes. We could say n! leaf no e n * n! as each leaf node is a concatenation will also take O	s, and then 1 odes for n length ttached to a (n) time. Thus,		
	Approach 2: At level 6, we have nodes; at level 4 we have 6!/2! total nodes in the tree in terms 1/n!). Now, the term in the brace n! * e whose value is around 2. Thus, the time complexity would thus, time complexity: O((n+1)!	nodesat level 0, we have 6!/ of n can be : n!(1/0! + 1/1! + 1/0) cket can be defined in terms of .718. The constant e can be dr ld be O(n! * n) where n is due for	6! nodes. so, the /2! + 1/3!+ f Euler's number: opped further.		
Example 13	(branches^depth) = O(2^N).	We can also get tighter runtime as O(1.6^N) if we consider that there might be just one call instead of 2 at the bottom of call stack sometimes.			
Example 14	From previous example, we de time. And, we have fib(1) + fib($2^2 + 2^3 \dots + 2^n = 2^n + 2^n$ run time is approx. 2^n	2) + $fib(3)$ + $fib(n)$ = 2^1 +			

Example 15	Now, here in this program we are doing memoization due to which the amount of work reduces to looking up fib(i - 1) and fib(i - 2) values in memo array at each call fib(i). Thus, we are doing a constant amount of work n times in n calls, hence time complexity: O(n)			
Example 16	The runtime is the number of times we can divide n by 2 until we get down to the base case 1. As, we know the number of times we can halve n until we get 1 is O (logN)			
Additional Prob	lems			
	The for loop iterates through b, thus time complexity is O (b)			
2	The recursive call iterates through b calls as it subtracts 1 in each iteration, thus time complexity is O(b)			
3	It does constant amount of work, thus time complexity is O(1)			
4	The variable count will eventually equal a/b. The while loop iterates through count times. Thus time complexity is O(a/b)			
5	The algorithm is actually doing a binary search to find the square root. Thus the runtime is O(logN)			

6	This is straightforward loop that stops when guess*guess > n or guess> sqrt(n); hence time complexity is O(sqrt(n))			
7	Ifa binary tree is not balanced, the max time to find an element would be the depth of the tree. The tree since it is imbalanced could be a straight list downwards and ave depth n. Thus, runtime is O(n)			
8	Without any ordering or sorting in a binary tree, we might need to traverse through all the nodes in the tree, thus the time complexity is O(n) where n is the number of nodes in the tree.			
9	The first call to appendToNew takes 1 copy. The second call takes 2 copies. The third call takes 3 copies. And so on. The total time will be sum through 1 to n, which is O(n^2)			
10	The runtime would be O(d) where d is the number of digits in the given number. A number with d digits can have a value upto 10^d. If n = 10^d, then d = log n. Thus, time complexity is O(log n) where the log is with base 10.			

	11	If the length of the string is k, t inOrder or sorted, takes O(k) of the string is c characters. No characters and k length would wish to construct astring length and b, thus the number of string Similarly here, that runtime woruntime to get all the strings of and check if they are sorted we	time. Also, suppose the length ow, to get strings of c be O(c^k). for example, you a 3 with just two characters a gs possible would be 2^3. buld be O(c^k). Thus, overall k length with c characters			
	12	Print of all the runtime for mergethen, for each element in a, wb-runtime would be O(a * log (blog b + a log b).	ve are doing binary search of			
Section IX	Interview Ques	tions				
Chapter 1	Arrays and Str					
	Hash Table					
	A hash table is a data structure that maps keys to values for efficient lookup.					
	Hash Table Implementation					
	Approach 1	We use an array of Linked List	s and a hash code function.			
		To insert a key (a string or any we follow the following steps:	other datatype) and value			
		or long. Two different keys cou	I. Compute the key's hashcode, which will usually be an itn or long. Two different keys could have the same hashcode, as there may be numerous keys but finite number of ints.			
		This could be done with some	2. Then, we map the hash code to an index in the array. This could be done with something like hash (key) % array_length. Two different hashcodes could of course map			
		3. At this index, there is a linked list of keys and values. Store the key and value in the index. We must use a Linked List to tackle collisions: you could have two different keys with same hashcode or two different hashcodes but same index				

