Stt864 Lab3

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```
setwd("C://Users//nan66//Google Drive//stt864//LAB3")
set.seed(52871775)
library(MASS)
```

Q1 Setting default path, loading need library and read data.

```
polls2008<-read.csv(file="2008-polls.csv",header=TRUE)
polls2012<-read.csv(file="2012-polls.csv",header=TRUE)
results2008<-read.csv(file="2008-results.csv",header=TRUE)
results2012<-read.csv(file="2012-results.csv",header=TRUE)
# select pollsters that conducted polls >5 states.
atleast5<-table(polls2008[,5])[table(polls2008[,5])>=5]
atleast5
```

```
##
##
                    ARG
                               ArizonaStateU
                                                     CapitalSurvey
                     78
##
                                            6
                                      EPICMRA FairleighDickinsonU
##
              ElwayPoll
##
##
     FinancialDynamics
                                     GfKRoper
                                                  InsiderAdvantage
##
             MaristColl
                                   MasonDixon
##
                                                         MonmouthU
##
                                                                  5
##
        MuhlenbergColl
                             OpinionResearch
                                                   PrincetonSurvey
##
                                           51
                                                                  5
##
           QuinnipiacU
                                   Rasmussen
                                                             Selzer
##
                                          359
              SienaColl
                                     SuffolkU
##
                                                         SurveyUSA
##
                                                                243
##
         UofCincinnati
                             UofNewHampshire
                                                      UofWisconsin
##
##
                  Zogby
##
                     16
```

```
#reformatting the poll and true results dataset as desired
#Dem win=1 Rep win=0
winers2008<-(results2008[,2]-results2008[,3]>0)+0
#name of 51 states
StateID2008<-results2008[,1]
Allresp<-NULL
for (sid in 1:51){
  ##operate on state=sid
    po08subID<-po08sub$State==StateID2008[sid]
    #polls (at least5),
    PoWin08SubSta<-po08sub[po08subID,]
    #Dem win=1 Rep win=0
    PoWin08Sta<-(PoWin08SubSta[,2]-PoWin08SubSta[,3]>0)+0
    #whether the polls is correct
    pollwinersIND<-(PoWin08Sta==winers2008[sid])+0</pre>
    #conbine it to "Allresp"
    Allresp<-c(Allresp,pollwinersIND)
}
#absolute difference between Supp rates of Dem and Rep.
margins2008<-abs(po08sub[,2]-po08sub[,3])
lagtime2008<-rep(0,dim(po08sub)[1])</pre>
electiondate2008<-c("Nov 04 2008")
EdDa08<-as.Date(electiondate2008, format="%b %d %Y")
for (i in 1:dim(po08sub)[1]){
    StDa08<-as.Date(as.character(po08sub[i,4]), format="%b %d %Y")
    lagtime2008[i] < -EdDa08-StDa08</pre>
}
data08<-cbind(Allresp,as.character(po08sub[,1]),margins2008,lagtime2008,
              as.character(po08sub[,5]))
Q3
# select the states with at least one failure prediction
# aka data08$Allresp=0
stateslist<-unique(data08[which(data08[,1]=="0"),2])</pre>
subdata08<-data08[data08[,2]%in%stateslist,]</pre>
Q4 Q5
# define new variables and fit a logistic regression model
resp<-as.integer(subdata08[,1])
statesFAC<-as.factor(subdata08[,2])</pre>
margins<-as.double(subdata08[,3])</pre>
lagtime<-as.double(subdata08[,4])</pre>
pollersFAC<-as.factor(subdata08[,5])</pre>
logitreg<-glm(resp~statesFAC+margins+lagtime+pollersFAC,family="binomial")</pre>
summary(logitreg)
##
## Call:
## glm(formula = resp ~ statesFAC + margins + lagtime + pollersFAC,
       family = "binomial")
##
```

