



# Learning in Drug Choice

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November 12, 2019

# Crawford and Shum (2005)

## Uncertainty and Learning in Pharmaceutical Demand

# Model

- Forward-looking physician maximizes patient's present-discounted expected utility

$$\max_{D \equiv \left\{ \{d_{ijt}\}_{j=1}^J \right\}_{t=1}^{\infty}} E_D \sum_{t=1}^{\infty} \beta^t d_{ijt} u_{ijt} (1 - \omega_{i,t-1})$$

- For patient  $i$ , drug  $j$  characterized by two time-invariant match values:
  - $\mu_{ij}$  - symptomatic effect
  - $\nu_{ij}$  - curative effect
- Each prescription yields two signals
  - $x_{ijt} \sim F(\mu_{ij}, \cdot)$  - symptomatic signal
  - $y_{ijt} \sim F(\nu_{ij}, \cdot)$  - curative signal

## Model

- Length of treatment unknown; prob of recovery endogenizes length
- Priors
  - Unobserved to econometrician
  - Diagnosis falls into one of  $K$  latent types

$$h_{oi} = \theta_k \text{ with probability } p_k$$
$$h_{it}(h_{i,t-1}, y_{ijt}) = \frac{\left(\frac{h_{i,t-1}}{1-h_{i,t-1}}\right) + d_{ijt}y_{ijt}}{1 + \left(\left(\frac{h_{i,t-1}}{1-h_{i,t-1}}\right) + d_{ijt}y_{ijt}\right)}$$

- Preferences

$$u(x_{ijt}, p_j, \varepsilon_{ijt}) = -\exp(-r * x_{ijt}) - \alpha p_j + \varepsilon_{ijt}$$

- Quasi-linear utility, CARA specification

## Learning

- Prior means

$$\begin{pmatrix} \mu_{ij} \\ \nu_{ij} \end{pmatrix} \sim N \left( \begin{pmatrix} \underline{\mu}_{ij} \\ \underline{\nu}_{ij} \end{pmatrix}, \begin{pmatrix} \underline{\sigma}_j^2 & 0 \\ 0 & \underline{\tau}_j^2 \end{pmatrix} \right)$$

- Distribution of signals, conditional on priors

$$\begin{pmatrix} x_{ijt} \\ y_{ijt} \end{pmatrix} \sim N \left( \begin{pmatrix} \mu_{ij} \\ \nu_{ij} \end{pmatrix}, \begin{pmatrix} \sigma_j^2 & 0 \\ 0 & \tau_j^2 \end{pmatrix} \right)$$

## Model

- Rational expectations - prior beliefs correspond to actual distribution of idiosyncratic match values
- Updating: (similar for posterior beliefs on curative match value)

$$\mu_{ij}^{t+1} = \frac{\frac{\mu_{ij}^t}{V_{ij}^t} + \frac{x_{ij,t+1}}{\sigma_j^2}}{\frac{1}{V_{ij}^t} + \frac{1}{\sigma_j^2}} \text{ or } \mu_{ij}^t$$

$$V_{ij}^{t+1} = \frac{1}{\frac{1}{\sigma_j^2} + \frac{1}{V_{ij}^{t+1}}} \text{ or } V_{ij}^t$$

# Model

- State variables
  - $i$ 's posterior mean match values,  $\mu_{ij}^t, \nu_{ij}^t$  for  $j = 1, \dots, 5$
  - counts of no. of times tried a drug,  $l_{ij}^t, j = 1, \dots, 5$
  - recovery probability for patient  $i$  at period  $t$ ,  $h_{it}$
  - $\varepsilon_{ijt}, j = 1, \dots, 5$
- Dynamic problem - solve via Bellman Equation
  - Policy: in period  $t$ ,  $i$  chooses  $j$  with highest value function
  - Approximate via variant of Keane and Wolpin (1994)



# Identification

- Key restrictions
  - drug's symptomatic effects only impact a patient's utility
  - curative effects only influence the recovery probabilities
- For  $(\underline{\mu}_j, \underline{\sigma}_j^2, \sigma_j, r)$ 
  - enter per period utility expression
  - $\underline{\mu}_j$  comes from initial prescription shares across patients
  - Difference in drug choice probabilities early vs. late in sequence help identify  $\underline{\sigma}_j^2$
  - $r$  vs.  $\sigma_j$ 
    - persistence in drug choices gives  $r$
    - extent to which rate of switching varies with  $l_{ij}^t$  identifies  $\sigma_j$

# Identification

- For  $(\underline{\nu}_j, \underline{\tau}_j^2, \tau_j, h_{0i})$ 
  - enters dynamic choice problem through expected recovery probability
  - $h_{0i}$  identified separately because it only enters healing probability; other 3 enter posterior mean and variance for curative match value
- Can identify  $\underline{\mu}_j$  separately from price coefficient,  $\alpha$ , because of functional form assumption;  $\underline{\mu}_j$  enters per period utility nonlinearly and  $\alpha$  enters linearly.

