# From social theories to models

Tutor: Lisette Espín-Noboa



# Overview

Time: 10:30 - 12:30

10:30 - 11:00	Social theories <ul> <li>Popularity</li> <li>Similarity</li> <li>Friend-of-friend</li> <li>Activity</li> </ul> <li>Network properties &amp; structure</li>
11:00 - 11:30	<ul> <li>Network models: Undirected</li> <li>Barabasi-Albert Preferential Attachment (PA)</li> <li>PA with homophily (PAH)</li> <li>PA with triadic closure (PATC)</li> <li>PAH with triadic closure (PATCH)</li> </ul>
11:30 - 12:00	<ul> <li>Network models: Directed</li> <li>Directed Homophily (DH)</li> <li>Directed Preferential Attachment (DPA)</li> <li>DPA with homophily (DPAH)</li> </ul>
12:00 - 12:30	Exercise #1

# Social theories

## Literature

Non-exhaustive list of material covered in this section.

- Jackson, M. O. (2008). Social and economic networks (Vol. 3). Princeton: Princeton university press.
- 2. Albert-László Barabás (2016). Network Science. (available online as an interactive book)
- 3. Jackson, M. O. (2019). The human network: How your social position determines your power, beliefs, and behaviors. Vintage.
- 4. Stadfeld, C., & Amati, V. (2021). Network mechanisms and network models. In Research Handbook on Analytical Sociology (pp. 432-452). Edward Elgar Publishing.
- 5. Gamper, M. (2022). Social Network Theories: An Overview. Social Networks and Health Inequalities, 35.
- 6. Karimi, F., & Oliveira, M. (2022). On the inadequacy of nominal assortativity for assessing homophily in networks. arXiv preprint arXiv:2211.10245.

#### What are social networks?

# Social networks consists of **actors** (nodes) and **relations** (edges)

- Actor → person, company, county
  - It may also include entities produced or generated by individuals, e.g., email, retweet.
- Relation → friendship, collaboration, partnership, trade, war, hierarchy
  - When the actor is a resource, the relation may represent a spreading dynamic, access to opportunities, etc.

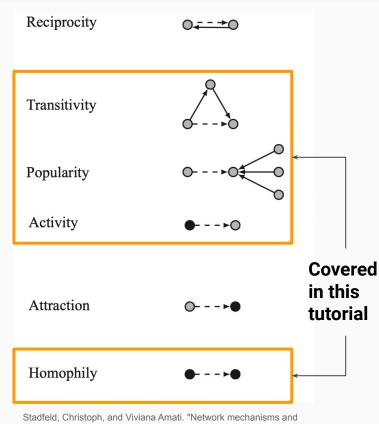


#### How do networks form?

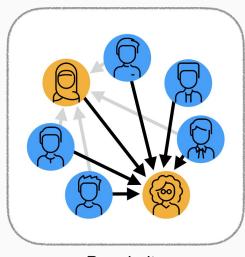
Social mechanisms in micro-level govern how we organize our social lifes and interact with others. Some of those social theories include: group identity theory, cultural evolutions, and broadly social psychology theories.

Prevalent **mechanisms** identified in social science literatures:

- Preferential attachment a.k.a. rich-get-richer or Matthew effect
- Homophily and assortative mixing
- Social balance and triadic closure



Stadfeld, Christoph, and Viviana Amati. "Network mechanisms and network models." Research Handbook on Analytical Sociology. Edward Elgar Publishing, 2021



**Popularity** 

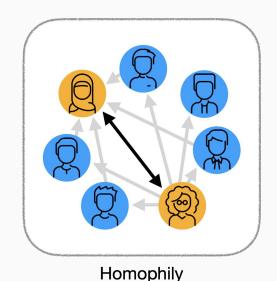
The tendency of actors to connect to those who receive ties from many others.

The structural position is defined by the **in-degree of the receiver** (target node) of an explained tie.

- Matthew effect mechanism in science discussed by Merton (1968).
   Increasing recognition of an actor's scientific work (e.g. number of ties in a citation network).
- Preferential attachment in the work of Barabási and Albert (1999).

The presence of a popularity mechanism is not sufficient evidence that a Matthew effect exists in a network, e.g., other actor **attributes**, such as the career stage or gender, might send similar signals that affect the beliefs of others.

$$P(a \to b) = P(b|a) = p_{ab} = \frac{k_b}{\sum_c k_c}$$

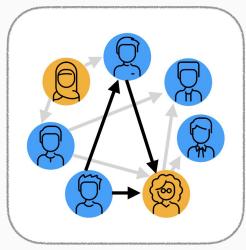


The tendency that <u>similar actors are more likely to connect</u> (Lazarsfeld, et al. 1954; McPherson et al. 2001). Its structural position is defined by **the** <u>attribute</u> <u>similarity of the sender and receiver</u> of the explained tie.

