



华南理工大学  
SOUTH CHINA UNIVERSITY OF TECHNOLOGY



# 大质量转移反应中团簇发射 机制研究

汇报人：王子涵      指导老师：冯兆庆

# 目录

1

研究背景

2

模型介绍

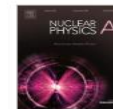
3

结果讨论

4

总结展望

# 1.研究背景——多核子转移反应



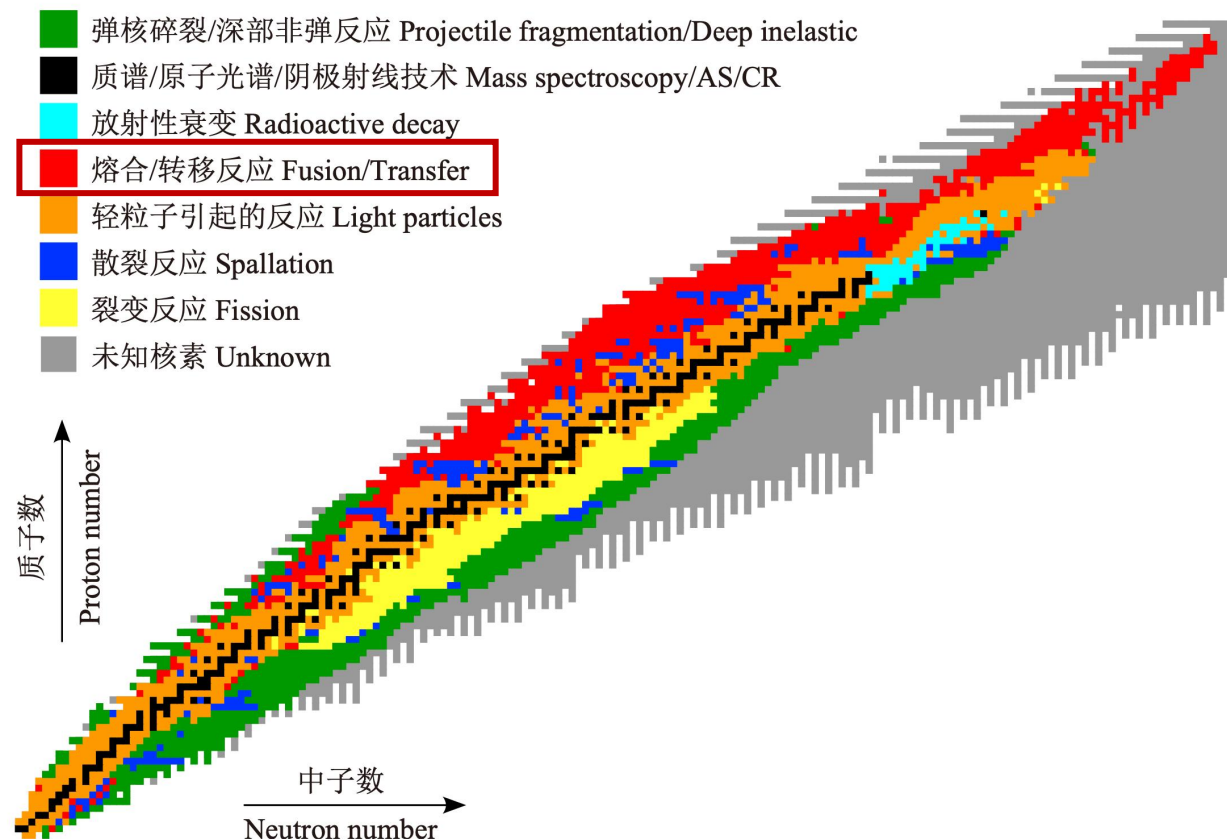
Nuclear Physics A  
Volume 176, Issue 2, 29 November 1971, Pages 284-288

In the multi-nucleon transfer (MNT) reactions:

- (1) Generate broad isotope distribution depending on transfer channels.
- (2) Angular and excitation energy of compound nucleus distribute widely.
- (3) Producing neutron-rich heavy and superheavy nuclei.

