

# **Analytics, have some humility: a statistical view of fourth down decision making**

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# In-game strategic decision making

- The mathematical basis of in-game strategic decision making is a *value function*  $V(x)$  which tells us the value of game-state  $x$
- In American football:
  1. Expected points (EP)
  2. Win probability (WP)
- Make the decision which maximizes the value of the next game-state
  - Make the fourth down decision in  $\{\text{Go}, \text{FG}, \text{Punt}\}$  which maximizes win probability

# Model Land

- Two ways to build these EP/WP models:
  1. Probabilistic state-space models
    - require detailed specification of all game-states, actions, and their transition probabilities; incredibly hard
    - “Gei gazinta hait” (Yiddish for “go in good health”)- explore these models on your own time, but will not be the subject of today’s talk
  2. Statistical models
    - Data-driven regression/ML models fit from historical data
    - Widely used today; we will focus on these models
    - We discovered several problems with the way they are implemented, fit, and applied

# **Expected points models**

# Well Known Expected Points Models

<b>Modeler</b>	<b>Model</b>	<b>Game-state Variables</b>	<b>Training set</b>	<b>Outcome Variable</b>
Romer (2006)	Instrumental variables regression	yardline	all plays	<i>Points of the next score, a real number in {7,3,2,0,-2,-3,-7}</i>
Burke (2009)	Linear regression with a spline	yardline	first down plays	$\wedge$
Yurko et al. (2018)	Multinomial logistic regression	yardline, down, log yards-to-go, time remaining, goal-to-go, under-two-minutes	all plays	<i>Outcome of the next score as categorical variable in {TD, FG, ...}</i> $EP = 7 \cdot \mathbb{P}(\text{TD}) + 3 \cdot \mathbb{P}(\text{FG}) + \dots$
Baldwin (2021)	XGBoost	yardline, down, yards-to-go, time remaining, timeouts, home, roof type, era	all plays	$\wedge$

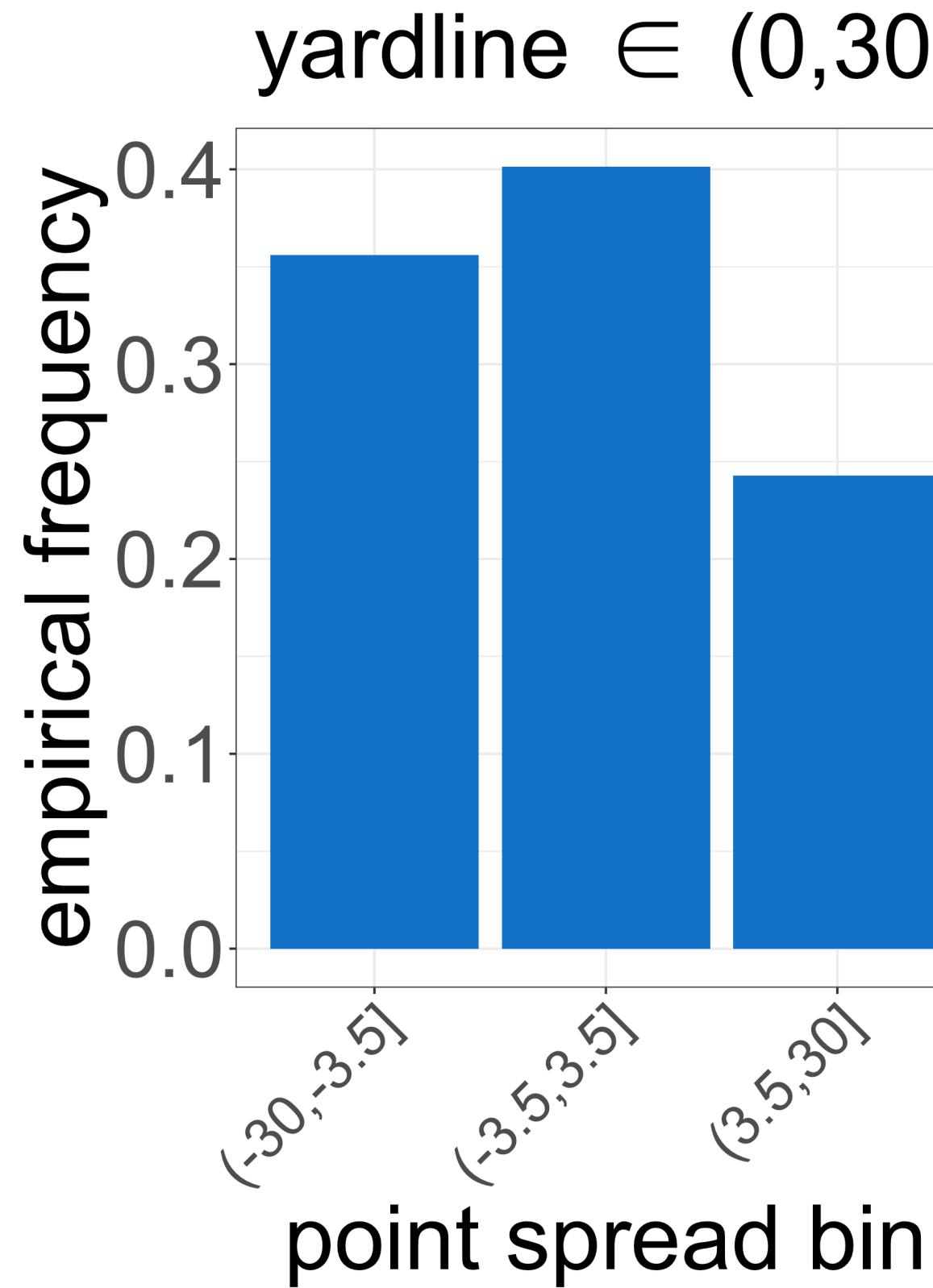
# EP models don't adjust for team quality

- Existing EP models are functions of yard-line, down, yards-to-go, time remaining, timeouts, etc.
- But these models don't adjust for team quality.
- Justification for omitting team quality:
  1. Models represent EP for an *average* offense facing an *average* defense, and so imply decision making for *average* teams.
  2. It is not easy to adjust for team quality alongside all these other variables, which have nonlinear relationships and interactions.

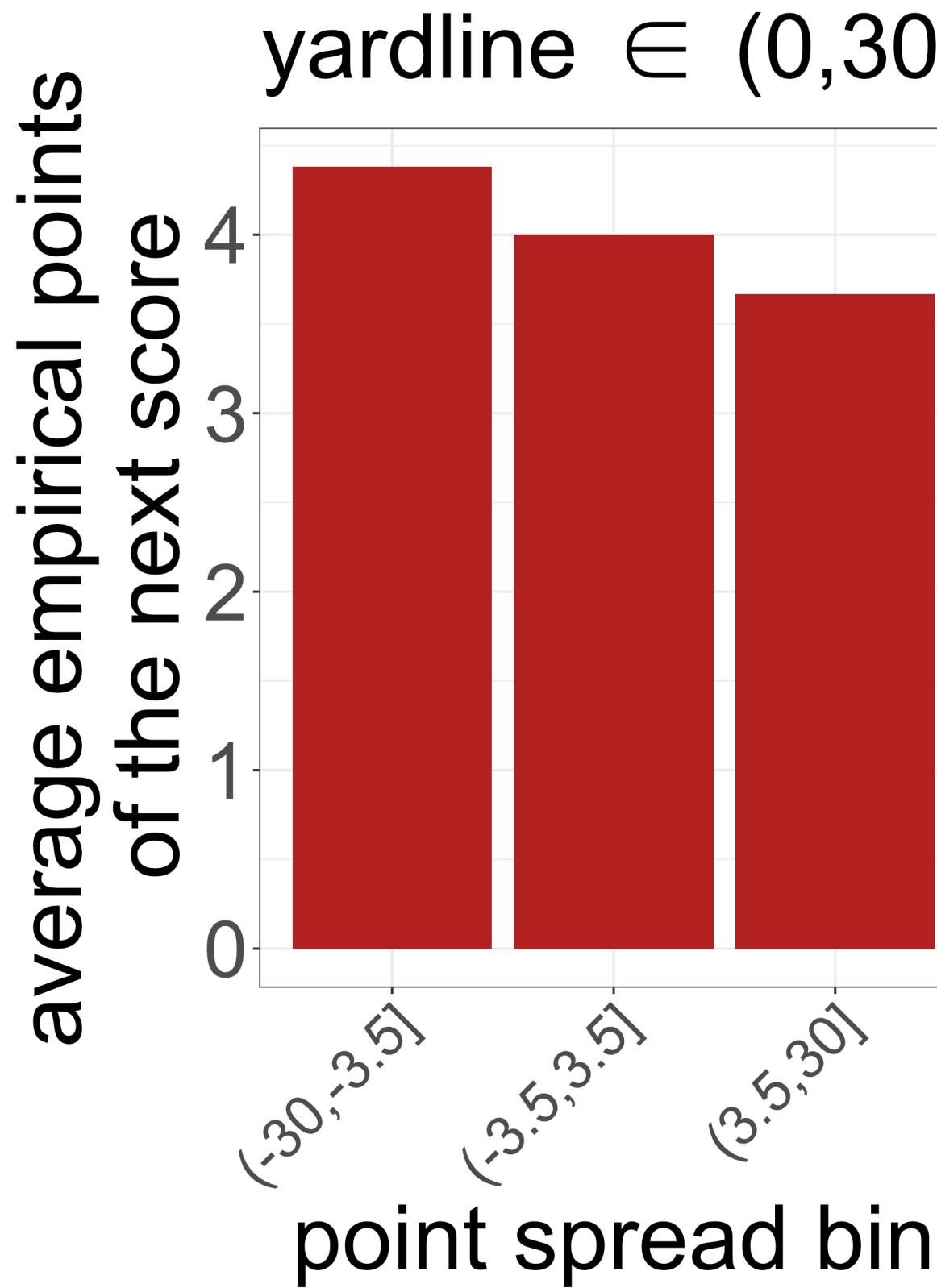
# Thought experiment

1. What is the probability that an “average” *NFL kicker* sinks a 70 yard field goal in neutral weather conditions?
2. What is the probability that *Justin Tucker* sinks a 70 yard field goal in neutral weather conditions?
3. What is the probability that a *randomly drawn kicker* sinks a 70 yard field goal in neutral weather conditions?