```
##
## Deviance Residuals:
       Min
                 10
                      Median
                                    30
                                            Max
  -2.5779
           -0.5603
                      0.2084
##
                                0.5631
                                         2.5537
## Coefficients:
                                 Estimate Std. Error z value Pr(>|z|)
##
## (Intercept)
                                 0.477331
                                            0.602829
                                                       0.792 0.428466
## statesFACFL
                                -1.647375
                                            0.547285
                                                      -3.010 0.002612 **
## statesFACGA
                                 1.354619
                                            1.157192
                                                        1.171 0.241756
## statesFACIN
                                -3.359969
                                            0.926903
                                                      -3.625 0.000289 ***
## statesFACMA
                                 2.064918
                                            1.233361
                                                        1.674 0.094087
## statesFACMI
                                -0.109506
                                            0.733656
                                                     -0.149 0.881348
                                                        1.733 0.083167
## statesFACMN
                                 1.576421
                                            0.909859
## statesFACMO
                                -0.427149
                                            0.614079
                                                     -0.696 0.486683
## statesFACMT
                                 1.572071
                                            1.165776
                                                        1.349 0.177491
## statesFACNC
                                -2.289227
                                                      -3.568 0.000359 ***
                                            0.641511
## statesFACND
                                 0.582515
                                            1.411664
                                                        0.413 0.679867
## statesFACNH
                                 0.608812
                                            0.770412
                                                       0.790 0.429386
## statesFACNJ
                                 0.562342
                                            0.953698
                                                       0.590 0.555429
## statesFACNM
                                 0.115791
                                            0.722887
                                                       0.160 0.872741
## statesFACNV
                                -0.782439
                                            0.620767
                                                      -1.260 0.207511
## statesFACNY
                                 1.106166
                                            1.220608
                                                       0.906 0.364808
## statesFACOH
                                -1.456813
                                            0.554890
                                                      -2.625 0.008655 **
## statesFACOR
                                                        2.010 0.044440 *
                                 2.466634
                                            1.227231
## statesFACPA
                                 0.999567
                                            0.706504
                                                       1.415 0.157125
                                                      -1.321 0.186595
## statesFACVA
                                -0.764514
                                            0.578862
## statesFACWA
                                 2.049390
                                            1.222229
                                                       1.677 0.093589
## statesFACWI
                                 1.724056
                                            0.952639
                                                        1.810 0.070332
## statesFACWV
                                 0.176470
                                            1.192351
                                                       0.148 0.882341
## margins
                                 0.243394
                                            0.038387
                                                        6.341 2.29e-10 ***
## lagtime
                                -0.010550
                                            0.001722
                                                      -6.128 8.89e-10 ***
## pollersFACEPICMRA
                                 1.884727
                                            1.341388
                                                        1.405 0.160004
## pollersFACInsiderAdvantage
                                            0.586503
                                                        1.418 0.156112
                                 0.831820
## pollersFACMaristColl
                                 1.899700
                                                        1.581 0.113883
                                            1.201596
## pollersFACMasonDixon
                                 0.368782
                                            0.590033
                                                       0.625 0.531958
## pollersFACMuhlenbergColl
                                -0.107470
                                            1.516623
                                                      -0.071 0.943508
## pollersFACQuinnipiacU
                                                       2.767 0.005658 **
                                 1.742448
                                            0.629726
## pollersFACRasmussen
                                 0.273553
                                            0.451894
                                                       0.605 0.544948
## pollersFACSienaColl
                                15.026258 542.747543
                                                       0.028 0.977913
## pollersFACSuffolkU
                                 1.166058
                                            0.920064
                                                        1.267 0.205024
## pollersFACSurveyUSA
                                 0.831435
                                            0.518039
                                                        1.605 0.108501
## pollersFACUofCincinnati
                                 0.399582
                                            1.113652
                                                       0.359 0.719742
## pollersFACUofNewHampshire
                                -1.361725
                                            1.333940
                                                      -1.021 0.307335
## pollersFACZogby
                                 0.501113
                                            0.745531
                                                       0.672 0.501484
## ---
## Signif. codes: 0 '***' 0.001 '**' 0.05 '.' 0.1 ' ' 1
##
  (Dispersion parameter for binomial family taken to be 1)
##
##
       Null deviance: 792.52
                              on 662
                                       degrees of freedom
## Residual deviance: 492.68 on 625 degrees of freedom
## AIC: 568.68
##
```

```
## Number of Fisher Scoring iterations: 15
```

Based on the fitted modle, statesFACFL, statesFACIN, statesFACNC, statesFACOH, statesFACOR, statesFACWV, margins, lagtime, pollersFACQuinnipiacU are significantly (p-value < 0.05) associated with Resp.

