

CSC 110: Week 2, Lecture 2

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Recap on numbers

- Two basic numeric data types: ints and floats
 - Ints are whole numbers with no decimal point
 - Floats are numbers with decimal point (even if that decimal part is .0)
- Zero-based numbering
- Arithmetic
 - Built-in operations: `*`, `/`, `+`, `-`, `**`, `//`, `%`, `abs`
 - Single-type expressions
 - Mixed-type expressions
- Type conversion
 - Implicit and explicit

Challenge problem from last class

- Using the built-in python functions, write a program that takes two numbers as inputs (prompting user for them) and finds the improper fractional representation and the mixed number representation of the division of the two numbers.
- What do we need to use?
 - Print statements
 - Input statements
 - % and // operators

Challenge problem from last class

```
#This is a program that answers the challenge problem from week 2 lecture1:  
#Using the built-in python functions, write a program that takes two numbers  
#as inputs (prompting user for them) and finds the improper fractional  
#representation and the mixed number representation of the division of  
#the two numbers.
```

```
def main():  
    print("This program gives the improper fraction and  
          mixed number representation of the division of two integers.")  
    print()  
    numerator = eval(input("Please enter the numerator: "))  
    denominator = eval(input("Please enter the denominator: "))  
  
    print("The improper fraction is ",numerator,"/",denominator,".")  
    print()  
    print("The mixed number representation is ",numerator//denominator,"",  
          numerator%denominator,"/",denominator,".")
```

```
main()
```

```
>>> import ChallengeProblemW2L1
```

```
This program gives the improper fraction and mixed number representation  
e division of two integers.
```

```
Please enter the numerator: 10
```

```
Please enter the denominator: 3
```

```
The improper fraction is 10 / 3 .
```

```
The mixed number representation is 3 1 / 3 .
```

```
>>>
```

What we will cover today

- Math library
 - Access to math functions
- Range and lists of integers
 - Loops, accumulators
- Precision, conversion, rounding, etc...

Math Library!

- Built-in functions provide basic math
- More complicated math requires the math library
 - Broader functions and constants
 - pi
 - e
 - Square root
 - Trigonometric functions (sine, cosine, tangent, arcsin, arccos, arctan)
 - Logarithms
 - Exponentials
 - Ceiling
 - Floor

Importing the math library

- Use the standard import statement.
 - `>>> import math`
 - Use math functions with the dot notation: `math.squareroot(<number>)`

```
>>> x=sqrt(4)
Traceback (most recent call last):
  File "<pyshell#14>", line 1, in <module>
    x=sqrt(4)
NameError: name 'sqrt' is not defined
>>> import math
>>> x= sqrt(4)
Traceback (most recent call last):
  File "<pyshell#16>", line 1, in <module>
    x= sqrt(4)
NameError: name 'sqrt' is not defined
>>> x = math.sqrt(4)
>>> x
2.0
```


Let's try it out

- Try to parse the following expressions in python
 - the square root of 121
 - $\log_2(64)$
 - $e^{\pi t}$, evaluated where $t = 2$
- What happens when we parse the expressions using variables and then change the variable assignment?

Looking at basic loops

- Last week the book introduced a loop using this range function

```
>>> for i in range(10):  
    print(i)
```

```
0  
1  
2  
3  
4  
5  
6  
7  
8  
9  
>>>
```

range(<integer>)

- This range function is a way of generating a set of integers
- When would this be helpful?
- Can be used in conjunction with a list

list(range(<integer>))

- Built-in way to make numbered lists
 - list(range(<integer>))
 - Zero-based numbering!

```
>>> list(range(10))  
[0, 1, 2, 3, 4, 5, 6, 7, 8, 9]
```

- The <integer> represents the number of elements in the list
 - Note: not equal to the largest value stored in the list. Why?

`list(range(<integer>,<integer>))`

- Built-in way to make lists that do not start at 0
 - Why might we want this to be the case?

```
>>> list(range(1,10))  
[1, 2, 3, 4, 5, 6, 7, 8, 9]  
>>>  
>>> list(range(10,20))  
[10, 11, 12, 13, 14, 15, 16, 17, 18, 19]  
...
```

Think-pair-share

- Think about the line: `list(range(<integer>,<integer>))`
 - What is the first argument?
 - What is second argument?
 - Does this change our understanding of the argument in `list(range(<integer>))`

`list(range(<integer>,<integer>,<integer>))`

- Built in way to make lists that don't count by 1
 - Can make even lists or lists that count by 3
 - Can make lists that count backwards

```
>>> list(range(0,10,2))  
[0, 2, 4, 6, 8]  
>>>  
>>> list(range(10,0,-1))  
[10, 9, 8, 7, 6, 5, 4, 3, 2, 1]
```


Let's try it out

- Try making a list that starts at 15, counts by 5s up to and including 100
 - [15, 20, ...100]
- Try making a loop that prints the multiples of 3 that are less than 63 and greater than 0
- Try making a list that prints from largest to smallest the numbers between 0 and 63 that are divisible by 3

Now, didn't we say something about loops?

- May want to loop over a set and accumulate the results
 - Running tally of total, product of a set of numbers
- Example, I run a bookstore. My list stores the number sold for each title. I want the total number of books sold.
 - I want to loop over the elements in the list and add them up
 - Need a running total: accumulator variable

Accumulator loops

- Say my bookstore list is [0,10,3,4,7,14]
- Accumulator variable tally is assigned to 0 at the start
- Loop over elements in the list, adding them to tally

Sample loop

```
>>> testlist = [0,10,3,4,7,14]
>>> testlist
[0, 10, 3, 4, 7, 14]
>>> type(testlist)
<class 'list'>
>>>
>>> tally = 0
>>> for i in testlist:
>>>     tally = tally+i

>>> tally
38
```


Precision in numeric types

- Ints are stored exactly
 - Fixed-size: 2^n values can be stored in n bits
 - What about long ints?
- Floats are stored as approximations
 - Can represent numbers larger than 2^n
 - Fixed precision

Ceiling, Floor, Round functions

- Ceiling: nearest integer larger than the value
- Floor: nearest integer smaller than the value
- Round: the closest integer (if the decimal is a 0.5 round up)

```
>>> math.ceil(3.75)
4
>>> math.ceil(-3.75)
-3
>>> math.floor(3.75)
3
>>> math.floor(-3.75)
-4
>>> round(3.75)
4
>>> round(-3.75)
-4
>>>
```

Be careful!

- Negative arguments can get tricky!
- Be sure that you understand the order of operations to whatever mathematical idea you are trying to implement

```
>>> abs(math.ceil(3.75))
4
>>> math.ceil(abs(-3.75))
4
>>> abs(math.ceil(-3.75))
3
>>>
```


Sample problems from the book

- Chapter 3 Q2
 - Write a program that calculates the cost per square inch of a circular pizza given its diameter and price
- Chapter 3, Q 6
 - Two points in a plane are specified using the coordinates (x_1, y_1) and (x_2, y_2) . Write a program that calculates the slope of a line through two (non-vertical) points entered by the user:
 - $\text{Slope} = (y_2 - y_1) / (x_2 - x_1)$