Stt864 Lab2

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Q1(a)

```
setwd("C://Users//caonan//Desktop//LAB2")
flintlead<-read.csv(file="Flint-water-lead-dataset.csv",header=FALSE)
colnames(flintlead)=c("SampleID","ZipCode","Ward", "Osec", "45sec", "120sec")
table(flintlead[2])</pre>
```

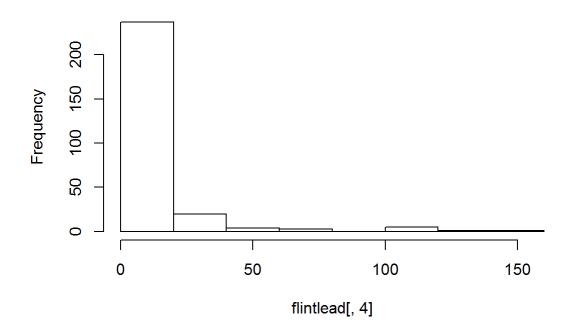
```
##
## 48502 48503 48504 48505 48506 48507 48529 48532
## 1 69 55 48 44 51 1 2
```

They are not evenly sampled.

Q1(b)

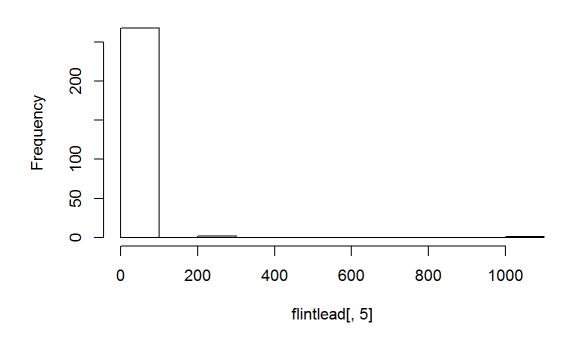
```
hist(flintlead[,4])
```

Histogram of flintlead[, 4]



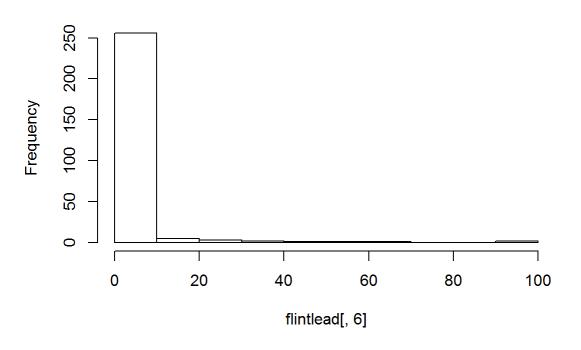
```
hist(flintlead[,5])
```

Histogram of flintlead[, 5]



hist(flintlead[,6])

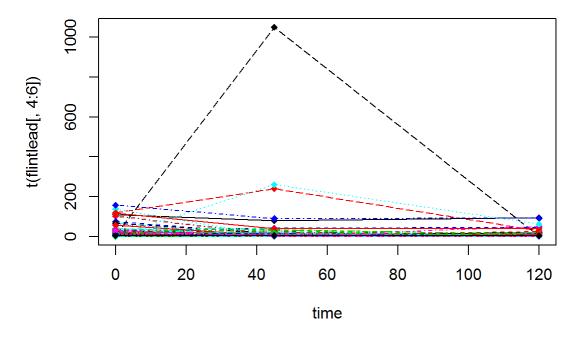
Histogram of flintlead[, 6]



All three histograms have

the shape of "L" Q1(c)

```
time<-c(0, 45, 120)
matplot(time, t(flintlead[,4:6]),pch=18,type="o")</pre>
```



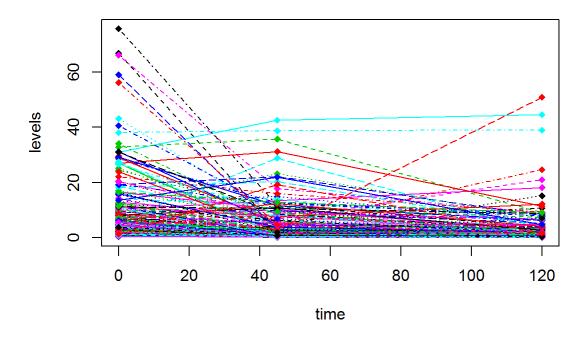
There's an extreme value

larger than 1000.

```
flintlead2<-flintlead[
  (flintlead[,4]<100)&(flintlead[,5]<100)&(flintlead[,6]<100),
]</pre>
```