		To retrieve the value pair by its key, we repeat the process. Compute the hash code by key, and then index by hashcode. Then, search through the Linked List for the value and its key.	If it is the worst case, collisions are very high, runtime would be O(N) where N is the number of keys. And, if it is the best case, collisions are minimum, look up time would be O(1)			
	Approach 2	We can implement a look up s search tree. This gives us O(l advantage of this approach is we no longer allocate a large a through keys in order.	ogN) lookup time. The potentially less space, since			
	ArrayList & Res	sizable Arrays				
	When you need an array-like datastructure with dynamic resizing, you should use an ArrayList.	that when the array is full, the	We can work backwards to comany elements we copied at eincrease to get an array of size N/8 ++ 2+ 1 = N. Therefore elements takes O(N) worktota insertion on an average takes though some insertions take Coworst case.	each capacity e N: N/2 + N/4 + , inserting N l. Thus, each O(1), even		
	StringBuilder					
	Normally, concatenating n strings of x characters each would take O (xn^2).					
		n reduce this complexity as it cre ing them to one string only if ne				
Oh amt = == 0	Limbort Links					
Chapter 2	Linked Lists		D. H. Palader C. C.			
	LinkedList is a datastructure representing a sequence of nodes.	Singly Linked List> there is a pointer to the next node	Doubly Linked List> there is a pointer to the next and previous nodes			

	,		Benefit of a Linked List is that one can add or remove items from the beginning of the list in constant time			
Chapter 3	Stacks and Queues					
			A stack does not offer constant-time access to the ith item. However, it allows constant time adds and removes as it does not require shifting elements around.	most useful case: recursive algorithms - one needs to push temporary data oto a stack as one recurses, but then remove them as one backtracks		
	Queue implements FIFO	Operations of a queue: add (item), remove(), peek(), isEmpty()	most useful case: breadth- first search and implementing a cache			
Chapter 4	Trees and Graphs					
	Searching a tree is more complicated than searching any linear data structure	The worst case and the average case time may vary wildly and we must evaluate both the aspects of any problem	Tree is actually a type of graph in which cycles / loops are not possible			
Trees	In programming, The root node ha	structure composed of nodes. each tree has a root node. as zero or more children. Each ero or more children and so	The nodes may be in any order and may have any data types as values and may or may not have links back to their parent nodes.	A node is called a leaf node if it has no children.		
Trees vs. binary trees	A binary tree is a tree in which each node has upto two children. Not all trees are binary trees.	For example, a 10-ary tree representing a bunch of phone numbers is not a binary tree.				
Binary Tree vs. Binary Search Tree	A binary search tree is a binary tree in which		This inequality condition must be true for all of a node's descendants, not just its immediate children.			

Balanced vs. unbalanced tree	not neccessarily perfectly balanced but ensures O(log n) times for insert and find	Two common types of balanced trees: Red-black trees and AVL trees			
Complete binary trees		y tree is a binary tree in which on the last level. To the extent the l			
Full binary tree	each node has e is no node having	ither 2 or zero children. There g only one child			
Perfect binary tree	All interior nodes nodes are at the	have two children and all leaf same level.	It must have exactly 2 ^k - 1 nodes where k is the number of levels.		
In-order traversal	"visit" the left branch, then the current node, and finally the right node	when performed on a binary search tree, it visits the nodes in ascending order.			
Pre-order traversal	"visits" the current node before its child nodes	The root is always the first node visited			
Post-order traversal	"visits" the current node after its child nodes	The root is always the last node visited			
Binary Heaps (min-heaps and max- heaps)	A min heap is a complete binary tree where each node is smaller than its children.	The root thus is the minimum element in the tree.	Two key operations: insert and extract-min		
Insert operation on min-heap	(looking left to rig We fix the tree by with its parent, un	ting at the next available spot ght on the bottommost level). y swapping the new element ntil we find an appropriate spot We essentially bubble up the	This takes O(logN) time, where N is the number of nodes in the heap.		

