

Applications

Tutor: Lisette Espín-Noboa

Overview

Time: 15:30 - 16:30

15:30 - 16:05

Representative samples

- Sampling bias & properties preserved
 - On synthetic networks
 - On real networks

16:05 - 16:40

Ranking inequalities

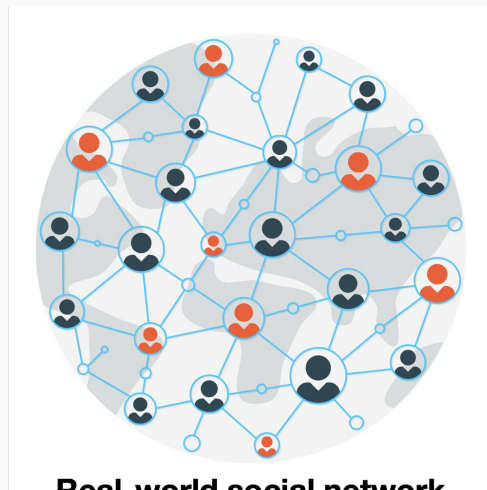
- Inequality
- Inequity
- Disparity

Literature

Non-exhaustive list of material covered in this section.

1. Espín-Noboa, L., Wagner, C., Strohmaier, M., & Karimi, F. (2022). Inequality and inequity in network-based ranking and recommendation algorithms. *Scientific reports*, 12(1), 1-14.
2. Karimi, F., Génois, M., Wagner, C., Singer, P. & Strohmaier, M. Homophily influences ranking of minorities in social networks. *Sci. Rep.*8 (2018).
3. Stoica, A.-A., Riederer, C. & Chaintreau, A. Algorithmic glass ceiling in social networks: The effects of social recommendations on network diversity. In *Proceedings of the 2018 World Wide Web Conference*, 923–932 (2018).
4. Fabbri, F., Bonchi, F., Boratto, L. & Castillo, C. The effect of homophily on disparate visibility of minorities in people recommender systems. In *Proceedings of the International AAAI Conference on Web and Social Media* 14, 165–175 (2020).

Biases in sampling

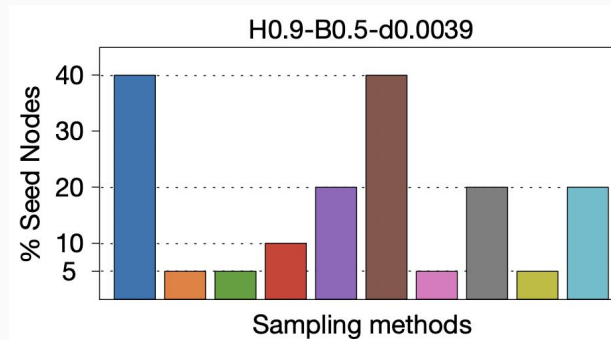
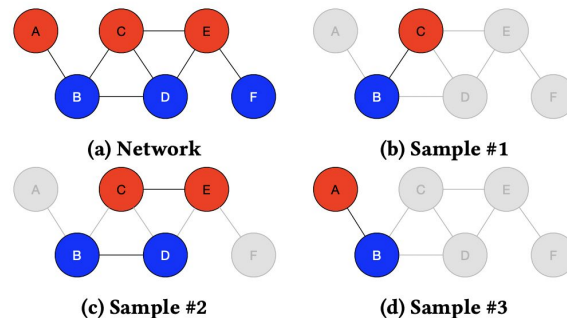


Real-world social network

(people with attributes)

(very big or proprietary)

Covered in this tutorial



Use case 1

Try multiple sampling methods and identify how representative that sample is compared to the whole network.

Use case 2

Identify the minimum sample size required per sampling method and type of network to achieve at most 20% error in classification.

Exercise

Open `3_exercise.ipynb`

Alternatively, you can open the notebook from Google Colab (you need a Google account):
bit.ly/snma2023-notebooks

1. Create 3 DPAH graphs
 - a. Make sure all of them have the same number of nodes `n`, edge density `d`, fraction of minority `f_m`, activities `plo_M` and `plo_m`, and random seed `seed`.
 - b. Make sure they have the same level of homophily within the majority group (e.g., `h_MM=0.5`) and vary only the homophily within the minority group, for example:
 - i. Graph 1: `h_MM=0.5` and `h_mm=0.1`
 - ii. Graph 2: `h_MM=0.5` and `h_mm=0.5`
 - iii. Graph 3: `h_MM=0.5` and `h_mm=0.9`
2. Make 6 random samples using the sampling techniques from `netin.sampling.*`
 - a. Make sure they all have the same `pseeds` (sample size)
3. Analysis:
 - a. Plot the graphs and the samples.
 - b. Plot the representation of groups for each sample
 - c. The CDF of the `in_degree` distribution and the CCDF of the `pagerank` distribution.
 - d. Which sample looks closest to the full data? Does it depend on `h`?