# Problem 1. EP models don't adjust for team quality



*Good  
teams have  
more plays*



*Good  
teams score  
more points*

Failing to adjust for team quality causes problems:

1. Models report EP for *randomly drawn teams*, not for average teams.
  - No team wants this!
  - No such thing as a decision made by a random team!
2. **selection bias** problem; EP models are especially wrong/biased

# We need to adjust for team quality

EP models that don't adjust for team quality are biased.

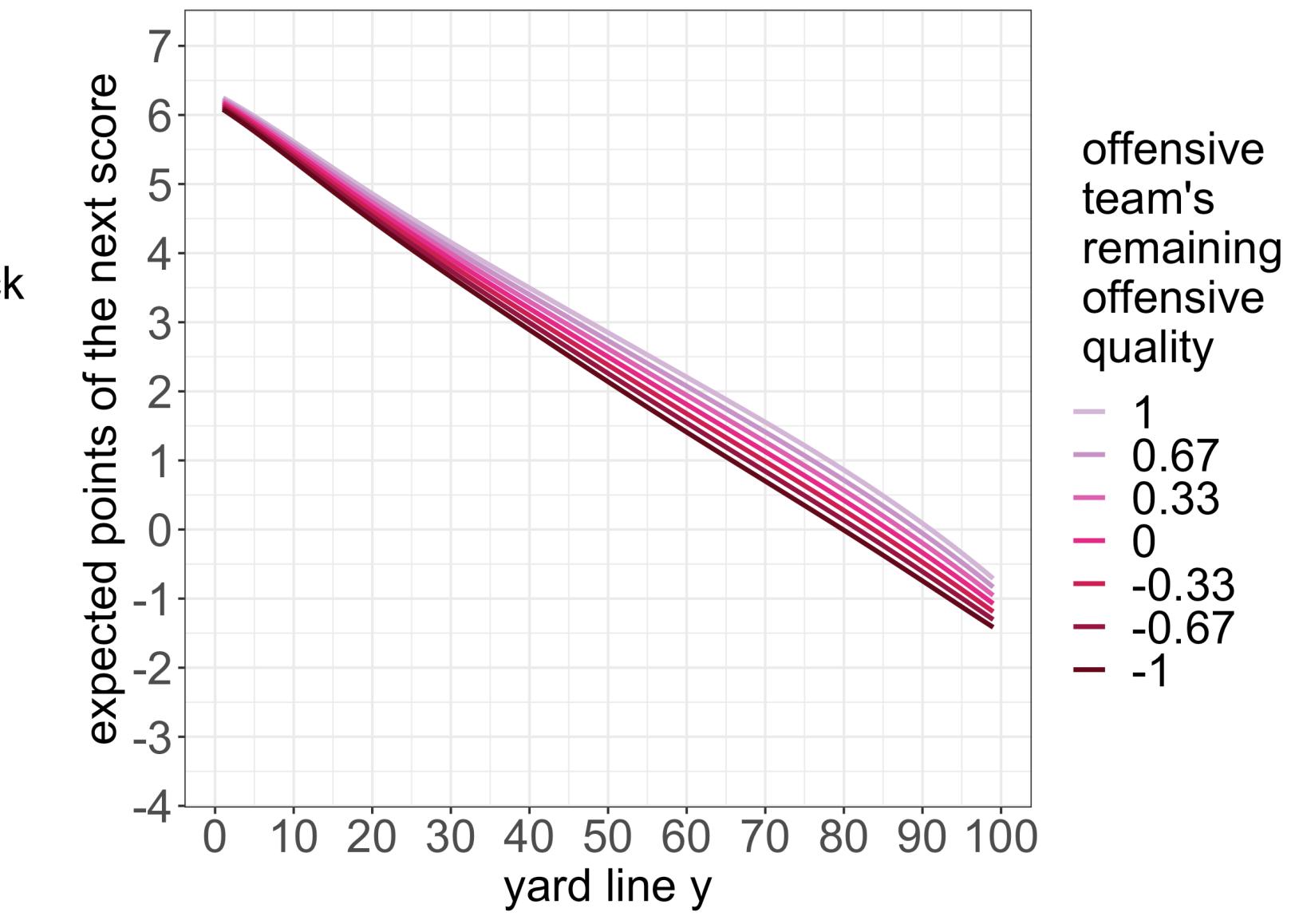
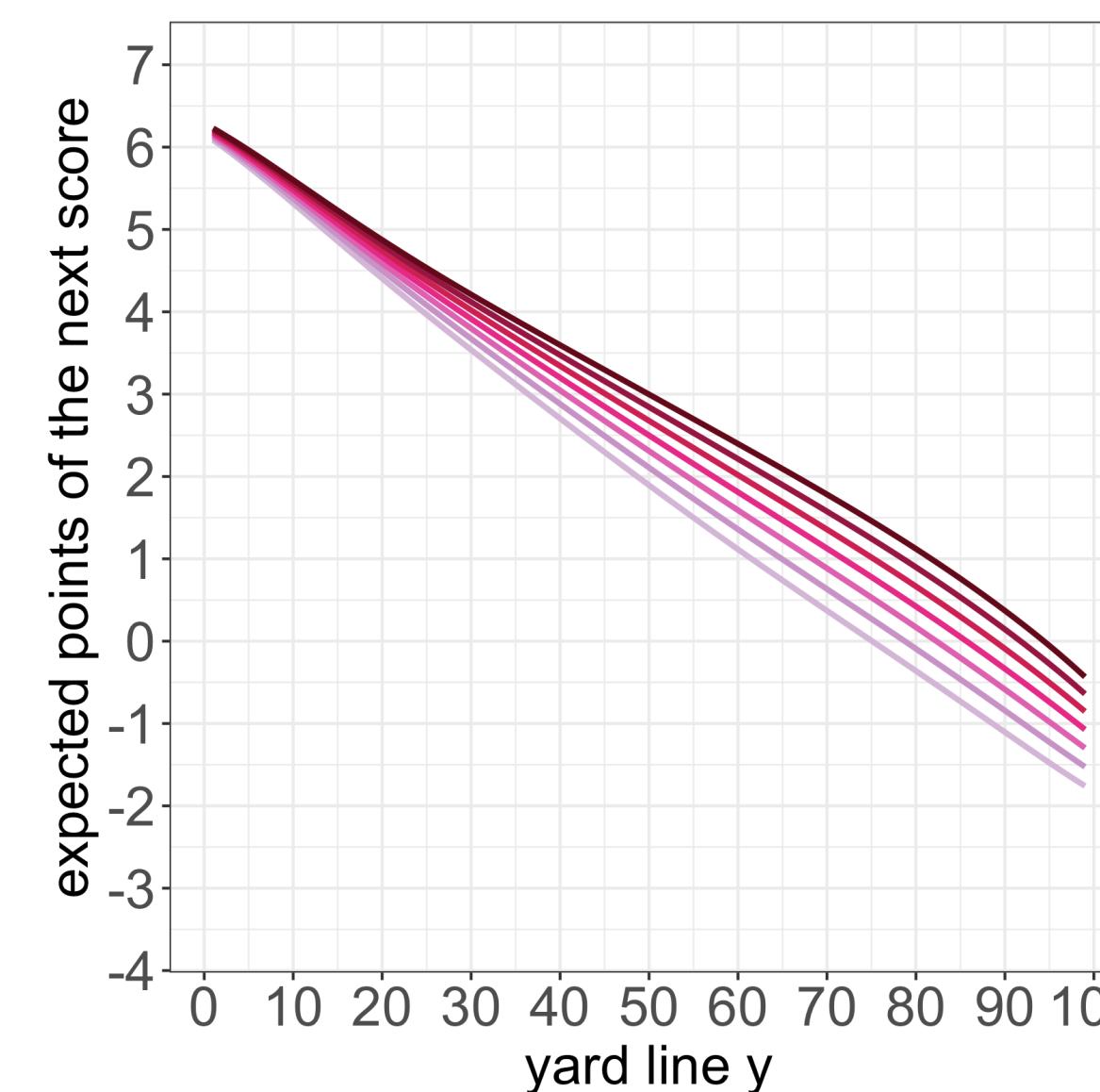
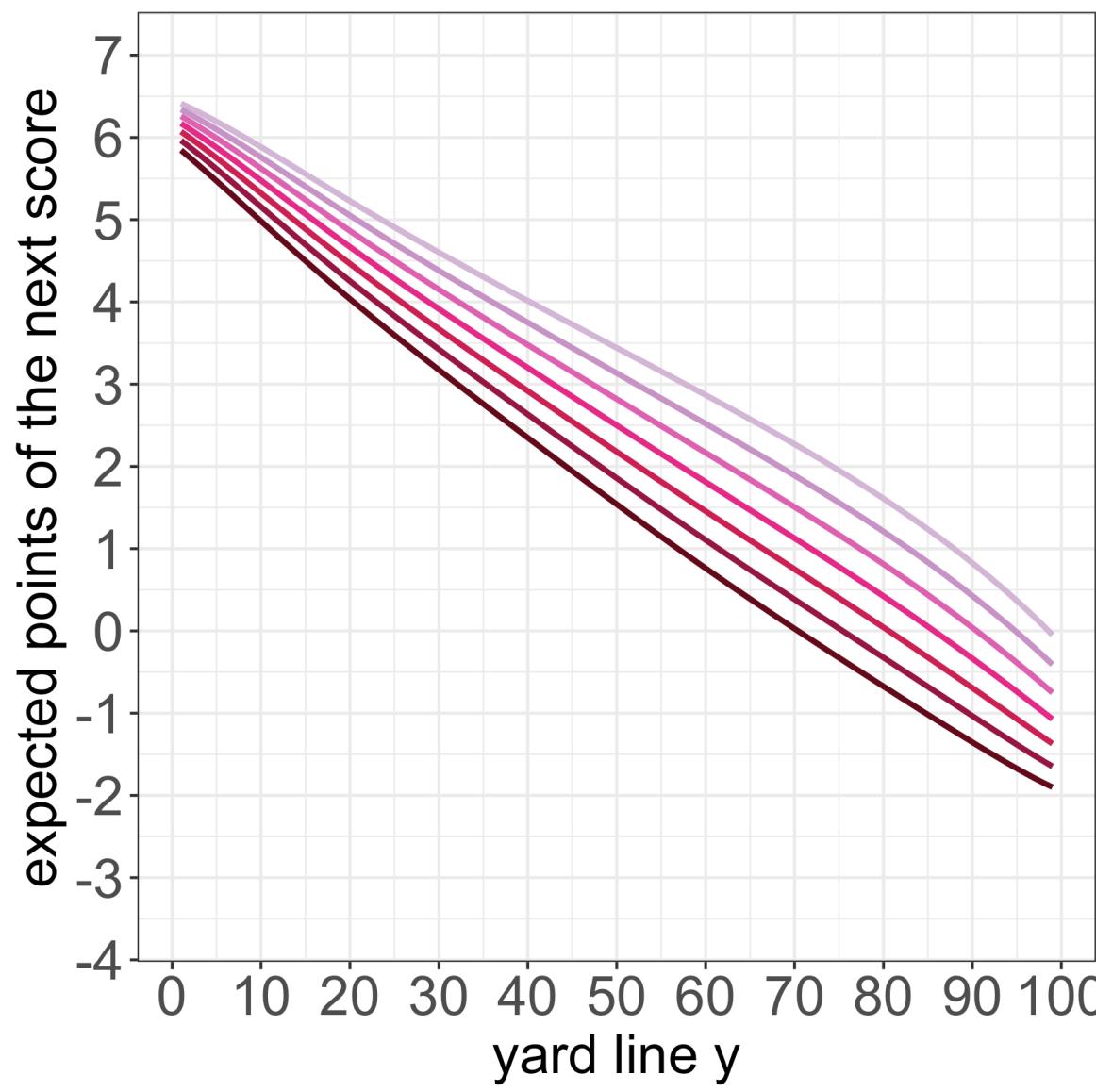
# Thought experiment 2