New isotopes<sup>29,30</sup>Mg, <sup>31,32,33</sup>Al, <sup>33,34,35,36</sup>Si, <sup>35,36,37,38</sup>P, <sup>39,40</sup>S and <sup>41,42</sup>Cl produced in bombardment of a <sup>232</sup>Th target with 290 MeV <sup>40</sup>Ar ions

A.G. Artukh, V.V. Avdeichikov<sup>†</sup>, G.F. Gridnev, V.L. Mikheev, V.V. Volkov, J. Wilczyński



Multi-nucleon transfer reactions (MNT) experiment progress

Lab.	Reaction system	References
Dubna	<sup>136</sup> Xe + <sup>208</sup> Pb	Phys. Rev. C 86, 044611 (2012)
	<sup>156,160</sup> Gd + <sup>186</sup> W	Phys. Rev. C 96, 064621 (2017)
GSI	<sup>238</sup> U + <sup>238</sup> U	Phys. Rev. Lett. 39, 385 (1977)
	<sup>48</sup> Ca + <sup>248</sup> Cm	Phys. Rev. Lett. 41, 469 (1978)
	<sup>48</sup> Ca + <sup>238</sup> U	Phys. Lett. B 748, 199 (2015)
		Eur. Phys. J. A 56, 224 (2020)
GANIL	<sup>238</sup> U + <sup>238</sup> U	IJMPE 17, 2235-2239 (2008)
	<sup>136</sup> Xe + <sup>198</sup> Pt	Phys. Rev. Lett. 115, 172503 (2015)
Argonne	<sup>136</sup> Xe + <sup>208</sup> Pb	Phys. Rev. C 91, 064615 (2015)
	<sup>204</sup> Hg + <sup>198</sup> Pt	Physics Letters B 771, 119-124 (2017)
RIKEN	<sup>238</sup> U + <sup>198</sup> Pt → <sup>241</sup> U	Phys. Rev. Lett. 130, 132502 (2023)



# 1. 研究背景——前平衡结团发射



## 前平衡结团发射机制的理论研究

PHYSICAL REVIEW C **107**, 054613 (2023)

Preequilibrium cluster emission in massive transfer reactions near the Coulomb barrier energy

Zhao-Qing Feng \*

School of Physics and Optoelectronics, South China University of Technology, Guangzhou 510640, China



(Received 2 January 2023; revised 21 March 2023; accepted 15 May 2023; published 22 May 2023)

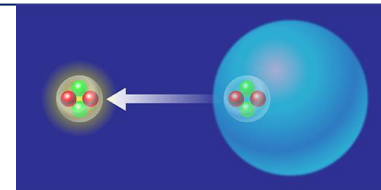
### ➤ The Dinuclear System (DNS) Model

➤ Phys. Rev. C **107**, 054613 (2023)

### ➤ The Exciton Model

- Rev. Nucl. Sci. **25**, 123 (1975)
- Phys. Rev. C **16**, 1404 (1977)
- Int. J. Mod. Phys. E **19**, 1134 (2010)

## 研究前平衡结团发射机制的重要意义



- the correlation of spatial configuration of nucleons
- the cluster structure of the stable or unstable nuclide
- the cluster formation mechanism in nuclear reactions
- the kinetic mechanism of MNT reactions
- ... ..



Physics Reports **374** (2003) 1–89

PHYSICS REPORTS

[www.elsevier.com/locate/physrep](http://www.elsevier.com/locate/physrep)

Cluster emission, transfer and capture in nuclear reactions

P.E. Hodgson<sup>a</sup>, E. Běták<sup>b,1</sup>

<sup>a</sup>The Denys Wilkinson Building, Department of Physics, University of Oxford, Oxford OX1 3RH, UK

<sup>b</sup>Institute of Physics, Slovak Academy of Sciences, 84228 Bratislava, Slovakia

Received 3 June 2002  
editor: G.E. Brown



# 1. 研究背景——前平衡结团发射



## 前平衡结团发射截面的实验测量

➤ IMP:  $^{12}\text{C} + ^{209}\text{Bi}$

2.B: 2.N

*Nuclear Physics A349* (1980) 285–300; © North-Holland Publishing Co., Amsterdam

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### PRODUCT CROSS SECTIONS FOR THE REACTION OF $^{12}\text{C}$ WITH $^{209}\text{Bi}^*$

