

# Applications

Tutor: Lisette Espín-Noboa

# Overview

Time: 15:30 - 16:30

15:30 - 16:00

Representative samples

- Sampling bias & properties preserved
  - On synthetic networks
  - On real networks

16:00 - 16:30

Ranking inequalities

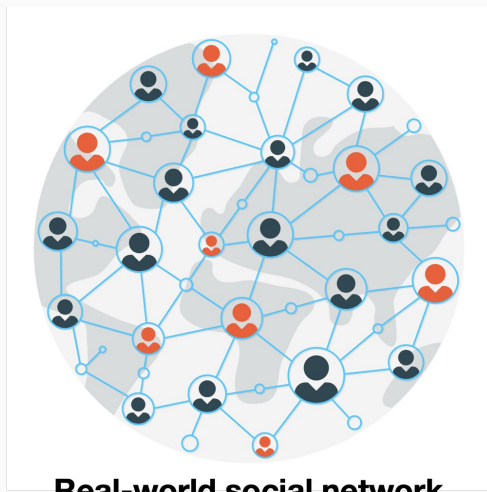
- Inequality
- Inequity
- Disparity

# Literature

Non-exhaustive list of material covered in this section.

1. Espín-Noboa, L., Wagner, C., Strohmaier, M., & Karimi, F. (2022). Inequality and inequity in network-based ranking and recommendation algorithms. *Scientific reports*, 12(1), 1-14.
2. Karimi, F., Génois, M., Wagner, C., Singer, P. & Strohmaier, M. Homophily influences ranking of minorities in social networks. *Sci. Rep.*8 (2018).
3. Stoica, A.-A., Riederer, C. & Chaintreau, A. Algorithmic glass ceiling in social networks: The effects of social recommendations on network diversity. In *Proceedings of the 2018 World Wide Web Conference*, 923–932 (2018).
4. Fabbri, F., Bonchi, F., Boratto, L. & Castillo, C. The effect of homophily on disparate visibility of minorities in people recommender systems. In *Proceedings of the International AAAI Conference on Web and Social Media* 14, 165–175 (2020).

# Biases in sampling



**Real-world social network**

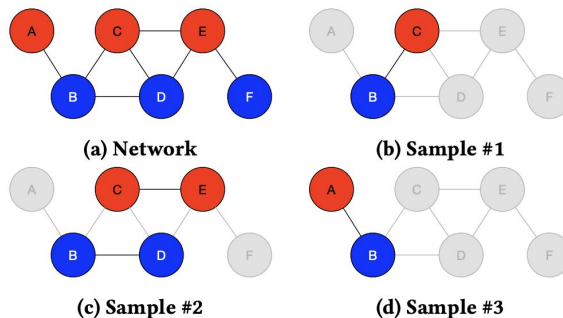
(people with attributes)

(very big or proprietary)

### **Social Network**

*Mechanism of edge formation:*

*Homophily & Preferential Attachment*

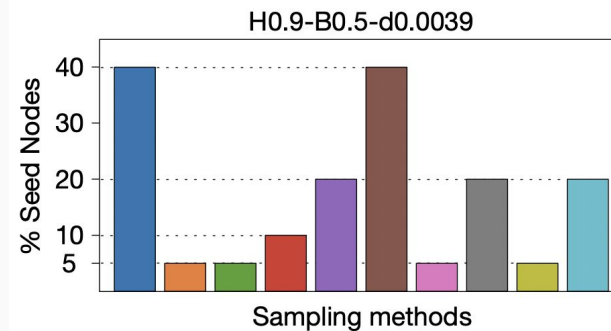


(a) Network

(b) Sample #1

(c) Sample #2

(d) Sample #3



### **Task 1:**

Try multiple sampling methods and identify when they fail given the type of network (homophily, density, etc)

### **Task 2:**

Identify the minimum sample size required per sampling method and type of network.

