

# RIScatter: Unifying Backscatter Communication and Reconfigurable Intelligent Surface

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**Abstract**—Backscatter Communication (BackCom) nodes harvest energy from and modulate information over external electromagnetic waves. Reconfigurable Intelligent Surface (RIS) adapts its phase shift response to alter channel strength in specific directions. In this paper, we show how those two different technologies (and their derivatives) can be unified into one architecture called RIScatter. RIScatter consists of dispersed or co-located scatter nodes, whose reflection states are adapted to partially modulate their information and partially engineer the wireless channel. The key is to render the probability distribution of reflection states as a joint function of the information source, Channel State Information (CSI), and relative priority of coexisting links. This enables RIScatter to softly bridge BackCom and RIS; reduce to either under specific distribution; or evolve in a mixed form for heterogeneous traffic control and universal hardware design. We also propose a low-complexity Successive Interference Cancellation (SIC)-free receiver that effectively exploits the properties of RIScatter. For a single-user multi-node network, we characterize the achievable primary-(total-)backscatter rate region by optimizing the input distribution at scatter nodes, the active beamforming at the Access Point (AP), and the energy decision regions at the user. Simulations demonstrate RIScatter nodes can recycle surrounding radios for backscatter modulation and passive beamforming.

**Index Terms**—Backscatter communication, reconfigurable intelligent surface, active-passive coexisting network, input distribution design, SIC-free receiver.

## I. INTRODUCTION

**F**UTURE wireless network is envisioned to provide high throughput, uniform coverage, pervasive connectivity, heterogeneous control, and cognitive intelligence for trillions of low-power devices. Backscatter Communication (BackCom) separates a transmitter into a Radio-Frequency (RF) carrier emitter with power-hungry elements (e.g., synthesizer and amplifier) and an information-bearing node with power-efficient components (e.g., harvester and modulator) [1]. The receiver (reader) can be either co-located or separated with the carrier emitter, known as Monostatic BackCom (MBC) and Bistatic BackCom (BBC) in Fig. 1(a) and 1(b), respectively. Relevant applications such as Radio-Frequency Identification (RFID) [2], [3] and passive sensor network [4], [5] have been extensively researched, standardized, and commercialized to embrace the Internet of Everything (IoE). However, conventional backscatter nodes only respond when externally inquired by a nearby reader. Ambient Backscatter Communication (AmBC) in Fig. 1(c) was proposed a decade ago where battery-free nodes recycle ambient signals (e.g., radio, television and Wi-Fi)

to harvest energy and establish connections [6]. It does not require dedicated power source, carrier emitter, or frequency spectrum, but the backscatter decoding is subject to the strong interference from the primary (legacy) link. To tackle this, cooperative AmBC [7] employs a co-located receiver to decode both coexisting links and the concept was further refined as Symbiotic Radio (SR) in Fig. 1(d) [8]. Specifically, the active transmitter generates RF wave carrying primary information, the passive node creates a rich-scattering environment and rides its own information, and the co-located receiver cooperatively decodes both links. In those BackCom applications, the scatter node is considered as an *information source* and the reflection pattern depends exclusively on the information symbol. On the other hand, Reconfigurable Intelligent Surface (RIS) in Fig. 1(e) is a smart signal reflector with numerous passive elements of adjustable phase shifts. It customizes the wireless environment for signal enhancement, interference suppression, scattering enrichment, and/or non-line-of-sight bypassing [9]. Each RIS element is considered as a *channel shaper* and the reflection pattern depends exclusively on the Channel State Information (CSI).

As a special case of Cognitive Radio (CR), active and passive transmissions coexist and interplay in AmBC and SR. Such a coexistence is classified into commensal (overlay), parasitic (underlay), and competitive (interfering) paradigms, and their achievable rate and outage performance were investigated in [10], [11]. For the co-located cooperative receiver, the Bit Error Rate (BER) performance of Maximum-Likelihood (ML), linear, and Successive Interference Cancellation (SIC) detectors are derived over flat fading channels [7]. However, the work assumed equal symbol duration and perfect synchronization for primary and backscatter links. Importantly, active-passive coexisting networks have three special and important properties:

- 1) Primary and backscatter symbols are superimposed by *double modulation* (i.e., multiplication coding);
- 2) Backscatter signal strength is much weaker than primary due to the *double fading* effect;
- 3) The spreading factor (i.e., backscatter symbol duration over primary) is usually large<sup>1</sup>.

The second property motivated [7], [8], [10], [11], [13]–[19] to view SR as a multiplicative Non-Orthogonal Multiple Access (NOMA) and perform SIC from primary to backscatter link. During primary decoding, the backscatter signal can be modelled as channel uncertainty or multiplicative interference when the spreading factor is large or small, respectively.

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<sup>1</sup>The load-switching interval of low-power backscatter modulators is usually 0.1 to 10  $\mu$ s [12], accounting for a typical spreading factor between 10 and  $10^3$ .

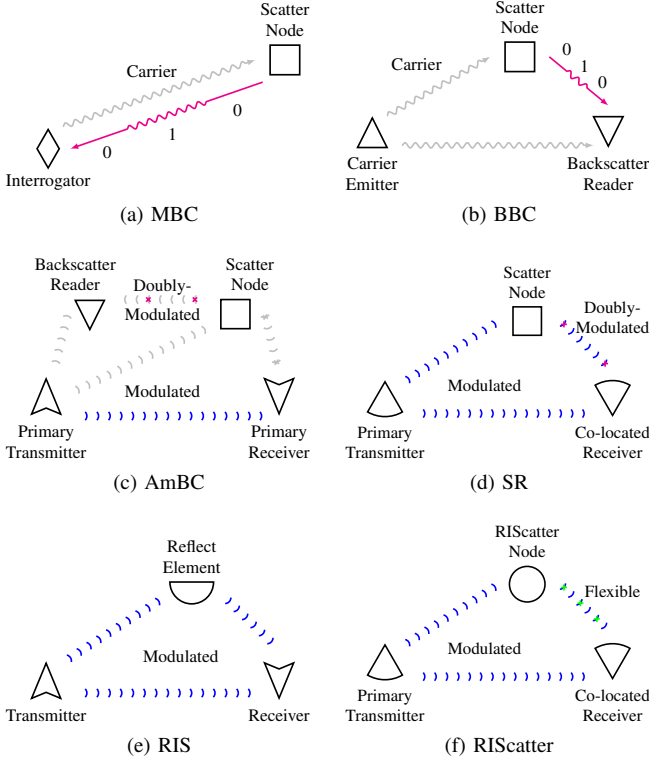


Fig. 1. Illustration of scattering applications. The blue flow(s) constitutes the primary link while the magenta/green flow denotes the backscatter link.

Decoding each backscatter symbol also requires multiple SIC followed by a Maximal Ratio Combining (MRC) over primary blocks, which is operation-intensive and CSI-sensitive. When the spreading factor is sufficiently large, the primary achievable rate under semi-coherent detection<sup>2</sup> asymptotically approaches its coherent counterpart and both links are decoded interference-free [13]. However, this severely limits the backscatter throughput and requires numerous SIC per backscatter symbol.

On the other hand, static RIS design with fixed reflection pattern per channel block has been extensively studied in wireless communication, sensing, and power literature [20]–[25]. Dynamic RIS performs time sharing between different phase shifts and introduces artificial channel diversity within each channel block. It was first proposed to fine-tune the Orthogonal Frequency-Division Multiplexing (OFDM) resource blocks [26] then extended to the downlink power and uplink information phases of Wireless Powered Communication Network (WPCN) [27]–[29]. However, dynamic RIS carries *no* additional information since the reflection state at each time slot is known to the receiver. RIS can also be used as an information source and prototypes have been developed for Phase Shift Keying (PSK) [30] and Quadrature Amplitude Modulation (QAM) [31]. From an information-theoretic perspective, the authors of [32] reported that joint transmitter-RIS encoding achieves the capacity of RIS-aided finite-input channel and using RIS as a naive passive beamformer to maximize the receive Signal-to-Noise Ratio (SNR) is generally suboptimal.

<sup>2</sup>In this paper, semi-coherent detection refers to the primary/backscatter decoding with known CSI and unknown backscatter/primary symbols.

This inspired RIS-empowered BackCom [33]–[42] to combine passive beamforming and backscatter modulation in the overall reflection pattern. In particular, *symbol level precoding* maps the information symbols to the optimized RIS coefficient sets [33], [34], *overlay modulation* superposes the information symbols over a common auxiliary matrix [35]–[38], *spatial modulation* switches between the reflection coefficient sets that maximize SNR at different receive antennas [39]–[41], and *index modulation* employs dedicated reflection elements (resp. information elements) for passive beamforming (resp. backscatter modulation) [42]. However, those joint designs incur advanced hardware architecture and high optimization complexity. Relevant literature also considers either Gaussian codebook [10], [11], [13]–[17], [37] that is impractical for low-power nodes or finite equiprobable inputs [7], [8], [18], [19], [33]–[36], [38]–[42] that does not fully exploit the CSI and properties of active-passive coexisting networks. Those problems are addressed in this paper and the contributions are summarized below.

*First*, we propose RIScatter as a novel protocol that unifies BackCom and RIS by adaptive reflection state (backscatter input) distribution design. The concept is shown in Fig. 1(f) where one or more RIScatter nodes ride over an active transmission and simultaneously modulate their information and engineer the wireless channel. A co-located receiver cooperatively decodes both coexisting links and each reflection state simultaneously acts as information and passive beamforming codewords. The reflection pattern of each node is semi-randomly chosen with the guidance of input distribution as a joint function of the information source, CSI, and Quality of Service (QoS)<sup>3</sup>. Such an adaptive channel coding boils down to the degenerate distribution of RIS when the primary link is prioritized, and outperforms the uniform distribution of BackCom (by accounting the CSI) when the backscatter link is prioritized. Joint and independent encoding are available when multiple RIScatter nodes are co-located and dispersed, respectively. Table I compares RIScatter to BackCom and RIS. However, two major challenges for RIScatter are the practical receiver and input distribution design. This is the first paper to unify BackCom and RIS from the perspective of input distribution.