Causal explanations:

- These may be cognitive processes about similarity attraction (Huston and Levinger 1978)
- Structural processes that are affected by existing baseline segregation and social distances in the social setting under study.

$$P(a \rightarrow b) = P(b|a) = p_{ab} = similarity(a, b)$$



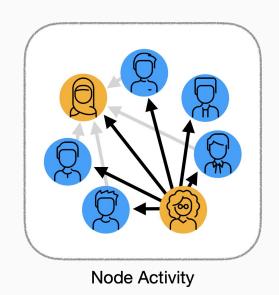
Transitivity

One of the central mechanisms that goes beyond the dyad and thus involves more than two actors: it expresses the tendency of actors to connect to others to whom they are indirectly tied to through a third actor. The structural position is defined by the presence of a "two-path" between the sender and the receiver of the explained tie.

#### Causal explanations:

- Differences in spatial or social distances and similarity attraction based on an actor attribute (Granovetter 1973).
- Actors may perceive cognitive dissonance and stress if they are not in a positive relationship with those they are indirectly positively tied to (Heider 1958).

$$P(a \rightarrow b) = P(b|a) = p_{ab} = p_{TC} \propto clustering(g)$$



The tendency that actors with specific attributes will be more likely to send ties. The structural positions are defined by attributes of the sender of the explained tie. Whether these differences relate to differences in networking resources is not further specified by the mechanism.

a •---⊳o b

$$P(a \to b) = P(b|a) = p_{ab} \propto activity(a)$$

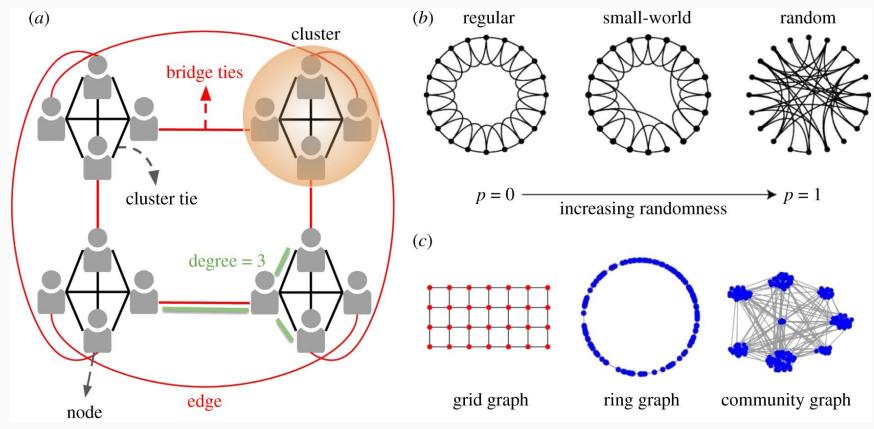
# Network properties and structure

# Important properties of social networks

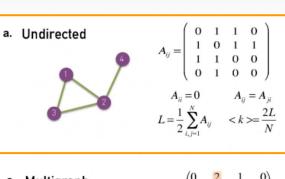
Connected components

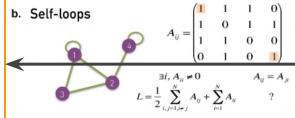
#	Graph	Node	Edge
1	Average and minimum degree	Degree (in/out)	Weights
2	Degree distribution (the probability that a randomly selected node in the network has degree k)	Centrality (e.g,. PageRank)	Shortest path
3	Adjacency matrix	Clustering coefficient	Homophilous type (MM, Mm, mm, mM)
4	Sparsity (out of the total possible number of edges, how many actually exist)	Activity (high activity = high outdegree)	
5	Diameter		ı
6	Average Path Length		

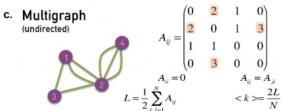
## Common structure (topology) of social networks

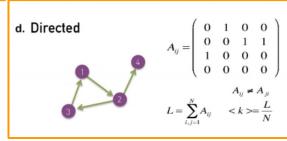


## Graphology (elementary property of the underlying graph)

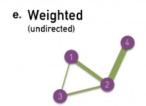






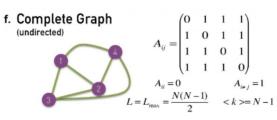






$$A_{ij} = \begin{pmatrix} 0 & 2 & 0.5 & 0 \\ 2 & 0 & 1 & 4 \\ 0.5 & 1 & 0 & 0 \\ 0 & 4 & 0 & 0 \end{pmatrix}$$