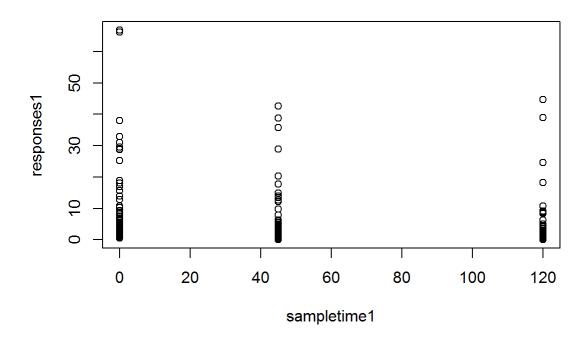
Q1(d)

There are some nonlinearity

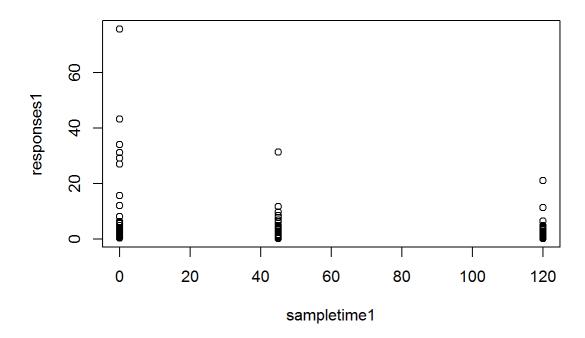


patterns Q2

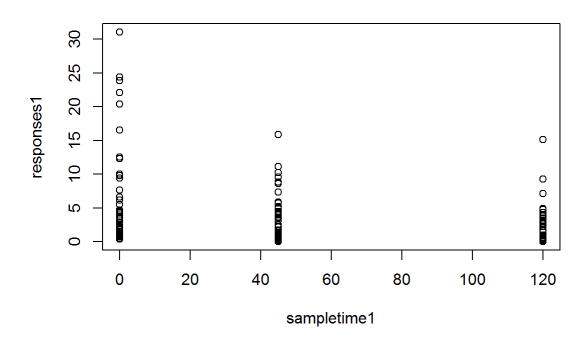
```
Coef_Matr1<-matrix(0,5,2)</pre>
Coef_Matr2<-matrix(0,5,3)</pre>
Sigma_Matr<-matrix(0,5,2)</pre>
for(i in 48503:48507){
zipcode<-which(flintlead2[,2]==i)</pre>
subsetflintlead<-flintlead2[zipcode,]</pre>
responses1<-unlist(subsetflintlead[,4:6])</pre>
sampletime1<-rep(time,each=dim(subsetflintlead)[1])</pre>
plot(sampletime1, responses1)
nlsreg1<-nls(responses1~theta1*exp(-sampletime1*theta2),</pre>
              start=list(theta1=5,theta2=0.02))
nlsreg2<-nls(responses1~theta1/(1+theta2*(exp(sampletime1*theta3))),</pre>
              start=list(theta1=2,theta2=-0.7,theta3=-0.025))
Coef Matr1[i-48502,]<-coef(nlsreg1)</pre>
Coef_Matr2[i-48502,]<-coef(nlsreg2)</pre>
Sigma_Matr[i-48502,]<-c(summary(nlsreg1)$sigma,summary(nlsreg2)$sigma)
print(summary(nlsreg1))
print(summary(nlsreg2))
```



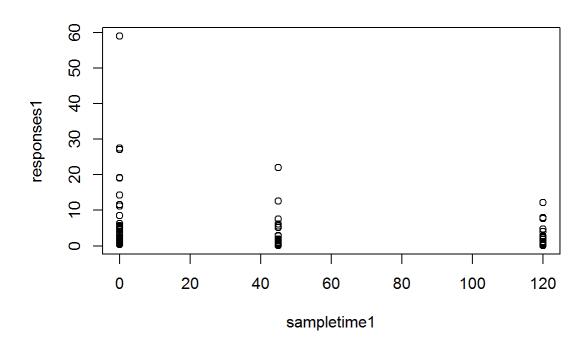
```
##
## Formula: responses1 ~ theta1 * exp(-sampletime1 * theta2)
##
## Parameters:
          Estimate Std. Error t value Pr(>|t|)
                     1.193044
                                7.772 3.84e-13 ***
## theta1 9.272776
## theta2 0.008745
                     0.003117
                                2.805 0.00552 **
## Signif. codes: 0 '***' 0.001 '**' 0.01 '*' 0.05 '.' 0.1 ' ' 1
## Residual standard error: 10.4 on 202 degrees of freedom
##
## Number of iterations to convergence: 4
## Achieved convergence tolerance: 9.347e-06
##
##
## Formula: responses1 ~ theta1/(1 + theta2 * (exp(sampletime1 * theta3)))
## Parameters:
           Estimate Std. Error t value Pr(>|t|)
## theta1 2.462919
                      5.532201
                                 0.445
                                           0.657
## theta2 -0.742616
                      0.575919
                               -1.289
                                           0.199
## theta3 -0.006411
                      0.025204
                               -0.254
                                           0.799
##
## Residual standard error: 10.41 on 201 degrees of freedom
## Number of iterations to convergence: 5
## Achieved convergence tolerance: 1.476e-07
```