BONUS exercise

Open `3_exercise.ipynb`

Alternatively, you can open the notebook from Google Colab (you need a Google account):

bit.ly/snma2023-notebooks

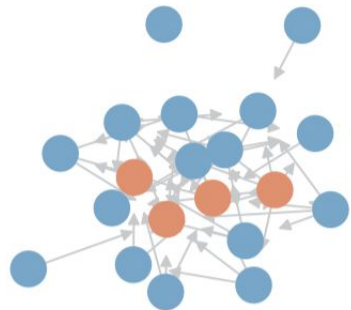
(30 min)

1. Load the `fb_friends` network, and make sure it is a `netin` graph.
2. Get to know the data (`.info()`)
3. Fit the `PA`, `PAH`, and the `PATC` models to the graph.
4. Visualize the graphs.
5. Compare their `degree` and `pagerank` distributions (plot the `pdf` and `cdf`).
6. Choose four sampling techniques and extract a sample for each network using a same sample size. What properties were preserved?

Ranking inequalities

Given a network,

Heterophilic
 $h_{MM} = 0.2$
 $h_{mm} = 0.2$



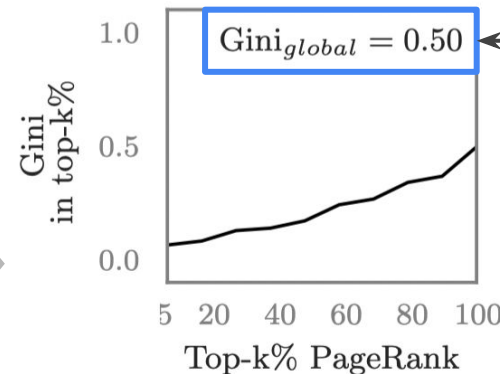
$n = 20$
 min (m) = 20% (fm)
 maj (M) = 80%

... and a ranking of its nodes

Ranked nodes
(PageRank)



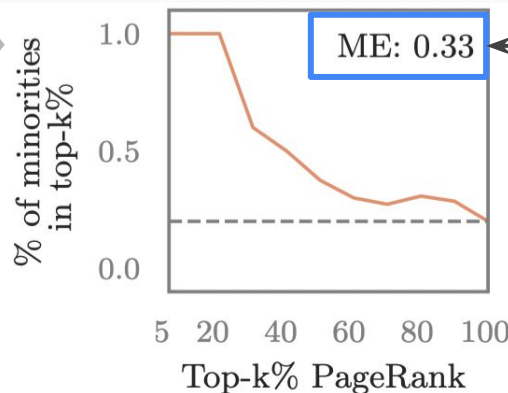
Measure:



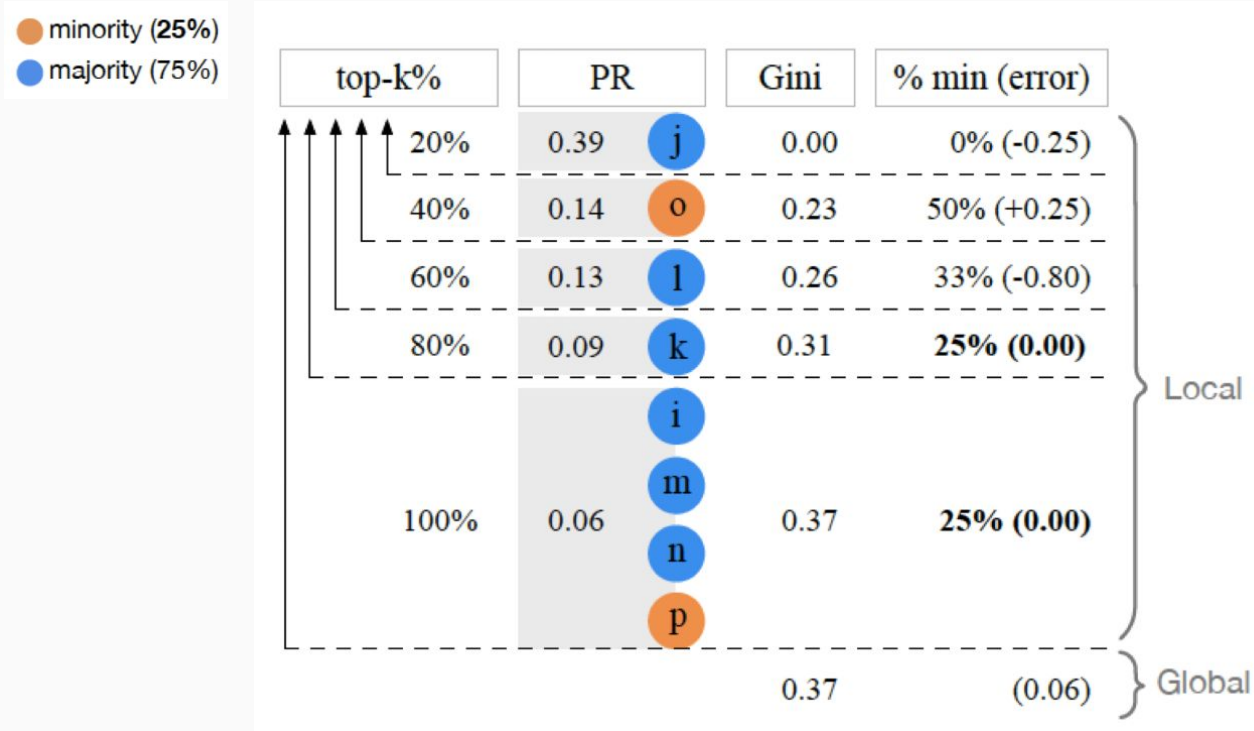
Inequality

Disparity

ME vs $Gini_{global}$

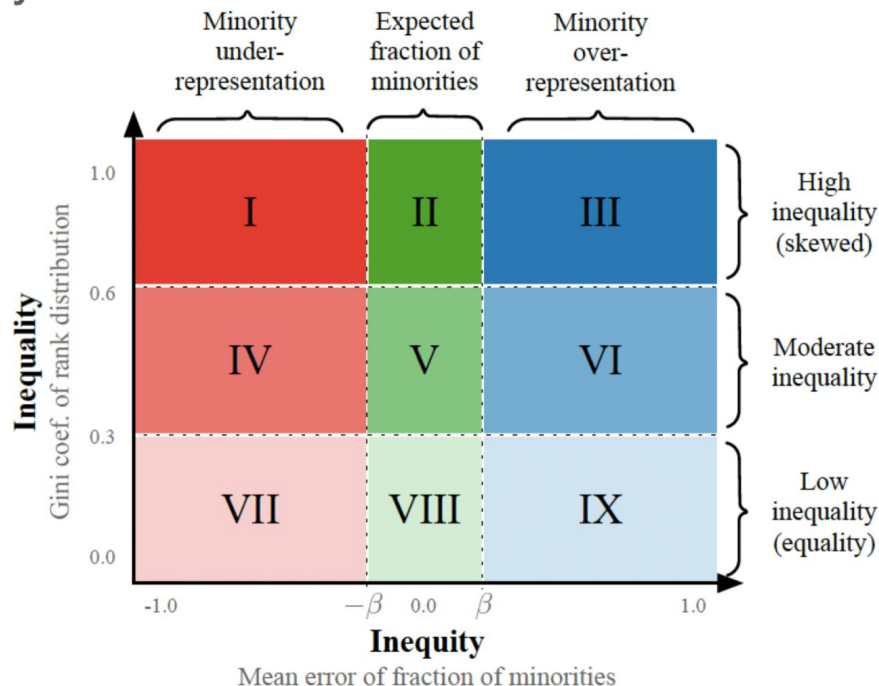
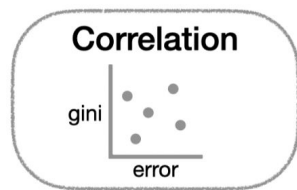


Inequity



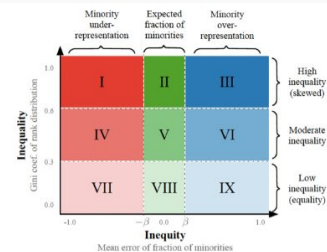
Inequality vs. Inequity

Regions of disparity



Inequality vs. Inequity in PageRank

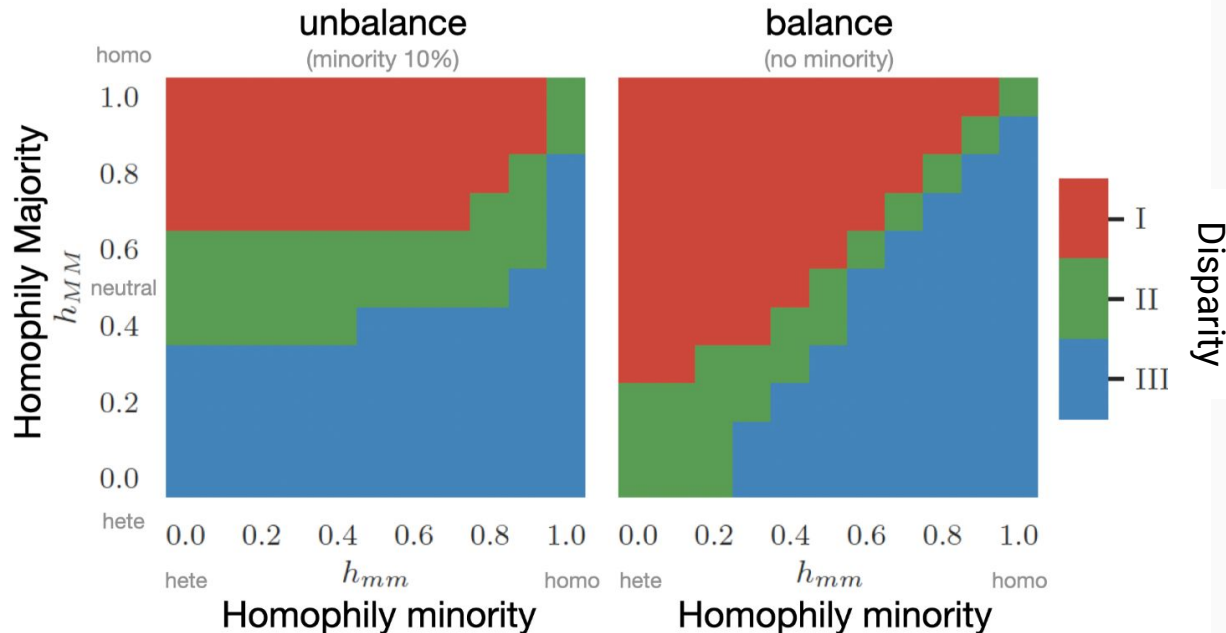
As a function of **H**omophily and **F**raction of minorities