Suppose I have the following 8 aspects of team quality, each on the same scale, built from play success, and without data bleed. Then build an EP model with these 8 metrics as covariates.

- Rank in terms of (*predictive*) importance:
  - A. Offensive team's quarterback quality
  - B. Offensive team's non-quarterback offensive quality
  - C. Defensive team's defensive quality against the pass
  - D. Defensive team's defensive quality against the run
  - E. Offensive team's defensive quality against the pass
  - F. Offensive team's defensive quality against the run
  - G. Defensive team's quarterback quality
  - H. Defensive team's non-quarterback offensive quality

# Impact of various aspects of team quality

- Created our own 8 measures of offensive & defensive quality
  - Carefully controlled for data bleed
  - All 4 offensive quality metrics are more impactful than the defensive quality metrics
  - Quarterback quality of *both* teams matters more than other aspects of team quality!
- Output from an additive multinomial logistic regression model (similar to Yurko et al.'s):



# Problem 2. So many variables...

- We need to adjust for team quality
- Wow, that's a lot of variables – team quality, yardline, down, yards-to-go, time remaining, etc. – with nonlinearities & interactions
- The task is not easy: we need to fit a very big and very complicated machine learning model, but we don't want to overfit

# Problem 2. Bias-Variance Tradeoff

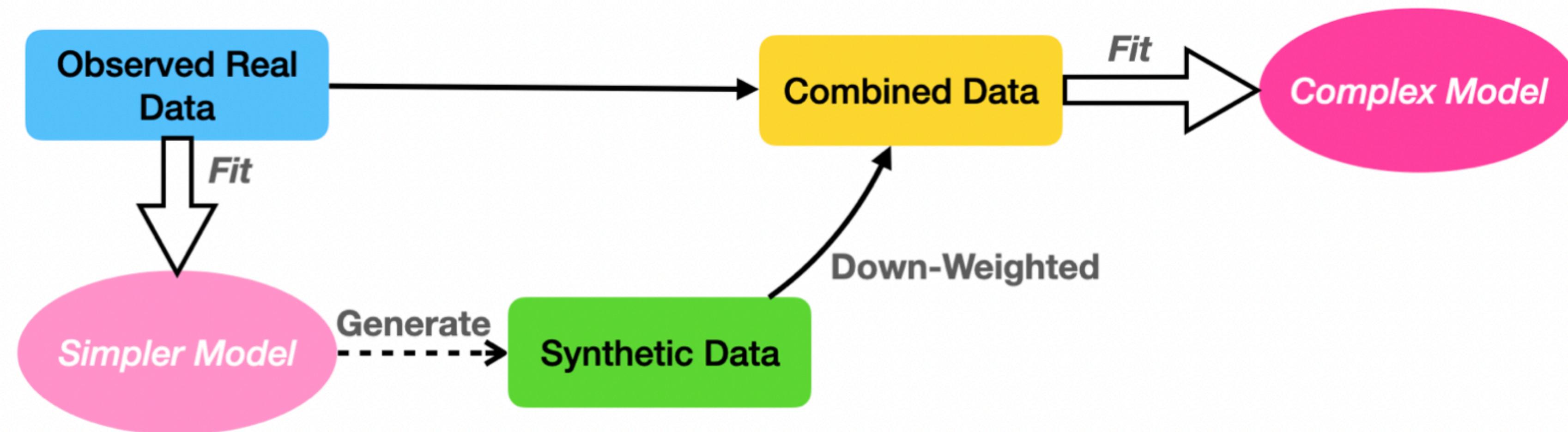
- We want to use machine learning to capture a complex high-dimensional function
- But ML models tend to aggressively overfit (play-by-play) data
- Typically deal with this using regularization or shrinkage towards simpler models
- Easily studied for parametric models in a Bayesian context; difficult for ML/trees

“The in-game models are not Bayesian. Congratulations to you if you can figure out how to do that. Most publicly available models are ... XGBoost models.”

— Brian Burke, Wharton Moneyball, 19 Sept. 2023

# Solution 2. Catalytic Priors to Mitigate Overfitting

- Inspired by Sam Kou's catalytic prior, we found a way to Laplace smooth tree ML models



# EP Model Comparison

Model name	Model type	Team quality	Out-of-sample MAE
Catalytic	<b>Catalytic XGBoost</b>	Yes	<b>3.744</b>
Yurko+	Multinomial logistic regression	Yes	3.749
Baldwin+	XGBoost classification	Yes	3.753
Baldwin (2021)	XGBoost classification	No	3.803
Yurko (2018)	Multinomial logistic regression	No	3.808
Burke (2009)	Linear regression	No	3.833
Romer (2006)	Instrumental variables regression	No	3.864

- EP models are biased and overfit, and we can improve upon that
- On subsets of plays our model is *much* better, and that can make a huge difference in decision making