*Second*, we address the first challenge and propose a practical receiver that semi-coherently decodes the backscatter information, recovers the reflection pattern, and coherently decodes the primary link. We consider backscatter energy detection and formulate a Discrete Memoryless Multiple Access Channel (DMMAC) over disjoint decision regions. Thanks to the double modulation and symbol-level passive precoding, the semi-coherent backscatter decoding is essentially part of channel training. Once the backscatter information is successfully decoded, its contribution can be modelled within composite channel as dynamic passive beamforming (rather than re-precoded and cancelled). It requires only one energy comparison and re-encoding per backscatter symbol and is much efficient than conventional decoding based on SIC and MRC. It is also suitable for arbitrary input distribution and spreading factor, which significantly improves backscatter throughput. This is the first paper to consider practical backscatter-primary

<sup>3</sup>QoS refers to the relative priority of the primary link.

TABLE I  
COMPARISON OF SCATTERING APPLICATIONS

	MBC/BBC	AmBC	SR (large spreading factor)	RIS	RIScatter
Information link(s)	Backscatter	Coexisting	Coexisting	Primary	Coexisting
Primary signal on backscatter decoding	Carrier	Multiplicative interference	Spreading code	—	Energy uncertainty
Backscatter signal on primary decoding	—	Multiplicative interference	CSI uncertainty	Passive beamforming	Dynamic passive beamforming
Cooperative devices	—	No	Primary transmitter and co-located receiver	—	Primary transmitter, scatter nodes, and co-located receiver
Sequential decoding	—	No	Primary-to-backscatter, SIC and MRC	—	Backscatter-to-primary, no SIC/MRC
Reflection pattern depends on	Information source	Information source	Information source	CSI	Information source, CSI, and QoS
Reflection state distribution	Equiprobable	Equiprobable	Equiprobable or Gaussian	Degenerate	Flexible
Load-switching speed	Fast	Slow	Slow	Quasi-static	Arbitrary

decoding scheme to exploit backscatter modulation as dynamic passive beamforming at the co-located receiver.

*Third*, we address the second challenge and consider a single-user multi-node Multiple-Input Single-Output (MISO) scenario. We characterize the achievable primary-(total-)backscatter rate region by optimizing the input distribution at RIScatter nodes, the active beamforming at the Access Point (AP), and the energy decision regions at the user under different QoS. A Block Coordinate Descent (BCD) algorithm is proposed where the Karush-Kuhn-Tucker (KKT) input distribution is numerically evaluated by limit of sequences, the active beamforming is optimized by Projected Gradient Descent (PGD), and the decision regions are refined by existing sequential quantizer for Discrete Memoryless Thresholding Channel (DMTC). Uniquely, we consider CSI, QoS, and backscatter constellation in the optimization and the input distribution result is applicable to general detection schemes. This is also the first paper to reveal the importance of backscatter input distribution and decision region designs in active-passive coexisting networks.

*Notations:* Italic, bold lower-case, and bold upper-case letters denote scalars, vectors and matrices, respectively.  $\mathbf{0}$  and  $\mathbf{1}$  denote zero and one array of appropriate size, respectively.  $\mathbb{I}^{x \times y}$ ,  $\mathbb{R}_+^{x \times y}$ , and  $\mathbb{C}^{x \times y}$  denote the unit, real nonnegative, and complex spaces of dimension  $x \times y$ , respectively.  $j$  denotes the imaginary unit.  $\text{diag}(\cdot)$  returns a square matrix with the input vector on its main diagonal and zeros elsewhere.  $\text{card}(\cdot)$  returns the cardinality of a set.  $\log(\cdot)$  denotes logarithm of base  $e$ .  $(\cdot)^*$ ,  $(\cdot)^T$ ,  $(\cdot)^H$ ,  $|\cdot|$ , and  $\|\cdot\|$  denote the conjugate, transpose, conjugate transpose (Hermitian), absolute value, and Euclidean norm operators, respectively.  $(\cdot)^{(r)}$  and  $(\cdot)^*$  denote the  $r$ -th iterated and optimal results, respectively. The distribution of a Circularly Symmetric Complex Gaussian (CSCG) random variable with zero mean and variance  $\sigma^2$  is denoted by  $\mathcal{CN}(0, \sigma^2)$ , and  $\sim$  means “distributed as”.

## II. RISCATTER

### A. Principles

RF wave scattering or reflecting are often manipulated by passive antennas or programmable metamaterial [43]. The former receives the impinging signals and reradiates some back to the space, while the latter reflects at the space-cell boundary and mainly applies a phase shift. In the scattered signal, the structural mode component depends on the scatterer geometry and material. It is usually modelled as a DC offset [1] or part of environment multipath [44]. On the other hand, the antenna mode component depends on the impedance mismatch and is widely exploited in scattering applications. For an antenna (resp. metamaterial) scatterer with  $M$  reflection states, the reflection coefficient at state  $m \in \mathcal{M} \triangleq \{1, \dots, M\}$  is

$$\Gamma_m = \frac{Z_m - Z^*}{Z_m + Z}, \quad (1)$$

where  $Z_m$  is the antenna load (resp. metamaterial cell) impedance at state  $m$ , and  $Z$  is the antenna input (resp. medium characteristic) impedance. Specifically,

- **BackCom:** The scatterer is an information source with random reflection pattern over time. The reflection coefficient at state  $m$  is used merely an information codeword [45]

$$\Gamma_m = \alpha_m \frac{c_m}{\max_{m'} |c_{m'}|}, \quad (2)$$

where  $\alpha_m \in \mathbb{I}$  is the amplitude scattering ratio and  $c_m$  is the constellation point.

- **RIS:** The scatterer is a channel shaper with deterministic reflection pattern over time. The reflection coefficient at state  $m$  is used merely a passive beamforming codeword [20]

$$\Gamma_m = \alpha_m \exp(j\theta_m), \quad (3)$$

where  $\theta_m$  is the phase shift.<sup>4</sup>

RIScatter generalizes BackCom and RIS from a probabilistic perspective. Each reflection coefficient is simultaneously an

<sup>4</sup>It is commonly assumed  $\alpha_m \ll 1$  in BackCom and  $\alpha_m = 1$  in RIS.



Fig. 2. Input distribution and reflection pattern of scattering applications. “PB”, “BB”, and “CB” refer to primary symbol block, backscatter symbol block, and channel block, respectively. Shadowing means presence of primary link. In this example, the optimal passive beamformer corresponds to state 2, and the spreading factor is 4 for RIScatter and 8 for AmBC/SR. BackCom and RIS can be viewed as extreme cases of RIScatter, where the input distribution boils down to uniform and degenerate, respectively.

information codeword and a passive beamforming codeword. As shown in Fig. 2, RIScatter nodes semi-randomly choose reflection states according to an input distribution that strikes a balance between backscatter modulation and passive beamforming.

**Remark 1.** Unlike dynamic RIS that simply performs a time sharing between reflection states, RIScatter conveys additional information by randomizing the reflection pattern over time while still guaranteeing the probability of occurrence of each state. Upon successful backscatter detection, the impact of RIScatter nodes on the primary link can be modelled as dynamic passive beamforming.

RIScatter nodes can be implemented, for example, by adding an integrated receiver [46] and adaptive encoder [47] to off-the-shelf passive RFID tags. The block diagram, equivalent circuit, and scatter model are illustrated in Fig. 3. To exploit the benefits of RIScatter, we also propose a low-complexity receiver that semi-coherently decodes the backscatter link, recovers the reflection pattern, and coherently decodes the primary link. The detail will be covered in Section II-B.

### B. System Model

As shown in Fig. 4, we consider a RIScatter system where a  $Q$ -antenna AP serves a single-antenna user and  $K$  nearby dispersed or co-located RIScatter nodes. All nodes have  $M$  available reflection states. In the primary point-to-point system, the AP transmits information to the user over a multipath channel<sup>5</sup> enhanced by RIScatter nodes. In the backscatter

multiple access system, the AP acts as carrier emitter, the RIScatter nodes modulate over scattered signal, and the user jointly decodes all node messages.<sup>6</sup> For simplicity, we consider a quasi-static block fading model and focus on a specific channel block where the CSI remains constant. Denote the AP-user direct channel as  $\mathbf{h}_D^H \in \mathbb{C}^{1 \times Q}$ , the AP-node  $k \in \mathcal{K} \triangleq \{1, \dots, K\}$  forward channel as  $\mathbf{h}_{F,k}^H \in \mathbb{C}^{1 \times Q}$ , the node  $k$ -user backward channel as  $\mathbf{h}_{B,k}$ , and the cascaded AP-node  $k$ -user channel as  $\mathbf{h}_{C,k}^H \triangleq \mathbf{h}_{B,k} \mathbf{h}_{F,k}^H \in \mathbb{C}^{1 \times Q}$ . We assume the direct and cascaded CSI are available at the AP and user<sup>7</sup>.

Let  $x_k \in \mathcal{X} \triangleq \{c_1, \dots, c_M\}$  be the coded backscatter symbol of node  $k$  and  $\mathbf{x}_{\mathcal{K}} \triangleq (x_1, \dots, x_K)$  be the backscatter symbol tuple of all nodes. Due to double modulation, the composite channel is a function of backscatter symbol tuple<sup>8</sup>

$$\mathbf{h}^H(\mathbf{x}_{\mathcal{K}}) \triangleq \mathbf{h}_D^H + \sum_k \alpha_k \mathbf{h}_{C,k}^H x_k \quad (4a)$$

$$= \mathbf{h}_D^H + \mathbf{x}^H \text{diag}(\boldsymbol{\alpha}) \mathbf{H}_C, \quad (4b)$$

where  $\alpha_k \in \mathbb{I}$  is the common amplitude scattering ratio of node  $k$ ,  $\boldsymbol{\alpha} \triangleq [\alpha_1, \dots, \alpha_K]^T \in \mathbb{I}^K$ ,  $\mathbf{x} \triangleq [x_1, \dots, x_K]^H \in \mathcal{X}^K$ , and  $\mathbf{H}_C \triangleq [\mathbf{h}_{C,1}, \dots, \mathbf{h}_{C,K}]^H \in \mathbb{C}^{K \times Q}$ .