1. In **balanced networks**, both groups are well represented if $h_{MM} = h_{MM}$

2. In **unbalanced networks**, minorities are well represented when majority is neutral and the minority is not too homophilic.

3. In **unbalanced and homophilic networks**, minorities are well represented when $h_{MM} > h_{MM}$.





Real-world social network
(people with attributes)



Ranking / RecSys.
(PageRank or WTF)

1. Identify network structure

Fraction min.
 $f_m=0.3$

Node activity
 $y_M = y_m = 3$

Density
 $d=0.0015$

Homophily Maj.
 $H_{MM}=0.8$

Homophily min.
 $H_{mm}=0.4$

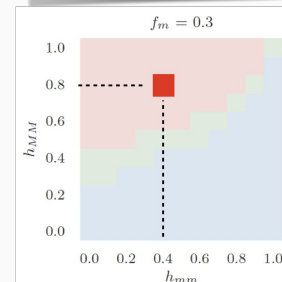
(Inequity is driven by homophily and fraction of minorities)

2. Identify inequality and inequity in ranking

OPEN

Inequality and inequity in network-based ranking and recommendation algorithms

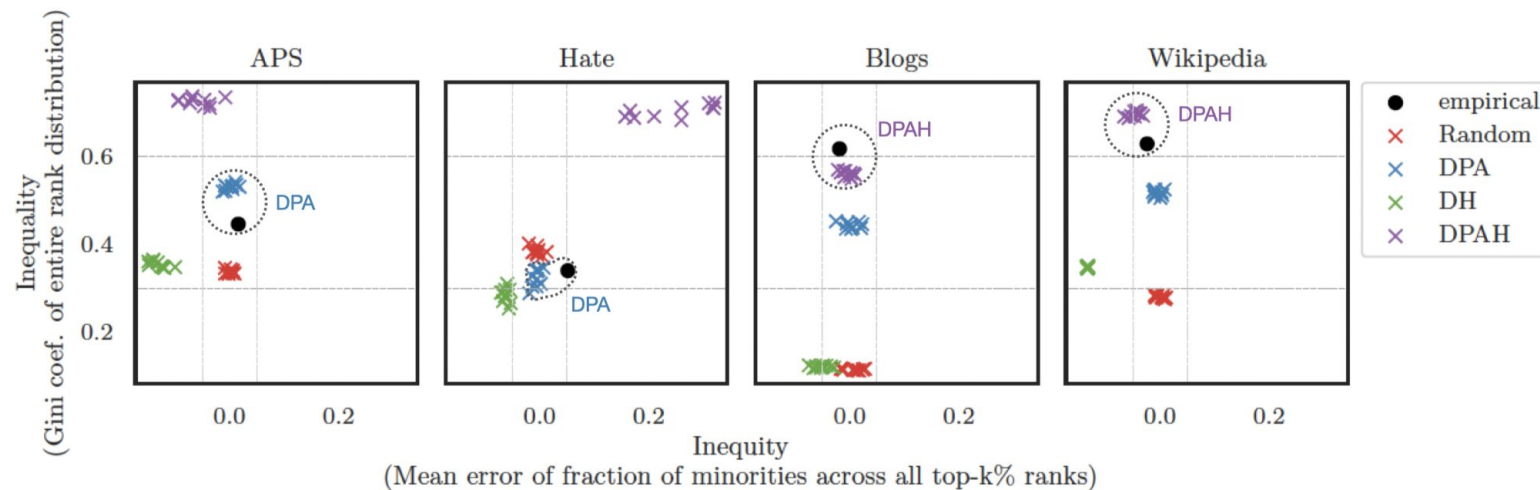
Lisette Espin-Noboa^{1,2,3}, Claudia Wagner^{4,5,6}, Markus Strohmaier^{1,4,6} & Fariba Karimi^{1,5,6}



On average minorities are
under-represented in top-k's
(Interventions needed)