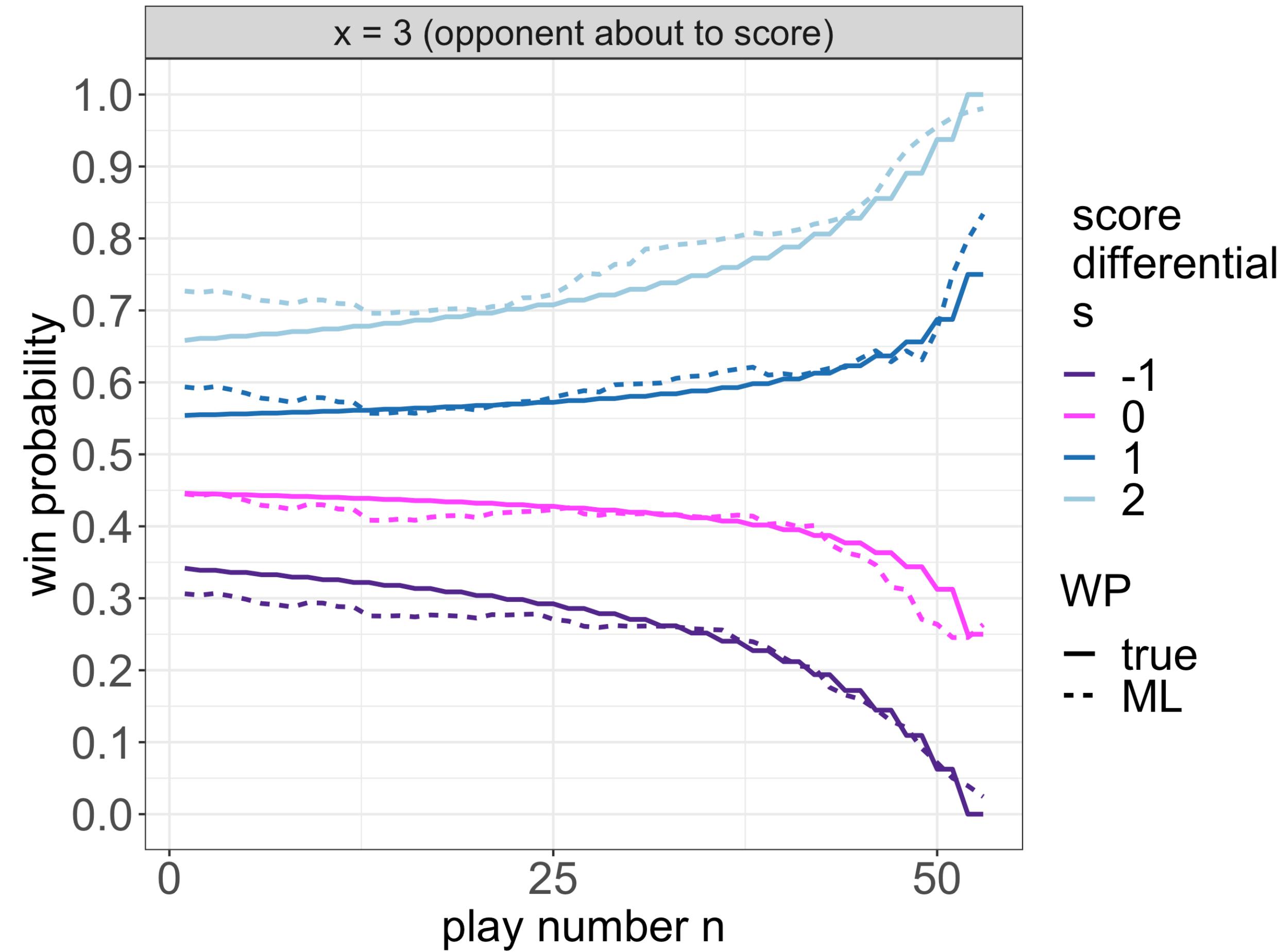
# **Win probability models**

# Problem 3. Highly Auto-Correlated Data

- Play-by-play dataset of  $\approx 500,000$  plays
- But, *not* 500,000 independent outcome variables
  - The response variable: 1 if the team with possession wins the game, else 0
- *Every game has only 1 winner* (auto-correlated data)
- Effective sample size is closer to 4,000 (num. games in the last 15 years)
- This is nowhere near enough data to experience the full variability of the nonlinear and interacting variables of score diff., time remaining, team quality, yardline, down, distance, timeouts, etc.

# WP Simulation

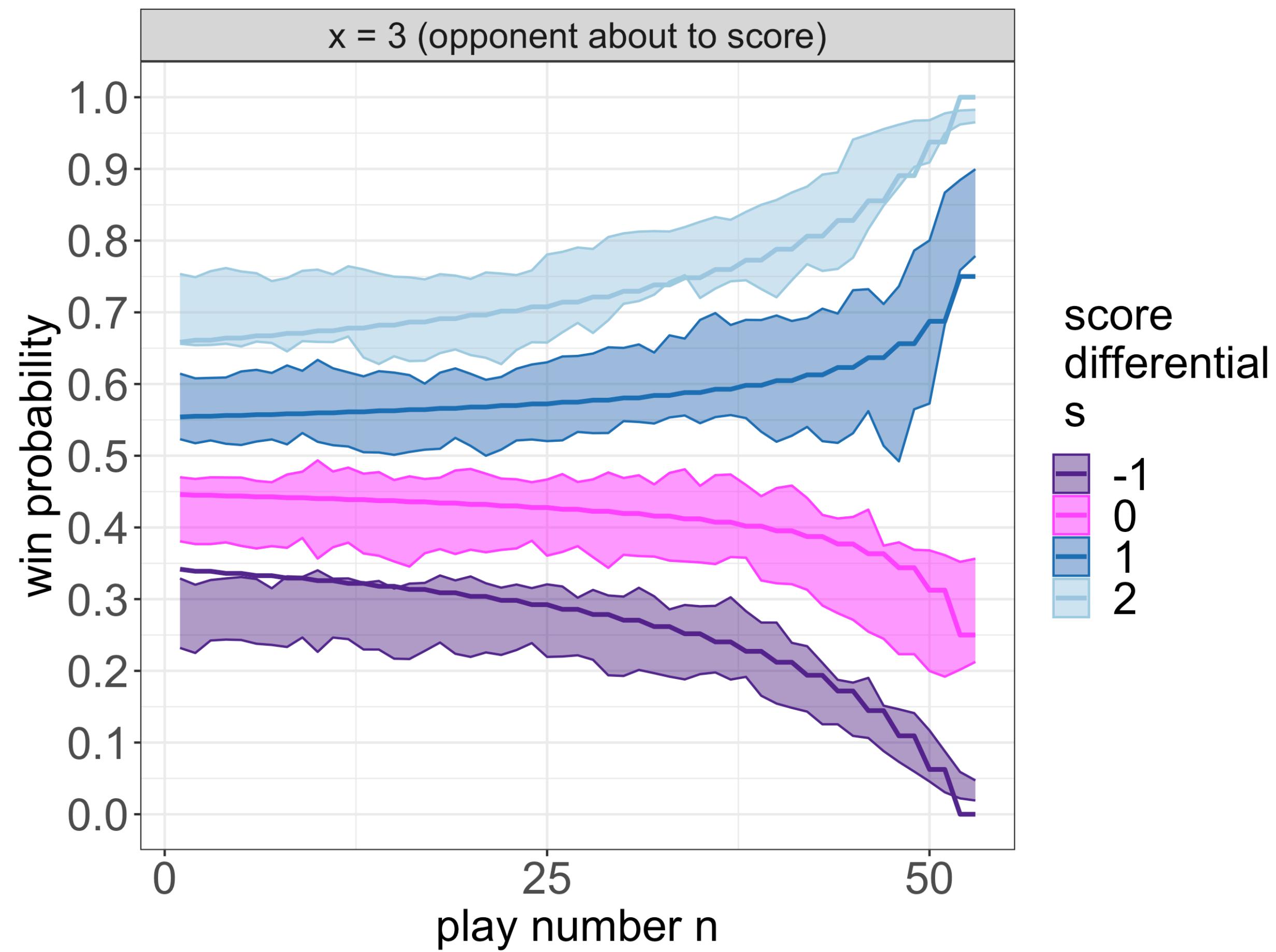
- To show you how hard it is to accurately fit WP using just  $\approx 4000$  games, we created a Random Walk version of football
- It's an extremely simple Random Walk but looks just like football!
- We can precisely calculate WP at every game-state
- Then, simulate a historical play-by-play dataset with auto-correlated win/loss response variable



- WP point estimates, fit using machine learning from one simulated dataset of simplified football plays, get the general trend right (are unbiased).

# WP Simulation

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- Bootstrapped WP confidence intervals, to achieve 90% coverage of true WP, need to be wide (8% WP on average).
- Real football exponentially more complex. Confidence intervals should be far wider.

# Quantifying uncertainty of the optimal fourth down decision

- Making fourth down decisions based solely on WP point estimates, which are highly uncertain, leads to overconfident decisions
- Quantify uncertainty in the 4th down decision by bootstrapping
  - the randomized cluster bootstrap accounts for autocorrelation
  - **boot %** – % of bootstrapped models which choose decision  $d \in \{\text{Go, FG, Punt}\}$

decision	WP	WP gain CI	boot %
Go for it	73.7%	[-3.7%, 4.5%]	53.8%
Field goal	72.2%		46.2%
Punt	65.5%		0.0%