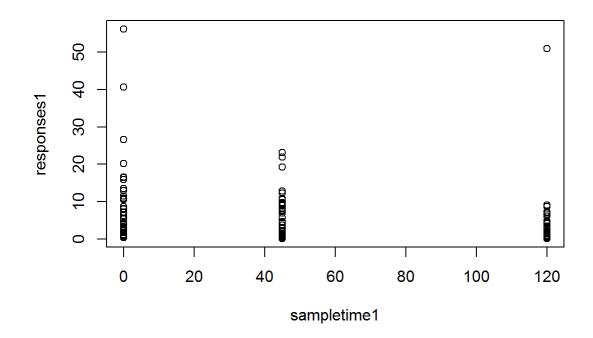
```
##
## Formula: responses1 ~ theta1 * exp(-sampletime1 * theta2)
##
## Parameters:
          Estimate Std. Error t value Pr(>|t|)
                      1.20428
                                6.204 5.24e-09 ***
## thetal 7.47117
                                         0.014 *
## theta2 0.01601
                      0.00644
                                2.486
## Signif. codes: 0 '***' 0.001 '**' 0.01 '*' 0.05 '.' 0.1 ' ' 1
## Residual standard error: 8.668 on 148 degrees of freedom
##
## Number of iterations to convergence: 6
## Achieved convergence tolerance: 5.917e-06
##
##
## Formula: responses1 ~ theta1/(1 + theta2 * (exp(sampletime1 * theta3)))
## Parameters:
           Estimate Std. Error t value Pr(>|t|)
                      3.973293
                                0.294
## thetal 1.167818
                                          0.769
## theta2 -0.847368
                      0.519010
                               -1.633
                                           0.105
## theta3 -0.007078
                      0.036573
                               -0.194
                                          0.847
##
## Residual standard error: 8.68 on 147 degrees of freedom
## Number of iterations to convergence: 4
## Achieved convergence tolerance: 9.57e-08
```



```
##
## Formula: responses1 ~ theta1 * exp(-sampletime1 * theta2)
##
## Parameters:
          Estimate Std. Error t value Pr(>|t|)
                     0.689998
                                8.539 1.89e-14 ***
## thetal 5.891855
## theta2 0.010384
                     0.003191
                                3.254 0.00142 **
## Signif. codes: 0 '***' 0.001 '**' 0.01 '*' 0.05 '.' 0.1 ' ' 1
## Residual standard error: 4.996 on 142 degrees of freedom
##
## Number of iterations to convergence: 6
## Achieved convergence tolerance: 8.061e-06
##
##
## Formula: responses1 ~ theta1/(1 + theta2 * (exp(sampletime1 * theta3)))
## Parameters:
           Estimate Std. Error t value Pr(>|t|)
## thetal 1.445314
                      2.643304
                                 0.547
                                          0.5854
                                          0.0804 .
## theta2 -0.762648
                      0.433083
                               -1.761
## theta3 -0.007398
                      0.023681
                               -0.312
                                          0.7552
## ---
## Signif. codes: 0 '***' 0.001 '**' 0.01 '*' 0.05 '.' 0.1 ' ' 1
## Residual standard error: 4.997 on 141 degrees of freedom
##
## Number of iterations to convergence: 5
## Achieved convergence tolerance: 1.254e-10
```



```
## Formula: responses1 ~ theta1 * exp(-sampletime1 * theta2)
##
## Parameters:
          Estimate Std. Error t value Pr(>|t|)
## thetal 6.501135
                     1.031689
                                6.301 4.69e-09 ***
## theta2 0.020066
                     0.008106
                                2.476
                                       0.0147 *
## ---
## Signif. codes: 0 '***' 0.001 '**' 0.01 '*' 0.05 '.' 0.1 ' ' 1
## Residual standard error: 6.742 on 124 degrees of freedom
##
## Number of iterations to convergence: 2
## Achieved convergence tolerance: 8.089e-06
##
##
## Formula: responses1 ~ theta1/(1 + theta2 * (exp(sampletime1 * theta3)))
##
## Parameters:
          Estimate Std. Error t value Pr(>|t|)
##
## thetal 1.23301
                      2.08397
                                0.592
## theta2 -0.81399
                      0.31537 - 2.581
                                         0.011 *
                      0.05044
## theta3 -0.01462
                               -0.290
                                         0.772
## ---
## Signif. codes: 0 '***' 0.001 '**' 0.01 '*' 0.05 '.' 0.1 ' ' 1
## Residual standard error: 6.744 on 123 degrees of freedom
## Number of iterations to convergence: 3
## Achieved convergence tolerance: 5.566e-08
```



```
##
## Formula: responses1 ~ theta1 * exp(-sampletime1 * theta2)
##
## Parameters:
          Estimate Std. Error t value Pr(>|t|)
##
## thetal 7.895872
                     1.072104
                                7.365 1.15e-11 ***
## theta2 0.009423
                     0.003454
                                2.728 0.00715 **
## ---
## Signif. codes: 0 '***' 0.001 '**' 0.01 '*' 0.05 '.' 0.1 ' ' 1
## Residual standard error: 7.973 on 148 degrees of freedom
##
## Number of iterations to convergence: 4
## Achieved convergence tolerance: 2.032e-06
##
##
## Formula: responses1 ~ theta1/(1 + theta2 * (exp(sampletime1 * theta3)))
##
## Parameters:
           Estimate Std. Error t value Pr(>|t|)
## thetal 2.121807
                      4.294901
                               0.494
                                           0.622
## theta2 -0.740089
                      0.524532
                               -1.411
                                          0.160
## theta3 -0.007429
                      0.027337
                               -0.272
                                           0.786
##
## Residual standard error: 7.984 on 147 degrees of freedom
##
## Number of iterations to convergence: 4
## Achieved convergence tolerance: 5.755e-08
```

