# Injecting Logical Background Knowledge into Embeddings for Relation Extraction

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※ 図表はすべて、論文および論文著者の作成したスライドからの引用です

#### Motivation

Problem: Relation Extraction [Riedel+ 13]

**Research Questions** 

Notation

Injecting Logic into Factorization (Proposed Method)

**MF: Matrix Factorization** 

Pre: Pre-Factorization Inference

Joint: Joint Optimization

#### **Experiments**

Settings

Extract Background Knowledge

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**Problem: Relation Extraction** 

[Riedel+ 13] やりたいこと

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### **Problem: Relation Extraction**

- ideitifying relations between named entities
- · motivation:

#### Freebase is incomplete

- Missing Facts: placeOfBirth attribute is missing for 71% of the people (Dong et al., 2014)
- Missing Entities: Contains no information about UCL Machine Reading Lab
- Missing Relations: May contain profAt(John Shawe-Taylor, UCL) but not givesLecturesAt(John Shawe-Taylor, UCL)
- · Machine reading and reasoning to the rescue!

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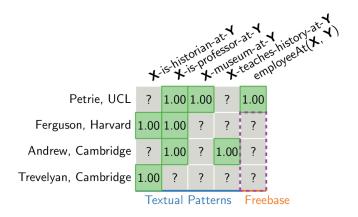
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#### Experiments

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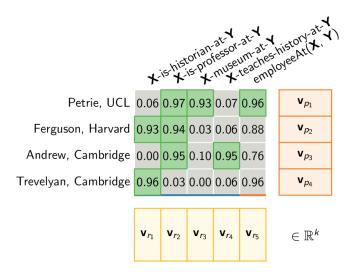
Extract Background Knowledge

## [Riedel+ 13]



- rows: entity-pairs of interest
- cols: textual patterns + Freebase relations

## [Riedel+ 13]



matrix Factorization = low-rank embedding

## Approach 1: Matrix Factorization (Low-rank Embedding)

- ✓ generalization
- ✓ tractable (computation is easy)
- hard to fix mistakes
- data sparsity

## Approach 2: Logical Inference (Rule-based)

- easy to modify and improve
- ✓ data sparsity
- easy to fix mistakes
- ✗ generalization
- ✗ intractable (e.g. Markov Logic Networks)

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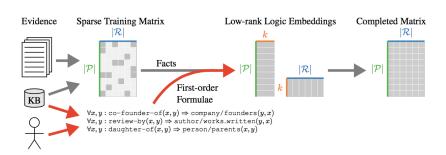
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## やりたいこと

• matrix factorization (low-rank embedding) に logical inference を組み込む



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## **Research Questions**

- How to inject logical background knowledge into embedding?
- Does injection of logic formulae into the embeddings of entity-pairs and lelations provide any *benefits*?
  - 行列分解に FOL で書かれた知識を導入することで どの程度予測精度が向上するか?
  - データの疎性に対して頑健か?
  - 「ならば」の非対称性を捉えた学習になっているか?

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## **Notation [1]**

- $\langle constant \rangle ::= e_i, e_j \in \mathcal{E}$ 
  - · named entities
  - e.g. Nolan
- $\langle predicate \rangle ::= r_m \in \mathcal{R}$ 
  - binary relations between the entities
  - 1. textual patterns (e.g. #2-co-founder-of-#1)
  - 2. Freebase relations (e.g. company/founders)
- \langle term \rangle ::= \langle constant \rangle | \langle varriable \rangle
  - using <u>function-free</u> first-order logic
  - no function symbols

## **Notation [2]**

- $\langle \text{ground atom} \rangle ::= r_m(e_i, e_j)$ 
  - predicates applied to constants
  - e.g. directorOf(NoLAN, INTERSTELLAR)
- $\mathbf{w} = \{r_m(e_i, e_j)\}$ : possible world
  - a set of ground atoms
  - = training data

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## **MF: Matrix Factorization**