```
FACWV, margins, lagtime, pollersFACQuinnipiacU are significantly (p-value<0.05) associated with Resp.
#Fit a simple logistic regression model without states as covariates
logitreg1<-glm(resp~margins+lagtime+pollersFAC,family="binomial")</pre>
summary(logitreg1)
##
## Call:
## glm(formula = resp ~ margins + lagtime + pollersFAC, family = "binomial")
##
## Deviance Residuals:
##
      Min
                1Q
                    Median
                                  3Q
                                          Max
                     0.3761
## -3.3334 -0.8649
                              0.7965
                                       2.1286
##
## Coefficients:
##
                               Estimate Std. Error z value Pr(>|z|)
## (Intercept)
                              -0.271191
                                          0.355706 -0.762
## margins
                               0.284972
                                          0.032126
                                                    8.870 < 2e-16 ***
                              ## lagtime
                               1.801304
                                         1.174831 1.533
## pollersFACEPICMRA
                                                            0.1252
## pollersFACInsiderAdvantage
                               0.475944
                                         0.498685 0.954
                                                            0.3399
                                         1.131871
## pollersFACMaristColl
                               1.824185
                                                    1.612
                                                            0.1070
## pollersFACMasonDixon
                               0.149939
                                         0.508331
                                                    0.295
                                                            0.7680
## pollersFACMuhlenbergColl
                               0.837409
                                          1.265836
                                                    0.662
                                                            0.5083
## pollersFACQuinnipiacU
                                          0.521115
                                                    1.999
                                                            0.0457 *
                               1.041485
## pollersFACRasmussen
                               0.028280
                                          0.378125
                                                    0.075
                                                            0.9404
## pollersFACSienaColl
                                                            0.9768
                              15.472666 531.264480
                                                    0.029
## pollersFACSuffolkU
                              0.878430
                                         0.877534
                                                    1.001
                                                            0.3168
## pollersFACSurveyUSA
                                                    1.077
                                                            0.2814
                              0.454879
                                          0.422271
## pollersFACUofCincinnati
                              -0.693628
                                          1.028374 -0.674
                                                            0.5000
## pollersFACUofNewHampshire
                              -0.685772
                                          1.189587 -0.576
                                                            0.5643
## pollersFACZogby
                              -0.490406
                                          0.655532 -0.748
                                                            0.4544
## ---
## Signif. codes: 0 '***' 0.001 '**' 0.05 '.' 0.1 ' ' 1
##
## (Dispersion parameter for binomial family taken to be 1)
##
      Null deviance: 792.52 on 662 degrees of freedom
## Residual deviance: 620.09 on 647
                                     degrees of freedom
## AIC: 652.09
##
## Number of Fisher Scoring iterations: 15
anova(logitreg1,logitreg)
## Analysis of Deviance Table
##
## Model 1: resp ~ margins + lagtime + pollersFAC
```

Model 2: resp ~ statesFAC + margins + lagtime + pollersFAC

Resid. Df Resid. Dev Df Deviance

##

```
## 1
           647
                   620.09
## 2
           625
                   492.68 22
                               127.41
anova(logitreg1,logitreg,test="Chisq")
## Analysis of Deviance Table
##
## Model 1: resp ~ margins + lagtime + pollersFAC
## Model 2: resp ~ statesFAC + margins + lagtime + pollersFAC
    Resid. Df Resid. Dev Df Deviance Pr(>Chi)
## 1
           647
                   620.09
## 2
           625
                   492.68 22 127.41 < 2.2e-16 ***
## Signif. codes: 0 '***' 0.001 '**' 0.05 '.' 0.1 ' ' 1
# reformating the 2012 poll data for prediction purpose
pollwiners2012<-(po12sub[,2]-po12sub[,3]>0)+0
margins2012<-abs(po12sub[,2]-po12sub[,3])
lagtime2012<-rep(0,dim(po12sub)[1])</pre>
electiondate2012<-c("Nov 06 2012")
EdDa12<-as.Date(electiondate2012, format="%b %d %Y")
for (i in 1:dim(po12sub)[1]){
  StDa12<-as.Date(as.character(po12sub[i,4]),format="%b %d %Y")
  lagtime2012[i] <- EdDa12 - StDa12</pre>
}
data12<-cbind(pollwiners2012, as.character(po12sub[,1]), margins2012, lagtime2012,
              as.character(po12sub[,5]))
```

Based on the LRT test, P-value < 2.2e-16, the categorical variable SA is very significant, the first logistic model with SA is better. Q6 Q7 Q8 Q9