Next, we consider the signal model within one backscatter block. The signal received by the user at primary block  $n \in \mathcal{N} \triangleq \{1, \dots, N\}$  is

$$y[n] = \mathbf{h}^H(\mathbf{x}_{\mathcal{K}}) \mathbf{w} s[n] + v[n], \quad (5)$$

where  $\mathbf{w} \in \mathbb{C}^Q$  is the active beamformer satisfying average transmit power constraint  $\|\mathbf{w}\|^2 \leq P$ ,  $s \sim \mathcal{CN}(0, 1)$  is the primary symbol, and  $v \sim \mathcal{CN}(0, \sigma_v^2)$  is the Additive White Gaussian Noise (AWGN) with average power  $\sigma_v^2$ . Let  $m_k \in \mathcal{M} \triangleq \{1, \dots, M\}$  be the reflection state index of node  $k$  and  $\mathbf{m}_{\mathcal{K}} \triangleq (m_1, \dots, m_K)$  be the state index tuple of all nodes. The backscatter symbol tuple  $\mathbf{x}_{\mathcal{K}}$  is a random variable that takes value  $x_{m_{\mathcal{K}}}$  when state tuple  $\mathbf{m}_{\mathcal{K}}$  is used. Conditioned on hypothesis  $\mathcal{H}_{\mathbf{m}_{\mathcal{K}}}$ , the receive signal per primary block follows CSCG distribution  $\mathcal{CN}(0, \sigma_{\mathbf{m}_{\mathcal{K}}}^2)$ , where

$$\sigma_{\mathbf{m}_{\mathcal{K}}}^2 = |\mathbf{h}^H(\mathbf{x}_{\mathbf{m}_{\mathcal{K}}}) \mathbf{w}|^2 + \sigma_v^2 \quad (6)$$

is its variance. Let  $z = \sum_n |y[n]|^2$  be the accumulated energy per backscatter block. Since  $z$  is the sum of  $N$  independent and identically distributed (i.i.d.) exponential variables, the conditional Probability Density Function (PDF) follows Gamma distribution

$$f(z|\mathcal{H}_{\mathbf{m}_{\mathcal{K}}}) = \frac{z^{N-1} \exp(-z/\sigma_{\mathbf{m}_{\mathcal{K}}}^2)}{\sigma_{\mathbf{m}_{\mathcal{K}}}^{2N} (N-1)!}. \quad (7)$$

The user first jointly decodes all backscatter messages under primary interference by performing energy detection over disjoint decision regions. For the ease of notation, we map the state index tuple  $\mathbf{m}_{\mathcal{K}}$  to  $l \in \mathcal{L} \triangleq \{1, \dots, L\}$ , where  $L \triangleq M^K$  and  $\sigma_1^2, \dots, \sigma_L^2$  forms an increasing sequence. Both notations are

<sup>6</sup>It is assumed that the signal going through two or more RIScatter nodes is too weak to be received by the user.

<sup>7</sup>The cascaded CSI can be estimated by sequential [49]–[51] or parallel [52] approaches for dispersed nodes, or group-based [53] or hierarchical [54] approaches for co-located nodes.

<sup>8</sup>(4a) and (4b) are often used in BackCom and RIS literature, respectively.

<sup>5</sup>It is assumed the primary symbol duration is much longer than multipath delay spread (no inter-symbol interference).



Fig. 3. Block diagram, equivalent circuit, and scatter model of a RIScatter node. The solid and dashed vectors represent signal and energy flows. The scatter antenna behaves as a constant power source, where the voltage  $V_0$  and current  $I_0$  are introduced by incident electric field  $\vec{E}_i$  and magnetic field  $\vec{H}_i$  [48].

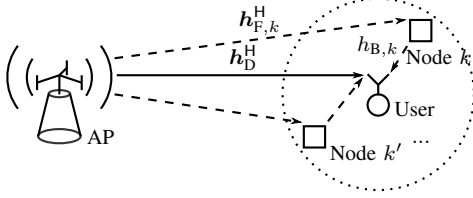


Fig. 4. A single-user multi-node RIScatter system.

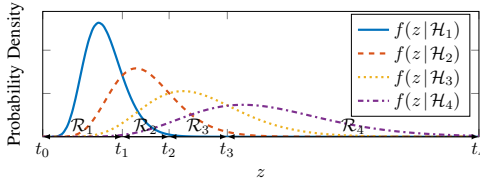


Fig. 5. PDF of accumulated energy per backscatter block conditioned on different reflection state hypotheses.

used interchangeably in the following context. The decision region of backscatter symbol tuple  $l$  is

$$\mathcal{R}_l \triangleq [t_{l-1}, t_l), \quad 0 \leq t_{l-1} \leq t_l, \quad (8)$$

where  $t_l$  is the energy decision threshold between hypotheses  $\mathcal{H}_l$  and  $\mathcal{H}_{l+1}$ . For a given decision threshold vector  $\mathbf{t} \triangleq [t_0, \dots, t_L]^T \in \mathbb{R}_+^{(L+1)}$ , we can formulate a DMMAC with transition probability from input  $x_{m_K}$  to output  $\hat{x}_{m'_K}$  as

$$P(\hat{x}_{m'_K} | x_{m_K}) = \int_{\mathcal{R}_{m'_K}} f(z | \mathcal{H}_{m_K}) dz, \quad (9)$$

over which input distribution of all RIScatter nodes can be designed. An example of energy detection is illustrated in Fig. 5.

**Remark 2.** The capacity-achieving decision region design for DMTC with non-binary inputs in arbitrary distribution remains an open issue. It was proved deterministic detectors can be rate-optimal, but non-convex decision regions (comprise non-adjacent partitions) are generally required and the optimal number of thresholds remains unknown [55], [56]. Hence, we limit the energy detector to convex deterministic decision regions and consider sequential threshold design.

After successful backscatter decoding, the user can re-encode for exact reflection pattern and obtain the composite channel by (4), then coherently decode the primary link. Such an SIC-free sequential decoding enables backscatter modulation and dynamic passive beamforming by only one energy comparison

and re-encoding per backscatter symbol. It also supports arbitrary input distribution and spreading factor for higher backscatter throughput.

### C. Achievable Rates

Denote the probability of node  $k$  choosing reflection state  $m_k$  as  $P_k(x_{m_k})$  and let  $\mathbf{p}_k \triangleq [P_k(c_1), \dots, P_k(c_M)]^T \in \mathbb{I}^M$ . For dispersed nodes with independent encoding, the probability of backscatter symbol tuple  $x_{m_K}$  is

$$P_{\mathcal{K}}(x_{m_K}) = \prod_{k \in \mathcal{K}} P_k(x_{m_k}). \quad (10)$$

Following [57], we define the backscatter information function between input value tuple  $x_{m_K}$  and output variable tuple  $\hat{x}_{\mathcal{K}}$  as

$$I_B(x_{m_K}; \hat{x}_{\mathcal{K}}) \triangleq \sum_{m'_K} P(\hat{x}_{m'_K} | x_{m_K}) \log \frac{P(\hat{x}_{m'_K} | x_{m_K})}{P_{\mathcal{K}}(\hat{x}_{m'_K})}, \quad (11)$$

where  $P_{\mathcal{K}}(\hat{x}_{m'_K}) = \sum_{m_K} P_{\mathcal{K}}(x_{m_K}) P(\hat{x}_{m'_K} | x_{m_K})$ . We also define the backscatter marginal information of  $x_{m_k}$  as

$$I_{B,k}(x_{m_k}; \hat{x}_{\mathcal{K}}) \triangleq \sum_{m_{\mathcal{K} \setminus \{k\}}} P_{\mathcal{K} \setminus \{k\}}(x_{m_{\mathcal{K} \setminus \{k\}}}) I_B(x_{m_K}; \hat{x}_{\mathcal{K}}), \quad (12)$$

where  $P_{\mathcal{K} \setminus \{k\}}(x_{m_{\mathcal{K} \setminus \{k\}}}) = \prod_{q \in \mathcal{K} \setminus \{k\}} P_q(x_{m_q})$ . Hence, the backscatter mutual information can be written as

$$I_B(x_{\mathcal{K}}; \hat{x}_{\mathcal{K}}) = \sum_{m_K} P_{\mathcal{K}}(x_{m_K}) I_B(x_{m_K}; \hat{x}_{\mathcal{K}}). \quad (13)$$

Once nodes are successfully decoded, we can re-encode and determine the composite channel by (4). The primary information function conditioned on  $x_{m_K}$  is

$$I_P(s; y | x_{m_K}) \triangleq \log \left( 1 + \frac{|\mathbf{h}^H(x_{m_K}) \mathbf{w}|^2}{\sigma_v^2} \right), \quad (14)$$

the primary marginal information of  $x_{m_k}$  is

$$I_{P,k}(s; y | x_{m_k}) \triangleq \sum_{m_{\mathcal{K} \setminus \{k\}}} P_{\mathcal{K} \setminus \{k\}}(x_{m_{\mathcal{K} \setminus \{k\}}}) I_P(s; y | x_{m_K}), \quad (15)$$

and the average primary mutual information is

$$I_P(s; y | x_{\mathcal{K}}) = \sum_{m_K} P_{\mathcal{K}}(x_{m_K}) I_P(s; y | x_{m_K}). \quad (16)$$

With a slight abuse of notation, we define the weighted sum information function, marginal information, and mutual information as

$$I(x_{m_K}) \triangleq \rho I_P(s; y | x_{m_K}) + (1 - \rho) I_B(x_{m_K}; \hat{x}_{\mathcal{K}}), \quad (17)$$

$$I_k(x_{m_k}) \triangleq \rho I_{P,k}(s; y | x_{m_k}) + (1 - \rho) I_{B,k}(x_{m_k}; \hat{x}_{\mathcal{K}}), \quad (18)$$

$$I(x_{\mathcal{K}}) \triangleq \rho I_P(s; y | x_{\mathcal{K}}) + (1 - \rho) I_B(x_{\mathcal{K}}; \hat{x}_{\mathcal{K}}), \quad (19)$$

where  $\rho \in \mathbb{I}$  is the relative QoS of the primary link. We notice the average primary rate (16) depends on the backscatter input distribution and active beamforming, while the total backscatter rate depends on the input distribution and DMMAC (9) that relates to the active beamforming and decision thresholds.