# Results

- Counterfactual 1: patients have complete info about match values (set perceived variances,  $(V_{ij}^t, R_{ij}^t) = 0$ )
  - discounted expected utility increases (though by small amount)
  - average number of drugs used increases
- Counterfactual 2: constrain patients to take the first drug they're prescribed
  - shuts down learning after 1st prescription
  - does not change simulated treatment lengths
  - lowers avg utility 6%
- Counterfactual 3: no diagnostic matching to patient "type"
  - expected utility decreases 11%, costs 40% higher than baseline
  - diagnostic matching at least as important as idiosyncratic learning

# Efficient Provision of Experience Goods: Evidence from Antidepressant Choice

# Goals of Paper

- Theory Testing
- Measurement
- Methodology

# Goals of the Paper

- Theory Testing
  - Do the pricing schemes of Shapiro (1983), Bergemann and Valimaki (2006) appear in markets in which consumer perceptions change with experience?
  - Can adherence information in observational data provide a measure of treatment effectiveness?
- Measurement
  - Identify the elasticity of patients/physicians with respect drug copayments and wholesale prices
  - Measure the dynamic response of patients and physicians to prices/promotion, in both costs and health.
  - Provide average adherence information by drug compound

## Goals of the Paper (continued)

- Methodology
  - Provide feasible estimation approach for dynamic discrete choice problems with large choice sets, given correlation in outcomes across alternatives.

Goals and RQ  
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Data  
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Learning Model  
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Estimates and Fit  
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Counterfactuals  
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# Research Question



## Research Questions

What policies can improve the efficiency of drug choice, maximizing adherence and patient health while minimizing the costs of treatment?

- Copayment schemes
  - Tiered policy
  - Uniform pricing
  - “Value-based” design (Chernew et al. (2007))
- Informational campaigns
  - Discourage use of “me-too” branded drugs
  - Endow general practitioners with psychiatrists’ preferences

## Research Questions (Continued)

- What information can observational studies contribute—beyond results from randomized trials—to judge the efficacy of different treatments?
  - Philipson and Hedges (1998) provide theoretical justification
  - Chan and Hamilton (2006) measure the benefits in the clinical trial setting
- With 20 products available, what assumptions permit estimation of the agent's learning process over this choice set?

## Market for Depression Care

- Major depression affects 6.5% of adults in the US annually
- US antidepressant market sales in 2008
  - \$9.6 Billion
  - 164 million monthly prescriptions (3rd ranked class)

Six subclasses: differ in their effect on serotonin, norepinephrine, or dopamine in the brain.

“First Generation”	“Second Generation”
TCA	SSRIs, SNRIs, NDRI, NaSSAs, SARIs

- Choice set: 13 compounds, 20 unique products

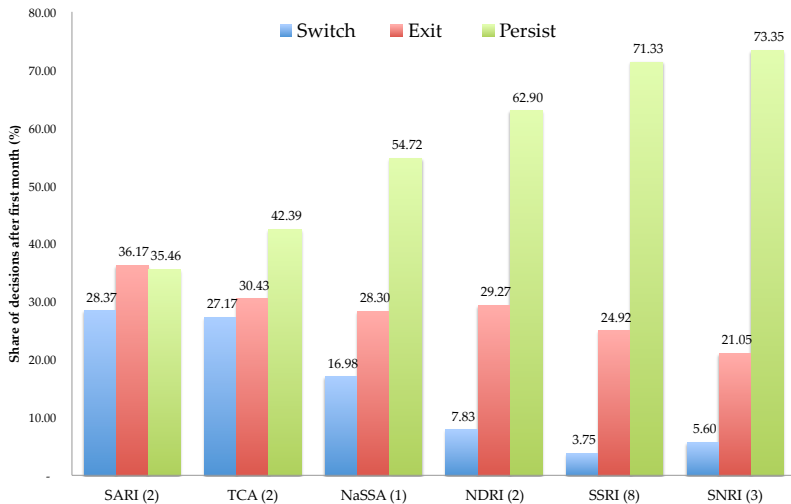
Source: Thomson Medstat Marketscan databases, 2003-2005.

