

## Computer Problem Solution

- a) Using the training data in **TrainingSamplesDCT8.mat**, what are reasonable estimates for the prior probabilities?

**Solution:**

Two priors probabilities,  $P_Y(\text{cheetah})$  and  $P_Y(\text{grass})$ , could be estimated based on the number of vectors in the training set. The estimation of  $P_Y(\text{cheetah})$  and  $P_Y(\text{grass})$  are:

$$P_Y(\text{cheetah}) = N_{FG}/(N_{FG} + N_{BG}) = 0.1919 \quad (1)$$

$$P_Y(\text{grass}) = N_{BG}/(N_{FG} + N_{BG}) = 0.8081 \quad (2)$$

where

$N_{BG}$  is the number of vectors in matrix **TrainsampleDCT\_BG**

$N_{FG}$  is the number of vectors in matrix **TrainsampleDCT\_FG**

- b) Using the training data in **TrainingSamplesDCT8.mat**, compute and plot the index histograms  $P_{X|Y}(x|\text{cheetah})$  and  $P_{X|Y}(x|\text{grass})$ .

**Solution:**

According to training data, the frequency histograms is the following picture:

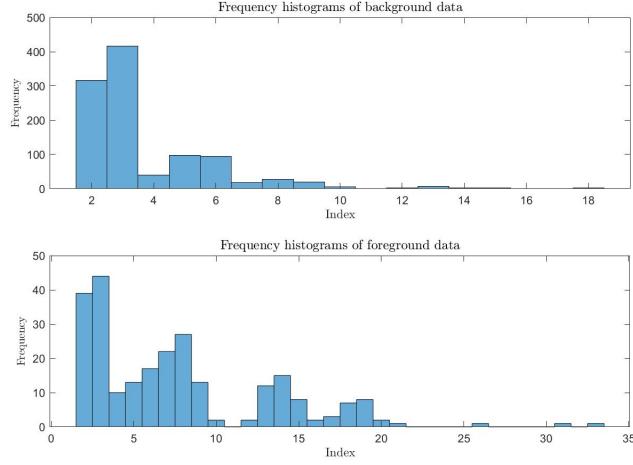


Figure 1: Frequency histograms

The index histograms of  $P_{X|Y}(x|\text{cheetah})$  and  $P_{X|Y}(x|\text{grass})$  is showed as following:

- c) For each block in the image **cheetah.bmp**, compute the feature X (index of the DCT coefficient with 2<sup>nd</sup> greatest energy). Compute the state variable Y using the minimum probability of error rule based on the probabilities obtained in a) and b). Store the state

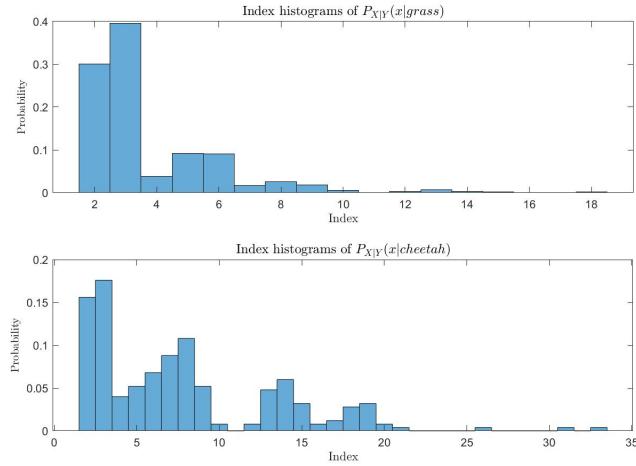


Figure 2: Index histograms

in an array A. Using the commands `imagedesc` and `colormap(gray(255))` create a picture of that array.