### III. RATE-REGION CHARACTERIZATION

To characterize the achievable primary-(total-)backscatter rate region for the RIScatter system, we aim to maximize the weighted sum rate with respect to input distribution  $\{\mathbf{p}_k\}_{k \in \mathcal{K}}$ , active beamforming  $\mathbf{w}$ , and decision thresholds  $\mathbf{t}$  by

$$\max_{\{\mathbf{p}_k\}_{k \in \mathcal{K}}, \mathbf{w}, \mathbf{t}} I(x_{\mathcal{K}}) \quad (20a)$$

$$\text{s.t.} \quad \mathbf{1}^\top \mathbf{p}_k = 1, \quad \forall k, \quad (20b)$$

$$\mathbf{p}_k \geq \mathbf{0}, \quad \forall k, \quad (20c)$$

$$\|\mathbf{w}\|^2 \leq P, \quad (20d)$$

$$t_{l-1} \leq t_l, \quad \forall l, \quad (20e)$$

$$\mathbf{t} \geq \mathbf{0}. \quad (20f)$$

Problem (20) generalizes conventional BackCom by allowing CSI- and QoS-adaptive input distribution and decision region design. It also generalizes the discrete RIS phase shift selection problem by stochastic reflection that relaxes the feasible domain from the vertices of  $M$ -dimensional probability simplex to the simplex itself. Problem (20) is highly non-convex and we propose a BCD algorithm that iteratively updates  $\{\mathbf{p}_k\}_{k \in \mathcal{K}}$ ,  $\mathbf{w}$  and  $\mathbf{t}$ .

#### A. Input Distribution

For any given  $\mathbf{w}$  and  $\mathbf{t}$ , we can construct the equivalent DMMAC by (9) and simplify (20) to

$$\max_{\{\mathbf{p}_k\}_{k \in \mathcal{K}}} I(x_{\mathcal{K}}) \quad (21a)$$

$$\text{s.t.} \quad (20b), (20c), \quad (21b)$$

which is convex when  $K=1$  or joint encoding<sup>9</sup> over  $K > 1$  co-located nodes. When the nodes are dispersed, problem (21) involves product term  $\prod_{k \in \mathcal{K}} P_k(x_{m_k})$  and is non-convex. Following [57], we first recast the KKT conditions to their equivalent forms then propose a numerical method that guarantees those conditions on convergence of sequences.

**Remark 3.** As demonstrated in [58], KKT conditions are generally necessary but insufficient for total rate maximization of DMMAC. We will later show by simulation that, for a moderate  $K$ , the average achievable rate regions of KKT and global-optimal input distributions completely coincide with each other.

**Proposition 1.** The KKT optimality conditions for problem (21) are equivalent to,  $\forall k, m_k$ ,

$$I_k^*(x_{m_k}) = I^*(x_{\mathcal{K}}), \quad P_k^*(x_{m_k}) > 0, \quad (22a)$$

$$I_k^*(x_{m_k}) \leq I^*(x_{\mathcal{K}}), \quad P_k^*(x_{m_k}) = 0. \quad (22b)$$

<sup>9</sup>Joint encoding formulates an equivalent source of  $M^K$  codewords, such that one can directly design  $P_{\mathcal{K}}(x_{m_{\mathcal{K}}})$ ,  $\forall m_{\mathcal{K}}$  instead of  $P_k(x_{m_k})$ ,  $\forall k, m_k$ .

#### Algorithm 1: Numerical KKT Input Distribution Evaluation by Limits of Sequence

**Input:**  $K, N, \mathbf{h}_D^H, \mathbf{H}_C, \boldsymbol{\alpha}, \mathcal{X}, \sigma_v^2, \rho, \mathbf{w}, \mathbf{t}, \epsilon$

**Output:**  $\{\mathbf{p}_k^*\}_{k \in \mathcal{K}}$

- 1: Set  $\mathbf{h}^H(x_{m_{\mathcal{K}}})$ ,  $\forall m_{\mathcal{K}}$  by (4)
- 2:  $\sigma_{m_{\mathcal{K}}}^2$ ,  $\forall m_{\mathcal{K}}$  by (6)
- 3:  $f(z|\mathcal{H}_{m_{\mathcal{K}}})$ ,  $\forall m_{\mathcal{K}}$  by (7)
- 4:  $P(x_{m'_k}|x_{m_{\mathcal{K}}})$ ,  $\forall m_{\mathcal{K}}, m'_k$  by (9)
- 5: Initialize  $r \leftarrow 0$
- 6:  $\mathbf{p}_k^{(0)} > \mathbf{0}$ ,  $\forall k$
- 7: Get  $P_{\mathcal{K}}^{(r)}(x_{m_{\mathcal{K}}})$ ,  $\forall m_{\mathcal{K}}$  by (10)
- 8:  $I_{\mathcal{K}}^{(r)}(x_{m_{\mathcal{K}}})$ ,  $\forall m_{\mathcal{K}}$  by (11), (14), (17)
- 9:  $I_k^{(r)}(x_{m_k})$ ,  $\forall k, m_k$  by (12), (15), (18)
- 10:  $I^{(r)}(x_{\mathcal{K}})$  by (13), (16), (19)
- 11: **Repeat**
- 12: Update  $r \leftarrow r+1$
- 13:  $\mathbf{p}_k^{(r)}$ ,  $\forall k$  by (23)
- 14: Redo step 7–10
- 15: **Until**  $I^{(r)}(x_{\mathcal{K}}) - I^{(r-1)}(x_{\mathcal{K}}) \leq \epsilon$

*Proof.* Please refer to Appendix A.  $\square$

For each RIScatter node, (22a) suggests each probable state should produce the same marginal information (averaged over all states of other nodes) while (22b) suggests any state with potentially less marginal information should not be used.

**Proposition 2.** For any strictly positive initializer  $\{\mathbf{p}_k^{(0)}\}_{k \in \mathcal{K}}$ , the KKT input probability of node  $k$  at state  $m_k$  is given by the converging point of the sequence

$$P_k^{(r+1)}(x_{m_k}) = \frac{P_k^{(r)}(x_{m_k}) \exp\left(\frac{\rho}{1-\rho} I_k^{(r)}(x_{m_k})\right)}{\sum_{m'_k} P_k^{(r)}(x_{m'_k}) \exp\left(\frac{\rho}{1-\rho} I_k^{(r)}(x_{m'_k})\right)}, \quad (23)$$

where  $r$  is the iteration index.

*Proof.* Please refer to Appendix B.  $\square$

For (23) at iteration  $r+1$ , the input distribution of node  $k$  is updated over  $\{\{\mathbf{p}_q^{(r+1)}\}_{q=1}^{k-1}, \{\mathbf{p}_q^{(r)}\}_{q=k}^K\}$ . The KKT input distribution design is summarized in Algorithm 1.

#### B. Active Beamforming

For any given  $\{\mathbf{p}_k\}_{k \in \mathcal{K}}$  and  $\mathbf{t}$ , problem (20) reduces to

$$\max_{\mathbf{w}} I(x_{\mathcal{K}}) \quad (24a)$$

$$\text{s.t.} \quad (20d), \quad (24b)$$

which is still non-convex due to the integration and entropy terms. To tackle this, we rewrite the DMMAC transition probability (9) as a regularized incomplete Gamma function in the series representation [59, Theorem 3]

$$\begin{aligned} Q\left(N, \frac{t_{l-1}}{\sigma_{m_{\mathcal{K}}}^2}, \frac{t_l}{\sigma_{m_{\mathcal{K}}}^2}\right) &= \frac{\int_{t_{l-1}/\sigma_{m_{\mathcal{K}}}^2}^{t_l/\sigma_{m_{\mathcal{K}}}^2} z^{N-1} \exp(-z) dz}{(N-1)!} \\ &= \exp\left(-\frac{t_{l-1}}{\sigma_{m_{\mathcal{K}}}^2}\right) \sum_{n=0}^{N-1} \frac{\left(\frac{t_{l-1}}{\sigma_{m_{\mathcal{K}}}^2}\right)^n}{n!} - \exp\left(-\frac{t_l}{\sigma_{m_{\mathcal{K}}}^2}\right) \sum_{n=0}^{N-1} \frac{\left(\frac{t_l}{\sigma_{m_{\mathcal{K}}}^2}\right)^n}{n!}. \end{aligned} \quad (25)$$



Its gradient with respect to  $\mathbf{w}^*$  can be derived as

$$\nabla_{\mathbf{w}^*} Q\left(N, \frac{t_{l-1}}{\sigma_{m_K}^2}, \frac{t_l}{\sigma_{m_K}^2}\right) = \frac{\mathbf{h}(x_{m_K}) \mathbf{h}^H(x_{m_K}) \mathbf{w}}{(\sigma_{m_K}^2)^2} g_{m_K}(t_{l-1}, t_l), \quad (26)$$

where  $g_{m_K}(t_{l-1}, t_l) \triangleq g_{m_K}(t_l) - g_{m_K}(t_{l-1})$  and

$$g_{m_K}(t_l) = t_l \exp\left(-\frac{t_l}{\sigma_{m_K}^2}\right) \left(-1 + \sum_{n=1}^{N-1} \frac{\left(n - \frac{t_l}{\sigma_{m_K}^2}\right) \left(\frac{t_l}{\sigma_{m_K}^2}\right)^{n-1}}{n!}\right). \quad (27)$$

On top of (25) and (26), we explicitly express the objective function (24a) and its gradient as (28) and (29) at the end of page 7, respectively. They allows problem (24) to be solved by the PGD method, where any unregulated beamformer  $\bar{\mathbf{w}}$  can be projected onto the feasible domain of average transmit power constraint (20d) by

$$\mathbf{w} = \sqrt{P} \frac{\bar{\mathbf{w}}}{\max(\sqrt{P}, \|\bar{\mathbf{w}}\|)}. \quad (30)$$

The PGD active beamforming optimization with step size  $\gamma$  refined by Backtracking Line Search (BLS) [60, Section 9.2] is summarized in Algorithm 2.

### C. Decision Threshold

For any given  $\{\mathbf{p}_k\}_{k \in \mathcal{K}}$  and  $\mathbf{w}$ , problem (20) reduces to

$$\max_{\mathbf{t}} I(x_{\mathcal{K}}) \quad (31a)$$

$$\text{s.t.} \quad (20e), (20f), \quad (31b)$$

which is still non-convex because variable  $\mathbf{t}$  appears on the limits of integration (9). Fortunately, we can further simplify problem (31) as a point-to-point rate-optimal quantizer design for a Discrete-input Continuous-output Memoryless Channel (DCMC), thanks to Remark 4 and 5.