- Includes active employees (and dependents) of large self-insured firms that contribute claims to the Marketscan database

Requirements for inclusion in sample

- Patients newly diagnosed in an outpatient visit with: major depression (296.2-3), related depression conditions (300.4, 309.0-1, 311)
- No concurrent diagnosis of manic disorders (296.0-1, 296.4-8) or schizophrenic disorders (295.0-9)
- Age between 18 and 64
- Visits a health professional with prescribing ability
- Not pregnant

Product Name	Subclass	Brand?	Daily dosing	Market Share (%)		
				2003	2004	2005
None	None	-	-	35.2	39.3	34.2
Citalopram HBr	SSRI	No	1	-	0.2	4.2
Celexa	SSRI	Yes	1	4.1	2.7	0.1
Lexapro	SSRI	Yes	1	13.8	13.0	12.0
Fluoxetine HCL	SSRI	No	1-2	7.3	11.5	10.6
Paroxetine HCL	SSRI	No	1	1.7	4.3	4.4
Paxil CR	SSRI	Yes	1	6.4	3.6	1.6
Zoloft	SSRI	Yes	1	12.5	10.6	9.6
Cymbalta	SNRI	Yes	1-2	-	0.5	2.4
Effexor-XR	SNRI	Yes	1	8.6	7.5	7.0
Bupropion HCL	NDRI	No	3	0.3	3.4	4.5
Wellbutrin XL	NDRI	Yes	1	6.5	5.7	5.1
Amitriptyline HCL	TCA	No	1	0.7	0.9	0.7
Mirtazapine	NaSSA	No	1	0.5	0.7	0.6
Trazodone HCL	SM	No	3	1.3	1.8	1.6
			Total # unique patients:	102,780		
			Total # of observations:	267,390		
			Total # unique plans:	307		



Switch/Quit/Persist across Classes after First Month

# Timing of Switches

Prescription count in episode	Length of Treatment Episode (# monthly prescriptions dispensed)							
	1	2	3	4	5	6	7	8
1	100.0	100.0	100.0	100.0	100.0	100.0	100.0	100.0
2		85.1	86.8	88.9	89.4	89.6	90.4	91.4
3			84.4	84.2	84.7	85.8	86.4	88.2
4				82.3	82.0	83.0	83.9	86.4
5					80.2	81.0	82.2	84.4
6						79.6	80.1	82.6
7							79.3	80.7
8								79.9
Share of dataset	56.7%	12.9%	9.3%	6.4%	4.4%	3.1%	2.1%	1.7%

## Hazard of switching

- Interpret as probability of finding a drug “ineffective”
- Condition on patient costs, doses/day, rate of side effects, patient diagnosis
- Find range of predicted prob of effectiveness

Class	Periods since the patient's initial diagnosis		
	Period 1	Period 2	Period 3
TCA	52.4	62.7	68.7
SSRI	66.1	74.2	78.6
SNRI	66.2	74.3	78.7
NDRI	61.1	70.2	75.1
NaSSA	59.2	68.5	73.7
SARI	43.7	55.1	61.8



# Learning Model

## Goal:

Estimate parameters of the agent's learning process using the timing and identity of observed switch/persist decisions

## Requires:

Predicted choice probabilities to match to observed choices

- (1) Discrete outcomes
- (2) Patient and physician priors
- (3) Updating process
- (4) Decision rule
  - myopic vs. forward-looking
  - independent vs. correlated choices

## (1) Discrete outcomes

- Patient and physician ( $i$ ) observe a discrete outcome,  $Y_{ijt}$ , under treatment  $j$  at time  $t$
- “Outcome” includes efficacy, price, side effects, ease of use, ...

## (1) Discrete outcomes

- Patient and physician ( $i$ ) observe a discrete outcome,  $Y_{ijt}$ , under treatment  $j$  at time  $t$
- “Outcome” includes efficacy, price, side effects, ease of use, ...
- $Y_{ijt}$  drawn from a Bernoulli distribution
- Probability of a successful outcome equals  $p_j$ :

$$Y_{ijt} \sim p_j^k (1 - p_j)^{1-k}, k \in \{0, 1\}$$

where  $k = 1$  if drug  $j$  proves effective in period  $t$

## (1) Discrete outcomes (continued)

Prior on  $p_j$

- Beta distribution with parameters  $(a_{j,0}, b_{j,0})$
- Mean and variance of Beta distribution:

$$\mu_{j,0} = \frac{a_{j,0}}{a_{j,0} + b_{j,0}}$$

$$v_{j,0} = \frac{a_{j,0}b_{j,0}}{(a_{j,0} + b_{j,0})^2(a_{j,0} + b_{j,0} + 1)}$$

where  $a_{j,0} > 0$  and  $b_{j,0} > 0$ .