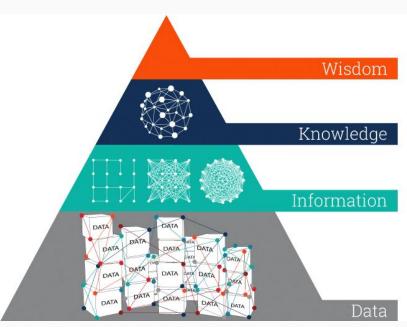
$$A_{ii} = 0 \qquad A_{ij} = A_{ji}$$



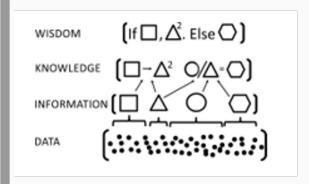
# Network models

## Why modeling social networks?

#### The wisdom hierarchy



Each step up
the pyramid
answers
questions
about and
adds value
to the initial data.



Page, S. E. (2018). *The model thinker: What you need to know to make data work for you.* Basic Books. https://www.ontotext.com/knowledgehub/fundamentals/dikw-pyramid/

#### The seven uses of Models

- 1. Reason: to identify conditions and deduce logical implications
- 2. **Explain:** To provide explanations for empirical phenomena
- 3. **Design:** to choose features of policies, institutions and rules
- 4. Communicate: to relate knowledge and understandings
- 5. Act: to guide policy choices and strategic actions
- 6. **Predict:** to make numerical and categorical predictions of future and unknown phenomena
- 7. Explore: to investigate possibilities and hypotheticals scenarios

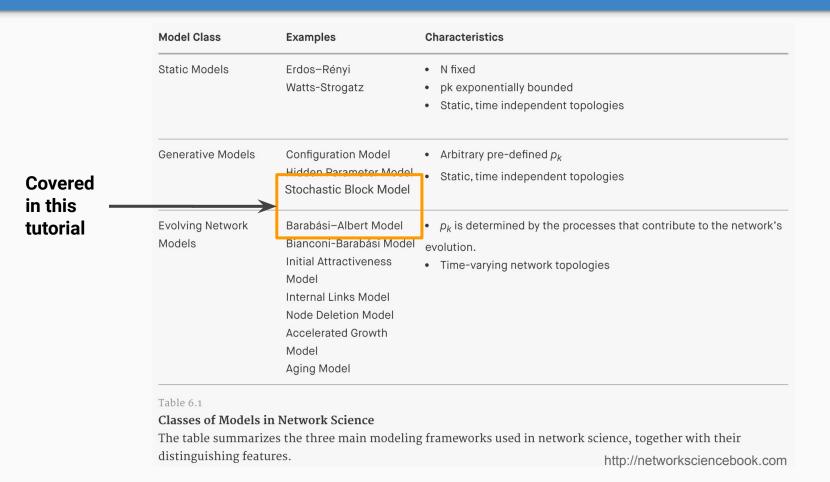
## Why modeling social networks?

Here I emphasis on the application of network models in ML and AI draw from our previous research and the below recent survey article

Steinbacher, M., Raddant, M., Karimi, F., Camacho Cuena, E., Alfarano, S., Iori, G., & Lux, T. (2021). Advances in the agent-based modeling of economic and social behavior. *SN Business & Economics*, *1*(7), 99.

# Network models ... and where to find them

#### Class of models in Network Science



# Pre-requisites

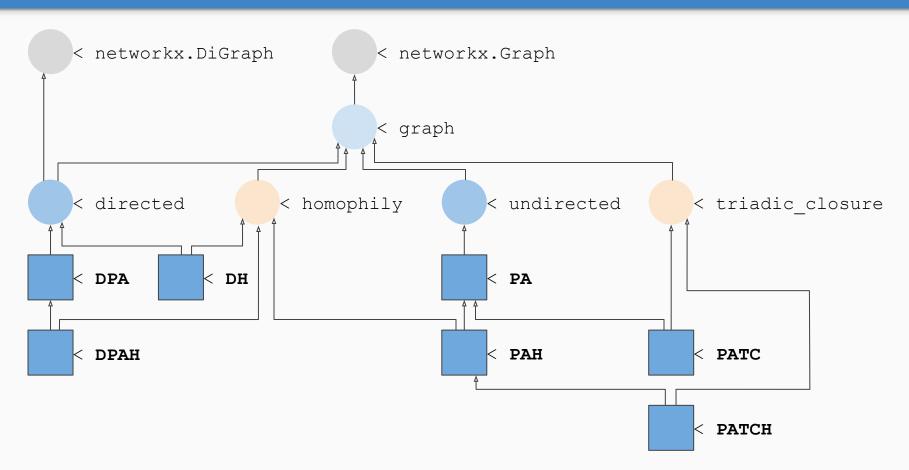
Follow these instructions in case you are using your own environment to run the exercises.