**Remark 4.** Energy detector design has no impact on the primary achievable rate since the composite channel (4) can always be reconstructed after backscatter decoding and re-encoding. It suggests any thresholding scheme maximizing the total backscatter rate (13) is also optimal for problem (31).

**Remark 5.** In terms of total backscatter rate, the potentially dispersed nodes with known input distribution can be viewed as an equivalent source with tuple codewords. As such, the

### Algorithm 2: Iterative Active Beamforming Optimization by PGD with BLS

**Input:**  $Q, N, \mathbf{h}_D^H, \mathbf{H}_C, \alpha, \mathcal{X}, P, \sigma_v^2, \rho, \{\mathbf{p}_k\}_{k \in \mathcal{K}}, \mathbf{t}, \alpha, \beta, \gamma, \epsilon$   
**Output:**  $\mathbf{w}^*$

- 1: Set  $\mathbf{h}^H(x_{m_K}), \forall m_K$  by (4)
- 2:  $P_K(x_{m_K}), \forall m_K$  by (10)
- 3: Initialize  $r \leftarrow 0$
- 4:  $\mathbf{w}^{(0)}, \|\mathbf{w}^{(0)}\|^2 \leq P$
- 5: Get  $(\sigma_{m_K}^{(r)})^2, \forall m_K$  by (6)
- 6:  $Q^{(r)}(N, \frac{t_{l-1}}{\sigma_{m_K}^2}, \frac{t_l}{\sigma_{m_K}^2}), \forall m_K, l$  by (25)
- 7:  $I^{(r)}(x_{\mathcal{K}})$  by (28)
- 8:  $\nabla_{\mathbf{w}^*} Q^{(r)}(N, \frac{t_{l-1}}{\sigma_{m_K}^2}, \frac{t_l}{\sigma_{m_K}^2}), \forall m_K, l$  by (26)
- 9:  $\nabla_{\mathbf{w}^*} I^{(r)}(x_{\mathcal{K}})$  by (29)
- 10: **Repeat**
- 11:   Update  $r \leftarrow r + 1$
- 12:    $\gamma^{(r)} \leftarrow \gamma$
- 13:    $\bar{\mathbf{w}}^{(r)} \leftarrow \mathbf{w}^{(r-1)} + \gamma \nabla_{\mathbf{w}^*} I^{(r-1)}(x_{\mathcal{K}})$
- 14:    $\mathbf{w}^{(r)}$  by (30)
- 15:   Redo step 5–7
- 16:   **While**  $I^{(r)}(x_{\mathcal{K}}) < I^{(r-1)}(x_{\mathcal{K}}) + \alpha \gamma \|\nabla_{\mathbf{w}^*} I^{(r-1)}(x_{\mathcal{K}})\|^2$
- 17:     Set  $\gamma^{(r)} \leftarrow \beta \gamma^{(r)}$
- 18:     Redo step 13–15
- 19:   **End While**
- 20:   Redo step 8, 9
- 21: **Until**  $\|\mathbf{w}^{(r)} - \mathbf{w}^{(r-1)}\| \leq \epsilon$

DMMAC (9) becomes a DMTC and problem (31) reduces to the rate-optimal quantization design for a DCMC.

Next, we constrain the feasible domain of problem (31) from continuous space  $\mathbb{R}_+^{L+1}$  to finite candidate set (i.e., fine-grained discrete energy levels)  $\mathcal{T}^{L+1}$ . As shown in Fig. 6, by introducing this extra analog-to-digital conversion, we can group adjacent high-resolution energy bins to construct backscatter decision regions. Thus, problem (31) can be recast as

$$\max_{\mathbf{t} \in \mathcal{T}^{L+1}} I_B(x_{\mathcal{K}}; \hat{x}_{\mathcal{K}}) \quad (32a)$$

$$\text{s.t.} \quad (20e), \quad (32b)$$

which can be solved by existing rate-optimal sequential

$$I(x_{\mathcal{K}}) = \sum_{m_K} P_K(x_{m_K}) \left( \rho \log \left( 1 + \frac{|\mathbf{h}^H(x_{m_K}) \mathbf{w}|^2}{\sigma_v^2} \right) + (1 - \rho) \sum_l Q\left(N, \frac{t_{l-1}}{\sigma_{m_K}^2}, \frac{t_l}{\sigma_{m_K}^2}\right) \log \frac{Q\left(N, \frac{t_{l-1}}{\sigma_{m_K}^2}, \frac{t_l}{\sigma_{m_K}^2}\right)}{\sum_{m'_K} P_K(x_{m'_K}) Q\left(N, \frac{t_{l-1}}{\sigma_{m'_K}^2}, \frac{t_l}{\sigma_{m'_K}^2}\right)} \right) \quad (28)$$

$$\begin{aligned} \nabla_{\mathbf{w}^*} I(x_{\mathcal{K}}) = & \sum_{m_K} P_K(x_{m_K}) \left( \rho \frac{\mathbf{h}(x_{m_K}) \mathbf{h}^H(x_{m_K}) \mathbf{w}}{\sigma_{m_K}^2} + (1 - \rho) \sum_l \left( \log \frac{Q\left(N, \frac{t_{l-1}}{\sigma_{m_K}^2}, \frac{t_l}{\sigma_{m_K}^2}\right)}{\sum_{m'_K} P_K(x_{m'_K}) Q\left(N, \frac{t_{l-1}}{\sigma_{m'_K}^2}, \frac{t_l}{\sigma_{m'_K}^2}\right)} + 1 \right) \right. \\ & \times \nabla_{\mathbf{w}^*} Q\left(N, \frac{t_{l-1}}{\sigma_{m_K}^2}, \frac{t_l}{\sigma_{m_K}^2}\right) - \frac{Q\left(N, \frac{t_{l-1}}{\sigma_{m_K}^2}, \frac{t_l}{\sigma_{m_K}^2}\right) \sum_{m'_K} P_K(x_{m'_K}) \nabla_{\mathbf{w}^*} Q\left(N, \frac{t_{l-1}}{\sigma_{m'_K}^2}, \frac{t_l}{\sigma_{m'_K}^2}\right)}{\sum_{m'_K} P_K(x_{m'_K}) Q\left(N, \frac{t_{l-1}}{\sigma_{m'_K}^2}, \frac{t_l}{\sigma_{m'_K}^2}\right)} \Bigg) \quad (29) \end{aligned}$$

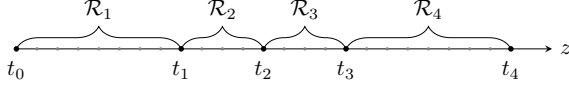


Fig. 6. The decision thresholds are selected from fine-grained discrete energy levels instead of continuous space. Each decision region consists of at least one neighbor energy bins.

quantizer designs for DMTC. To obtain global optimal solution, [61] started from the quadrangle inequality and proposed a Dynamic Programming (DP) method accelerated by the Shor-Moran-Aggarwal-Wilber-Klawe (SMAWK) algorithm with computational complexity  $\mathcal{O}(L^2(\text{card}(\mathcal{T}) - L))$ , while [62] started from the optimality condition for three neighbor thresholds and presented a traverse-then-bisect algorithm with complexity  $\mathcal{O}(\text{card}(\mathcal{T})L\log(\text{card}(\mathcal{T})L))$ . In Section IV, both schemes will be compared with the ML scheme [63]

$$t_l^{\text{ML}} = N \frac{\sigma_{l-1}^2 \sigma_l^2}{\sigma_{l-1}^2 - \sigma_l^2} \log \frac{\sigma_{l-1}^2}{\sigma_l^2}, \quad l \in \mathcal{L} \setminus \{L\}, \quad (33)$$

which is generally suboptimal for problem (31) unless all RISscatter nodes are with equiprobable inputs.

#### IV. SIMULATION RESULTS

In this section, we provide numerical results to evaluate the proposed input distribution, active beamforming, and backscatter decision designs for the considered RISscatter system. We assume the AP-user distance is 10 m and at least one RISscatter nodes are randomly dropped in a disk centered at the user with radius  $r$ . The AP is with an average transmit power budget  $P = 36$  dBm and all nodes employs  $M$ -QAM with  $\alpha = 0.5$ . For all channels involved, we consider a distance-dependent path loss model

$$L(d) = L_0 \left( \frac{d_0}{d} \right)^\gamma, \quad (34)$$

together with a Rician fading model

$$\mathbf{H} = \sqrt{\frac{\kappa}{1+\kappa}} \bar{\mathbf{H}} + \sqrt{\frac{1}{1+\kappa}} \tilde{\mathbf{H}}, \quad (35)$$

where  $d$  is the transmission distance,  $L_0 = -30$  dB is the reference path loss at  $d_0 = 1$  m,  $\kappa$  is the Rician K-factor,  $\bar{\mathbf{H}}$  is the deterministic line-of-sight component with unit-magnitude entries, and  $\tilde{\mathbf{H}}$  is the Rayleigh fading component with standard i.i.d. CSCG entries. We choose  $\gamma_D = 2.6$ ,  $\gamma_F = 2.4$ ,  $\gamma_B = 2$ , and  $\kappa_D = \kappa_F = \kappa_B = 5$  for direct, forward and backward links. The finite decision threshold domain  $\mathcal{T}$  is obtained by  $b$ -bit uniform discretization over the critical interval defined by the confidence bounds of edge hypotheses (i.e., lower bound of  $\mathcal{H}_1$  and upper bound of  $\mathcal{H}_L$ ) with confidence  $1 - \varepsilon$ . We set  $b = 9$  and  $\varepsilon = 10^{-3}$ . All achievable rate points/regions are averaged over  $10^3$  channel realizations.

##### A. Evaluation of Proposed Algorithms

1) *Initialization*: To characterize each achievable rate region, we progressively obtain all boundary points by successively increasing the primary QoS  $\rho$  and solving problem (20). For

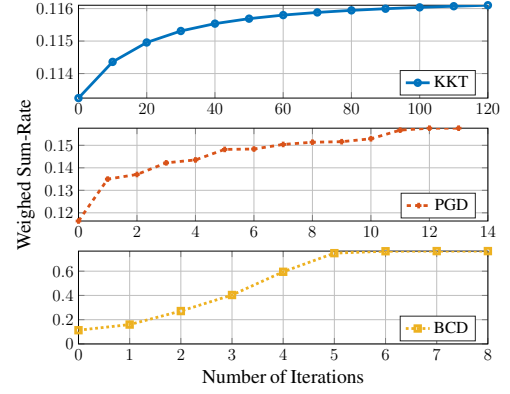


Fig. 7. Typical convergence curves at  $\rho = 0$  for  $Q = 4$ ,  $K = 8$ ,  $M = 2$ ,  $N = 20$ ,  $\sigma_v^2 = -40$  dBm and  $r = 2$  m.