- $\{0,1\}^{|\mathcal{P}|\times|\mathcal{R}|}$  の行列を、 $\mathbb{R}^{|\mathcal{P}|\times k}$  の行列と  $\mathbb{R}^{k\times|\mathcal{R}|}$  の行列の 積に分解する
- · training data
  - $w = \{r_m(e_i, e_j)\}$ : possible world
- model to learn
  - $V = \left\{ v_{(e_i, e_j)} \right\} \cup \left\{ v_{r_m} \right\}$ : model
  - $\mathbf{v}_{(e_i,e_i)} \in \mathbb{R}^k$ : entity pair  $(e_i,e_j)$  のベクトル表現
  - $v_{r_m} \in \mathbb{R}^k$ : relation  $r_m$  のベクトル表現
- · objective function

$$p(\boldsymbol{w}|\boldsymbol{V}) = \prod_{r_m(e_i,e_j) \in \boldsymbol{W}} \sigma(\boldsymbol{v}_{r_m} \cdot \boldsymbol{v}_{(e_i,e_j)}) \prod_{r_m(e_i,e_j) \notin \boldsymbol{W}} \left(1 - \sigma(\boldsymbol{v}_{r_m} \cdot \boldsymbol{v}_{(e_i,e_j)})\right)$$

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## **Pre: Pre-Factorization Inference**

- 1. トレーニングデータを,logical formulae に従って拡充
  - logical formula: e.g.  $\forall x, y : r_s(x, y) \implies r_t(x, y)$
- 2. 行列分解

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## **Joint: Joint Optimization**

- F
- a logical formula
- 38
- a training set of logical formulae
- 1. ground atoms (facts)
- 2. logical background knowledge

## **Objective Function**

$$\min_{\mathbf{V}} \left( \sum_{\mathcal{F} \in \mathfrak{F}} \mathcal{L}([\mathcal{F}]) + \lambda \sum_{\mathbf{v} \in \mathbf{V}} \|\mathbf{v}\|_{2}^{2} \right)$$

- $[\mathcal{F}] := p(\mathcal{F}|V)$ 
  - the marginal probability that the formula  $\ensuremath{\mathcal{F}}$  is true under the model
  - ・論文ではp(w|V)と記載
- $\mathcal{L}([\mathcal{F}]) := -\log([\mathcal{F}])$

optimize using AdaGrad  $\rightarrow$  We need to calculate

- the marginal probabilities  $[\mathcal{F}]$
- the gradients of the losses  $\partial \mathcal{L}([\mathcal{F}])/\partial v$

for every  $\mathcal{F} \in \mathfrak{F}$ 

## **Ground Atom**

- if  $\mathcal{F} = r_m(e_i, e_j)$  then
- $[\mathcal{F}] = \sigma(v_{r_m} \cdot v_{(e_i, e_j)})$

$$\partial[\mathcal{F}]/\partial \mathbf{v}_{(e_i,e_j)} = [\mathcal{F}](1 - [\mathcal{F}])\mathbf{v}_{r_m}$$
 (2)

$$\partial[\mathcal{F}]/\partial \mathbf{v}_{r_m} = [\mathcal{F}](1 - [\mathcal{F}])\mathbf{v}_{(e_i, e_j)}$$
(3)

$$\partial \mathcal{L}([\mathcal{F}])/\partial \mathbf{v}_{(e_i,e_j)} = -[\mathcal{F}]^{-1}\partial [\mathcal{F}]/\partial \mathbf{v}_{(e_i,e_j)}$$
 (4)

$$\partial \mathcal{L}([\mathcal{F}])/\partial \mathbf{v}_{r_m} = -[\mathcal{F}]^{-1}\partial [\mathcal{F}]/\partial \mathbf{v}_{r_m}.$$
 (5)

## **Logical "And" (A Set of Ground Atoms)**

- $[\mathcal{A} \land \mathcal{B}] = [\mathcal{A}][\mathcal{B}]$ 
  - provided both formula concern non-overlapping sets of ground atoms
  - 重なりがある場合は互いに素な集合に分ければよい
- if  $\mathcal{F} = \mathcal{F}_1 \wedge \cdots \wedge \mathcal{F}_n$  then
  - $[\mathcal{F}] = \prod_{\mathcal{F}_i \in \mathcal{F}} [\mathcal{F}_i]$
  - $\mathcal{L}([\mathcal{F}]) = \sum_{\mathcal{F}_i \in \mathcal{F}} \mathcal{L}([\mathcal{F}_i])$
- 以後.
  - 論理式=論理式が満たすべき ground atoms の集合
  - ・モデル V に対する論理式の条件付確率 = 論理式をなす ground atom の条件付き確率  $(\sigma(v_{r_m}\cdot v_{(e_i,e_j)}))$  の総積