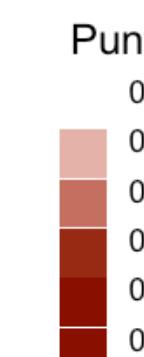
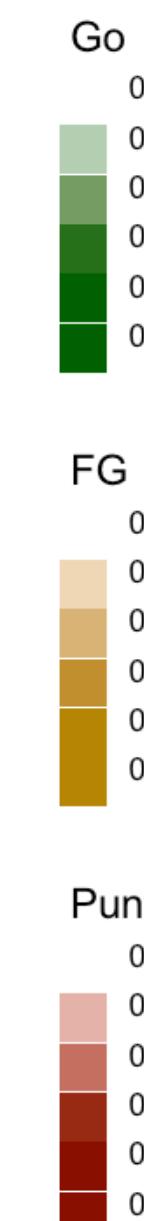
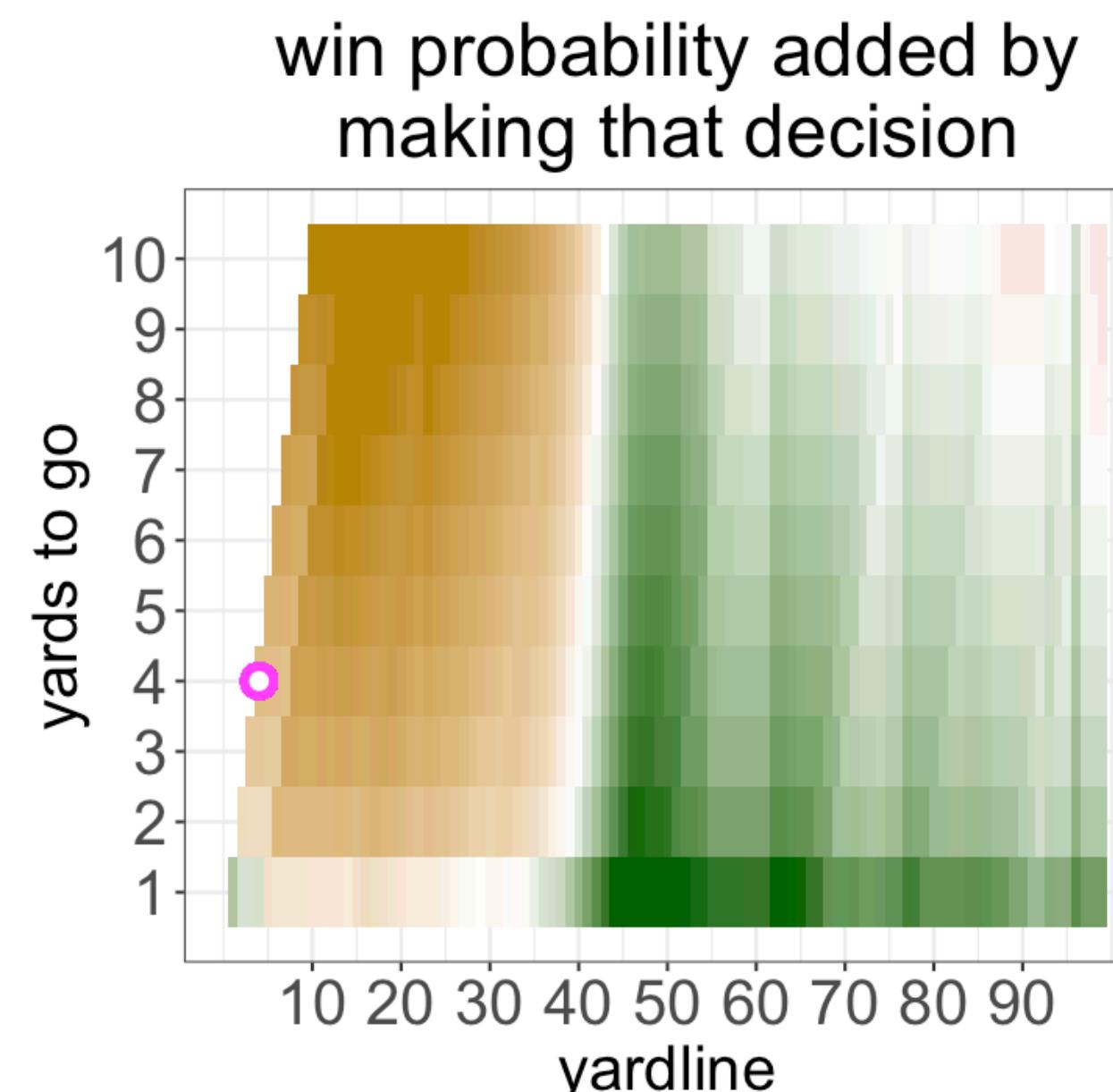
# **Example Plays: How Fourth Down Decision Making Changes**

# Example 1

- CHI @ NYJ in Week 12 of 2022

**FG looks like a strong decision based on the WP point estimate (+2%).**  
*Traditional analytics recommendation: Field goal attempt.*

Down 7, 4th & 4, 4 yards from opponent endzone						
Qtr 1, 6:00   Timeouts: Off 3, Def 3   Point Spread: 8.5						
decision	WP	success prob	WP if fail	WP if succeed	SD of WP	baseline coach %
Field goal	18.3%	98.6%	11.0%	18.4%	0.9%	85.1%
Go for it	16.2%	44.5%	11.0%	22.8%	5.9%	14.8%
Punt	9.9%					0.0%



# Example 1

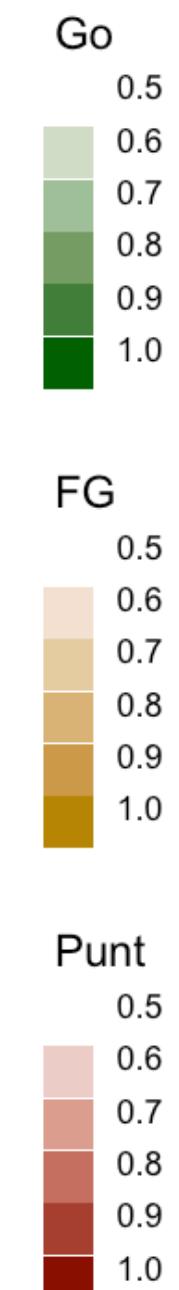
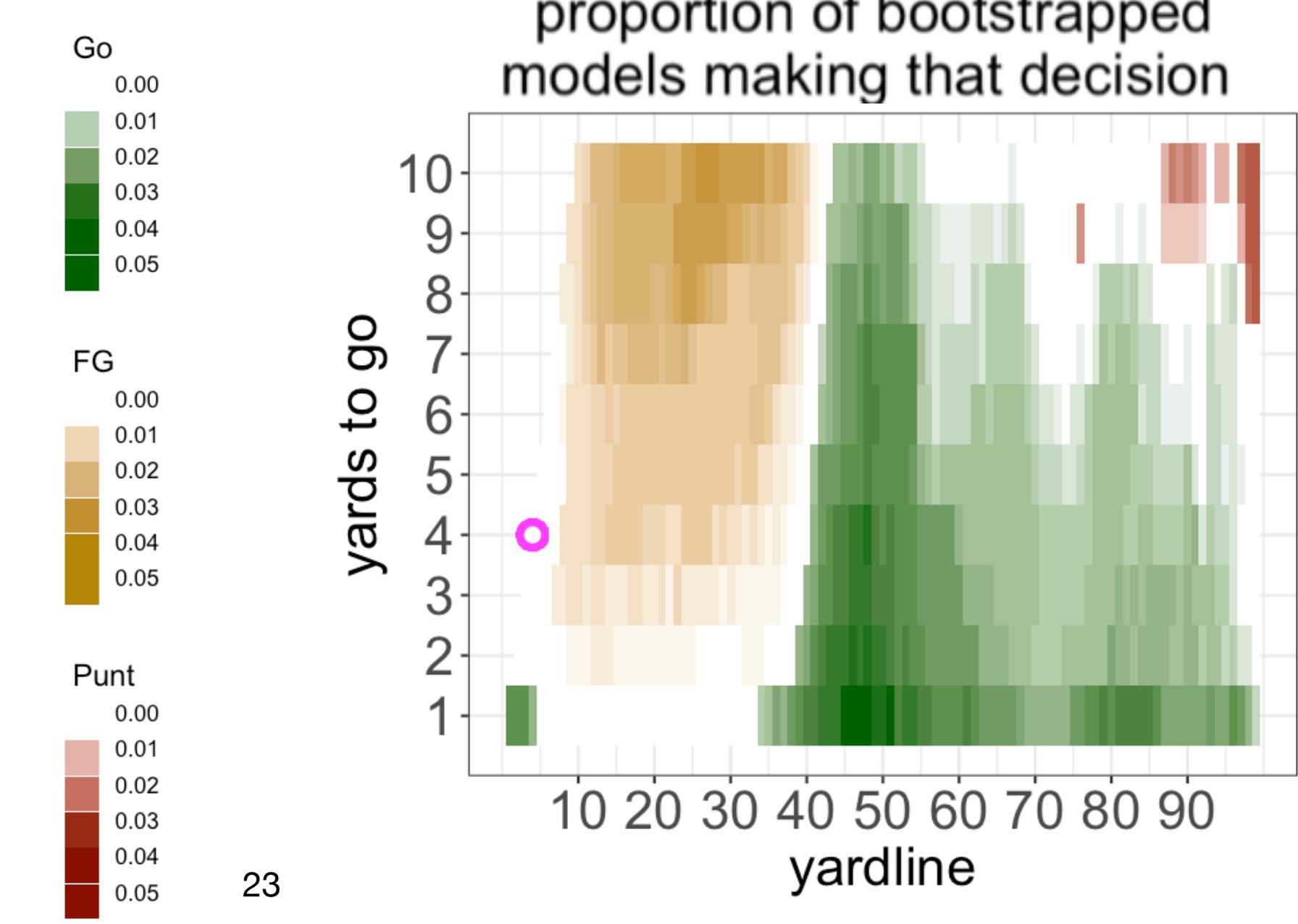
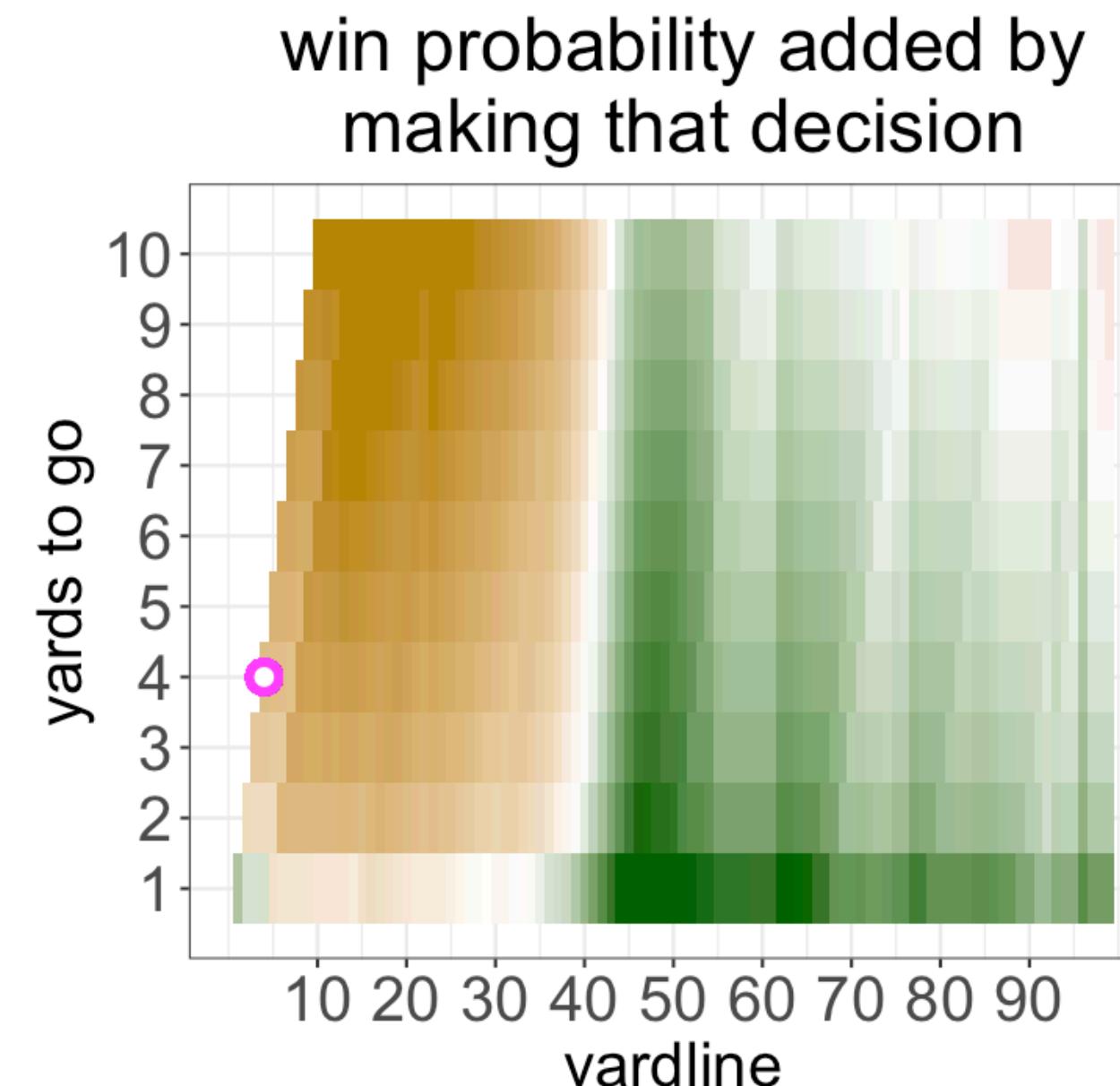
- CHI @ NYJ in Week 12 of 2022

