```
\begin{array}{ll} Mcons_{\alpha} & : M\alpha \\ Mcons_{\alpha}^{st} & : (\sigma \rightarrow \alpha \sigma) \\ Mcons_{\alpha}^{res} & : (\alpha | \epsilon) \\ Mcons_{\alpha}^{prs} & : (\sigma \rightarrow (\alpha | \epsilon) \times \sigma) \times \sigma) \end{array}
```

 $try^{prs}\ k\ err\ pm = lift^{st}(lift^{st}(try^{res}k(\lambda e_1.try^{res}(>>=)^{id}(\lambda e_2.fail^{prs}(e_1+e_2)))err))pm: (\alpha \to M\beta) \to (\epsilon \to M\beta) \to Mcons_{\alpha}^{prs} \to Mcons_{\beta}^{prs})$ 

$$\frac{try^{res}: (\alpha \rightarrow M\beta) \rightarrow (\epsilon \rightarrow M\beta) \rightarrow Mcons_{\alpha}^{res} \rightarrow Mcons_{\beta}^{res}}{try^{res}(>>=)^{id}: (\alpha \rightarrow M\beta)} \underbrace{\begin{array}{c} fail^{prs}: \epsilon \rightarrow Mcons_{\alpha}^{prs} & \frac{e_1: \epsilon - e_2: \epsilon}{e_1 + e_2: \epsilon} \\ \hline fail^{prs}(e_1 + e_2) : Mcons_{\alpha}^{prs} & \frac{try^{res}(>>=)^{id}: (\epsilon \rightarrow M\beta) \rightarrow Mcons_{\alpha}^{res} \rightarrow Mcons_{\beta}^{res}}{\lambda e_2. fail^{prs}(e_1 + e_2): \epsilon \rightarrow Mcons_{\alpha}^{prs}} \\ \hline \\ \hline fry^{res}(>>=)^{id}: (\lambda e_2. fail^{prs}(e_1 + e_2)) : Mcons_{\alpha}^{res} \rightarrow Mcons_{\beta}^{res} \\ \hline \\ \lambda e_1. try^{res}(>>=)^{id}: (\lambda e_2. fail^{prs}(e_1 + e_2)) : \epsilon \rightarrow Mcons_{\alpha}^{res} \rightarrow Mcons_{\beta}^{res} \\ \hline \end{array}$$

$$\frac{try^{res}: (\alpha \to M\beta) \to (\epsilon \to M\beta) \to Mcons_{\alpha}^{res} \to Mcons_{\beta}^{res} \quad k: (\alpha \to M\beta)}{try^{res}k: (\epsilon \to M\beta) \to Mcons_{\alpha}^{res} \to Mcons_{\beta}^{res}} \qquad \lambda e_1.try^{res}(>>=)^{id} \left(\lambda e_2.fail^{prs}(e_1 + e_2)\right): \epsilon \to Mcons_{\alpha}^{res} \to Mcons_{\beta}^{res}$$

$$\text{Contradiction: application of } try^{res}k \text{ expects } (\epsilon \to M\beta) \text{ but got } (\epsilon \to Mcons_{\alpha}^{res} \to Mcons_{\beta}^{res})$$

```
try^{prs}\ k\ err\ pm = lift^{st}(lift^{st\_ctxt}(try^{res}k(\lambda e_1.try^{res}return^{id}(\lambda e_2.fail^{prs}(e_1+e_2))err)))pm: (\alpha \rightarrow Mcons^{prs}_{\beta}) \rightarrow (\epsilon \rightarrow Mcons^{prs}_{\beta}) \rightarrow Mcons^{prs}_{\beta}) \rightarrow (\epsilon \rightarrow M
```

$$\frac{try^{res}:(\alpha\rightarrow Mcons_{\beta}^{res})\rightarrow(\epsilon\rightarrow Mcons_{\beta}^{res})\rightarrow Mcons_{\alpha}^{res}\rightarrow Mcons_{\alpha}^{res}}{try^{res}return^{id}:(\epsilon\rightarrow Mcons_{\beta}^{res})\rightarrow Mcons_{\alpha}^{res}\rightarrow Mcons_{\beta}^{res}} - return^{id}:(\alpha\rightarrow Mcons_{\beta}^{res})}{try^{res}return^{id}:(\epsilon\rightarrow Mcons_{\beta}^{res})\rightarrow Mcons_{\alpha}^{res}\rightarrow Mcons_{\beta}^{res}} - Mcons_{\beta}^{res}} - return^{id}:(\alpha\rightarrow Mcons_{\beta}^{res})\rightarrow Mcons_{\alpha}^{res}\rightarrow Mcons_{\beta}^{res}} - return^{id}(\lambda e_{2}.fail^{prs}(e_{1}+e_{2}):Kons_{\beta}^{res})} - return^{id}(\lambda e_{2}.fail^{prs}(e_{1}+e_{2})):Mcons_{\alpha}^{res}\rightarrow Mcons_{\beta}^{res}} - return^{id}(\lambda e_{2}.fail^{prs}(e_{1}+e_{2})):Mcons_{\beta}^{res}\rightarrow Mcons_{\beta}^{res} - r$$