$\rho = 0$  where the backscatter link is prioritized, we initialize Algorithm 1 and 2 by uniform input distribution and Maximum Ratio Transmission (MRT) towards the sum cascaded channel  $\sum_k \mathbf{h}_{C,k}^H$ , respectively. At the following points, both algorithms are initialized by the final solutions at the previous point.

2) *Convergence*: In Fig. 7, we plot the weighted sum of primary and total backscatter rates at  $\rho = 0$  for KKT, PGD and BCD algorithms on the first call. For  $K = 8$  and  $M = 2$ , Algorithm 1 typically takes around 100 fast iterations to converge to the KKT input distribution. For  $Q = 4$ , around 10 iterations are required for Algorithm 2 to converge. Overall, the initial BCD algorithm requires at most 5 iterations to converge. At the following points (not presented here), the convergence of all three algorithms are much faster thanks to the progressive initialization. We conclude the proposed algorithms have good convergence performances.

##### B. Comparison of Scattering Applications

On top of the setup in Fig. 4, we consider RISscatter and the following benchmark applications:

- *Legacy*: Active transmission without scatterers.
- *BBC*: The primary symbol becomes deterministic  $s[n] = 1$  and the receive signal becomes

$$y^{\text{BBC}}[n] = \left( \mathbf{h}_D^H + \sum_k \alpha_k \mathbf{h}_{C,k}^H \right) \mathbf{w} + v[n]. \quad (36)$$

The total backscatter rate of coherent decoding approaches  $K \log M$  when  $N$  is sufficiently large.

- *AmBC*: The user decodes both links independently and semi-coherently by treating the other as interference. The primary achievable rate is approximately<sup>10</sup>

$$I_p^{\text{AmBC}}(s; y) \approx \log \left( 1 + \frac{|\mathbf{h}_D^H \mathbf{w}|^2}{\sum_k |\alpha_k \mathbf{h}_{C,k}^H \mathbf{w}|^2 + \sigma_v^2} \right), \quad (37)$$

while the total backscatter rate follows (13) with uniform input distribution.

- *SR*: For a sufficiently large  $N$ , the average primary rate under semi-coherent detection asymptotically approaches

<sup>10</sup>To provide a preliminary benchmark, we regard the scattered component  $\sum_k \alpha_k \mathbf{h}_{C,k}^H \mathbf{w} s[n]$  as AWGN during primary decoding [13].



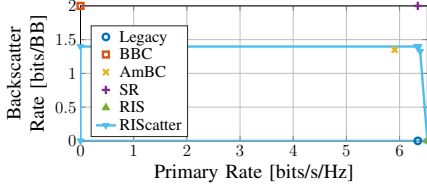


Fig. 8. Typical achievable rate region/points of scattering applications for  $Q=1$ ,  $K=1$ ,  $M=4$ ,  $N=10^3$ ,  $\sigma_v^2=-40\text{dBm}$  and  $r=2\text{m}$ .

(16) with uniform input distribution [13]. When  $s[n]$  is successfully decoded and the direct interference  $\mathbf{h}_D^H \mathbf{w} s[n]$  is perfectly cancelled, the intermediate signal is

$$\hat{y}^{\text{SR}}[n] = \sum_k \alpha_k \mathbf{h}_{C,k}^H x_k \mathbf{w} s[n] + v[n]. \quad (38)$$

The total backscatter rate of coherent decoding approaches  $K \log M$  when  $N$  is sufficiently large.

- *RIS*: The reflection pattern is deterministic and the total backscatter rate is zero. The primary achievable rate is a special case of (16)

$$I_P^{\text{RIS}}(s; y | x_K) = I_P(s; y | x_{m_K^*}) = \log \left( 1 + \frac{|\mathbf{h}^H(x_{m_K^*}) \mathbf{w}|^2}{\sigma_v^2} \right), \quad (39)$$

where  $m_K^* = \arg \max_{m_K} I_P^{\text{RIS}}(s; y | x_{m_K})$ .

Fig. 8 compares the typical achievable rate region/points of RIScatter and the strategies above. *First*, we observe BBC and SR achieve the best backscatter performance thanks to coherent decoding. For SR, this comes with the cost of  $N$  re-encoding, precoding, subtraction together with a time-domain MRC per backscatter symbol. *Second*, the average primary rate slightly decreases/increases in the presence of a AmBC/RIS node and the benefit of SR is not obvious. This is because the cascaded channel is usually orders of magnitude weaker than the direct channel. RIS always ensures constructive superposition of direct and scattered components while SR only creates a quasi-static rich-scattering environment that marginally enhances the average primary rate. When  $N$  is moderate, the randomly scattered signals should be modelled as interference rather than multipath components and the SR point should move towards the AmBC point. *Third*, RIScatter enables a flexible primary-backscatter tradeoff with adaptive input distribution design. In terms of maximum primary achievable rate, RIScatter coincides with RIS and outperforms the others using deterministic reflection pattern. On the other hand, for a large  $N$ , the maximum backscatter achievable rate of RIScatter is lower than BBC and SR but higher than AmBC. This is because both RIScatter and AmBC employ semi-coherent energy detection, and the adaptive channel coding of RIScatter provides better performance than equiprobable inputs of AmBC especially at the low SNR of double fading. When multiple antenna is available at the AP, active beamforming can be optimized for RIScatter nodes and the backscatter rate gain over AmBC can be even larger.

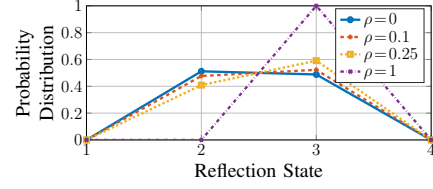


Fig. 9. Typical RIScatter reflection state distribution at different  $\rho$  for  $Q=1$ ,  $K=1$ ,  $M=4$ ,  $N=20$ ,  $\sigma_v^2=-40\text{dBm}$  and  $r=2\text{m}$ .

### C. Input Distribution under Different QoS

The objective is to demonstrate RIScatter nodes can leverage CSI- and QoS-adaptive input distribution design to balance backscatter modulation and passive beamforming. For one RIScatter node with  $M=4$ , we evaluate the KKT input distribution<sup>11</sup> at different QoS and present the result in Fig. 9. At  $\rho=0$  where the backscatter performance is prioritized, the optimal input distribution is 0 on two states and nearly uniform on the other two. This is inline with Shannon's observation that binary antipodal inputs can be good enough for channel capacity at the low SNR [64]. Due to the weak scattered signal, the conditional energy PDF under different hypotheses can be closely spaced as in Fig. 5. The extreme states producing the lowest/highest energy are always assigned with non-zero probability and the middle ones may not provide enough energy difference and thus end up unused. At  $\rho=1$  where the primary performance is prioritized, the optimal input distribution is 1 at the state that maximizes the primary SNR and 0 at the others. That is, the reflection pattern becomes deterministic and the RIScatter node boils down to a discrete RIS element. Increasing  $\rho$  from 0 to 1 provides a smooth transition from backscatter modulation to passive beamforming and proves RIScatter unifies BackCom and RIS from a probabilistic perspective.

### D. Rate Region by Different Schemes

1) *Input Distribution*: We compare these input distribution designs for problem (21):

- *Cooperation*: Joint nodes encoding using a  $K$ -dimensional probability array  $P_K(x_{m_K})$  by Algorithm 1;
- *Exhaustion*: Exhaustive search over the  $M$ -dimensional probability simplex with resolution  $\Delta p=10^{-2}$ ;
- *KKT*: Numerical KKT evaluation by Algorithm 1;
- *Equiprobable*: Uniform input distribution for all nodes.

For dispersed nodes, joint encoding is inapplicable and we consider these independent input distribution recovery methods (from the joint probability array):

- *Marginalization*: Marginal probability distributions;
- *Decomposition*: Normalized rank-1 Canonical Polyadic (CP) decomposition tensors by `Tensor Toolbox` [65];
- *Randomization*: Gaussian randomization with the guidance of correlation matrix [66].

Fig. 10(a) shows the average achievable rate regions for those designs. We observe Cooperation provides the outer bound and joint encoding can be beneficial. The average rate

<sup>11</sup>Problem (21) is convex when  $K=1$  and the KKT solution is global optimal.

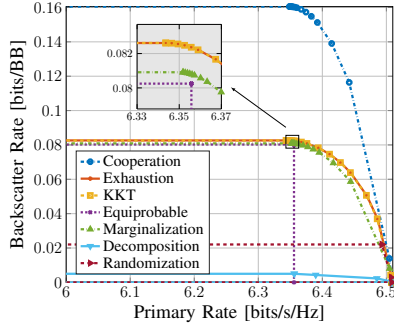
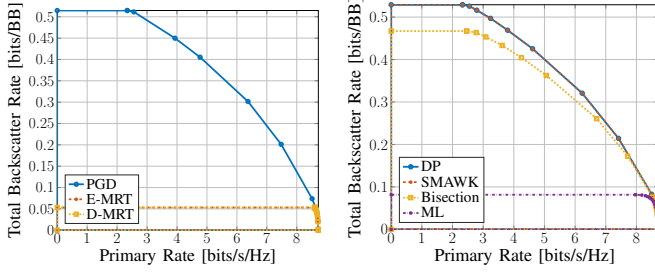
(a) Input Distribution,  $Q = 1$ (b) Active Beamforming,  $Q = 4$  (c) Decision Threshold,  $Q = 4$ 

Fig. 10. Average primary-total-backscatter rate regions by different input distribution, active beamforming, and decision threshold schemes for  $K=2$ ,  $M=4$ ,  $N=20$ ,  $\sigma_v^2 = -40\text{dBm}$  and  $r=2\text{m}$ .

performance of Exhaustion and KKT completely coincide with each other, demonstrating KKT input distribution is favorable for a moderate  $K$  as mentioned in Remark 3. Equiprobable experiences minor backscatter and major primary rate losses without exploiting CSI and QoS. Both rate gaps should be larger when  $M$  and/or  $K$  increase. For the recovery methods, the simple Marginalization provides a close performance to KKT, but Randomization and Decomposition fail our expectations for most channel realizations. Those observations emphasize the importance of (joint) adaptive RIScatter encoding and demonstrate the advantage of the proposed KKT input distribution design.