…と考える

## **Complex Logical Formulae**

#### **Negation**

•  $[\neg \mathcal{A}] = 1 - [\mathcal{A}]$ 

### **Other Logical Connectives** (∧,¬を用いて)

- $[\mathcal{A} \vee \mathcal{B}] = [\neg(\mathcal{A} \wedge \mathcal{B})] = [\mathcal{A}] + [\mathcal{B}] [\mathcal{A}][\mathcal{B}]$
- $[\mathcal{A} \implies \mathcal{B}] = [\neg \mathcal{A} \lor \mathcal{B}] = \cdots = [\mathcal{A}]([\mathcal{B}] 1) + 1$

#### **Universal Quantifier**

- if  $\mathcal{F} = \forall x, y \in \mathcal{E} : \mathcal{G}(x, y)$  then
- $[F] = [\forall x, y \in \mathcal{E} : \mathcal{G}(x, y)] = [\land_{x,y \in \mathcal{E}} \mathcal{G}(x, y)]$

#### **More Complex Logical Formulae**

以上を再帰的にに適用

## "Implications"

• if 
$$\mathcal{F} = \forall x, y \in \mathcal{E} : r_s(x, y) \implies r_t(x, y)$$

• 
$$\mathcal{F}_{ij} := r_s(e_i, e_j) \implies r_t(e_i, e_j)$$

• 
$$[\mathcal{F}] = \prod_{(e_i, e_i) \in \mathcal{P}} [F_{ij}]$$

• 
$$\mathcal{L}([\mathcal{F}]) = \sum_{(e_i, e_j) \in \mathcal{P}} \mathcal{L}([F_{ij}])$$

$$[\mathcal{F}_{ij}] = [r_s(e_i, e_j)] ([r_t(e_i, e_j)] - 1) + 1$$
(6)
$$\frac{\partial \mathcal{L}([\mathcal{F}_{ij}])}{\partial \mathbf{v}_{r_s}} = -[\mathcal{F}_{ij}]^{-1} ([r_t(e_i, e_j)] - 1) \frac{\partial [r_s(e_i, e_j)]}{\partial \mathbf{v}_{r_s}}$$

$$\frac{\partial \mathcal{L}([\mathcal{F}_{ij}])}{\partial \mathbf{v}_{r_t}} = -[\mathcal{F}_{ij}]^{-1} [r_s(e_i, e_j)] \frac{\partial [r_t(e_i, e_j)]}{\partial \mathbf{v}_{r_t}}$$
(7)
$$\frac{\partial \mathcal{L}([\mathcal{F}_{ij}])}{\partial \mathbf{v}_{e_i, e_j}} = -[\mathcal{F}_{ij}]^{-1} ([r_t(e_i, e_j)] - 1) \frac{\partial [r_s(e_i, e_j)]}{\partial \mathbf{v}_{e_i, e_j}}$$

$$-[\mathcal{F}_{ij}]^{-1} [r_s(e_i, e_j)] \frac{\partial [r_t(e_i, e_j)]}{\partial \mathbf{v}_{e_i, e_j}}.$$
(8)

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#### **Experiments**

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Extract Background Knowledge Results / Consideration

### **Data**

knowledge base completion of Freebase [Bollacker+ 08] with textual data from the NYTimes corpus [Sandhaus 08]

- R
- 151 Freebase relations
- 3,960 textual (surface) patterns
- $\mathcal{P} \subseteq \mathcal{E} \times \mathcal{E}$ 
  - 41,913 entity-pairs of interest
- $\mathcal{R} \times \mathcal{P}$ 
  - 118,781 training facts
  - including 7,293 Freebase relations (alignments between entity-pairs and Freebase relations)

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## **Extract Background Knowledge**

- 1. 全教師データで行列分解
- 2. すべての  $(r_s, r_t) \in \mathcal{R} \times \mathcal{R}$  (ただし  $r_t$  は Freebase relation) について  $[\forall (e_i, e_j) \in \mathcal{P}r_s(e_i, e_j) \implies r_s(e_i, e_j)]$  を計算
- 3. 上位 100 件から手動で 36 件をフィルタリング

| Formula   | Score |
|---|-------|
| $\forall x,y: \#2$ -unit-of- $\#1(x,y) \Rightarrow \text{org/parent/child}(x,y)$              | 0.97  |
| $\forall x,y: \texttt{\#2-city-of-\#1}(x,y) \Rightarrow \texttt{location/containedby}(x,y)$   | 0.97  |
| $orall x,y:$ #2-minister-#1 $(x,y)\Rightarrow$ person/nationality $(x,y)$                    | 0.97  |
| $\forall x,y: \texttt{\#2-executive-\#1}(x,y) \Rightarrow \texttt{person/company}(x,y)$       | 0.96  |
| $\forall x,y: \texttt{\#2-co-founder-of-\#1}(x,y) \Rightarrow \texttt{company/founders}(y,x)$ | 0.96  |