## (2) Updating process

After  $t$  trials of treatment  $j$ :

- add to  $a_{j,0}$  the number of successes observed
- add to  $b_{j,0}$  the number of failures observed

Why?

- Beta is conjugate prior for Bernoulli likelihood. So, posterior distribution of  $p_j$  is Beta.

Caveat

- In the application, successes and failures not observed; I integrate over the discrete number of possible realizations.

### (3) Decision Rule: Options

(1) 'Bayesian Myopic' at  $(T + 1)$  after updating using  $\hat{Y}_{ij}$ :

$$\max_{j \in 1, \dots, J} E(p_{i,j,T+1} | a_0, b_0, \hat{Y}_{ij}) + \varepsilon_{ijt} = \mu_{j,T+1} + \varepsilon_{ijt}$$

- Experience on  $j$  for periods  $t = 1, \dots, T$  in vector  $\hat{Y}_{ij}$
- Choose what to consume at  $T + 1$
- $\varepsilon_{ijt}$  represents idiosyncratic tastes for  $j$  at  $t$

## (3) Decision Rule: Options

(2) 'Forward-Looking' at  $(T + 1)$  after updating using  $\hat{Y}_{ij}$ :

$$\max_{j \in 1, \dots, J} \mu_{j, T+1} + h(V(p_{i,j, T+1} | a_0, b_0, \hat{Y}_{ij})) + \varepsilon_{ijt}$$

### (3) Decision Rule: Forward-Looking Problem

The physician and patient choose a sequence of drugs to maximize the expected discounted sum of outcomes,  $Y_t$ :

$$\int \dots \int E_{p_1, \dots, p_J} \left( \sum_{t=1}^{\infty} \delta^{t-1} Y_t \right) d\Pi^{(1)}(p_1) \dots d\Pi^{(J)}(p_J) \quad (1)$$

- $\delta$  is given and  $p = (p_1, \dots, p_J)$  is the unknown vector of probabilities that a drug  $j \in 1, \dots, J$  is effective.
- the agent forms independent priors,  $\Pi$ , on the elements of  $p$
- The state variables include the number of successes and failures under each choice



### (3) Decision Rule: Forward-Looking Solutions

#### Solutions:

- Dynamic Programming, via Rust (1987) and Hotz and Miller (1993)
- Keane and Wolpin (1984), simulation and interpolation
- Gittins' (1979) index rule: Break  $J$ -dimensional problem into  $J$  continue-quit decisions, one for each choice
  - Inner maximization: solve 1-dim optimal stopping problem for each  $j$ . Save discounted expected value, the “index”
  - Outer maximization: choose  $j$  with the maximal index value

## (3) Decision Rule: Forward-Looking Solutions

Requirements for Gittins' Index:

1. the decision-maker selects only one option at  $t$
2. options not chosen remain in their initial state
3. each option is independent
4. options not selected do not contribute to the individual's outcome

More on Gittins

### (3) Decision Rule: Forward-Looking Solutions

My approach (computable via forward induction):

- Use index rule, treating each drug compound choice as independent
  - unobservables not correlated across drug choices
- Use index rule with explicit nesting structure
  - use drug classes as nests, within which choices may be correlated
  - unobservables not correlated across drug classes

### (3) Decision Rule: Index Rule form

Apply forward induction rule

$$G(\Pi_t^{(j)}) = \mu_{j,t} + \sqrt{v_{j,t}} * \left[ \psi \left( \frac{v_{j,t}}{h(\delta) * \sigma^2(\mu_{j,t})} \right) \right]$$

- $(\mu_{j,t}, v_{j,t})$ , are the mean and variance of the posterior beta distribution for  $p_j$ , the probability that drug  $j$  is effective.
- $\psi(\cdot)$  represents the closed-form numerical approximation to the boundary of the one-dimensional optimal stopping problem for each drug (Chang and Lai (1987))