JIN GEN-MING

*Institute of Modern Physics, Academia Sinica, Lanzhou, The People's Republic of China<sup>†</sup>*  
and

*The Niels Bohr Institute, Copenhagen Ø, Denmark*

XIE YUAN-XIANG, ZHU YONG-TAI, SHEN WEN-GING, SUN XI-JUN, GUO JUN-SHENG,  
LIU GUO-XING, YU JU-SHENG and SUN CHI-CHANG

*Institute of Modern Physics, Academia Sinica, Lanzhou, The People's Republic of China*

and

J. D. GARRETT

*The Niels Bohr Institute, Copenhagen Ø, Denmark*

Received 18 June 1980

E

NUCLEAR REACTIONS  $^{209}\text{Bi}(^{12}\text{C}, ^{12}\text{C}), (^{12}\text{C}, \text{X}), (^{12}\text{C}, \text{F}), E = 61\text{--}73\text{ MeV}$ ; measured  $\sigma(\theta, \text{elastic}), \sigma(\theta, \text{evaporation residue}), \sigma(\text{fission}), \sigma(E_x, \theta); ^{209}\text{Bi}(^{12}\text{C}, \text{Li}), (^{12}\text{C}, \text{Be}), (^{12}\text{C}, \text{B}), E = 73\text{ MeV}$ ; measured  $\sigma(E_{\text{Li}}, \theta), \sigma(\text{Be}, \theta), \sigma(\text{B}, \theta)$ .  $^{221}\text{Ac}$  deduced fission barriers.

➤ *Nucl. Phys. A349* (1980) 285-300

➤ RIKEN:  $^{14}\text{N} + ^{159}\text{Tb}, ^{169}\text{Tm}, ^{181}\text{Ta}, ^{197}\text{Au}, ^{209}\text{Bi}$

2.B: 2.N

*Nuclear Physics A334* (1980) 127–143; © North-Holland Publishing Co., Amsterdam

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### PREEQUILIBRIUM $\alpha$ -PARTICLE EMISSION IN HEAVY-ION REACTIONS

H. UTSUNOMIYA<sup>†</sup>, T. NOMURA, T. INAMURA, T. SUGITATE<sup>††</sup> and T. MOTOBAYASHI<sup>‡</sup>

*Cyclotron Laboratory, The Institute of Physical and Chemical Research, Wako-shi, Saitama, 351, Japan*

Received 19 September 1979

**Abstract:** [The  $\alpha$ -particle emission following  $^{14}\text{N}$ -induced reactions on various heavy targets at 85–115 MeV has been studied. Cross sections of heavy residual nuclei produced after  $\alpha$ -emission were measured in the case of the  $^{209}\text{Bi}$  target and were found to be close to the angle-integrated cross sections of  $\alpha$ -particles, indicating that the  $\alpha$ -emission mainly takes place in a binary process. The measured angular distributions of  $\alpha$ -particles are pronouncedly forward-peaked, while the energy spectra are always characterized by the Maxwellian distribution even at forward angles and reproduced excellently by the statistical evaporation formula when nuclear temperature is treated as a free parameter. The resultant value of the temperature is high (4–6 MeV) at forward angles and decreases monotonically with increasing emission angles.]

The energy and angular distributions of protons, deuterons and tritons were also measured in the  $^{181}\text{Ta} + ^{14}\text{N}$  reaction at 115 MeV. The results are similar to those of  $\alpha$ -particles. In particular, nuclear temperatures turned out nearly equal to each other, being consistent with the hot-spot interpretation for the relevant preequilibrium light-particle emission.