Empirical Networks

Model selection (best fit)



Exercise

Open `4_exercise.ipynb`

Alternatively, you can open the notebook from Google Colab (you need a Google account):
bit.ly/snma2023-notebooks

(30 min)

Comparing the effect of homophily in ranking by pagerank

1. Create 9 `DPAH` graphs
 - a. Make sure all of them have the same number of nodes `n`, edge density `d`, fraction of minority `f_m`, activities `plo_M=plo_m`, and random seed `seed`.
 - b. Make sure they have different values of homophily `h_MM` and `h_mm` as follows:
 - i. Graphs 1-3: `h_MM=0.1` and `h_mm \in \{0.1, 0.5, 0.9\}`
 - ii. Graphs 4-6: `h_MM=0.5` and `h_mm \in \{0.1, 0.5, 0.9\}`
 - iii. Graphs 7-9: `h_MM=0.9` and `h_mm \in \{0.1, 0.5, 0.9\}`
2. Analysis:
 - a. Plot the edge-type counts
 - b. Plot the probability density function of their pagerank distributions
 - c. Plot the inequality of the pagerank
 - d. Plot the inequity of the pagerank
 - e. Plot the disparity of the pagerank.

Bonus exercise

Open `4_exercise.ipynb`

Alternatively, you can open the notebook from Google Colab (you need a Google account):
bit.ly/snma2023-notebooks

(30 min)

Comparing the effect of preferential attachment and homophily in ranking by pagerank

1. Generate 3 directed graphs; one for each model: DPA, DH, and DPAH
2. Make sure all of them have the same number of nodes n , edge density d , fraction of minority f_m , activities $p_{lo_M}=p_{lo_m}$, homophily h_{MM} and h_{mm} , and random seed `seed`, if applicable.
3. Plot the disparity of their pagerank.

Classification

(not covered today)

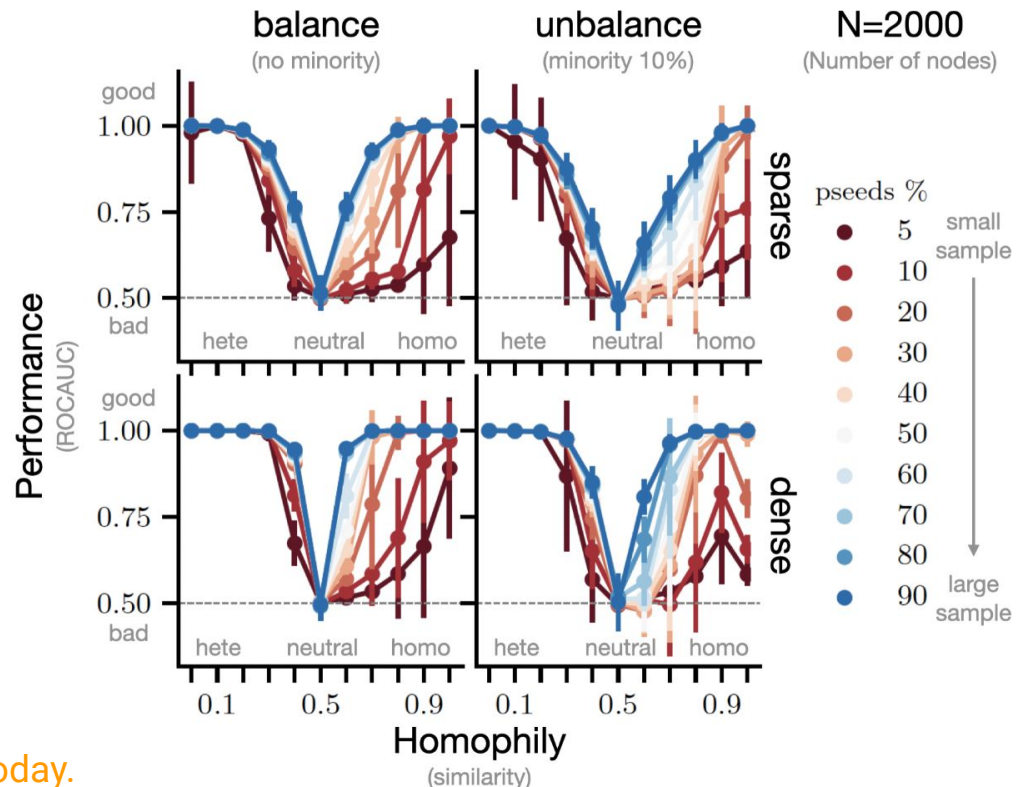
Network structure vs. Classification performance

1. **Neutral networks** ($H=0.5$) cannot be classified better than a random classifier.

2. **Homophilic networks** ($H>0.5$) achieve lower performance than heterophilic networks when samples are small.

3. **Denser networks** achieve higher performance compared to sparse networks.