var(flintlead2[,4])

```
Q3 The leaf levels decrease over the flushing time.  [H_0 : \mu_120] = \mu_0 ; H_a : \mu_{120} \neq \mu_0 . ]
```

```
## [1] 131.2726
var(flintlead2[,6])
## [1] 31.56412
var.test(flintlead2[,4],flintlead2[,6])
##
##
   F test to compare two variances
##
## data: flintlead2[, 4] and flintlead2[, 6]
## F = 4.1589, num df = 261, denom df = 261, p-value < 2.2e-16
## alternative hypothesis: true ratio of variances is not equal to 1
## 95 percent confidence interval:
## 3.261173 5.303799
## sample estimates:
## ratio of variances
             4.158919
##
```

```
t.test(flintlead2[,4],flintlead2[,6],var.equal=FALSE,paired=F)
```

```
##
## Welch Two Sample t-test
##
## data: flintlead2[, 4] and flintlead2[, 6]
## t = 6.5749, df = 379.65, p-value = 1.613e-10
## alternative hypothesis: true difference in means is not equal to 0
## 95 percent confidence interval:
## 3.633291 6.733495
## sample estimates:
## mean of x mean of y
## 7.719229 2.535836
```

It's an efficient way.

Q4

```
Contam_48503<-flintlead2[flintlead2[,2]==48503,4]
Contam_48504<-flintlead2[flintlead2[,2]==48504,4]
Contam_48505<-flintlead2[flintlead2[,2]==48505,4]
Contam_48506<-flintlead2[flintlead2[,2]==48506,4]
Contam_48507<-flintlead2[flintlead2[,2]==48507,4]
Contam_48507<-flintlead2[flintlead2[,2]==48507,4]</pre>
Contam<-c(Contam_48503,Contam_48504,Contam_48505,Contam_48506,Contam_48507)
```