**Solution:**

Given a 8\*8 block from the image `cheetah.bmp`, we can easily compute an array of 8\*8 frequency coefficients by using function `dct2` on Matlab. Feature X would be index of the 2<sup>nd</sup> greatest DCT coefficient. Given  $X = x$  in one block, according to the minimum probability of error rule, we can pick state of cheetah if:

$$\frac{P_{X|Y}(x|cheetah)}{P_{X|Y}(x|grass)} > T = \frac{P_Y(grass)}{P_Y(cheetah)} \quad (3)$$

where

$P_{X|Y}(x|cheetah)$  and  $P_{X|Y}(x|grass)$  are the estimation we get from training data.

$P_Y(cheetah)$  and  $P_Y(grass)$  are the estimation we get from training data.

$T$  is the threshold.

Then we mask the top left corner of the 8\*8 block as 1, regarding this pixel belongs to cheetah. Otherwise, we mask 0. By using a sliding window that moves by one pixel at each step, finally we get a array A containing the mask indicates which blocks contain grass and which contain the cheetah.

- d) The array A contains a mask that indicates which blocks contain grass and which contain the cheetah. Compare it with the ground truth provided in image `cheetah mask.bmp` (shown below on the right) and compute the probability of error of your algorithm.

**Solution:**

The comparision between ground truth and picture generated from array A is showed as

following:

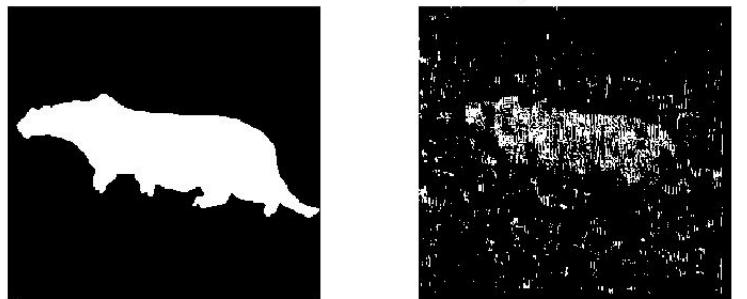


Figure 3: Comparision

The probabilities of error is 16.90%, as showed in the figure above.