4. **Network size** mainly affects ROCAUC variance. Larger networks produce more stable results. (not shown here)





Real-world social network
(people with attributes)



What you get
(people with no attributes)

1. Identify network structure

Inference in OSNs via Lightweight Partial Crawls

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Class balance
 $B=0.3$

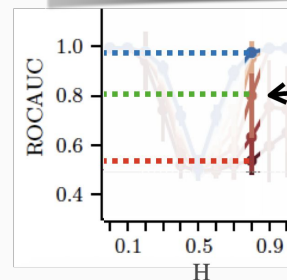
Homophily
 $H=0.8$

2. Identify ROCAUC range for that network

RESEARCH

Explaining Classification Performance and Bias via Network Structure and Sampling Technique

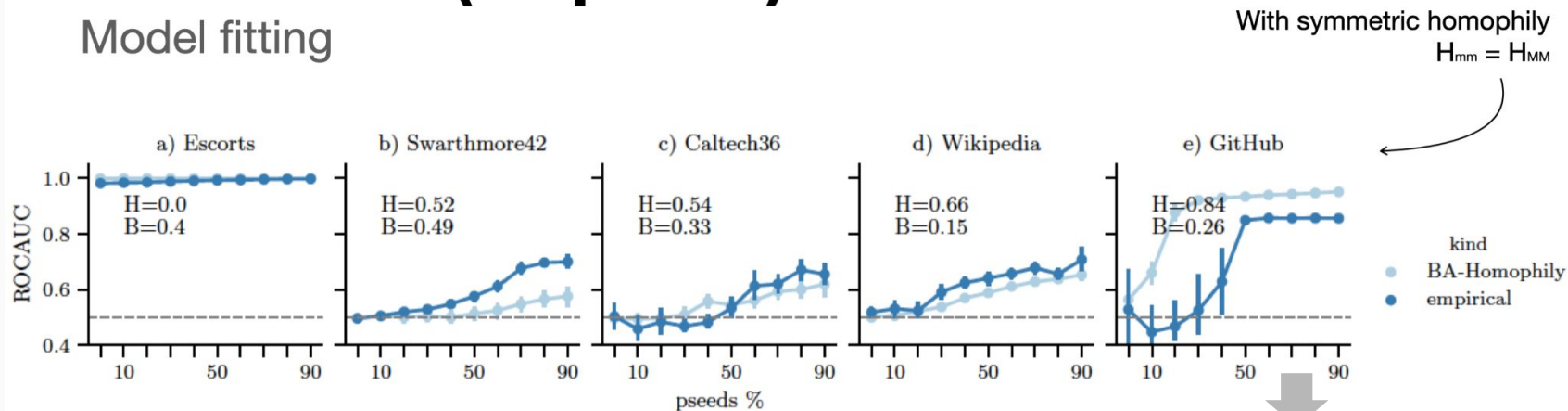
Lisette Espin-Noboa, Fariba Karimi, Bruno Ribeiro, Kristina Lerman and Claudia Wagner