### Table 1: Sample Extracted Formulae: Top implica-

## Metric

(weighted) mean average precision (*MAP*, *wMAP*) on manually annotated predictions for Freebase relations

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## 1. Zero-shot Relation Learning

- Freebase relations  $\subseteq \mathcal{R} \times \mathcal{E} \times \mathcal{E}$  をすべて隠して、当てる
- background knowledge は使う

| Relation                     | #   | MF   | Inf  | Post | Pre  | Joint |
|------------------------------|-----|------|------|------|------|-------|
| person/company               | 102 | 0.07 | 0.03 | 0.15 | 0.31 | 0.35  |
| location/containedby         | 72  | 0.03 | 0.06 | 0.14 | 0.22 | 0.31  |
| author/works_written         | 27  | 0.02 | 0.05 | 0.18 | 0.31 | 0.27  |
| person/nationality           | 25  | 0.01 | 0.19 | 0.09 | 0.15 | 0.19  |
| parent/child                 | 19  | 0.01 | 0.01 | 0.48 | 0.66 | 0.75  |
| person/place_of_birth        | 18  | 0.01 | 0.43 | 0.40 | 0.56 | 0.59  |
| person/place_of_death        | 18  | 0.01 | 0.24 | 0.23 | 0.27 | 0.23  |
| neighborhood/neighborhood_of | 11  | 0.00 | 0.00 | 0.60 | 0.63 | 0.65  |
| person/parents               | 6   | 0.00 | 0.17 | 0.19 | 0.37 | 0.65  |
| company/founders             | 4   | 0.00 | 0.25 | 0.13 | 0.37 | 0.77  |
| film/directed_by             | 2   | 0.00 | 0.50 | 0.50 | 0.36 | 0.51  |
| film/produced_by             | 1   | 0.00 | 1.00 | 1.00 | 1.00 | 1.00  |
| MAP                          |     | 0.01 | 0.23 | 0.34 | 0.43 | 0.52  |
| Weighted MAP                 |     | 0.03 | 0.10 | 0.21 | 0.33 | 0.38  |

Table 2: Zero-shot Relation Learning: Average and

## 2. Relations with Few Distant Labels

- Freebase relations  $\subseteq \mathcal{R} \times \mathcal{E} \times \mathcal{E}$  を一部隠して、当てる
- トレーニングデータとして使う Freebase relations (distant labels) の割合を変化させる

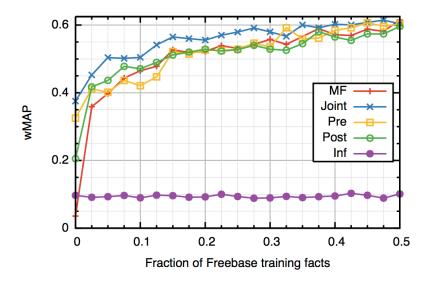


Figure 2: Relations with Few Distant Labels:

## 3. Comparison on Complete Data

- Freebase relations  $\subseteq \mathcal{R} \times \mathcal{E} \times \mathcal{E}$  をすべて使う
- 先行研究 [Riedel+13] の matrix factorization model "F" との性能比較
- ただし [Riedel+13] 中の「もっとも良い」モデルである "NF" や "NFE" とは比較されていない

## 4. Analysis of Asymmetry in the Predictions

- 学習に利用した logical formulae はすべて  $\forall x, y : r_s(x, y) \implies r_t(x, y)$  の形
- 学習されたモデルは " $\Longrightarrow$ " の非対称性を捉えられているか?
- Joint は捉えられているように見える

|   | MF   | Pre  | Joint |
|---|------|------|-------|
| $[\forall x, y : r_s(x, y) \implies r_t(x, y)]$ | 0.94 | 0.96 | 0.97  |
| $[\forall x, y : r_t(x, y) \implies r_s(x, y)]$ |      |      |       |