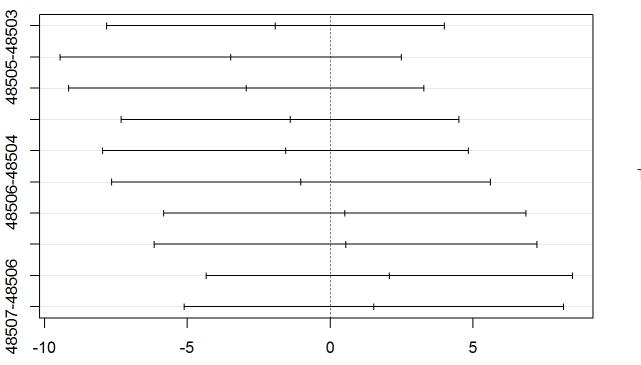
```
L<-c(0,0,0,0,0)
 for(i in 48503:48507){
   L[i-48502]<-length(which(flintlead2[,2]==i))
 groups = factor(rep(48503:48507,L))
 bartlett.test(Contam, groups)
 ##
 ## Bartlett test of homogeneity of variances
 ##
 ## data: Contam and groups
 ## Bartlett's K-squared = 23.248, df = 4, p-value = 0.000113
 qchisq(0.95, 5-1)
 ## [1] 9.487729
Variaices are significantly different.
 kruskal.test(Contam~groups)
 ##
 ## Kruskal-Wallis rank sum test
 ##
 ## data: Contam by groups
 ## Kruskal-Wallis chi-squared = 6.7637, df = 4, p-value = 0.1489
 Aov_Test<-aov(Contam~groups)
 Aov_Test
 ## Call:
       aov(formula = Contam ~ groups)
 ##
 ##
 ## Terms:
 ##
                      groups Residuals
 ## Sum of Squares
                      418.61 33713.38
 ## Deg. of Freedom
                                    253
 ##
 ## Residual standard error: 11.54359
 ## Estimated effects may be unbalanced
 TH<-TukeyHSD(Aov_Test)
      Tukey multiple comparisons of means
 ##
        95% family-wise confidence level
 ##
 ##
```

Fit: aov(formula = Contam ~ groups)

```
##
## $groups
                     diff
##
                                lwr
                                         upr
                                                  p adj
## 48504-48503 -1.9178094 -7.826461 3.990842 0.8997634
## 48505-48503 -3.4796961 -9.458864 2.499472 0.4994098
## 48506-48503 -2.9403389 -9.164833 3.284155 0.6927650
## 48507-48503 -1.4054494 -7.314101 4.503202 0.9658620
## 48505-48504 -1.5618867 -7.970945 4.847172 0.9627494
## 48506-48504 -1.0225295 -7.661047 5.615988 0.9932672
## 48507-48504 0.5123600 -5.830963 6.855683 0.9994589
## 48506-48505 0.5393571 -6.162001 7.240715 0.9994664
## 48507-48505 2.0742467 -4.334812 8.483305 0.9007102
## 48507-48506 1.5348895 -5.103628 8.173407 0.9691931
```

plot(TH)

95% family-wise confidence level



There's no

Differences in mean levels of groups

siginificant difference. Q5

```
for(i in 48503:48507){
    time0<-0
    theta1hat<-Coef_Matr1[i-48502,1]
    theta2hat<-Coef_Matr1[i-48502,2]
    meany<-theta1hat*exp(-time0*theta2hat)
    sigmahat<-Sigma_Matr[i-48502,1]
    y90quantile<-qnorm(0.9, meany, sigmahat)
    print(i)</pre>
```

```
print(y90quantile)
}
```

```
## [1] 48503

## [1] 22.59692

## [1] 48504

## [1] 18.5802

## [1] 48505

## [1] 12.29387

## [1] 48506

## [1] 15.14081

## [1] 48507

## [1] 18.11319
```