At least 20% of nodes in training sample to achieve ROCAUC > 0.8

Real-world (empirical) networks

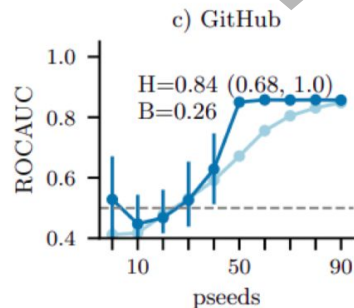
Model fitting



A more realistic representation

With asymmetric homophily

$$H_{mm} \neq H_{MM}$$

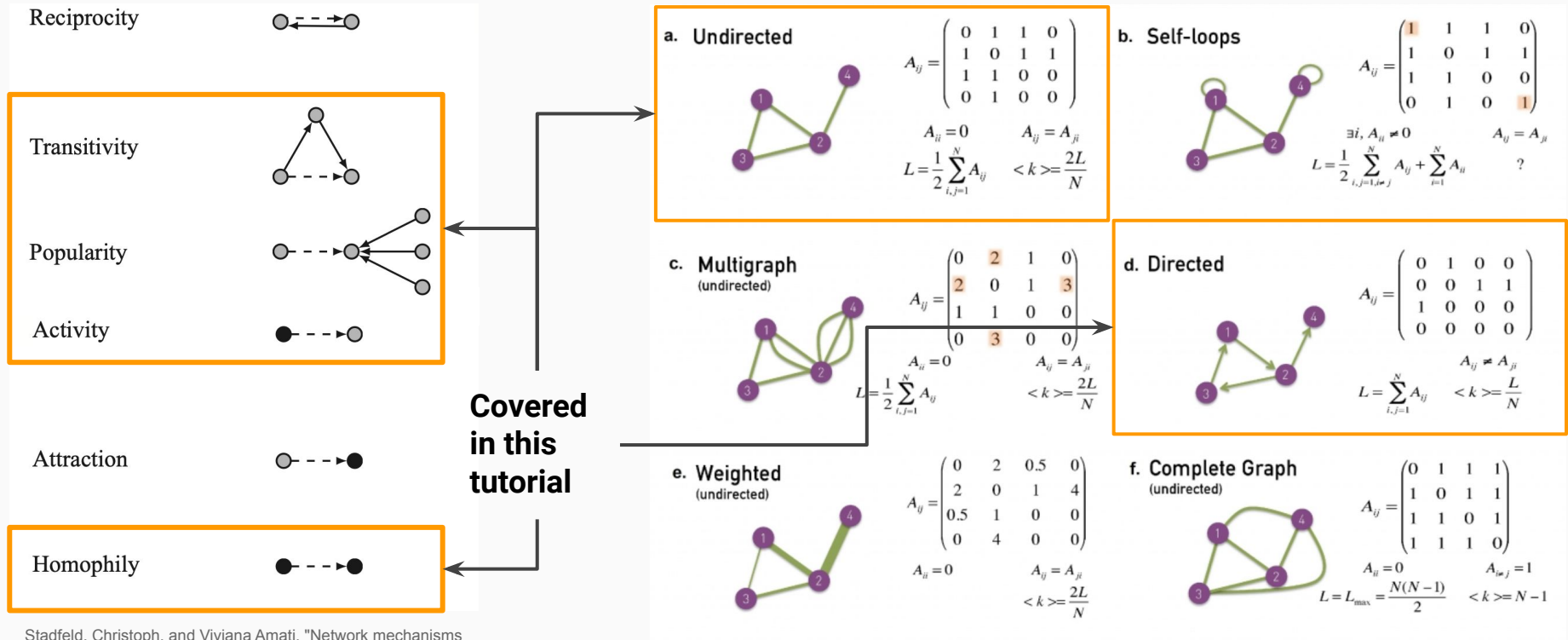


Closing remarks

Challenges & open questions

Tutor: Lisette Espín-Noboa

We need more realistic models!

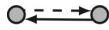


Stadfeld, Christoph, and Viviana Amati. "Network mechanisms and network models." Research Handbook on Analytical Sociology. Edward Elgar Publishing, 2021

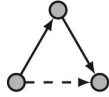
<http://networksciencebook.com/chapter/2#summary2>

We need more realistic models!

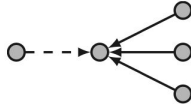
Reciprocity



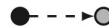
Transitivity



Popularity



Activity



What about these other types

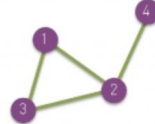
Attraction



Homophily



a. Undirected

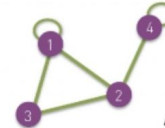


$$A_{ij} = \begin{pmatrix} 0 & 1 & 1 & 0 \\ 1 & 0 & 1 & 1 \\ 1 & 1 & 0 & 0 \\ 0 & 1 & 0 & 0 \end{pmatrix}$$

$$A_{ii} = 0 \quad A_{ij} = A_{ji}$$

$$L = \frac{1}{2} \sum_{i,j=1}^N A_{ij} \quad \langle k \rangle = \frac{2L}{N}$$

b. Self-loops

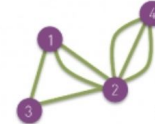


$$A_{ij} = \begin{pmatrix} 1 & 1 & 1 & 0 \\ 1 & 0 & 1 & 1 \\ 1 & 1 & 0 & 0 \\ 0 & 1 & 0 & 1 \end{pmatrix}$$

$$\exists i, A_{ii} \neq 0 \quad A_{ij} = A_{ji}$$

$$L = \frac{1}{2} \sum_{i,j=1, i \neq j}^N A_{ij} + \sum_{i=1}^N A_{ii} \quad ?$$

c. Multigraph (undirected)

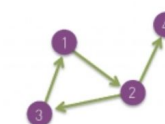


$$A_{ij} = \begin{pmatrix} 0 & 2 & 1 & 0 \\ 2 & 0 & 1 & 3 \\ 1 & 1 & 0 & 0 \\ 0 & 3 & 0 & 0 \end{pmatrix}$$

$$A_{ii} = 0 \quad A_{ij} = A_{ji}$$

$$L = \frac{1}{2} \sum_{i,j=1}^N A_{ij} \quad \langle k \rangle = \frac{2L}{N}$$

d. Directed

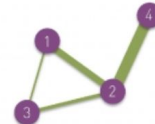


$$A_{ij} = \begin{pmatrix} 0 & 1 & 0 & 0 \\ 0 & 0 & 1 & 1 \\ 1 & 0 & 0 & 0 \\ 0 & 0 & 0 & 0 \end{pmatrix}$$

$$A_{ij} \neq A_{ji}$$

$$L = \sum_{i,j=1}^N A_{ij} \quad \langle k \rangle = \frac{L}{N}$$

e. Weighted (undirected)