### (3) Decision Rule: Index Rule form

$$G(\Pi_t^{(j)}) = \mu_{j,t} + \sqrt{v_{j,t}} * \left[ \psi \left( \frac{v_{j,t}}{h(\delta) * \sigma^2(\mu_{j,t})} \right) \right]$$

$$\mu_{j,t} = \frac{a_{j,t}}{a_{j,t} + b_{j,t}}$$

$$v_{j,t} = \frac{a_{j,t} b_{j,t}}{(a_{j,t} + b_{j,t})^2 (a_{j,t} + b_{j,t} + 1)}$$

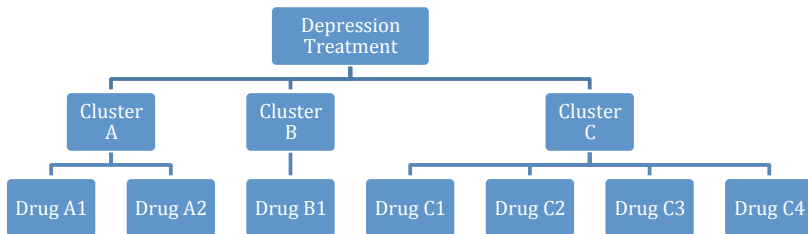
$$\sigma^2(\mu_{j,t}) = \mu_{j,t} * (1 - \mu_{j,t})$$

Experimentation incentive diminishes when:

- $\delta$  is small,  $h(\delta)$  is large
- when past experience diminishes  $v_{j,t}$
- when  $\sigma^2(\mu_{j,t})$  is large

### (3) Decision Rule: Index Rule with Correlation

via Pandey et al. (2007)



- Cluster by drug class
- Sum outcomes over all trials of drugs within the class

$$a_{c,t} = \sum_j 1\{j \in c\} * a_{j,t}$$

$$b_{c,t} = \sum_j 1\{j \in c\} * b_{j,t}$$

### (3) Decision Rule: Index Rule with Correlation

- Index rule for the class

$$G(\Pi_t^{(c)}) = \mu_{c,t} + \sqrt{v_{c,t}} * \left[ \psi \left( \frac{v_{c,t}}{h(\delta) * \sigma^2(\mu_{c,t})} \right) \right]$$

- Drug class choice probability

$$\text{Prob}_{c,t} = \frac{\exp(G(\Pi_t^{(c)}))}{1 + \sum_{s=1}^{C-1} \exp(G(\Pi_t^{(s)}))}$$

- Drug compound choice probability

$$\begin{aligned} \text{Prob}_{j \in c, t} &= \text{Prob}_{c,t}(\text{Prob}_{j,t} | 1\{c \text{ chosen}\}) \\ &= \text{Prob}_{c,t} * \frac{\exp(G(\Pi_t^{(j)}))}{\sum_{k \in c} \exp(G(\Pi_t^{(k)}))} \end{aligned}$$

## Econometric Model

- Parameterize  $p_j$  using beta regression model

$$\begin{aligned}p_j|X_{ij} &\sim \text{Beta}(a_0, b_0) \\ \mu(X_{ij}; \gamma_1) &= \frac{a_0}{a_0 + b_0} = \frac{\exp(X_{ij}\gamma_1)}{1 + \exp(X_{ij}\gamma_1)} \\ \phi(\gamma_2) &= a_0 + b_0 = \exp(\gamma_2)\end{aligned}$$

where  $\mu$  is prior mean,  $\phi$  is the prior precision of  $p_j$

- The prior variance of  $p_j$  is:

$$V(p_j|X_{ij}) = \frac{\mu(1 - \mu)}{1 + \phi}$$

- For a fixed  $\mu$ , the larger the value of  $\phi$ , the smaller the variance in  $p_j$ .



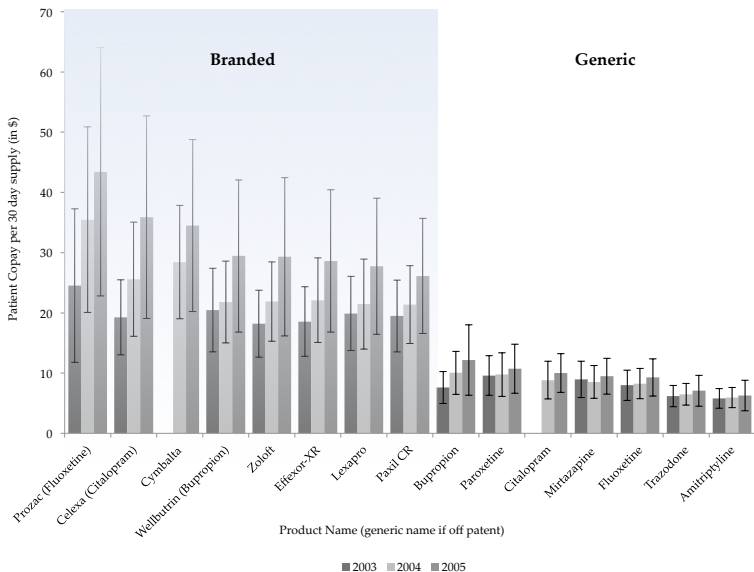


Figure 1: Patient Copayments by Product and Year (standard deviation across insurance plans shown)