**FG looks like a strong decision based on the WP point estimate,  
but we don't have enough data to trust our own point estimate.**

*Our recommendation: Coach's discretion.*

- For many plays the optimal decision is uncertain!

Down 7, 4th & 4, 4 yards from opponent endzone								
Qtr 1, 6:00   Timeouts: Off 3, Def 3   Point Spread: 8.5								
decision	WP	WP gain CI	boot %	success prob	WP if fail	WP if succeed	SD of WP	baseline coach %
Field goal	18.3%	[-3.7%, 4.4%]	42.3%	98.6%	11.0%	18.4%	0.9%	85.1%
Go for it	16.2%		57.7%	44.5%	11.0%	22.8%	5.9%	14.8%
Punt	9.9%		0.0%					0.0%



# Example 2

- WAS @ IND in Week 8 of 2022

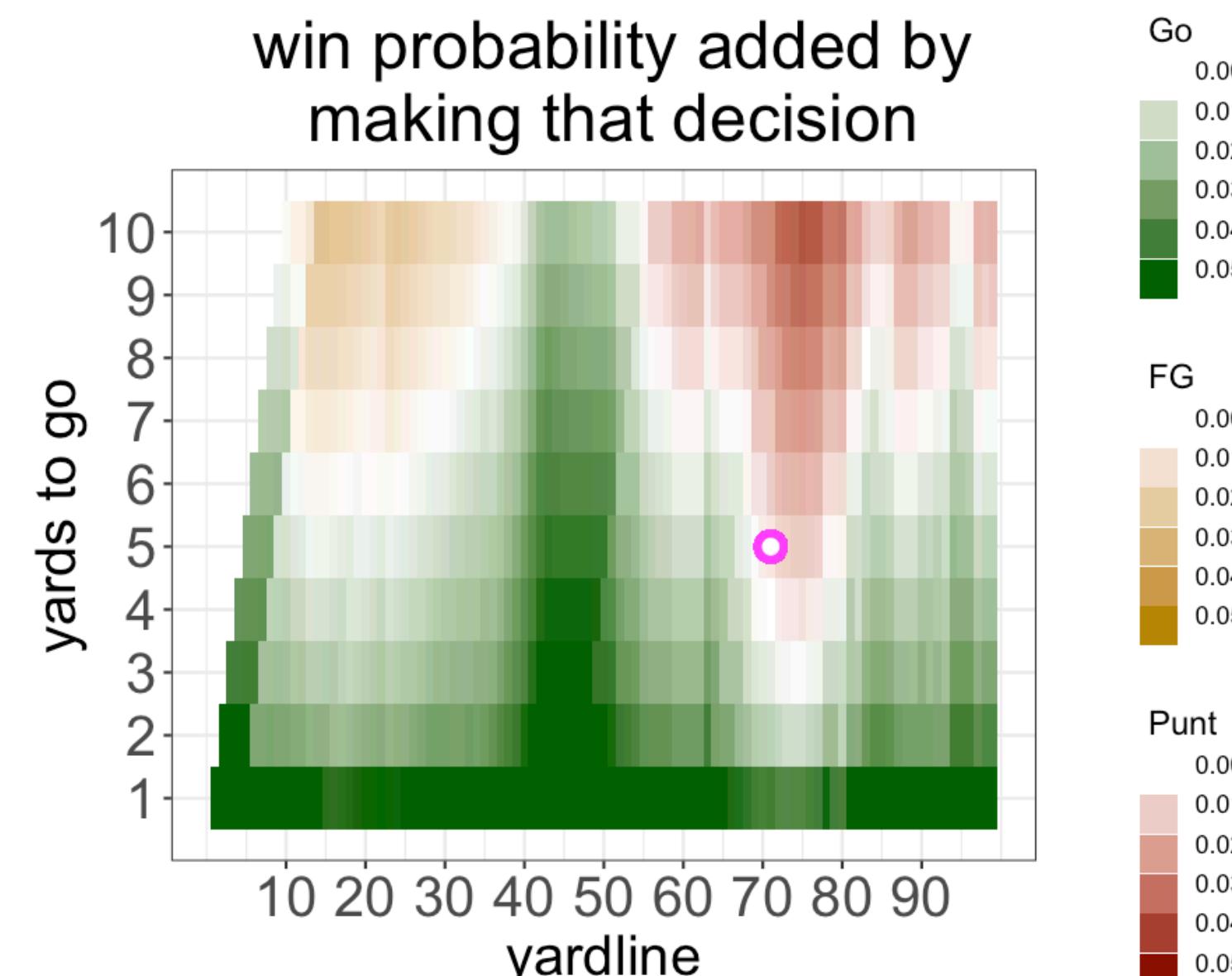
**Punt has a tiny estimated edge over Go (+0.05%).**

*Traditional analytics recommendation: Tossup, or slight lean towards punt.*

Up 1, 4th & 5, 71 yards from opponent endzone

Qtr 3, 6:00 | Timeouts: Off 3, Def 3 | Point Spread: 3

decision	WP	success prob	WP if fail	WP if succeed	SD of WP	baseline coach %
Punt	44.6%					93.3%
Go for it	44.1%	44.4%	34.4%	56.3%	10.8%	6.7%
Field goal	34.4%	0.0%	34.4%	56.0%	0.0%	0.0%



# Example 2

- WAS @ IND in Week 8 of 2022

Punt has a tiny estimated edge over Go,  
but we are confident that the edge is there.