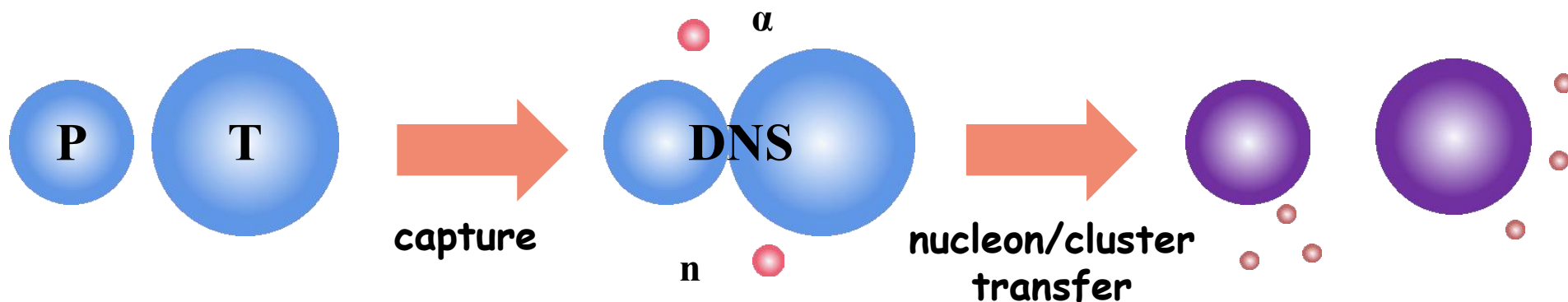
E

NUCLEAR REACTIONS  $^{159}\text{Tb}, ^{169}\text{Tm}, ^{181}\text{Ta}, ^{197}\text{Au}, ^{209}\text{Bi}(^{14}\text{N}, \text{X}), E = 85\text{--}115\text{ MeV}$ ; measured  $\sigma(E, \theta)$  for p, d, t,  $\alpha$  and  $\sigma$  for reaction residues; Si detectors.

➤ *Nucl. Phys. A334* (1980) 127-143



## 2.模型介绍——双核系统模型



➤ 冯兆庆. 近垒重离子熔合反应和超重核合成机制研究[D]. 甘肃: 中国科学院近代物理研究所, 2007

### ➤ 前平衡结团发射截面:

$$\sigma_v(E_k, \theta, t) = \sum_{J=0}^{J_{\max}} \sum_{Z_1=Z_v}^{Z_{\max}} \sum_{N_1=N_v}^{N_{\max}} \sigma_{\text{cap}}(E_{c.m.}, J) \times \int f(B) \times P(Z_1, N_1, E_1(E_{c.m.}, J), t, B) \times \boxed{P_v(Z_v, N_v, E_k)} dB$$

$$v = n, p, d, t, {}^3\text{He}, \alpha, {}^6, {}^7\text{Li}, {}^8, {}^9\text{Be}$$

结团发射概率:  $P_v(Z_v, N_v, E_k) = \Delta t \frac{\Gamma_v}{\hbar}, \quad \Delta t = 0.5 \times 10^{-22} \text{ s}$



## 2.模型介绍——双核系统模型



### ➤ capture:

➤ 俘获截面: 
$$\sigma_{cap} = \frac{\pi \hbar^2 (2J+1) T(E_{c.m.}, J)}{2 \mu E_{c.m.}} \quad \mu = m_n \frac{A_P A_T}{A_P + A_T}$$

➤ 穿透概率: 
$$T(E_{c.m.}, J) = \int f(B) T(E_{c.m.}, J, B) dB$$

1. for the light and medium systems: the Hill-Wheeler formula ➤ *Phys. Rev., 1953, 89: 1102-1145*

2. for the heavy systems: the classical trajectory approach

$$T(E_{c.m.}, J, B) = 0, \quad E_{c.m.} < B + \frac{J(J+1)\hbar^2}{2\mu R_C^2}, \quad T(E_{c.m.}, J, B) = 1, \quad E_{c.m.} > B + \frac{J(J+1)\hbar^2}{2\mu R_C^2}$$

### ➤ 位垒分布函数:

高斯型 
$$f(B) = \frac{1}{N} \exp\left(-\left(\frac{B - B_m}{\Delta}\right)^2\right)$$

$$\Delta = (B_C - B_S) / 2$$

$$B_m = (B_C + B_S) / 2$$

$$\int f(B) dB = 1$$

➤ *Phys. Rev., 2001, C64: 034606*

➤ *Phys. Rev., 2001, C65: 014607*

# 2.模型介绍——双核系统模型

➤ transfer:

➤ 主方程:

只考虑核子n, p转移:

$$\begin{aligned} \frac{dP(Z_1, N_1, E_1, t)}{dt} &= \sum_{Z'_1} W_{Z_1, N_1; Z'_1, N_1}(t) [d_{Z_1, N_1} P(Z'_1, N_1, E'_1, t) - d_{Z'_1, N_1} P(Z_1, N_1, E_1, t)] \\ &+ \sum_{N'_1} W_{Z_1, N_1; Z_1, N'_1}(t) [d_{Z_1, N_1} P(Z_1, N'_1, E'_1, t) - d_{Z_1, N'_1} P(Z_1, N_1, E_1, t)] \\ &\times [d_{Z_1, N_1} P(Z_1, N'_1, E'_1, t) - d_{Z_1, N'_1} P(Z_1, N_1, E_1, t)]. \end{aligned}$$

$$\begin{aligned} W_{Z_1, N_1; Z'_1, N_1} &= \frac{\tau_{mem}(Z_1, N_1, E_1; Z'_1, N_1, E'_1)}{d_{Z_1, N_1} d_{Z'_1, N_1} \hbar^2} \\ &\times \sum_{i, i'} |\langle Z'_1, N_1, E'_1, i' | V | Z_1, N_1, E_1, i \rangle|^2 \end{aligned}$$

核子n, p转移+结团d, t, 3He, 4He转移:

$$\begin{aligned} \frac{dP(Z_1, N_1, E_1, \beta_1, B, t)}{dt} &= \sum_{Z'_1=Z_1 \pm 1} W_{Z_1, N_1, \beta_1; Z'_1, N_1, \beta'_1}(t) [d_{Z_1, N_1} P(Z'_1, N_1, E'_1, \beta'_1, B, t) - d_{Z'_1, N_1} P(Z_1, N_1, E_1, \beta_1, B, t)] \\ &+ \sum_{N'_1=N_1 \pm 1} W_{Z_1, N_1, \beta_1; Z_1, N'_1, \beta'_1}(t) [d_{Z_1, N_1} P(Z_1, N'_1, E'_1, \beta'_1, B, t) - d_{Z_1, N'_1} P(Z_1, N_1, E_1, \beta_1, B, t)] \\ &+ \sum_{Z'_1=\pm 1, N'_1=N_1 \pm 1} W_{Z_1, N_1, \beta_1; Z'_1, N'_1, \beta'_1}^d(t) [d_{Z_1, N_1} P(Z'_1, N'_1, E'_1, \beta'_1, B, t) - d_{Z'_1, N'_1} P(Z_1, N_1, E_1, \beta_1, B, t)] \\ &+ \sum_{Z'_1=\pm 1, N'_1=N_1 \pm 2} W_{Z_1, N_1, \beta_1; Z'_1, N'_1, \beta'_1}^t(t) [d_{Z_1, N_1} P(Z'_1, N'_1, E'_1, \beta'_1, B, t) - d_{Z'_1, N'_1} P(Z_1, N_1, E_1, \beta_1, B, t)] \\ &+ \sum_{Z'_1=\pm 2, N'_1=N_1 \pm 1} W_{Z_1, N_1, \beta_1; Z'_1, N'_1, \beta'_1}^{3He}(t) [d_{Z_1, N_1} P(Z'_1, N'_1, E'_1, \beta'_1, B, t) - d_{Z'_1, N'_1} P(Z_1, N_1, E_1, \beta_1, B, t)] \\ &+ \sum_{Z'_1=\pm 2, N'_1=N_1 \pm 2} W_{Z_1, N_1, \beta_1; Z'_1, N'_1, \beta'_1}^{\alpha}(t) [d_{Z_1, N_1} P(Z'_1, N'_1, E'_1, \beta'_1, B, t) - d_{Z'_1, N'_1} P(Z_1, N_1, E_1, \beta_1, B, t)]. \end{aligned}$$

$$W_{Z_1, N_1; Z'_1, N'_1}^s = G_s \frac{\tau_{mem}(Z_1, N_1, E_1; Z'_1, N'_1, E'_1)}{d_{Z_1, N_1} d_{Z'_1, N'_1} \hbar^2} \sum_{ii'} |\langle i' | V | i \rangle|^2$$