2) *Active Beamforming*: We consider three typical active beamforming schemes for problem (24):

- *PGD*: Iterative PGD optimization by Algorithm 2;
- *E-MRT*: MRT towards the ergodic composite channel  $\sum_{m_K} P_K(x_{m_K}) \mathbf{h}^H(x_{m_K})$ ;
- *D-MRT*: MRT towards the direct channel  $\mathbf{h}_D^H$ .

Fig. 10(b) presents the average achievable rate regions for those schemes. In the low- $\rho$  regime, the proposed PGD beamformer significantly outperforms both MRT schemes in terms of total backscatter rate. This is because the semi-coherent backscatter decoding relies on the *relative difference* of accumulated energy under different symbol tuples. Such an energy diversity is enhanced by PGD that effectively exploits backscatter constellation and input distribution knowledge rather than simply maximizing the direct/ergodic SNR. As  $\rho$  increases, the primary equivalent SNR outweighs the backscatter energy difference in (28) and PGD beamformer becomes closer to both MRT schemes. At  $\rho=1$ , both PGD and E-MRT boil down to MRT towards the composite channel. The difference

between E-MRT and D-MRT is insignificant when RIScatter nodes are dispersed. Those observations prove the proposed PGD active beamforming design can exploit the CSI, QoS, and backscatter constellation to balance the primary equivalent SNR and backscatter energy difference and enlarge the achievable rate region.

3) *Decision Threshold*: We evaluate the following decision threshold strategies for problem (32):

- *DP*: Benchmark DP method for sequential quantizer [61];
- *SMAWK*: DP accelerated by the SMAWK algorithm [61];
- *Bisection*: The traverse-then-bisect algorithm [62];
- *ML*: Maximum likelihood detector (33) [63].

Fig. 10(c) reveals the average achievable rate region for those strategies. The distribution-aware schemes DP, SMAWK and Bisection ensure higher total backscatter rate than ML. This is because the total backscatter rate (13) is a function of both input distribution and decision regions, and the rate-optimal threshold design heavily depends on input distribution. For example, the backscatter symbol tuples with zero input probability should be assigned with empty decision regions in order to increase the success detection rates of other hypotheses. It highlights the importance of joint input distribution and decision threshold design in rate maximization problems.

### E. Rate Region under Different Configurations

In this study, we choose  $Q = 4$ ,  $K = 8$ ,  $M = 2$ ,  $N = 20$ ,  $\sigma_v^2 = -40\text{dBm}$  and  $r = 2\text{m}$  as a reference.

1) *Number of Nodes*: Fig. 11(a) reveals how the number RIScatter nodes  $K$  influence the primary-backscatter tradeoff. Interestingly, we observe that increasing  $K$  has a larger benefit on the total backscatter rate than primary. This is because each RIScatter node not only affects the primary equivalent SNR but also influences the relative energy difference that other nodes can create. To maximize the total backscatter rate, some nodes closer to the user may need to sacrifice their own rate and use the state that *minimizes* the composite channel strength, in order to increase the backscatter rate of other nodes. This accounts for the significant primary rate decrease in the low- $\rho$  regime. On the other hand, when the primary link is prioritized, the RIScatter nodes boil down to RIS elements and enjoy a conventional passive array gain  $N^2$ .

2) *Number of States*: Fig. 11(b) shows the relationship between available reflection states (i.e., QAM order)  $M$  and achievable rate regions. We notice increasing the reflection states has a marginal effect on both primary and total backscatter rates. This is because once the scope of reflection coefficient is determined, using denser constellation points only creates marginal phase resolution and energy diversity for primary and backscatter links. Due to the maximum amplitude normalization in (2), the average rate region of 8-QAM (points on rectangle border) is smaller than that of 4-QAM (points on square vertices), and the 4 points on the rectangle edges are less frequently used. On the other hand, 16-QAM provides significant higher backscatter rate benefit than primary. It motivates one to use high-resolution metamaterial units as RIScatter nodes.

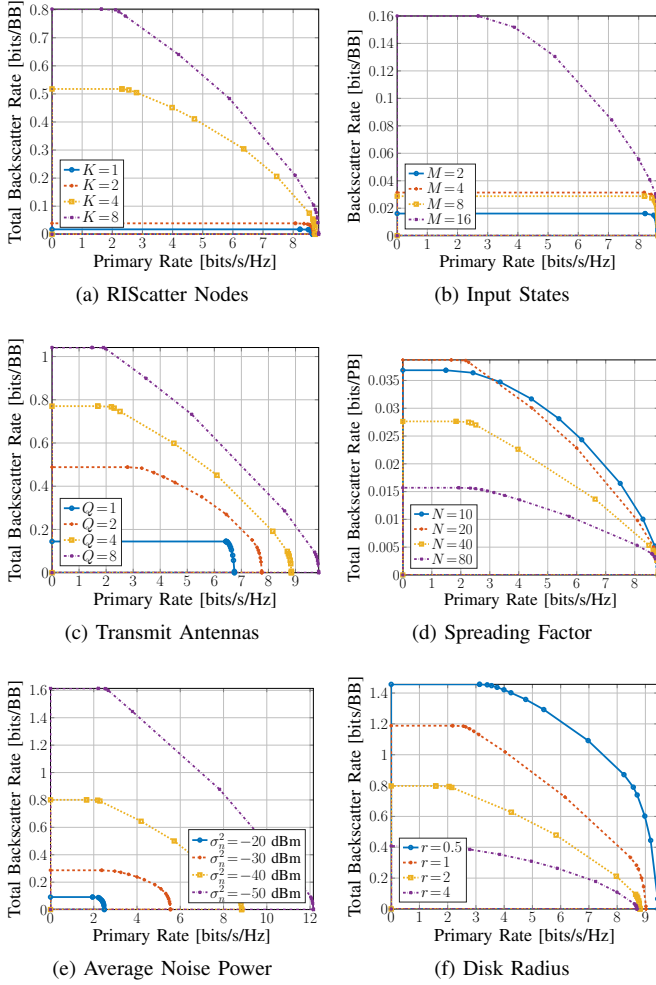


Fig. 11. Average primary-total-backscatter rate regions for different system configurations.

3) *Number of Transmit Antennas*: Fig. 11(c) illustrates the impact of transmit antennas  $Q$  on the average performance. As  $Q$  increases, more scattered paths are available to PGD and the channel diversity can be further exploited to enhance the primary equivalent SNR and backscatter energy difference, which enlarges the achievable rate region. It emphasizes the importance of multi-antenna RIScatter systems and demonstrate the effectiveness of the proposed PGD design.

4) *Spreading factor*: Fig. 11(d) presents how the spreading factor  $N$  affects the achievable rate region. Please notice here the unit of total backscatter rate is bits per primary block to indicate throughput. Apparently, using a very large  $N$  can severely constrain the backscatter throughput, since the gain in energy certainty (by law of large numbers) cannot withstand the loss in gross rate. As  $N \rightarrow \infty$ , RIScatter nodes boil down to RIS elements with fixed reflection pattern during whole channel block and the total backscatter rate approaches 0. On the other hand, when  $N$  is too small, the equivalent DMMAC (9) has very high error probabilities and the energy detection is thus unreliable. It explains the observation that  $N = 10$  provides lower backscatter throughput than  $N = 20$ . Therefore, we conclude the design of spreading factor  $N$  in RIScatter

systems should accommodate multiple factors (e.g., data rate requirements, load switching constraints at the nodes, and signal processing capability at the user).

5) *Average Noise Power*: Fig. 11(e) depicts the impact of average noise power  $\sigma_v^2$  on average rate regions. It shows the proposed practical semi-coherent backscatter energy detection is suitable for a wide range of noise levels. When  $\sigma_v^2$  relatively high, one can choose a larger  $N$  to maintain the backscatter SNR for better energy detection performance.

6) *Coverage Disk Radius*: Fig. 11(f) shows the relationship between disk radius  $r$  and achievable rate region. We observe both primary and backscatter performance are enhanced when nodes are located closer to the user. This is because the double fading effect is less severe for near-far setups. In a multi-user RIScatter system with dispersed nodes, each node may be assigned to the nearest user to guarantee uniformly good performance for both links.

## V. CONCLUSION

This paper introduced RIScatter as a low-power scatter protocol that simultaneously provides backscatter modulation and passive beamforming by smart input distribution design. Starting from scattering principles, we showed how RIScatter nodes generalize information nodes of BackCom and reflect elements of RIS as special cases, how they can be built over existing passive scatter devices, and how they simultaneously encode self information and assist legacy transmission. We also propose a practical SIC-free receiver that exploits the properties of active-passive coexisting networks to maintain primary benefit and improve backscatter throughput. The achievable primary-total-backscatter rate region is then studied for a single-user multi-node RIScatter system, where the input distribution, active beamforming, and decision thresholds are iteratively updated. Numerical results not only validated the proposed algorithms but also emphasized the importance of adaptive input distribution and cooperative decoding for both primary and backscatter links.

One possible future direction is to consider backscatter detection over the received signal domain rather than energy domain, where multi-antenna [67] and learning-based approaches can be promising. Another interesting question is how to design RIScatter node and receiver in a multi-user system to fully exploit the dynamic passive beamforming that naturally origins from backscatter modulation.