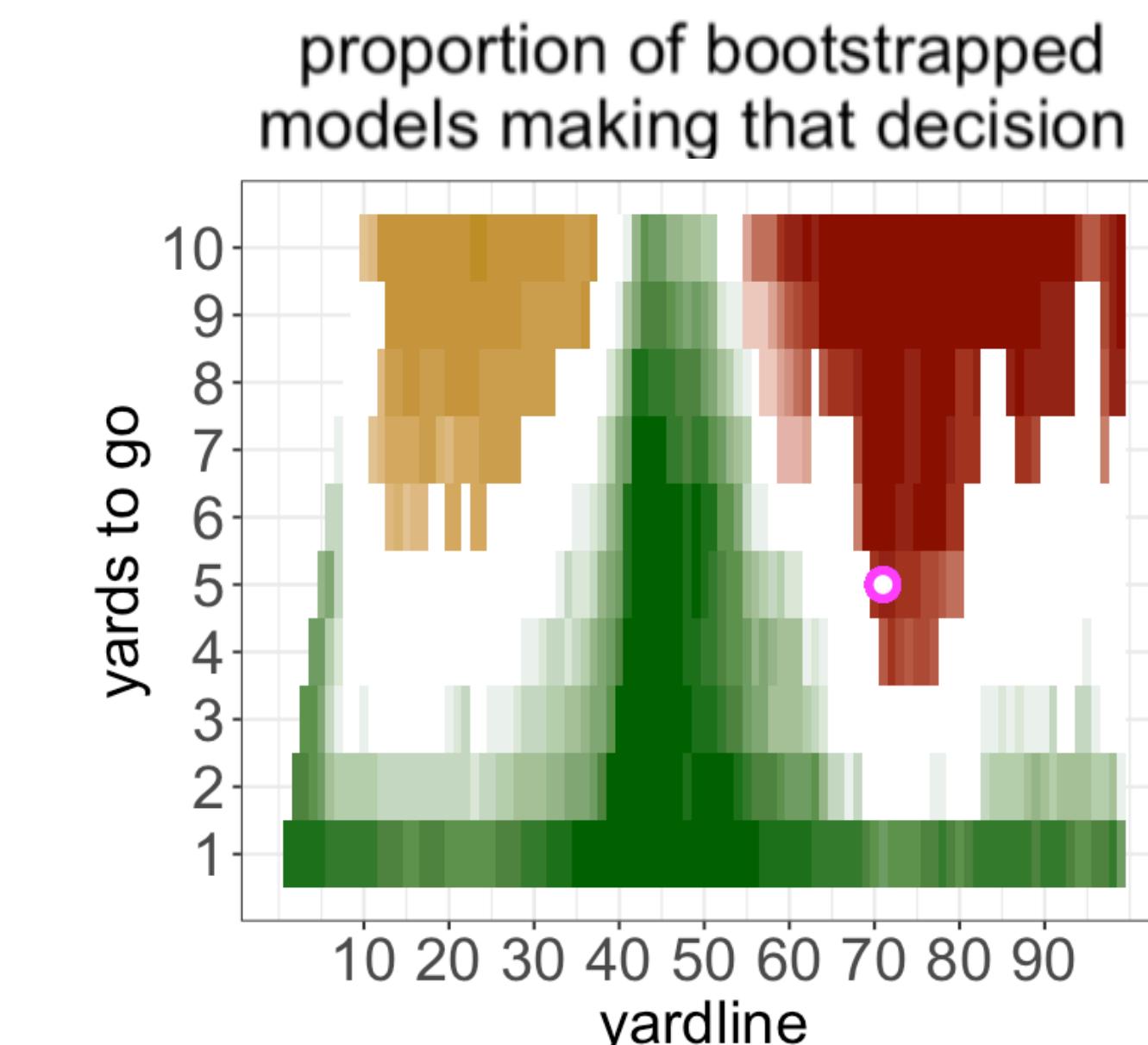
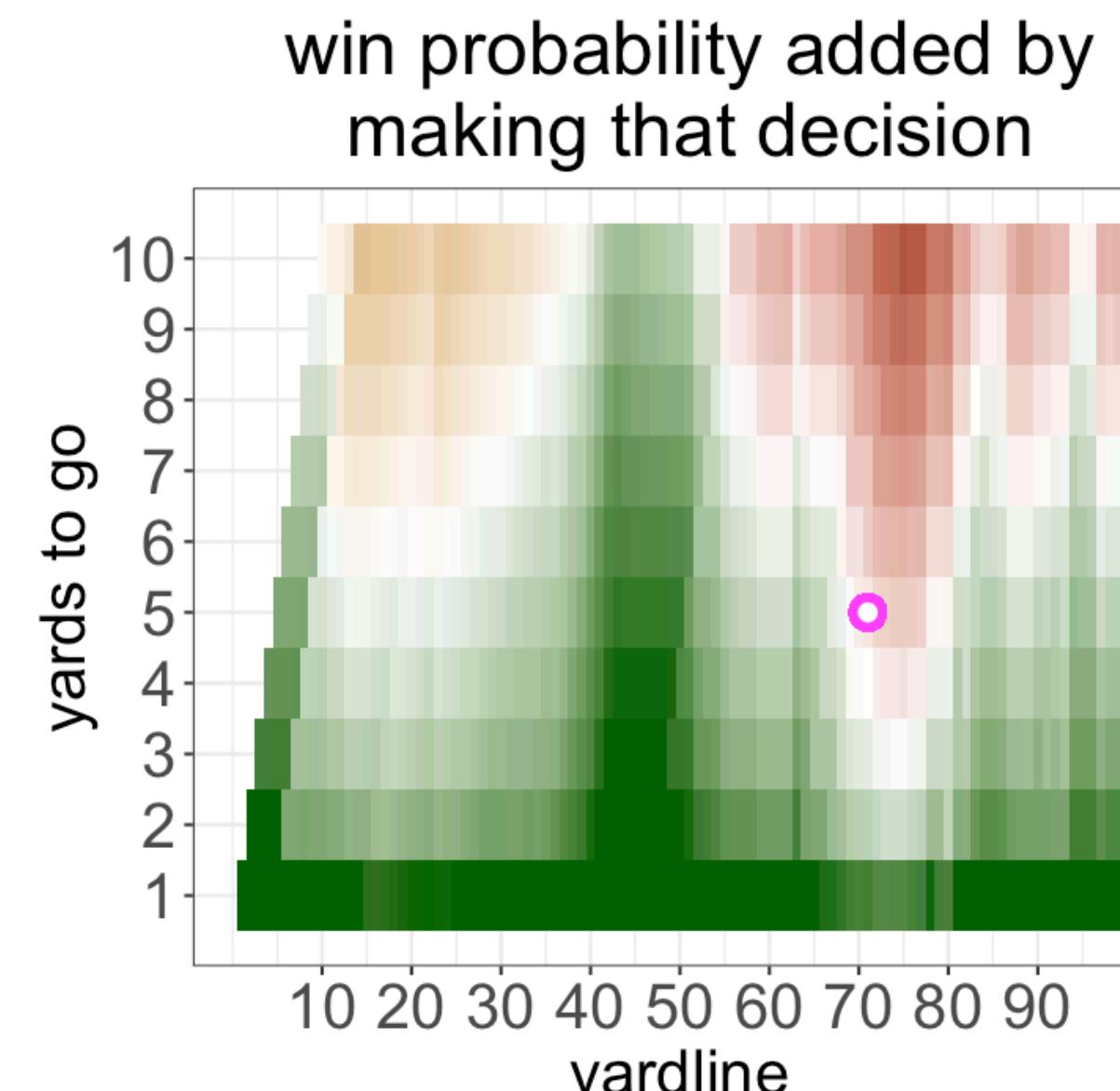
*Our recommendation: Punt (but not a tragedy if the coach overrides).*

- Eeking out these tiny (but confident) edges are valuable because many more of them occur per game.

Up 1, 4th & 5, 71 yards from opponent endzone

Qtr 3, 6:00 | Timeouts: Off 3, Def 3 | Point Spread: 3

decision	WP	WP gain CI	boot %	success prob	WP if fail	WP if succeed	SD of WP	baseline coach %
Punt	44.6%	[0.0%, 4.8%]	96.2%					93.3%
Go for it	44.1%		3.8%	44.5%	34.4%	56.3%	10.9%	6.7%
Field goal	34.4%		0.0%	0.0%	34.4%	56.0%	0.0%	0.0%

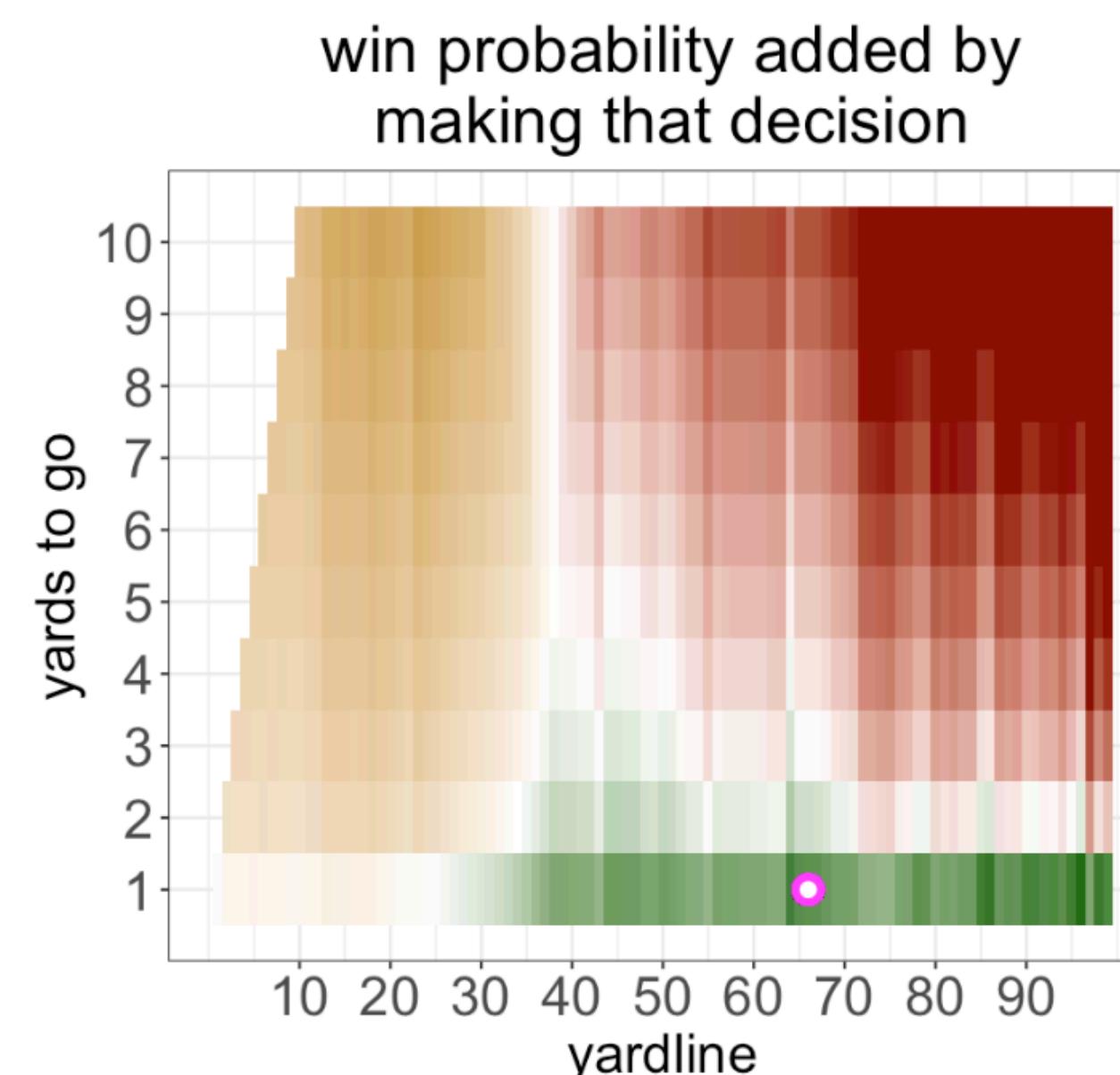


# Example 3

- LV @ LA in Week 14 of 2022

**Go is a strong decision based on the WP point estimate (+3.5%).**  
*Traditional analytics recommendation: Strong Go!*

Up 6, 4th & 1, 66 yards from opponent endzone						
Qtr 4, 2:00   Timeouts: Off 3, Def 3   Point Spread: -6.5						
decision	WP	success prob	WP if fail	WP if succeed	SD of WP	baseline coach %
Go for it	92.3%	68.8%	78.1%	98.7%	9.6%	22.9%
Punt	88.8%					77.1%
Field goal	78.1%	0.0%	78.1%	98.0%	0.0%	0.0%