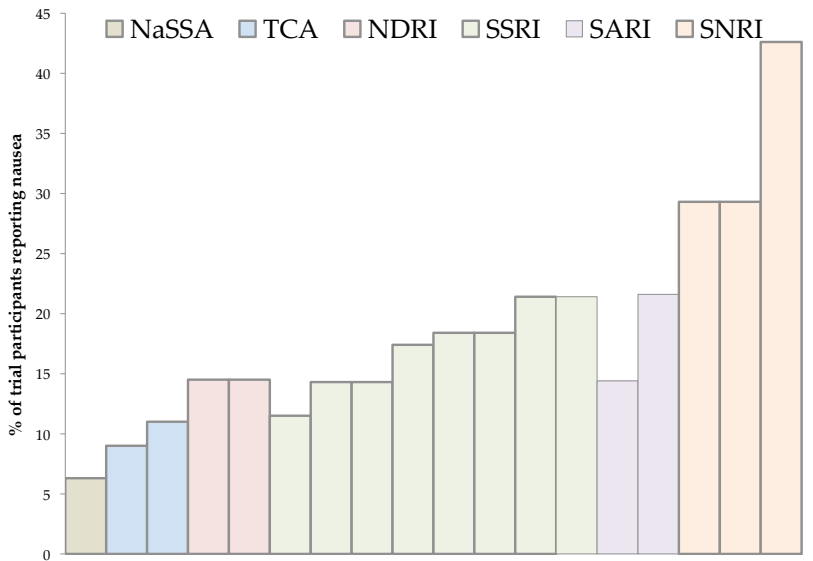


Figure 2: Nausea Side Effects in Clinical Trials

# Identification

Goal: recover  $\gamma = (\gamma_1, \gamma_2)$ , in the mean and precision of  $p_j$

1. Identity of choice throughout the sequence of treatments
  - Identifies expected mean outcome under available choices following standard arguments
2. Information on drug characteristics from clinical trial data, external sources
3. Timing of observed switches
  - Identifies precision of the agents' priors
  - Slowing switching, condition on  $\mu$ , higher uncertainty in agents' priors
  - Errors assumed idiosyncratic

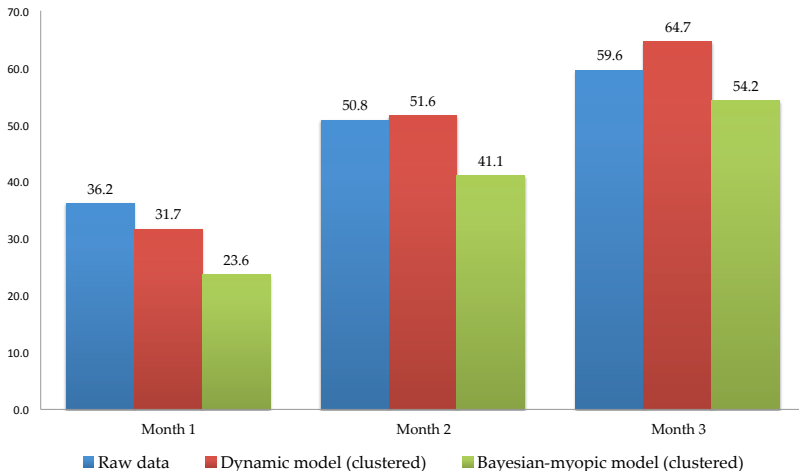
# Results, via maximum likelihood

Covariates in prior mean	(1) Two-Level Gittins Index Model		(2) Two-level Bayesian- Myopic Model	
	Est	Std. Err	Est	Std. Err
1{SSRI}	99.16	8.72	-0.84	6.75
1{SNRI}	-22.58	2.23	-69.23	10.74
1{NDRI}	-43.09	5.77	-73.38	7.33
1{NaSSA}	-35.36	8.47	-15.08	3.24
1{SARI}	-40.03	2.04	-7.62	18.92
1{TCA}	-72.44	4.36	-13.72	8.88
1{more than 1 dose needed per day}	-76.77	3.66	-20.69	18.94
percentage of nausea reports in trials	-15.62	5.20	9.23	47.77
1{reformulation}	13.91	15.96	70.17	2.99
1{branded}	-9.80	4.93	3.23	1.54
copayment, in \$/day	-81.58	19.58	-3.42	2.26
log(precision)	-3.28	2.61	-32.06	0.02