```
# Focusing on the states in the state list of 2008
# select the states with at least one failure prediction
# aka data08$Allresp=0
subdata12<-data12[data12[,2]%in%stateslist,]</pre>
# Predict with logistic and simple logistic model
margins2012<-as.double(subdata12[,3])
lagtime2012<-as.double(subdata12[,4])</pre>
pollersFAC2012<-as.factor(subdata12[,5])</pre>
StateName<-c("FL","MI","MO","CO")
n < -c(0,0,0,0)
SSE < -c(0,0,0,0)
SSE1 < -c(0,0,0,0)
# Pred for Q6
Pred < -matrix(0,4,4)
rownames(Pred) <-StateName</pre>
colnames(Pred)<-c("LDemWin","LRepWin","sLDemWin","sLRepWin")</pre>
# Pred for Q7
Pred1<-matrix(0,4,4)</pre>
rownames (Pred1) <- StateName
colnames(Pred1)<-c("LDemWin", "LRepWin", "sLDemWin", "sLRepWin")</pre>
# log regression CI for Q8
PredCI<-matrix(0,4,4)
```

```
rownames(PredCI)<-StateName</pre>
colnames(PredCI)<-c("DemWinLow", "DemWinUp", "RepWinLow", "RepWinUp")</pre>
# sample log regression CI for Q8
PredCI1<-matrix(0,4,4)
rownames(PredCI1) <- StateName
colnames(PredCI1)<-c("DemWinLow", "DemWinUp", "RepWinLow", "RepWinUp")</pre>
# bootstrap CI of log regression for Q8
BSCI<-matrix(0,4,4)
rownames (BSCI) <-StateName
colnames(BSCI)<-c("DemWinLow", "DemWinUp", "RepWinLow", "RepWinUp")
# bootstrap CI of sample log regression for Q8
BSCI1<-matrix(0,4,4)
rownames (BSCI1) <- StateName
colnames(BSCI1)<-c("DemWinLow", "DemWinUp", "RepWinLow", "RepWinUp")</pre>
# Weighted Pred of log regression for Q9
S.Pred < -matrix(0,4,4)
rownames(S.Pred)<-StateName</pre>
colnames(S.Pred)<-c("LDemWin","LRepWin","sLDemWin","sLRepWin")</pre>
# computation of weight of pollers for Q9
poNum<-length(pollers)</pre>
ErrRates<-rep(0,poNum)</pre>
for (poID in 1:poNum){
  PoPred08<-NULL
  PoPredRt<-NULL
  Po08Rt<-NULL
  StateID<-NULL
  PoPred08<-po08sub[po08sub[,5]==pollers[poID],]
  PoPredRt<-(PoPred08[,2]>PoPred08[,3])+0
  StateID<-PoPred08[,1]
  Po08Rt<-winers2008[StateID]
  ErrRates[poID] <-sum(1-(PoPredRt==winers2008[StateID]))/length(PoPredRt)</pre>
}
PoRank<-rank(ErrRates)
Weight<-1/(PoRank^2)
PollWeight<-data.frame(pollers, Weight)</pre>
#the loop
StateFACName<-sort(unique(subdata08[,2]))</pre>
PollerFACName<-sort(unique(subdata08[,5]))</pre>
for (k in 1:4){
    # number of locations
    NOpolls<-sum(subdata12[,2] == StateName[k])
    locations<-which(subdata12[,2]==StateName[k])</pre>
    n[k] <-length(locations)</pre>
    # clearance of variables in the loop
    probDemwin<-NULL</pre>
    probGopwin<-NULL
    subWeight<-NULL
    XStateFac<-(StateFACName==StateName[k])+0</pre>
```