Q6

```
library(MASS)
f<-function(theta1,theta2,x){
    return(theta1*exp(-theta2*x))
Db_hat<-function(theta1,theta2,x){</pre>
  D<-cbind(exp(-theta2*x), -x*theta1*exp(-theta2*x))</pre>
  return(D)
G_hat<-function(theta1,theta2,x){</pre>
  G<-matrix(c(exp(-theta2*x), -x*theta1*exp(-theta2*x)), nrow=1, ncol=2)
  return(G)
CI<-function(para1,para2,sig,X,x0,alpha){</pre>
  D<-Db_hat(para1,para2,X)</pre>
  G<-G_hat(para1,para2,x0)
  delta < -qnorm(1-0.5*alpha)*sig*sqrt(G%*%(ginv(t(D)%*%D))%*%t(G))
  up<-f(para1,para2,x0)+delta
  low<-f(para1,para2,x0)-delta
  Interval<-c(low,up)</pre>
  return(Interval)
for (i in 48503:48507){
    theta1hat<-Coef_Matr1[i-48502,1]
    theta2hat<-Coef_Matr1[i-48502,2]
    sigmahat<-Sigma_Matr[i-48502,1]
    zipcode<-which(flintlead2[,2]==i)</pre>
    subsetflintlead<-flintlead2[zipcode,]</pre>
    sampletime1<-rep(time,each=dim(subsetflintlead)[1])</pre>
    CI_0<-CI(thetalhat,theta2hat,sigmahat,sampletime1,0,0.05)
    CI_45<-CI(theta1hat,theta2hat,sigmahat,sampletime1,45,0.05)
    CI_120<-CI(theta1hat,theta2hat,sigmahat,sampletime1,120,0.05)
    print(i)
    print(CI_0)
    print(CI_45)
    print(CI_120)
```

```
## [1] 48503
## [1] 6.934453 11.611099
## [1] 4.670611 7.841846
## [1] 1.190047 5.303978
## [1] 48504
## [1] 5.110824 9.831508
## [1] 1.740264 5.529863
## [1] -0.4501431 2.6383149
## [1] 48505
## [1] 4.539483 7.244226
## [1] 2.743593 4.641413
## [1] 0.5700071 2.8194663
## [1] 48506
## [1] 4.479061 8.523208
## [1] 0.8759067 4.3947681
## [1] -0.4776228 1.6478710
## [1] 48507
## [1] 5.794586 9.997158
## [1] 3.722932 6.611094
## [1] 0.7413708 4.3558711
```

Q7

```
responses_ALL<-unlist(flintlead2[,4:6])
sampletime_All<-rep(time,each=dim(flintlead2)[1])
Zip<-rep(flintlead2[,2],each=3)
Zip_F<-factor(Zip)
nlsreg_zip<-lm(responses_ALL~Zip_F+sampletime_All)
nlsreg_zip</pre>
```

```
##
## Call:
## lm(formula = responses_ALL ~ Zip_F + sampletime_All)
##
## Coefficients:
##
      (Intercept)
                        Zip_F48503
                                         Zip_F48504
                                                          Zip_F48505
##
          4.87272
                           1.37922
                                            2.27728
                                                             2.30172
##
       Zip F48506
                        Zip F48507
                                         Zip F48529
                                                          Zip F48532
          2.11136
                           1.33564
                                           17.27028
                                                             3.02231
##
## sampletime_All
         -0.03771
##
```

Q8

```
for(i in 48503:48507){
   BootS_Times<-100
   N<-nrow(flintlead2)
   Num<-150
   meany_Accumul<-0
   sigma_Accumul<-0
   for(step in 1:BootS_Times){</pre>
```

```
Sample_Num<-sample(1:N,Num,replace = FALSE)</pre>
    Boot_Sample<-flintlead2[Sample_Num,]</pre>
    time0<-0
    zipcode_BS<-which(Boot_Sample[,2]==i)</pre>
    subsetflintlead_BS<-Boot_Sample[zipcode_BS,]</pre>
    responses_BS<-unlist(subsetflintlead_BS[,4:6])</pre>
    sampletime_BS<-rep(time,each=dim(subsetflintlead_BS)[1])</pre>
    nlsreg1_BS<-nls(responses_BS~theta1*exp(-sampletime_BS*theta2),</pre>
             start=list(theta1=5,theta2=0.02))
    thetalhat_BS<-coef(nlsreg1_BS)[1]</pre>
    theta2hat_BS<-coef(nlsreg1_BS)[2]</pre>
    meany_BS<-theta1hat_BS*exp(-time0*theta2hat_BS)</pre>
    sigmahat_BS<-summary(nlsreg1_BS)$sigma</pre>
    meany_Accumul<-meany_Accumul+meany_BS</pre>
    sigma_Accumul<-sigma_Accumul+sigmahat_BS^2</pre>
y90quantile_BS<-qnorm(0.9, (meany_Accumul/BootS_Times), sqrt(sigma_Accumul/BootS_Times))
print(i)
print(y90quantile_BS)
```

```
## [1] 48503

## [1] 22.03907

## [1] 48504

## [1] 18.58857

## [1] 48505

## [1] 12.16529

## [1] 48506

## [1] 15.20029

## [1] 48507

## [1] 18.04
```