Extract-min operation on min-heap	The minimum element of a min-heap is always at the top.	for extracting the min element, we remove the minimum element and swap it with the last element in the heap (the bottommost, rightmost element). Then, we bubble down this element, swapping it with one of its children until the min-heap property is restored.	This takes O(logN) time, where N is the number of nodes in the heap.				
Tries (Prefix trees)	characters are s down the tree m nodes (sometim	t of an n-ary tree in which stored at each node. Each path ay represent a word. The * es called "null nodes") are dicate complete words.	The actual implementation of these * nodes might be a special type of child (such as a TreminatingTrieNode, which inherits from Trie node). Or, we could use just a boolean flag that terminates within the parent node.	A node in a trie could have anywhere from 1 through ALPHABET_SIZE + 1 children (or, 0 through ALPHABET_SIZE if a boolean flag is used instead of * node)		A trie is usally used to store the entire (English) language for quick prefix lookups.	While a hashtable can quickly look up whether a string is a valid word or not, it cannot tell us if a string is a prefix of a any valid word. A trie can do this very quickly.
	if a string is a valid string in O	In situations, when we search prefixes repeatedly, (e.g. looking then MANY), we might pass an current node in the tree. This work child of MAN, rather than starting	ng up M, then MA, then MAN, round a reference to the will allow us to check if Y is a				
Graphs		a graph but not all graphs are imply a connected graph	A graph is simply a collection of nodes with edges between (some of) them.	Graphs can either be directed or undirected.	An uncyclic graph is one without cycles.		

There are common to represe graph:	ways most common way to	The graph class is used because, unlike in a tree, you can't necessarily reach all the nodes from a single node.	An array (or a hashtable) of lists (arrays, arraylists, linkedlists, etc.) can store the adjacency list.		
	Adjacency matrix: An adjacency matrix is a NXN boolean matrix where N is the number of nodes, a true value indicates the presence of an edge from node i to j. In an undirected graph, adjacency matrix would be symmetric whereas in a directed graph, it need not be symmetric.	through all the nodes to identineighbors.	es, but they ason is in asily iterate de whereas in an I need to iterate		
Two way search a		Breadth-first search: we start at the root and explore each neighbor before going to any children. To find the shortest path or any path between two nodes, BFS is simpler.	DFS is recursive whereas a BFS uses a queue.		
	Pre-order and other forms of traversals are an example of DFS. The key difference is we must check if a node has been visited or else we might get stuck in an infinite loop.				
Bidirection search	destination node. It operates BFS, one from each node. W have found a path(formed by	by running two simultaneous hen their searches collide, we merging two paths). If the forward from s and backwards			

	BFS vs. bidirectional search	BFS is the single search from s to t that collides after four levels whereas bidirectional search is actually two searches (one from s and another from t) that collides after four levels total (two levels each)	Basically, if every node has at most k adjacent nodes and the shortest path from node s to node t has length d, then in BFS, time complexity would be O(k^d) as it would be searching k nodes at each level whereas in bidirectional graph, time complexity would be O (k^d/2) because they would collide midway. Hence it is more time efficient.		
Chapter 5	Bit Manipulatio	n			
	Bit Manipulatio	n By Hand			
	Question	Calculation			
	0110 + 0010	1000			
	0011 * 0101	1111			
	0110 + 0110	1100	Equivalent to 0110 * 2 which is equivalent to shifting 0110 left by 1		
	0011 + 0010	101			
	0011 * 0011	1001			
	0100 * 0011	1100	0100 is 4 in binary numbers and multiplying by 4 is just shifting left by 2 places		
	0110 - 0011	0011			
	1101 >> 2	0011	You shift all the bits and the extra bits fall off the end. So your bits are marching right and zeros march in from the left to take their places		
	1100 ^ (~1101)	1111	it is a^(~a). if you XOR a bit with its own negated value, the result is 1		
	1000 - 0110	0010			
	1101 ^ 0101	1000			