```
XPollerFAC<-(PollerFACName==pollersFAC2012[k])+0</pre>
X<-matrix(0,n[k],nrow(vcov(logitreg)))</pre>
Xs<-matrix(0,n[k],nrow(vcov(logitreg1)))</pre>
# container of predictions
LogPR<-cbind(as.double(subdata12[locations,1]),</pre>
    rep(0,n[k]))
sLogPR<-cbind(as.double(subdata12[locations,1]),</pre>
    rep(0,n[k]))
DeLogPR<-cbind(as.double(subdata12[locations,1]),</pre>
    rep(0,n[k]))
DesLogPR<-cbind(as.double(subdata12[locations,1]),</pre>
    rep(0,n[k]))
counts<-0
for (i in locations){
    counts<-counts+1
    LogDPs <- data.frame(statesFAC=StateName[k],
         margins=margins2012[i],lagtime=lagtime2012[i],
         pollersFAC=pollersFAC2012[i])
    sLogDPs<-data.frame(margins=margins2012[i],</pre>
         lagtime=lagtime2012[i],pollersFAC=pollersFAC2012[i])
    LogPR[counts,2]<-unlist(predict(logitreg,LogDPs,</pre>
         type="response"))
    sLogPR[counts,2]<-unlist(predict(logitreg1,sLogDPs,</pre>
         type="response"))
    X[counts,]<-c(1,XStateFac[2:length(XStateFac)],margins2012[i],</pre>
                    lagtime2012[i], XPollerFAC[2:length(XPollerFAC)])
    Xs[counts,]<-c(1,margins2012[i],lagtime2012[i],XPollerFAC[2:length(XPollerFAC)])</pre>
}
P1<-LogPR[,1]*LogPR[,2]+(1-LogPR[,1])*(1-LogPR[,2])
P2 < -sLogPR[,1] * sLogPR[,2] + (1-sLogPR[,1]) * (1-sLogPR[,2])
# Predictions for Q6
Pred[k,1]<-mean(P1)</pre>
Pred[k,2]<-mean(1-P1)</pre>
Pred[k,3] < -mean(P2)
Pred[k,4]<-mean(1-P2)
# Predictions for Q7
Pred1[k,1] < -mean(P1 > 0.5 + 0)
Pred1[k,2]<-mean(P1<0.5+0)</pre>
Pred1[k,3]<-mean(P2>0.5+0)
Pred1[k,4] < -mean(P2 < 0.5 + 0)
# Q8.1
# clearance of containers
GL<-rep(0,nrow(vcov(logitreg)))</pre>
GsL<-rep(0,nrow(vcov(logitreg1)))</pre>
# define the function of var of two models
```

```
for(t in 1:n[k]){
    GL < -LogPR[t,2] * (1-LogPR[t,2]) * (-1)^(LogPR[t,1]+1) * X[t,]/n[k]+0
    GsL < -sLogPR[t,2] * (1-sLogPR[t,2]) * (-1)^(sLogPR[t,1]+1) * Xs[t,]/n[k]+0
  }
#
    varp < -(sumGL/n[k]) %*%vcov(logitreg) %*%t((sumGL/n[k]))
    varp1 < -(sumGsL/n[k]) %*%vcov(logitreg) %*%t((sumGsL/n[k]))
    PredCI[k,1] <-mean(P1)-qnorm(0.975)*sqrt(GL%*%vcov(logitreg)%*%GL)</pre>
    PredCI[k,2] <-mean(P1)+qnorm(0.975)*sqrt(GL%*%vcov(logitreg)%*%GL)</pre>
    PredCI[k,3]<-1-PredCI[k,2]</pre>
    PredCI[k,4]<-1-PredCI[k,1]</pre>
    PredCI1[k,1] <-mean(P2)-qnorm(0.975)*sqrt(GsL%*%vcov(logitreg1)%*%GsL)
    PredCI1[k,2]<-mean(P2)+qnorm(0.975)*sqrt(GsL%*%vcov(logitreg1)%*%GsL)</pre>
    PredCI1[k,3]<-1-PredCI1[k,2]</pre>
    PredCI1[k,4]<-1-PredCI1[k,1]</pre>
    # Q8.2 Bootstrap prediction CI
    xStar<-NULL
    xStar1<-NULL
    for (boot in 1:500){
        BS.sample<-sample(P1,n[k],replace=TRUE)
        xStar[boot] <-mean(BS.sample)</pre>
        BS.sample1<-sample(P2,n[k],replace=TRUE)
        xStar1[boot] <-mean(BS.sample)</pre>
    }
    BSCI[k,1]<-mean(xStar)-qnorm(0.975)*sd(xStar)</pre>
    BSCI[k,2]<-mean(xStar)+qnorm(0.975)*sd(xStar)
    BSCI[k,3] < -mean(1-xStar) - qnorm(0.975)*sd(1-xStar)
    BSCI[k,4] < -mean(1-xStar) + gnorm(0.975) * sd(1-xStar)
    BSCI1[k,1]<-mean(xStar1)-qnorm(0.975)*sd(xStar1)</pre>
    BSCI1[k,2]<-mean(xStar1)+qnorm(0.975)*sd(xStar1)</pre>
    BSCI1[k,3] < -mean(1-xStar1) - qnorm(0.975)*sd(1-xStar1)
    BSCI1[k,4] < -mean(1-xStar1) + qnorm(0.975)*sd(1-xStar1)
    subPoName<-subdata12[subdata12[,2] == StateName[k],5]</pre>
    subWeight<-rep(0,NOpolls)</pre>
    for (f in 1:NOpolls){
      subWeight[f]<-PollWeight[PollWeight[,1]==subPoName[f],2]</pre>
    }
    W.P1<-P1*subWeight/sum(subWeight)
    W.P2<-P2*subWeight/sum(subWeight)</pre>
    W.P1.C<-(1-P1)*subWeight/sum(subWeight)
    W.P2.C<-(1-P2)*subWeight/sum(subWeight)</pre>
    S.Pred[k,1] < -sum(W.P1)
    S.Pred[k,2] < -sum(W.P1.C)
    S.Pred[k,3] < -sum(W.P2)
    S.Pred[k,4] < -sum(W.P2.C)
}
```

outputs:

```
#Out put of Q6
Pred
```

LDemWin LRepWin sLDemWin sLRepWin

```
## FL 0.5530233 0.4469767 0.5779907 0.4220093
## MI 0.8434990 0.1565010 0.8421328 0.1578672
## MO 0.3170803 0.6829197 0.2893665 0.7106335
## CO 0.4906724 0.5093276 0.5221877 0.4778123
#Out put of Q7s
Pred1
         LDemWin
                   LRepWin sLDemWin sLRepWin
## FL 0.57777778 0.4222222 0.6000000 0.4000000
## MI 0.93750000 0.0625000 0.9375000 0.0625000
## MO 0.07692308 0.9230769 0.1538462 0.8461538
## CD 0.52631579 0.4736842 0.4736842 0.5263158
#Actuall election results in 2012
results2012[results2012[,1]%in%StateName,]
##
      State Dem Rep
## 6
         CO 51.2 46.5
## 10
        FL 50.0 49.1
## 23
        MI 54.3 44.8
        MO 44.3 53.9
## 25
The prediction in Q6 is much more accurate in FL, MI & MO, however, in CO, the prediction in Q7 is better.
#Out put of Q8
PredCI
      DemWinLow DemWinUp RepWinLow RepWinUp
## FL 0.5516019 0.5544446 0.4455554 0.4483981
## MI 0.8398646 0.8471333 0.1528667 0.1601354
## MO 0.2934515 0.3407092 0.6592908 0.7065485
## CO 0.4795976 0.5017472 0.4982528 0.5204024
PredCI1
##
      DemWinLow DemWinUp RepWinLow RepWinUp
## FL 0.5775599 0.5784215 0.4215785 0.4224401
## MI 0.8402742 0.8439914 0.1560086 0.1597258
## MO 0.2749453 0.3037877 0.6962123 0.7250547
## CO 0.5138625 0.5305130 0.4694870 0.4861375
BSCI
      DemWinLow DemWinUp RepWinLow RepWinUp
## FL 0.4840409 0.6217617 0.37823827 0.5159591
## MI 0.7564992 0.9284138 0.07158616 0.2435008
## MO 0.2131528 0.4203838 0.57961618 0.7868472
## CO 0.3626699 0.6277566 0.37224340 0.6373301
```

BSCI1

```
## FL 0.4840409 0.6217617 0.37823827 0.5159591
## MI 0.7564992 0.9284138 0.07158616 0.2435008
## M0 0.2131528 0.4203838 0.57961618 0.7868472
## CO 0.3626699 0.6277566 0.37224340 0.6373301
```

#Out put of Q9 S.Pred

```
## LDemWin LRepWin sLDemWin sLRepWin
## FL 0.6099908 0.3900092 0.7777139 0.2222861
## MI 0.8713073 0.1286927 0.8814376 0.1185624
## MO 0.3189026 0.6810974 0.2979604 0.7020396
## CO 0.5571267 0.4428733 0.5809884 0.4190116
```

Intervals based on delta-method are most accurate.