# Homework assignment#1 (Chap3)

TA Hint: 2020-1103

Due: 2020-1110

# (A) Exercises

- 3.1 Explain why problem formulation must follow goal formulation.
- 3.5 Consider the n-queens problem using the "efficient" incremental formulation given on page 72. Explain why the state space has at least  $\sqrt[3]{n!}$  states and estimate the largest n for which exhaustive exploration is feasible. (*Hint*: Derive a lower bound on the branching factor by considering the maximum number of squares that a queen can attack in any column.)
- **3.10** Define in your own words the following terms: state, state space, search tree, search node, goal, action, transition model, and branching factor.
- **3.14** Which of the following are true and which are false? Explain your answers.
  - a. Depth-first search always expands at least as many nodes as A\* search with an admissible heuristic.
  - **b.** h(n) = 0 is an admissible heuristic for the 8-puzzle.
  - c. A\* is of no use in robotics because percepts, states, and actions are continuous.
  - **d**. Breadth-first search is complete even if zero step costs are allowed.
  - e. Assume that a rook can move on a chessboard any number of squares in a straight line, vertically or horizontally, but cannot jump over other pieces. Manhattan distance is an admissible heuristic for the problem of moving the rook from square A to square B in the smallest number of moves.
- **3.21** Prove each of the following statements, or give a counterexample:
  - a. Breadth-first search is a special case of uniform-cost search.
  - **b**. Depth-first search is a special case of best-first tree search.
  - **c.** Uniform-cost search is a special case of A\* search.
- 3.25 The heuristic path algorithm (Pohl, 1977) is a best-first search in which the evaluation function is f(n) = (2 w)g(n) + wh(n). For what values of w is this complete? For what values is it optimal, assuming that h is admissible? What kind of search does this perform for w = 0, w = 1, and w = 2?

- **3.26** Consider the unbounded version of the regular 2D grid shown in Figure 3.9. The start state is at the origin, (0,0), and the goal state is at (x,y).
  - **a**. What is the branching factor *b* in this state space?
  - **b**. How many distinct states are there at depth k (for k > 0)?
  - **c**. What is the maximum number of nodes expanded by breadth-first tree search?
  - d. What is the maximum number of nodes expanded by breadth-first graph search?
  - **e.** Is h = |u x| + |v y| an admissible heuristic for a state at (u, v)? Explain.
  - **f**. How many nodes are expanded by  $A^*$  graph search using h?
  - **g**. Does h remain admissible if some links are removed?
  - **h**. Does h remain admissible if some links are added between nonadjacent states?
- **3.29** Prove that if a heuristic is consistent, it must be admissible. Construct an admissible heuristic that is not consistent.

# (B) Pseudo codes documentation

#### Code #1

## Code #2

```
function BREADTH-FIRST-SEARCH(problem) returns a solution, or failure

node ← a node with STATE = problem.INITIAL-STATE, PATH-COST = 0

if problem.GOAL-TEST(node.STATE) then return SOLUTION(node)

frontier ← a FIFO queue with node as the only element

explored ← an empty set

loop do

if EMPTY?(frontier) then return failure

node ← POP(frontier) /* chooses the shallowest node in frontier */

add node.STATE to explored

for each action in problem.ACTIONS(node.STATE) do

child ← CHILD-NODE(problem, node, action)

if child.STATE is not in explored or frontier then

if problem.GOAL-TEST(child.STATE) then return SOLUTION(child)

frontier ← INSERT(child, frontier)
```

```
function UNIFORM-COST-SEARCH(problem) returns a solution, or failure

node ← a node with STATE = problem.INITIAL-STATE, PATH-COST = 0
frontier ← a priority queue ordered by PATH-COST, with node as the only element
explored ← an empty set
loop do

if EMPTY?(frontier) then return failure

node ← POP(frontier) /* chooses the lowest-cost node in frontier */
if problem.GOAL-TEST(node.STATE) then return SOLUTION(node)
add node.STATE to explored
for each action in problem.ACTIONS(node.STATE) do

child ← CHILD-NODE(problem, node, action)
if child.STATE is not in explored or frontier then
frontier ← INSERT(child, frontier)
else if child.STATE is in frontier with higher PATH-COST then
replace that frontier node with child
```