1011 & (~0 << 2)	1011 & 1100 = 1000	~0 is a sequence of 1's, so ~0 << 2 is 1100.			
Bit Facts and 1	ricks				
	following expressions:				
x ^ 0s = x	x & 0s = 0s	x 0s = x			
x ^ 1s = ~x	x & 1s = x	x 1s = 1s			
x ^ x = 0s	x & x = x	x x = x			
Two's complements	nent Representation and pers				
whereas a negathe 2s complem	er is represented as itself tive number is represented by ent of its absolute value with a ndicating that its a negative	For an N-bit number, the two's complement is taken with respect to 2^N.			
In other words, the binary representation of -K as a N- bit number is concat(1, 2^(N- 1) - K)	For example, -3 in 4 bits: concat(1, 2^3 - 3) = concat(1, 5 which is 101) = 1101	Another way is first onvert the binary representation of the negative number, for example 3 is 011, thus inverting it would be 100. Add 1 to it to get 101 and then prepend it with the sign bit = 1101			
Some common	representations:	The absolute values of the integers on the left and right side always sum to 2 ³	The values on the left and the right are identical other than the sign bit		
Positive values	Representation	Negative values	Representation		
7	0111	-1	1111		
6	0110	-2	1110		
5	0101	-3	1101		
4	0100	-4	1100		
3	0011	-5	1011		
· · · · · · · · · · · · · · · · · · ·	·	1			

2	0010	-6	1010		
1	0001	-7	1001		
0	0000		1001		
0	0000				
Arithmetic vers	una Lagiaal Shift				
	sus Logical Shift				
Two types of right shift operations: Arithmetic shift (>>) which is essentially divide by 2 and logical shift (>>>)	In a logical shift, we shift the bits and put a 0 in the sign / most significant bit. For example, -75 i.e. 10110101 >>> 1 = 01011010 i.e. 90	In an arithmetic shift, we shift the values to the right but fill in the new bits with the value of the sign bit. For example, -75 i.e. 10110101 >> 1 = 11011010 (-38)			
Common Bit Ta	asks And Setting				
1. Get Bit					
00010000. By pe	fts 1 over by i bits, creating a va- erforming AND with the num, was compare that to 0. If the new va Otherwise it is 0.	e clear all other bits but the bit			
boolean getBit(ir	nt num, int i){				
return ((num & (1<< i) != 0);}				
2. Set Bit					
operation with th	ver i bits, creating a value like 0 ne given num, only the value at ame as the other bits of the ma	i bit will change and the rest			
int setBit(int num	n, int i){				
return num (1<	<i);}< td=""><td></td><td></td><td></td><td></td></i);}<>				
3. ClearBit					
number like 1110	erates in almost the reverse of solution of solutions and solutions of solutions are solutions. This clears the solutions of solutions are solutions.	f it (00010000) and negating			

int clearBit(int num, int i){			
int mask = ~(1< <i);< td=""><td></td><td></td><td></td></i);<>			
return num & mask;}			
To clear all the bits from the most significant bit thro create a mask with a 1 at ith bit (1 << i). Then, we s gives the sequence of zeros followed by i ones. We with this mask to leave just the last i bits.	ubtract 1 from it, which		
int clearBitMSBThroughI(int num, int i){			
int mask = (1< <i) -="" 1;<="" td=""><td></td><td></td><td></td></i)>			
return num & mask;}			
To clear all bits from i through 0 (inclusive), we take (which is -1) and shift it left by i + 1 bits. This gives if ollowed by i+1 zeroes			
int clearBitsIThrough0(int num, int i){			
int mask = (-1 << (i+1));			
return num & mask;}			