## APPENDIX

### A. Proof of Proposition 1

Denote the Lagrange multipliers associated with (20b) and (20c) as  $\{\nu_k\}_{k \in \mathcal{K}}$  and  $\{\lambda_{k,m_k}\}_{k \in \mathcal{K}, m_k \in \mathcal{M}}$ , respectively. The Lagrangian function of problem (21) is

$$-I(x_{\mathcal{K}}) + \sum_k \nu_k \left( \sum_{m_k} P_k(x_{m_k}) - 1 \right) - \sum_k \sum_{m_k} \lambda_{k,m_k} P_k(x_{m_k}) \quad (40)$$

and the KKT conditions are,  $\forall k, m_k$ ,

$$-\nabla_{P_k^*(x_{m_k})} I^*(x_{\mathcal{K}}) + \nu_k^* - \lambda_{k,m_k}^* = 0, \quad (41a)$$

$$\lambda_{k,m_k}^* = 0, \quad P_k^*(x_{m_k}) > 0, \quad (41b)$$

$$\lambda_{k,m_k}^* \geq 0, \quad P_k^*(x_{m_k}) = 0, \quad (41c)$$

where directional derivative is explicitly written as

$$\nabla_{P_k^*(x_{m_k})} I^*(x_{\mathcal{K}}) = I_k^*(x_{m_k}) - (1-\rho). \quad (42)$$

Combining (41) and (42), we have

$$I_k^*(x_{m_k}) = \nu_k^* + (1-\rho), \quad P_k^*(x_{m_k}) > 0, \quad (43a)$$

$$I_k^*(x_{m_k}) \leq \nu_k^* + (1-\rho), \quad P_k^*(x_{m_k}) = 0, \quad (43b)$$

such that

$$\sum_{m_k} P_k^*(x_{m_k}) I_k^*(x_{m_k}) = \nu_k^* + (1-\rho). \quad (44)$$

On the other hand, by definition (18) we have

$$\sum_{m_k} P_k^*(x_{m_k}) I_k^*(x_{m_k}) = I^*(x_{\mathcal{K}}), \quad (45)$$

where the right-hand side is irrelevant to  $k$ . (43), (44), and (45) together complete the proof.

### B. Proof of Proposition 2

We first prove sequence (23) is non-decreasing in weighted sum mutual information. Let  $P_{\mathcal{K}}(x_{m_{\mathcal{K}}}) = \prod_{q \in \mathcal{K}} P_q(x_{m_q})$  and  $P'_{\mathcal{K}}(x_{m_{\mathcal{K}}}) = P'_k(x_{m_k}) \prod_{q \in \mathcal{K} \setminus \{k\}} P_q(x_{m_q})$  be two probability distributions with potentially different marginal for tag  $k$  at state  $m_k$ , and define an intermediate function  $J(P_{\mathcal{K}}(x_{m_{\mathcal{K}}}), P'_{\mathcal{K}}(x_{m_{\mathcal{K}}}))$  as (46) at the end of page 12. It is straightforward to verify  $J(P_{\mathcal{K}}(x_{m_{\mathcal{K}}}), P_{\mathcal{K}}(x_{m_{\mathcal{K}}})) = I(x_{\mathcal{K}})$  and  $J(P_{\mathcal{K}}(x_{m_{\mathcal{K}}}), P'_{\mathcal{K}}(x_{m_{\mathcal{K}}}))$  is a concave function for a fixed  $P'_{\mathcal{K}}(x_{m_{\mathcal{K}}})$ . Setting  $\nabla_{P_k^*(x_{m_k})} J(P_{\mathcal{K}}(x_{m_{\mathcal{K}}}), P'_{\mathcal{K}}(x_{m_{\mathcal{K}}})) = 0$ , we have

$$S'_k(x_{m_k}) - S'_k(x_{i_k}) + (1-\rho) \log \frac{P_k(x_{i_k})}{P_k^*(x_{m_k})} = 0, \quad (47)$$

where  $i_k \neq m_k$  is the reference state and

$$\begin{aligned} S'_k(x_{m_k}) &\triangleq I'_k(x_{m_k}) + (1-\rho) \sum_{m_{\mathcal{K}} \setminus \{k\}} P_{\mathcal{K} \setminus \{k\}}(x_{m_{\mathcal{K}} \setminus \{k\}}) \\ &\quad \times \sum_{m'_k} P(\hat{x}_{m'_k} | x_{m_{\mathcal{K}}}) \log P'_{\mathcal{K}}(x_{m_{\mathcal{K}}}). \end{aligned} \quad (48)$$

Evidently,  $\forall m_k \neq i_k$ , (47) boils down to

$$P_k^*(x_{m_k}) = \frac{P'_k(x_{m_k}) \exp\left(\frac{\rho}{1-\rho} I'_k(x_{m_k})\right)}{\sum_{m'_k} P'_k(x_{m'_k}) \exp\left(\frac{\rho}{1-\rho} I'_k(x_{m'_k})\right)}. \quad (49)$$

Since  $P_k(x_{i_k}) = 1 - \sum_{m_k \neq i_k} P_k^*(x_{m_k})$  has exactly the same form as (49), the choice of reference state  $i_k$  does not matter and (49) is indeed optimal  $\forall m_k \in \mathcal{M}$ . That is, for a fixed  $P'_{\mathcal{K}}(x_{m_{\mathcal{K}}})$ , choosing  $P_k(x_{m_k})$  by (49) ensures

$$J(P_{\mathcal{K}}(x_{m_{\mathcal{K}}}), P'_{\mathcal{K}}(x_{m_{\mathcal{K}}})) \geq I'(x_{\mathcal{K}}). \quad (50)$$

On the other hand, we also have

$$\Delta \triangleq I(x_{\mathcal{K}}) - J(P_{\mathcal{K}}(x_{m_{\mathcal{K}}}), P'_{\mathcal{K}}(x_{m_{\mathcal{K}}})) \quad (51a)$$

$$\begin{aligned} &= (1-\rho) \sum_{m_k} \frac{P'_k(x_{m_k}) f'_k(x_{m_k})}{\sum_{m'_k} P'_k(x_{m'_k}) f'_k(x_{m'_k})} \sum_{m''_k} P(\hat{x}_{m''_k} | x_{m_k}) \\ &\quad \times \log \frac{\sum_{m'_k} P'_k(x_{m'_k}) P(\hat{x}_{m''_k} | x_{m'_k}) f'_k(x_{m'_k})}{\sum_{m'_k} P'_k(x_{m'_k}) P(\hat{x}_{m''_k} | x_{m'_k}) f'_k(x_{m'_k})} \end{aligned} \quad (51b)$$

$$\begin{aligned} &\geq (1-\rho) \sum_{m_k} \frac{P'_k(x_{m_k}) f'_k(x_{m_k})}{\sum_{m'_k} P'_k(x_{m'_k}) f'_k(x_{m'_k})} \sum_{m''_k} P(\hat{x}_{m''_k} | x_{m_k}) \\ &\quad \times \left(1 - \frac{\sum_{m'_k} P'_k(x_{m'_k}) P(\hat{x}_{m''_k} | x_{m'_k}) f'_k(x_{m'_k})}{\sum_{m'_k} P'_k(x_{m'_k}) P(\hat{x}_{m''_k} | x_{m'_k}) f'_k(x_{m'_k})}\right) \end{aligned} \quad (51c)$$

$$= 0, \quad (51d)$$

where  $f'_k(x_{m_k}) \triangleq \exp\left(\frac{\rho}{1-\rho} I'_k(x_{m_k})\right)$  and the equality holds if and only if (49) converges. (50) and (51) together imply  $I(x_{\mathcal{K}}) \geq I'(x_{\mathcal{K}})$ . Since mutual information is bounded above, we conclude the sequence (23) is non-decreasing and convergent in mutual information.

Next, we prove any converging point of sequence (23), denoted as  $P_k^*(x_{m_k})$ , fulfills KKT conditions (22). To see this, let

$$D_k^{(r)}(x_{m_k}) \triangleq \frac{P_k^{(r+1)}(x_{m_k})}{P_k^{(r)}(x_{m_k})} = \frac{f_k^{(r)}(x_{m_k})}{\sum_{m'_k} P_k^{(r)}(x_{m'_k}) f_k^{(r)}(x_{m'_k})}. \quad (52)$$

As sequence (23) is convergent, any state with  $P_k^*(x_{m_k}) > 0$  need to satisfy  $D_k^*(x_{m_k}) \triangleq \lim_{r \rightarrow \infty} D_k^{(r)}(x_{m_k}) = 1$ , namely

$$I_k^*(x_{m_k}) = \frac{1-\rho}{\rho} \log \sum_{m'_k} P_k^*(x_{m'_k}) f_k^*(x_{m'_k}), \quad (53)$$

which is reminiscent of (43a) and (22a). That is, given  $P_k^{(0)}(x_{m_k}) > 0$ , any converging point with  $P_k^*(x_{m_k}) > 0$  must satisfy (22a). On the other hand, we assume  $P_k^*(x_{m_k})$  does not satisfy (22b), such that for any state with  $P_k^*(x_{m_k}) = 0$ ,

$$I_k^*(x_{m_k}) > I^*(x_{\mathcal{K}}) = \sum_{m'_k} P_k^*(x_{m'_k}) I_k^*(x_{m'_k}), \quad (54)$$

where the equality inherits from (19). Since the exponential function is monotonically increasing, we have  $f_k^*(x_{m_k}) > \sum_{m'_k} P_k^*(x_{m'_k}) f_k^*(x_{m'_k})$  and  $D_k^*(x_{m_k}) > 1$ . Considering  $P_k^{(0)}(x_{m_k}) > 0$  and  $P_k^*(x_{m_k}) = 0$ , it contradicts with

$$P_k^{(r)}(x_{m_k}) = P_k^{(0)}(x_{m_k}) \prod_{n=1}^r D_k^{(n)}(x_{m_k}). \quad (55)$$

That is, given  $P_k^{(0)}(x_{m_k}) > 0$ , any converging point with  $P_k^*(x_{m_k}) = 0$  must satisfy (22b). The proof is thus completed.

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$$J(P_{\mathcal{K}}(x_{m_{\mathcal{K}}}), P'_{\mathcal{K}}(x_{m_{\mathcal{K}}})) \triangleq \sum_{m_{\mathcal{K}}} P_{\mathcal{K}}(x_{m_{\mathcal{K}}}) \left( \rho \log \left( 1 + \frac{|\mathbf{h}^H(x_{m_{\mathcal{K}}}) \mathbf{w}|^2}{\sigma_v^2} \right) + (1-\rho) \sum_{m'_k} P(\hat{x}_{m'_k} | x_{m_{\mathcal{K}}}) \log \frac{P(\hat{x}_{m'_k} | x_{m_{\mathcal{K}}}) P'_{\mathcal{K}}(x_{m_{\mathcal{K}}})}{P'_{\mathcal{K}}(\hat{x}_{m'_k}) P_{\mathcal{K}}(x_{m_{\mathcal{K}}})} \right). \quad (46)$$

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