Alternatively, you can run all the exercises in the cloud. We have prepared notebooks to run in Google Colab (more details later).

- Download and install conda conda.io/projects/conda/en/stable/user-guide/install/download.html
- 2. Create an environment with python 3.9 or later conda create -n "snma" python=3.9 jupyterlab
- Activate your newly created conda environment conda activate snma
- 4. Clone the tutorial in your computer git clone <a href="https://github.com/snma-tutorial/www2023.git">https://github.com/snma-tutorial/www2023.git</a>
- 5. Install the dependencies

```
conda install pip
pip install -r requirements.txt
```

## The netin python package (alpha)



# Undirected networks

#### PA

preferential attachment

#### **PATC**

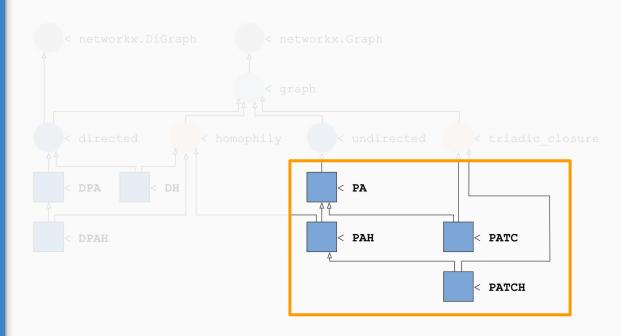
PA + triadic closure

#### **PAH**

PA + homophily

#### **PATCH**

PAH + triadic closure



# class netin.PA(...)

Creates a new PA instance. An undirected graph with preferential attachment.

### **Parameters**

n: int

number of nodes (minimum=2)

k: int

minimum degree of nodes (minimum=1)

f m: float

fraction of minorities (minimum=1/n, maximum=(n-1)/n)

seed: object

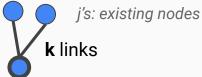
seed for random number generator

#### **STEP 1:**

k = 2

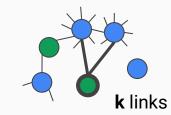


#### **STEP 2:**



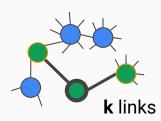
i: new node (and then existing node)

#### STEP $3 \le s \le n$ :



# class netin.PAH(...)

#### STEP $3 \le s \le n$ :



$$p_{ab} = \frac{h_{ab}k_b}{\sum_c h_{ac}k_c}$$

Creates a new PAH instance. An undirected graph with preferential attachment and homophily.

#### **Parameters**

n: int

number of nodes (minimum=2)

k: int

minimum degree of nodes (minimum=1)

f\_m: float

fraction of minorities (minimum=1/n, maximum=(n-1)/n)

h\_MM: float

homophily (similarity) between majority nodes (minimum=0, maximum=1.)

h\_mm: float

homophily (similarity) between minority nodes (minimum=0, maximum=1.)

seed: object

seed for random number generator

# class netin.PATC(...)

Creates a new PATC instance. An undirected graph with preferential attachment and triadic closure.

#### **Parameters**

n: int

number of nodes (minimum=2)

k: int

minimum degree of nodes (minimum=1)

f\_m: float

fraction of minorities (minimum=1/n, maximum=(n-1)/n)

tc: float

probability of a new edge to close a triad (minimum=0, maximum=1.)

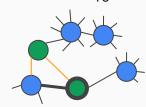
seed: object

seed for random number generator

#### STEP $3 \le s \le n$ :

k times

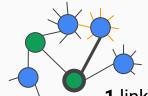
Case 1: p<sub>TC</sub>



1 link (closes a triangle)

Target 'b' with more nodes in common with 'a'

Case 2:  $(1 - p_{TC})$ 



$$p_{ab} = \frac{k_b}{\sum_c k_c}$$

**1** link (via preferential attachment)

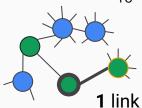
# class netin.PATCH(...)

STEP  $3 \le s \le n$ :

k times

Case 1: p<sub>TC</sub>

Case 2:  $(1 - p_{TC})$ 



$$p_{ab} = \frac{h_{ab}k_b}{\sum_c h_{ac}k_c}$$

(via preferential attachment and homophily)

Creates a new PATCH instance. An undirected graph with preferential attachment, homophily, and triadic closure.

