Homework 3 Linear Regression: Experiment

CSE 847: Machine Learning

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Question1:

$$f(\omega) = \frac{1}{2} ||X\omega - y||_2^2 + \frac{\lambda}{2} ||\omega||_2^2$$
$$f'(\omega) = X^T X - X^T y + \lambda \omega$$
$$Let f'(\omega) = 0$$
$$X^T X \omega - X^T y + \lambda \omega = 0$$
$$\hat{\omega}_{Ridge} = \frac{X^T y}{\lambda I + X^T X}$$

The following function is used to compute the $\hat{\omega}_{Ridge}$ with the given x and y.

Question2: The following function is used to compute the MSE with the given $\hat{\omega}_{Ridge}$ x and y.

The follow codes are used to compute the MSE of different λ and plot them in the same figure.

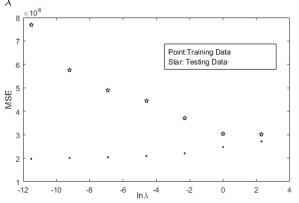
Following are the output results of both training and testing dataset

LamdaError =

1.0e+04 *

```
0.0000 0.0000 0.0000 0.0000 0.0000 0.0001 0.0010 1.9695 2.0060 2.0385 2.0919 2.2076 2.4731 2.7165 7.691 5.7532 4.9061 4.4405 3.6995 3.0518 3.0057
```

The plot of MSE of training and testing data under different



Question3: To perform 5-fold cross validation

```
Lamda(1:7) = [1e-5, 1e-4, 1e-3, 1e-2, 1e
-1, 1, 10]

for i=1 : 1 : 7

    for k=1 : 1 : 5

    KFC_testX=x_train(2+48*(k
-1):1+48*k,1:64)
```

```
KFC_{testY}=y_{train}(2+48*(k
                     -1):1+48*k,1)
                 KFC_{train}X(1:194,1:64) =
                     x_train([1:1+48*(k-1)
                     ,2+48*k:242],1:64)
                 KFC\_trainY=y\_train
                     ([1:1+48*(k-1),2+48*k
                     :242])
                 KFC_w=RidgeReg(KFC_trainX,
                      KFC_trainY, Lamda(i))
                 KFC_MSE(k) = MSE(KFC_w,
                     KFC_testX , KFC_testY)
         end
        Lam_MSE(i) = mean(KFC_MSE)
end
Lam_MSE
```

Lam_MSE =

1.0e+05 *

1.2870 0.9394 0.6376 0.4533 0.3369 0.2889 0.2801

It shows that the best λ for estimated from the training data is 10

```
.m file for the codes in HW3:
https://github.com/snotman/CSE847-Machine-
Learning-Project/tree/master/HW3
```