## Code #4

```
function Depth-Limited-Search (problem, limit) returns soln/fail/cutoff
Recursive-DLS (Make-Node (Initial-State [problem]), problem, limit)

function Recursive-DLS (node, problem, limit) returns soln/fail/cutoff
cutoff-occurred? ← false

if Goal-Test [problem] (State [node]) then return Solution (node)
else if Depth [node] = limit then return cutoff
else for each successor in Expand (node, problem) do
result ← Recursive-DLS (successor, problem, limit)
if result = cutoff then cutoff-occurred? ← true
else if result ≠ failure then return result
if cutoff-occurred? then return cutoff else return failure
```

```
function Iterative-Deepening-Search( problem) returns a solution, or failure  \begin{array}{l} \text{inputs: } problem, \text{ a problem} \\ \text{for } depth \leftarrow 0 \text{ to } \infty \text{ do} \\ result \leftarrow \text{Depth-Limited-Search(} problem, depth) \\ \text{if } result \neq \text{cutoff then return } result \end{array}
```

```
function DEPTH-LIMITED-SEARCH(problem, limit) returns a solution, or failure/cutoff return RECURSIVE-DLS(Make-Node(problem.INITIAL-STATE), problem, limit) function RECURSIVE-DLS(node, problem, limit) returns a solution, or failure/cutoff if problem.Goal-Test(node.State) then return Solution(node) else if limit = 0 then return cutoff else cutoff\_occurred? \leftarrow false \\ for each action in problem.Actions(node.State) do \\ child \leftarrow Child-Node(problem, node, action) \\ result \leftarrow Recursive-DLS(child, problem, limit - 1) \\ if result = cutoff then cutoff\_occurred? \leftarrow true \\ else if result \neq failure then return result \\ if cutoff\_occurred? then return cutoff else return failure
```

## Code #6

```
function RECURSIVE-BEST-FIRST-SEARCH(problem) returns a solution, or failure
   return RBFS(problem, MAKE-NODE(problem.INITIAL-STATE), \infty)
function RBFS(problem, node, f_limit) returns a solution, or failure and a new f-cost limit
  if problem.GOAL-TEST(node.STATE) then return SOLUTION(node)
  successors \leftarrow [\ ]
  for each action in problem.ACTIONS(node.STATE) do
      add CHILD-NODE(problem, node, action) into successors
  if successors is empty then return failure, \infty
  for each s in successors do /* update f with value from previous search, if any */
      s.f \leftarrow \max(s.g + s.h, node.f)
  loop do
      best \leftarrow \text{the lowest } f\text{-value node in } successors
      if best.f > f\_limit then return failure, best.f
      alternative \leftarrow the second-lowest f-value among successors
      result, best. f \leftarrow RBFS(problem, best, min(f\_limit, alternative))
      if result \neq failure then return result
```

```
function SMA*(problem) returns a solution sequence
 inputs: problem, a problem
 static: Queue, a queue of nodes ordered by f-cost
 Queue ← MAKE-QUEUE({MAKE-NODE(INITIAL-STATE[problem])})
 loop do
      if Queue is empty then return failure
      n \leftarrow deepest least-f-cost node in Queue
      if GOAL-TEST(n) then return success
      s \leftarrow \text{NEXT-SUCCESSOR}(n)
      if s is not a goal and is at maximum depth then
        f(s) \leftarrow \infty
      else
        f(s) \leftarrow MAX(f(n),g(s)+h(s))
      if all of n's successors have been generated then
        update n's f-cost and those of its ancestors if necessary
      if SUCCESSORS(n) all in memory then remove n from Queue
      if memory is full then
        delete shallowest, highest-f-cost node in Queue
        remove it from its parent's successor list
        insert its parent on Queue if necessary
      insert s in Queue
  end
```