\*Includes interactions between speciality and drug class, diagnosis severity and drug class

## Fit - Adherence Rate

**Observed and predicted share of patients exiting drug care in the first three months of treatment**



## Fit: Predicted Choices by Individual

Panel A: Percentage of patients who have exited care in the first three months of treatment

Model	t=1	t=2	t=3
Raw data	36.2	50.8	59.6
Dynamic model, clustered by type	31.7	51.6	64.7
Bayesian myopic model, clustered by type	23.6	41.1	54.2

Panel B: Percentage of patients for whom the obs choice equals the model's top predictions

Examination	t=1	t=2	t=3
Compare to top 3 ranked by dynamic model	44.9	62.7	74.3
Compare to top 3 ranked by Bayesian-myopic model	48.5	65.7	76.7
Compare to top 5 ranked by dynamic model	70.8	72.8	78.9
Compare to top 5 ranked by Bayesian-myopic model	66.3	74.6	79.0

- Kullback-Leibler Information Criterion: 11.95
- At the 95% critical value, the data favors the two-level dynamic model over the one-level model.

# Counterfactuals: Shares in the First Month

Counterfactual policies	None	TCA	NDRI	SSRI	SNRI	NaSSA	SARI
<b>Pricing</b>							
Baseline	31.7	4.9	12.1	31.9	12.1	2.4	4.9
All copayments set to \$5	31.1	4.8	11.9	33.1	11.9	2.4	4.8
Value-based design	16.5	6.6	16.5	34.1	16.5	3.3	6.6
<b>Informational campaigns</b>							
Baseline	31.7	4.9	12.1	31.9	12.1	2.4	4.9
Discourage use of reformulations	31.8	4.9	12.2	31.7	12.2	2.4	4.9
Psychiatrists' priors	31.6	4.8	12.1	32.2	12.1	2.4	4.8

## Counterfactuals: Calculating dollar value of health

- Berndt et al. (2002) provides recovery rates of first 16 weeks of care (via expert panel)
  - e.g. Patient on SSRI for  $> 30$  days has .28 rate of recovery, .60 rate of partial recovery
- Convert each individual's choice to an expected number of weeks with full/partial symptoms over first 16 weeks

Treatment	Full (wks)	Partial (wks)
No Drug Care	11.9	2.8
SSRI, $\leq 30$ days	10.3	3.9
SSRI, $> 30$ days	7.3	5.9

- Lave et al. (1998): disutility from full depression, -.41
- Covert utility change (in weeks) to dollars using \$100,000 value of year of life (Cutler (2004))



# Counterfactuals: Cost and health comparison

	Three month drug costs per patient (in \$)	Value of utility gain from symptomatic recovery (in \$)
Baseline	67.25	929.90
Effects of copayment policies		
	Change in three month drug costs per patient (in \$)	Change in symptomatic recovery (in \$)
All copayments set to \$5	30.28	10.42
Value-based design	3.13	193.35
Effects of informational campaigns		
	Change in three month drug costs per patient (in \$)	Change in symptomatic recovery (in \$)
Discourage use of reformulation products	(0.04)	(1.85)
Endow all physicians with psychiatrists' priors	0.65	2.18

# Counterfactuals: New Protocol

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		(1)	(2)	(3)	(4)	(5)		
		Prob drug is effective, hazard model	Prob drug is effective, dynamic model	Texas Medication Algorithm Project (1998)	APA Guidelines, Second Edition (2000,2005)	Comparative effectiveness review; AHRQ (2007)	Hazard Model	Dynamic Model
Product	Class							
Amitriptyline	TCA	51.7	0.0		X			
Bupropion	NDRI	60.5	0.0	X	X	X	X	
Wellbutrin XL	NDRI	61.8	0.0	X	X	X	X	
Citalopram	SSRI	72.0	55.7	X	X	X	X	X
Celexa	SSRI	66.1	59.4	X	X	X	X	X
Cymbalta	SNRI	67.4	0.0		X	X	X	
Lexapro	SSRI	64.6	81.1	X	X	X	X	X
Fluoxetine	SSRI	70.6	100.0	X	X	X	X	X
Prozac	SSRI	65.5	50.6	X	X	X	X	
Mirtazapine	NaSSA	59.2	0.0			X	X	
Nefazodone	SARI	41.7	0.0	X				
Nortriptyline	TCA	53.0	0.0		X			
Paroxetine	SSRI	69.3	97.0	X	X	X	X	X
Paxil CR	SSRI	58.3	97.9	X	X	X	X	X
Zoloft	SSRI	62.4	77.2	X	X	X	X	X
Trazodone	SARI	45.7	0.0					
Effexor	SNRI	60.2	0.0	X	X	X	X	
Effexor-XR	SNRI	71.1	0.0	X	X	X	X	