#### **Parameters**

n: int

number of nodes (minimum=2)

k: int

minimum degree of nodes (minimum=1)

f m: float

fraction of minorities (minimum=1/n, maximum=(n-1)/n)

h MM: float

homophily (similarity) between majority nodes (minimum=0, maximum=1.)

h\_mm: float

homophily (similarity) between minority nodes (minimum=0, maximum=1.)

tc: float

probability of a new edge to close a triad (minimum=0, maximum=1.)

- F. Karimi, M. Génois, C. Wagner, P. Singer, & M. Strohmaier "Homophily influences ranking of minorities in social networks" Scientific reports 2018
- P. Holme and B. J. Kim, "Growing scale-free networks with tunable clustering" Phys. Rev. E 2002.
- PATCH: Forthcoming...

# Directed networks

#### **DPA**

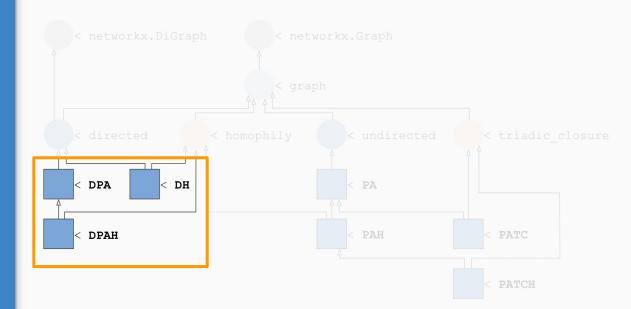
preferential attachment

#### DH

homophily

#### **DPAH**

DPA + homophily



# class netin.DPA(...)

**Do** while density < d:

Step 1: choose a **source** node (using the activity of all nodes)

Step 2: choose a **target** node \* (using preferential attachment → in\_degree)

\* target nodes must have out\_degree > 0 (should have been picked as source at least once)

Creates a new DPA instance. A directed graph with preferential attachment.

#### **Parameters**

n: int
number of nodes (minimum=2)

d: float
edge density (minimum=0, maximum=1)

f\_m: float fraction of minorities (minimum=1/n, maximum=(n-1)/n)

plo\_M: float
 activity (out-degree power law exponent) majority group (minimum=1)

plo\_m: float
 activity (out-degree power law exponent) minority group (minimum=1)

seed: object seed for random number generator

# class netin.DH(...)

**Do** while density < d:

Step 1: choose a **source** node (using the activity of all nodes)

Step 2: choose a **target** node \* (using mixing matrix → homophily within/across groups)

\* target nodes must have out\_degree > 0 (should have been picked as source at least once)

```
Parameters
n: int
   number of nodes (minimum=2)
d: float
   edge density (minimum=0, maximum=1)
f m: float
   fraction of minorities (minimum=1/n, maximum=(n-1)/n)
plo_M: float
   activity (out-degree power law exponent) majority group (minimum=1)
plo m: float
   activity (out-degree power law exponent) minority group (minimum=1)
h MM: float
   homophily within majority group (minimum=0, maximum=1)
h mm: float
   homophily within minority group (minimum=0, maximum=1)
seed: object
```

seed for random number generator

Creates a new DH instance. A directed graph with homophily.

#### Directed networks

# class netin.DPAH(...)

**Do** while density < d:

Step 1: choose a **source** node (using the activity of all nodes)

Step 2: choose a **target** node \* (using mixing matrix and preferential attachment)

\* target nodes must have out\_degree > 0 (should have been picked as source at least once)

Creates a new DPAH instance. A directed graph with preferential attachment and homophily.

#### **Parameters**

seed for random number generator

```
n: int
   number of nodes (minimum=2)
d: float
   edge density (minimum=0, maximum=1)
f m: float
   fraction of minorities (minimum=1/n, maximum=(n-1)/n)
plo M: float
   activity (out-degree power law exponent) majority group (minimum=1)
plo m: float
   activity (out-degree power law exponent) minority group (minimum=1)
h MM: float
   homophily within majority group (minimum=0, maximum=1)
h mm: float
   homophily within minority group (minimum=0, maximum=1)
seed: object
```

## Exercise

#### Task:

- 1. Generate 3 undirected graphs.
- 2. Get to know them (attributes, visualize them, etc.)
- 3. Plot and compare their type of edges (MM, Mm, mm, mM).
- 4. Plot and compare the pdf of their degree distributions.

Repeat for other graphs and check the effects of other mechanisms.

(30 min)

## Open 1\_exercise.ipynb

1. Alternatively, you can open the notebook from Google Colab (you need a Google account):

bit.ly/snma2023-notebooks

# Lunch break

see you back at 13:30