## Appendix

The following is the Matlab code.

```
1 clear all
2 %%
3 %Training
4 %Read the TrainingSamplesDCT_8.mat file
5 load('dataset/TrainingSamplesDCT_8.mat');
6 %Save TrainsampleDCT_BG and TrainsampleDCT_FG in temporary value
7 train_BG = TrainsampleDCT_BG;
8 train_FG = TrainsampleDCT_FG;
9
10 %Find the second largest value in each row of matrix train_BG
11 [MBG,NBG] = max(train_BG,[],2);
12 train_BG(bsxfun(@eq, train_BG , MBG)) = -1; % Set the largest
value in each row to -inf
```

```
13 [M_BG,N_BG] = max(train_BG,[],2);  
14  
15 %Find the second largest value in each row of matrix train_FG  
16 [M_FG,N_FG] = max(train_FG,[],2);  
17 train_FG(bsxfun(@eq, train_FG, M_FG)) = -1; % Set the largest  
    value in each row to -inF  
18 [M_FG,N_FG] = max(train_FG,[],2);  
19  
20 %Plot the frequency histogram  
21 subplot(2,1,1);  
22 h1 = histogram(N_BG);  
23 ylim([0, 500]);  
24 ylabel('Frequency', 'interpreter', 'latex', 'FontSize', 10);  
25 xlabel('Index', 'interpreter', 'latex');  
26 title({['Frequency histograms of background data']}, 'Fontsize',12,  
    'interpreter', 'latex');  
27 subplot(2,1,2);  
28 h2 = histogram(N_FG);  
29 ylim([0, 50]);  
30 ylabel('Frequency', 'interpreter', 'latex', 'FontSize', 10);  
31 xlabel('Index', 'interpreter', 'latex');  
32 title({['Frequency histograms of foreground data']}, 'Fontsize',12,  
    'interpreter', 'latex');  
33 %Save the statistic data  
34 F_x_BG = zeros(1,64);  
35 F_x_BG(min(N_BG):max(N_BG)) = h1.Values;  
36 F_x_FG = zeros(1,64);  
37 F_x_FG(min(N_FG):max(N_FG)) = h2.Values;  
38 %Save the histogram figure  
39 set(gcf, 'Position',[400,100,900,600]);  
40 saveas(gcf, ['Images/histograms1.jpg']);  
41 close(gcf);  
42  
43 %Calculate the estimation of class-conditionals for two classes  
    and priors probabilities  
44 P_x_BG = F_x_BG ./ sum(F_x_BG);  
45 P_x_FG = F_x_FG ./ sum(F_x_FG);  
46 P_BG = size(train_BG,1) / (size(train_BG,1) + size(train_FG,1));  
47 P_FG = size(train_FG,1) / (size(train_BG,1) + size(train_FG,1));  
48  
49 % %Plot the index histogram  
50 subplot(2,1,1);
```

```
51 h1 = histogram(N_BG, 'Normalization', 'pdf');
52 ylim([0, 0.4]);
53 ylabel('Probability', 'interpreter', 'latex', 'FontSize', 10);
54 xlabel('Index', 'interpreter', 'latex');
55 title({{'Index histograms of $$P_{X|Y}(x| grass)$$'}}, 'Fontsize',
      ,12, 'interpreter', 'latex');
56 subplot(2,1,2);
57 h2 = histogram(N_FG, 'Normalization', 'pdf');
58 ylim([0, 0.2]);
59 ylabel('Probability', 'interpreter', 'latex', 'FontSize', 10);
60 xlabel('Index', 'interpreter', 'latex');
61 title({{'Index histograms of $$P_{X|Y}(x| cheetah)$$'}}, 'Fontsize',
      ,12, 'interpreter', 'latex');
62 %Save the histogram figure
63 set(gcf, 'Position', [400,100,900,600]);
64 saveas(gcf, ['Images/histograms2.jpg']);
65 close(gcf);
66
67 %Read original image
68 I = imread('dataset/cheetah.bmp');
69 I = im2double(I);
70 %Define the loop numbers
71 loop_row = size(I,1) - 8 + 1;
72 loop_column = size(I,2) - 8 + 1;
73
74 mask = zeros(size(I));
75 position_ref = load('dataset/Zig-Zag Pattern.txt');
76 T = P_BG / P_FG; % Caculate the threshold
77
78 for i=1:1:loop_row
79     for j=1:1:loop_column
80         block = I(i:i+7,j:j+7);
81         DCT_block = dct2(block);
82         DCT_block = abs(DCT_block);
83         [x,y] = find(DCT_block==max(DCT_block(:))); % Find the
               largest coefficient
84         DCT_block(x,y) = -1; % Set the largest value as -1
85         [x,y] = find(DCT_block==max(DCT_block(:))); % Find the
               second largest coefficient and its position
86         feature = position_ref(x,y) + 1;
87         %Decide the binary mask
```

```
88 %           %Before decide the mask, we should caluate two class-
89 %           conditionals
90 %           P_FG_Decision = P_x_FG(1,feature) * P_FG / (P_x_FG(1,
91 %           feature)* P_FG + P_x_BG(1,feature) * P_BG);
92 %           P_BG_Decision = P_x_BG(1,feature) * P_BG / (P_x_FG(1,
93 %           feature)* P_FG + P_x_BG(1,feature) * P_BG);
94 %           if P_x_FG(1,feature)/P_x_BG(1,feature) > T
95 %               mask(i,j) = 1;
96 %           end
97 %       end
98 %       subplot(1,2,1)
99 %       I = imread('dataset/cheetah_mask.bmp');
100 %       I = im2double(I);
101 %       imshow(I);
102 %       subplot(1,2,2)
103 %       imshow(mask);
104 %       %Calculate the probability of error
105 %       error = length(find((mask-I)^=0)) / (size(I,1) * size(I,2));
106 %       title({['Probability of error is ',num2str(error*100,'%.2f'), '%',
107 %           ]}, 'FontSize', 12, 'interpreter', 'latex');
108 %       %set(gcf, 'Position', [900,600]);
109 %       saveas(gcf, ['Images/segmentation.jpg']);
110 %       close(gcf);
```