# Exercise

Open `3_exercise.ipynb`

Alternatively, you can open the notebook from Google Colab (you need a Google account):  
[bit.ly/snma2023-notebooks](https://bit.ly/snma2023-notebooks)

1. Create 3 DPAH graphs
  - a. Make sure all of them have the same number of nodes `n`, edge density `d`, fraction of minority `f_m`, activities `plo_M` and `plo_m`, and random seed `seed`.
  - b. Make sure they have the same level of homophily within the majority group (e.g., `h_MM=0.5`) and vary only the homophily within the minority group, for example:
    - i. Graph 1: `h_MM=0.5` and `h_mm=0.1`
    - ii. Graph 2: `h_MM=0.5` and `h_mm=0.5`
    - iii. Graph 3: `h_MM=0.5` and `h_mm=0.9`
2. Make 6 random samples using the sampling techniques from `netin.sampling.*`
  - a. Make sure they all have the same `pseeds` (sample size)
3. Analysis:
  - a. Plot the graphs and the samples.
  - b. Plot the representation of groups for each sample
  - c. The CDF of the `in_degree` distribution and the CCDF of the `pagerank` distribution.
  - d. Which sample looks closest to the full data? Does it depend on `h`?

# BONUS exercise

Open `3_exercise.ipynb`

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(30 min)

1. Load the `fb_friends` network, and make sure it is a `netin` graph.
2. Get to know the data (`.info()`)
3. Fit the `PA`, `PAH`, and the `PATC` models to the graph.
4. Visualize the graphs.
5. Compare their `degree` and `pagerank` distributions (plot the `pdf` and `cdf`).

# Ranking inequalities





**Real-world social network**  
(people with attributes)



**Ranking / RecSys.**  
(PageRank or WTF)

## 1. Identify network structure

Fraction min.  
 $f_m=0.3$

Node activity  
 $y_M = y_m = 3$

Density  
 $d=0.0015$

Homophily Maj.  
 $H_{MM}=0.8$

Homophily min.  
 $H_{mm}=0.4$

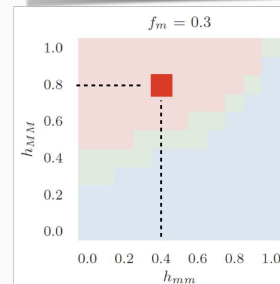
(Inequity is driven by homophily and fraction of minorities)

## 2. Identify inequality and inequity in ranking

OPEN

### Inequality and inequity in network-based ranking and recommendation algorithms

Lisette Espin-Noboa<sup>1,2,3</sup>, Claudia Wagner<sup>1,4,5</sup>, Markus Strohmaier<sup>1,4,6</sup> & Fariba Karimi<sup>1,5</sup>



On average minorities are  
under-represented in top-k's  
(Interventions needed)

# Exercise

Open `4_exercise.ipynb`

Alternatively, you can open the notebook from Google Colab (you need a Google account):  
[bit.ly/snma2023-notebooks](https://bit.ly/snma2023-notebooks)

(30 min)

## Comparing the effect of homophily in ranking by pagerank

1. Create 9 DPAH graphs
  - a. Make sure all of them have the same number of nodes  $n$ , edge density  $d$ , fraction of minority  $f_m$ , activities  $p_{lo\_M}=p_{lo\_m}$ , and random seed  $seed$ .
  - b. Make sure they have different values of homophily  $h_{MM}$  and  $h_{mm}$  as follows:
    - i. Graphs 1-3:  $h_{MM}=0.1$  and  $h_{mm} \in \{0.1, 0.5, 0.9\}$
    - ii. Graphs 4-6:  $h_{MM}=0.5$  and  $h_{mm} \in \{0.1, 0.5, 0.9\}$
    - iii. Graphs 7-9:  $h_{MM}=0.9$  and  $h_{mm} \in \{0.1, 0.5, 0.9\}$
2. Analysis:
  - a. Plot the edge-type counts
  - b. Plot the probability density function of their pagerank distributions
  - c. Plot the inequality of the pagerank
  - d. Plot the inequity of the pagerank
  - e. Plot the disparity of the pagerank.

# Bonus exercise

Open `4_exercise.ipynb`

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[bit.ly/snma2023-notebooks](https://bit.ly/snma2023-notebooks)

(30 min)

Comparing the effect of preferential attachment and homophily in ranking by pagerank

1. Generate 3 directed graphs; one for each model: DPA, DH, and DPAH
2. Make sure all of them have the same number of nodes  $n$ , edge density  $d$ , fraction of minority  $f_m$ , activities  $p_{lo\_M}=p_{lo\_m}$ , homophily  $h_{MM}$  and  $h_{mm}$ , and random seed `seed`, if applicable.
3. Plot the disparity of their pagerank.

# Closing remarks

Challenges & open questions

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