CSE 5526 - Autumn 2018
Introduction to Neural Networks
Homework #4
Due Tuesday, Nov. 13

Grader: Hao Zhang
Office: 474 Dreese Lab
Office hours: 11:30-12:30 T & 1:00-2:00 W
Email: zhang.6720@osu.edu

Problem 1. For a winner-take-all network with 5 neurons, the function of each neuron is defined as

$$y_i(t+1) = \varphi\left((S-1)y_i(t) - \sum_{j \neq i} y_j(t)\right)$$

where S is the number of output neurons, and the activation function is defined as

$$\varphi(x) = \begin{cases} 0 & if\ x < 0 \\ x & if\ 0 \leq x \leq 1 \\ 1 & if\ x > 1 \end{cases}$$

The above network receives the input vector at time step 0, $\mathbf{x}^T = (0.2, 0.2, 0.3, 0.4, 0.3)$. Find the network output at time step 1 and 2.

Problem 2. The following figure shows the final weight vectors of a self-organizing map that has been trained on two-dimensional input vectors which were drawn from a uniform distribution over the triangular area. Lines between units (represented by dots) connect neighboring neurons. Draw the diagram of a network that has undergone such self-organization. Specify the elements of the network and their connections (no detailed values are needed).
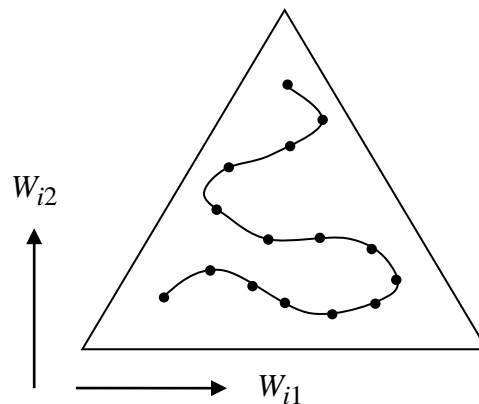
Problem 3. Exercise 13.4 in textbook (p. 728) – refer to lecture notes for the definitions of weight matrix and energy function. In addition to parts **(a)**-**(c)**:

    (d) Write down the energy function in terms of x_i's.