## Final Grade Calculation: A Guide for the Perplexed

Let M be your Midterm exam score. Let F be your Final exam score. Your final grade for this course will be:

$$G = 0.3M + 0.3F + 0.4J^A$$

, where  $J^A$  is your adjusted non-exam score.

The adjusted non-exam score is an adjustment of your "raw" non-exam score J. In this course,

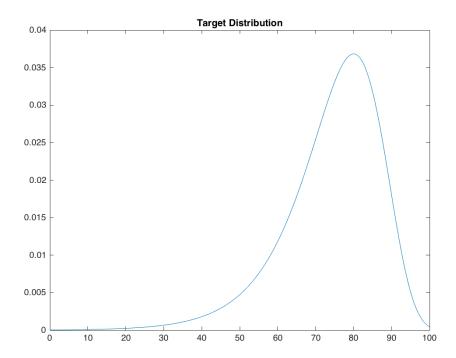
$$J = \frac{\text{sum of your homework scores}}{\text{total homework points}} \times 100$$

## How we adjust the non-exam score

In order to ensure fairness, it is desirable that non-exam scores across different sessions of the same course taught by different professors are comparable<sup>1</sup>. One way to do this is to adjust the non-exam scores such that their mean is the same in every class. For example, suppose there are only three students in one class: A, B, and C. Their "raw" non-exam scores are J(A) = 60, J(B) = 70, J(C) = 80. Then the mean non-exam score for this class is 70. Suppose our target mean is 80 (i.e., we could like the mean of adjusted non-exam scores to be 80 in each class), then to make the adjustment, we will let  $J^A = \frac{8}{7}J$ . As a result, the adjusted non-exam scores for the three students are  $J^A(A) = 68.6$ ,  $J^A(B) = 80$ ,  $J^A(C) = 91.4$ . This practice is called curving.

<sup>&</sup>lt;sup>1</sup> Since we already take exams together.

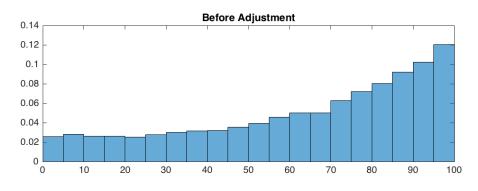
In addition to targeting the mean, we can also target the entire distribution. For example, we might want the distribution of  $J^A$  to look like this in every class:



To do this, we can use statistical methods that can help us transform any distribution of J into our target distribution of  $J^{A2}$ . Figure 1 shows one such example. Given an arbitrary set of J scores, we are able to transform its distribution, which is plotted in the upper panel, into a distribution that looks like our target distribution of  $J^A$ , which is plotted in the lower panel. Figure 2 shows how this transformation works. For example,  $J = 10 \Rightarrow J^A = 51$ ,  $J = 30 \Rightarrow J^A = 62$ ,  $J = 60 \Rightarrow J^A = 72$ ,  $J = 70 \Rightarrow J^A = 75$ ,  $J = 80 \Rightarrow J^A = 79$ ,  $J = 90 \Rightarrow J^A = 84$ , and  $J = 100 \Rightarrow J^A = 100$ . Note that in making the transformation, we change the distribution of non-exam scores while preserving their ranking, i.e. if J(A) < J(B), then  $J^A(A) < J^A(B)$ .

<sup>&</sup>lt;sup>2</sup> Here is one method.

Figure 1



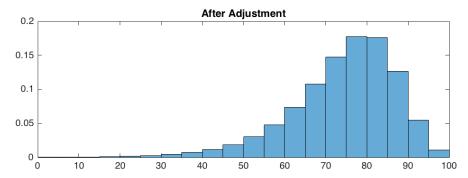


Figure 2