## Estimation: Likelihood form

When we assume independent products, the likelihood for individual  $i$  in period  $t$  is:

$$\prod_{j=1}^J E_{\varepsilon_{i1t}, \dots, \varepsilon_{iJt}} (1\{G_{ijt}(\Pi_t^{(j)}) + \varepsilon_{ijt} > G_{ikt}(\Pi_t^{(k)}) + \varepsilon_{ikt} \text{ for all } k \neq j\}^{d_{ijt}})$$
$$= \prod_{j=1}^J \left( \frac{\exp(G_{ijt}(X_{ij}, \hat{Y}_{i,j,t-1}; \gamma))}{1 + \sum_k \exp(G_{ikt}(X_{ik}, \hat{Y}_{i,k,t-1}; \gamma))} \right)^{d_{ijt}}$$

- $G_{ijt}$  is the index rule
- $d_{ijt} = 1$  if  $i$  chooses drug  $j$  in period  $t$
- $\hat{Y}_{i,l,t-1}$  is a vector of realized outcomes under treatments  $l = 1, \dots, J$  during the previous  $(t-1)$  periods
- $\varepsilon_{ijt}$  follow an extreme value distribution

## Estimation: Likelihood form

- $(\hat{Y}_{i,1,t-1}, \dots, \hat{Y}_{i,J,t-1})$  are latent
- Sum over the possible sequences of outcomes, weighting by the probability of observing those sequences

$$\sum_s \omega_{i,s} \prod_{j=1}^J \left( \frac{\exp(G_{ijt}(X_{ij}, \hat{Y}_{i,j,t-1}^s; \gamma))}{1 + \sum_k \exp(G_{ikt}(X_{ik}, \hat{Y}_{i,k,t-1}^s; \gamma))} \right)^{d_{ijt}}$$

- $\omega_{i,s}$  is the probability of observing one of  $s \in S$  possible sequences; follows a discrete binomial distribution
- $\hat{Y}_{i,j,t-1}^s$  represents discrete counts of successes and failures realized over  $(t-1)$  periods.
- Under rational expectations, the parameters that underlie  $\omega_{i,s}$  equal the parameters of the agents' priors.

# Estimation: Likelihood form

With dependency across the drugs via clusters

$$\sum_s \omega_{i,s} \prod_{c=1}^C \left[ \left( \frac{\exp(G_{ict}(\Pi_t^{(c),s}))}{1 + \sum_m^{C-1} \exp(G_{imt}(\Pi_t^{(m),s}))} \right)^{d_{ict}} \prod_{j \in c} \left( \frac{\exp(G_{ijt}(\Pi_t^{(j),s}))}{\sum_k^{J_c} \exp(G_{ikt}(\Pi_t^{(k),s}))} \right)^{d_{ijt}} \right]$$

where drug  $j$  is a choice contained in class  $c$ .

- Calculate the choice probabilities at two levels:
  1. the probability of a class being chosen
  2. the conditional probability of a drug being chosen, conditional on the class choice

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## Decision Rule: Index Solution

- $X_k(t)$  - the state variables of the choice problem at  $t$  (depends on  $\hat{Y}_{t-1}$ )
- At  $t$ , the agent chooses  $j$  if and only if:

$$G_j(X_j(t)) = \max_{k \in \{1, \dots, J\}} G_k(X_k(t))$$

$$G_j(x_j(t)) = \sup_{\tau \geq t} \left\{ \frac{E_t [\sum_{r=t}^{\tau} \beta^{r-t} R_j(X_j(r)) | x_j(t)]}{E_t [\sum_{r=t}^{\tau} \beta^{r-t} | x_j(t)]} \right\}$$

- $R_j(X_j(r))$  - the returns from option  $j$  given the state variables at time  $r$

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