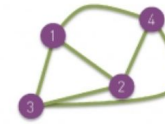


$$A_{ij} = \begin{pmatrix} 0 & 2 & 0.5 & 0 \\ 2 & 0 & 1 & 4 \\ 0.5 & 1 & 0 & 0 \\ 0 & 4 & 0 & 0 \end{pmatrix}$$

$$A_{ii} = 0 \quad A_{ij} = A_{ji}$$

$$\langle k \rangle = \frac{2L}{N}$$

f. Complete Graph (undirected)



$$A_{ij} = \begin{pmatrix} 0 & 1 & 1 & 1 \\ 1 & 0 & 1 & 1 \\ 1 & 1 & 0 & 1 \\ 1 & 1 & 1 & 0 \end{pmatrix}$$

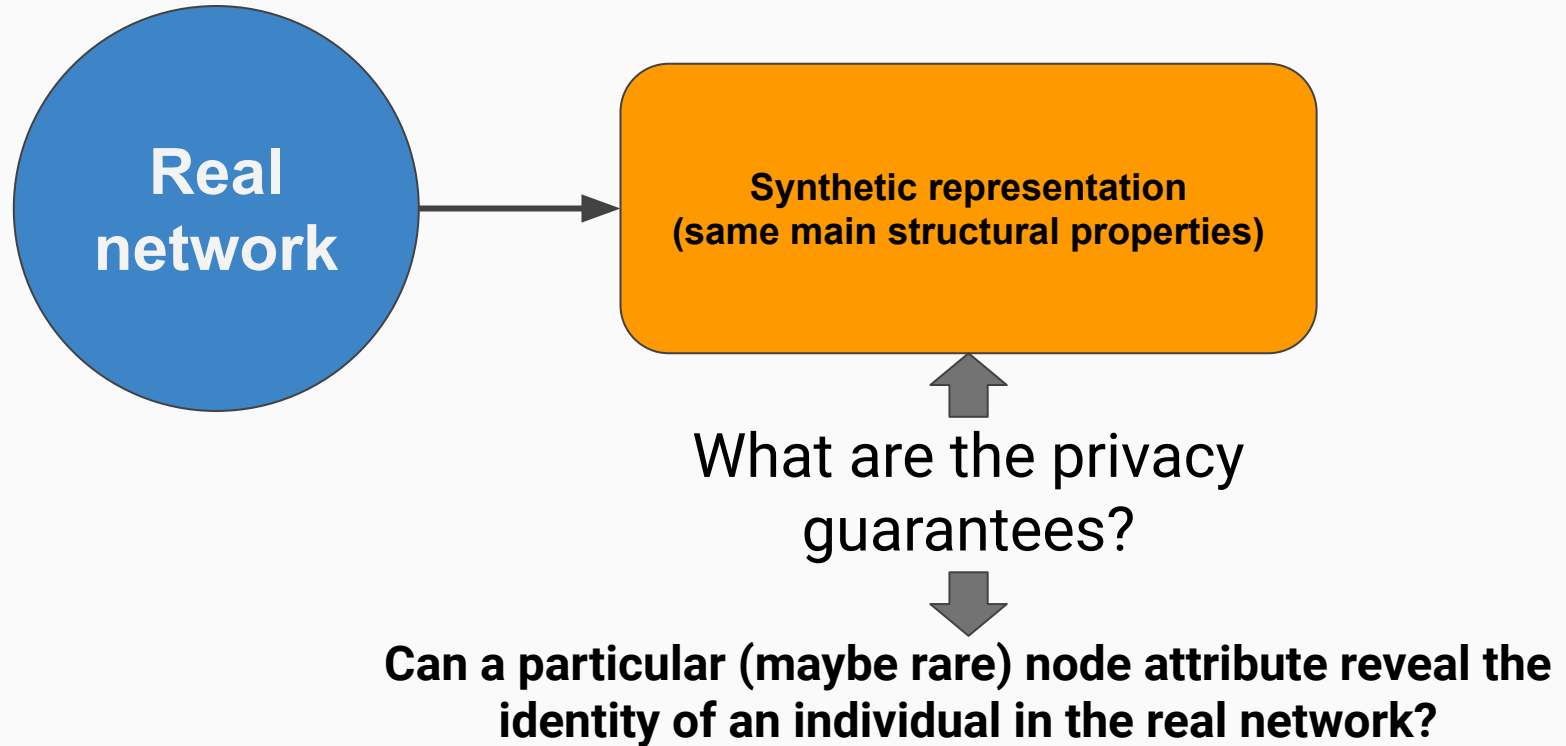
$$A_{ii} = 0 \quad A_{ij} = 1$$

$$L = L_{\max} = \frac{N(N-1)}{2} \quad \langle k \rangle = N-1$$

Stadfeld, Christoph, and Viviana Amati. "Network mechanisms and network models." Research Handbook on Analytical Sociology. Edward Elgar Publishing, 2021

<http://networksciencebook.com/chapter/2#summary2>

Do synthetic networks solve privacy issues for data sharing?



We appreciate your feedback.
Thank you very much!



bit.ly/snma2023-survey