# Example 3

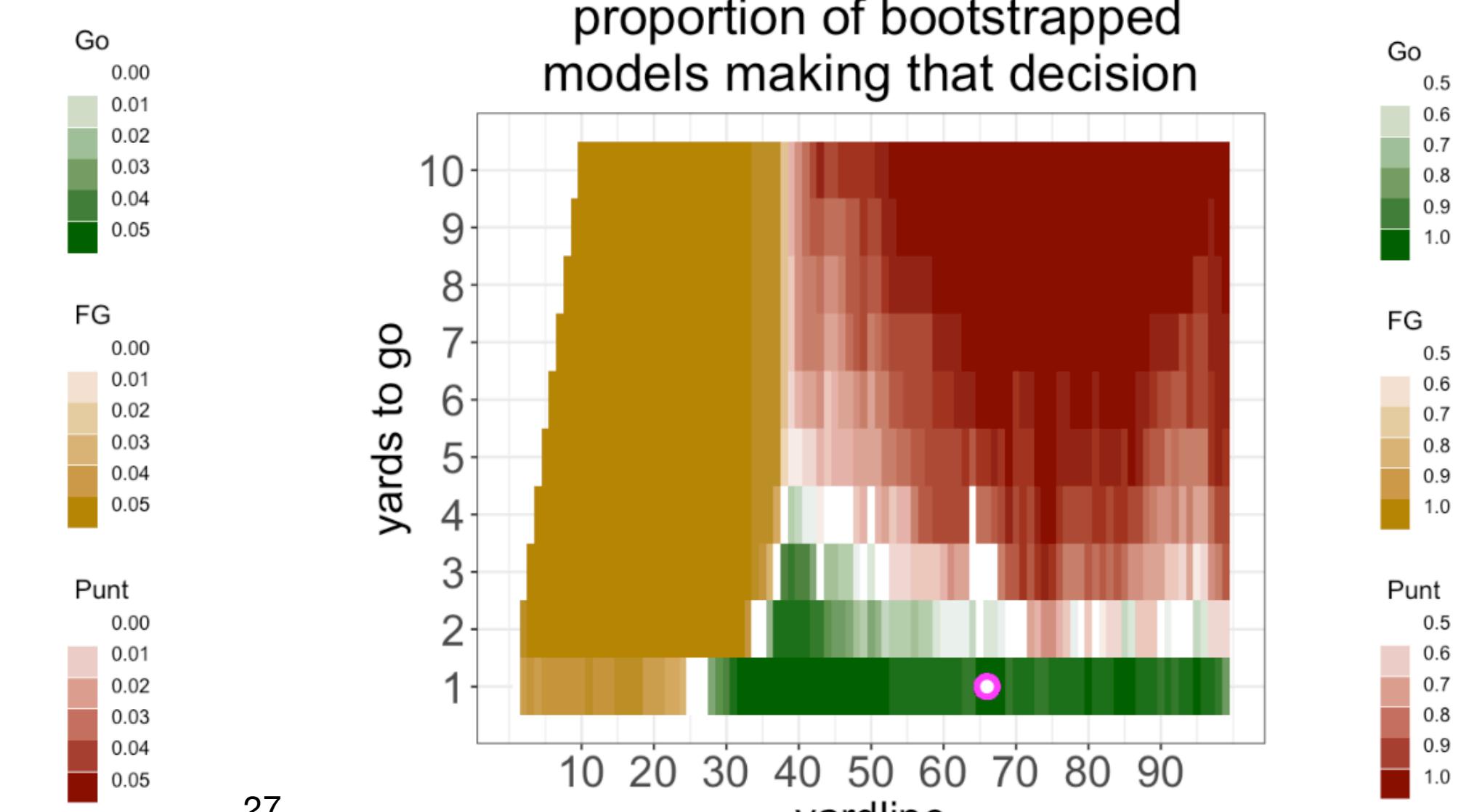
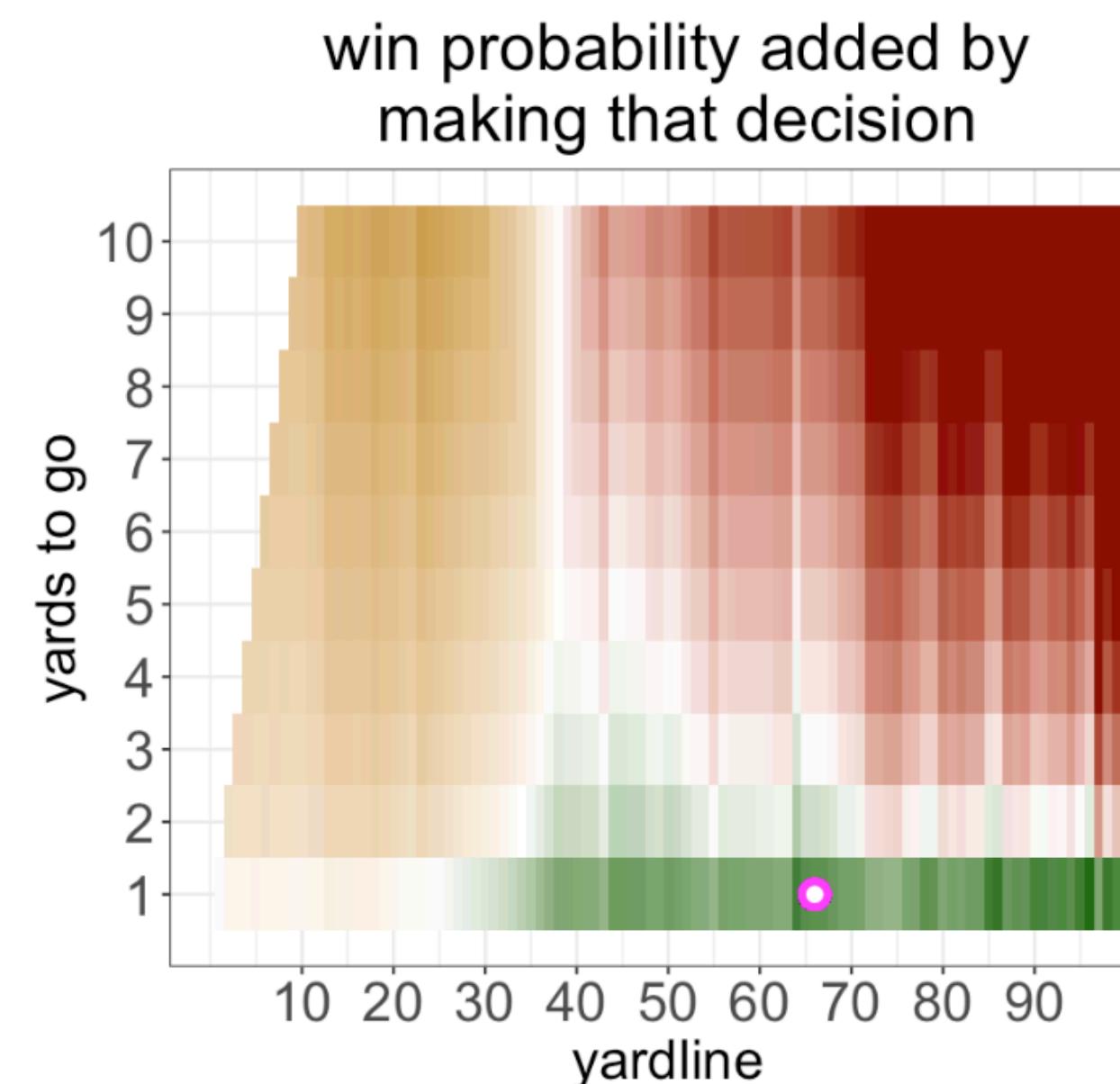
- LV @ LA in Week 14 of 2022

**Go is a strong decision based on the WP point estimate, and we are certain it is the best decision.**

*Our recommendation: Strong Go!*

(LV punted, then LA won after a Mayfield 98 yard game winning drive).

Up 6, 4th & 1, 66 yards from opponent endzone								
decision	WP	WP gain CI	boot %	success prob	WP if fail	WP if succeed	SD of WP	baseline coach %
Go for it	92.3%	[0.6%, 5.0%]	100.0%	68.8%	78.1%	98.7%	9.6%	22.9%
Punt	88.8%		0.0%					77.1%
Field goal	78.1%		0.0%	0.0%	78.1%	98.0%	0.0%	0.0%



# Analytics, Have Some Humility

- Team quality *must* be incorporated into EP/WP models
- We need shrinkage to mitigate overfitting in our ML models
- ***Humility:*** There are not enough games to fit an accurate statistical WP model to precisely learn the right fourth down decision at many game-states
- Far fewer 4th down decisions are as obvious as analysts widely claim

- Thank you!
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