➤ Nucl. Phys. A 771, 50 (2006)

➤ Nucl. Phys. A 816, 33 (2009)

➤ Phys. Rev. C 76, 044606 (2007)

➤ Phys. Rev. C 108, L051601 (2023)



## 2.模型介绍——双核系统模型



### ➤ transfer:

### ➤ 前平衡粒子的动能分布:

the Monte Carlo method,  $\epsilon_v = (0, E^* - B_v - V_c - E_{rot})$

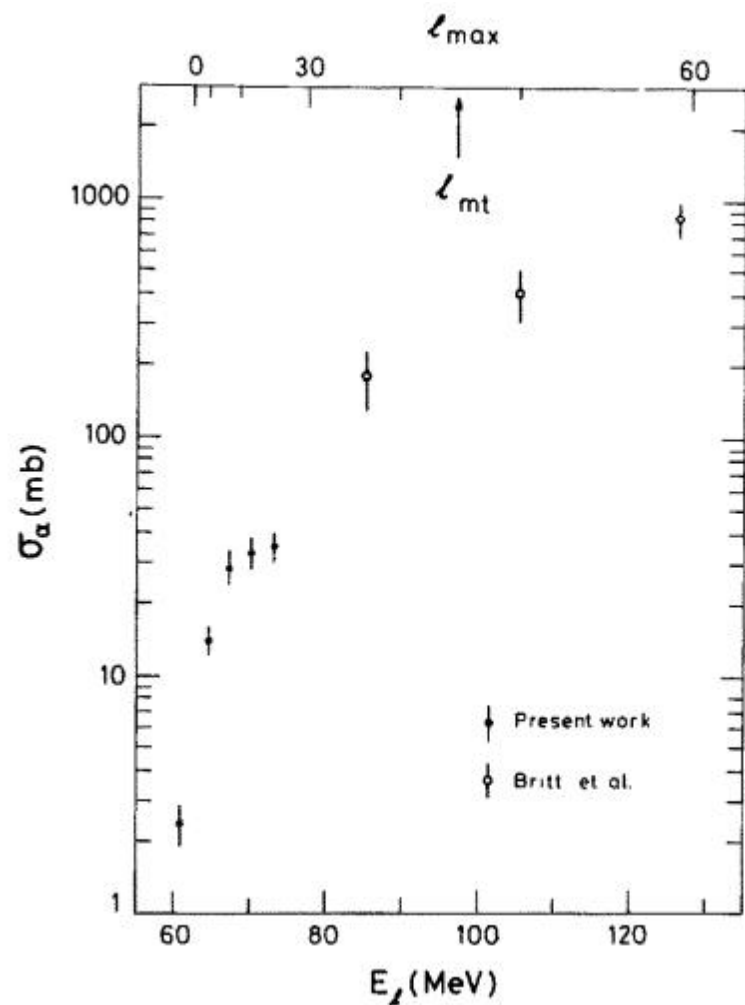
### 1.中子: Watt Spectrum

$$\frac{dN_n}{d\epsilon_n} = C_n \frac{\epsilon_n^{1/2}}{T_w^{3/2}} \exp\left(-\frac{\epsilon_n}{T_w}\right) \quad T_w = 1.7 \pm 0.1 \text{ MeV}$$

➤ *Phys. Rev. C 45, 719 (1992)*

### 2.带电粒子: Boltzmann Distribution

$$\frac{dN_v}{d\epsilon_v} = 8\pi E_k \left(\frac{m}{2\pi T_v}\right)^{1/2} \exp\left(-\frac{\epsilon_v}{T_v}\right) \quad T_v = \sqrt{\frac{E^*}{a}}, \quad a = A/12$$



IMP:  $^{12}\text{C} + ^{209}\text{Bi}$

## 2.模型介绍——双核系统模型



➤ transfer:

➤ 前平衡粒子的角分布:

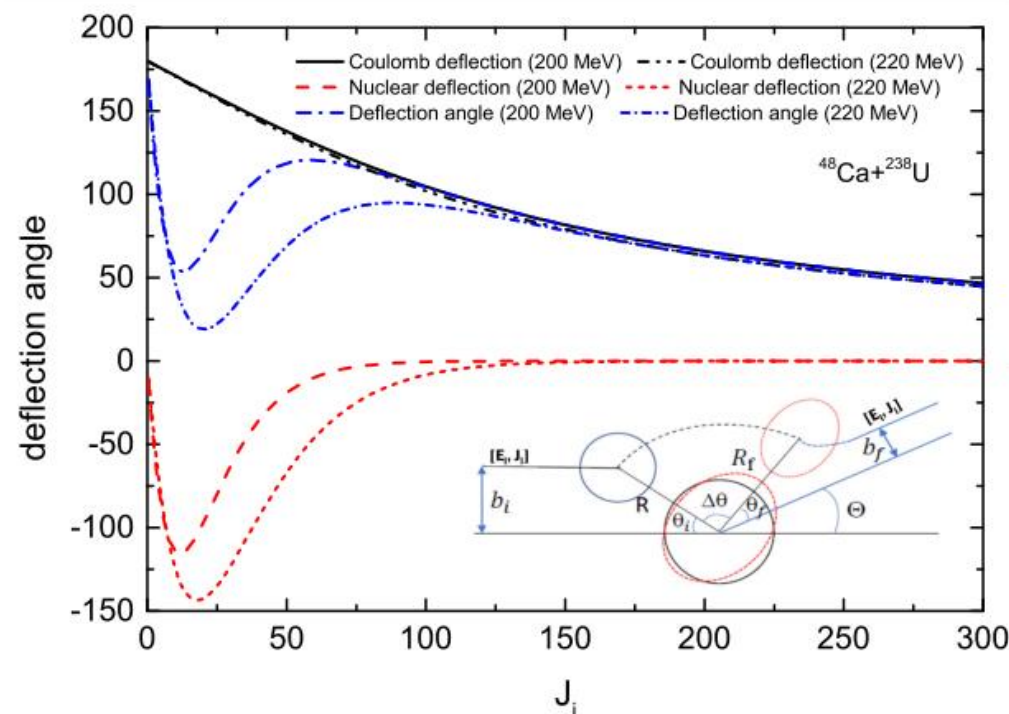
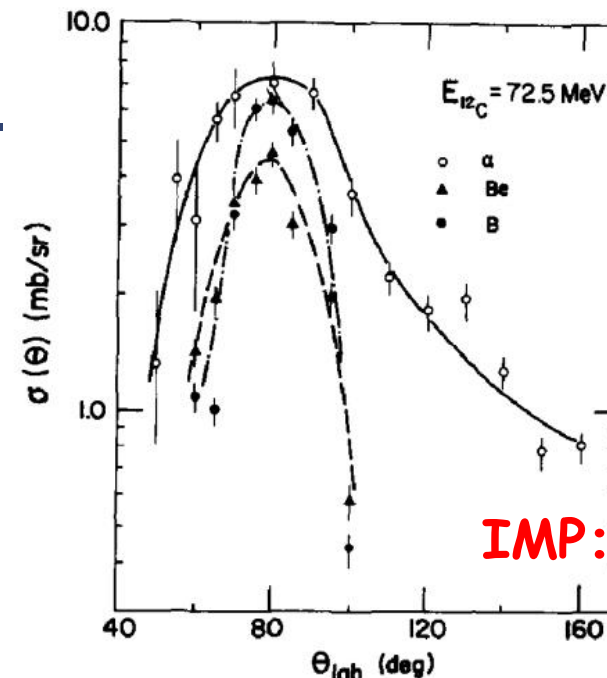
the deflection function method

$$\Theta(J_i) = \Theta_C(J_i) + \Theta_N(J_i),$$

1.库仑偏转  $\Theta(J_i)_C = 2 \arctan \frac{Z_p Z_t e^2}{2E_{c.m.} b}$

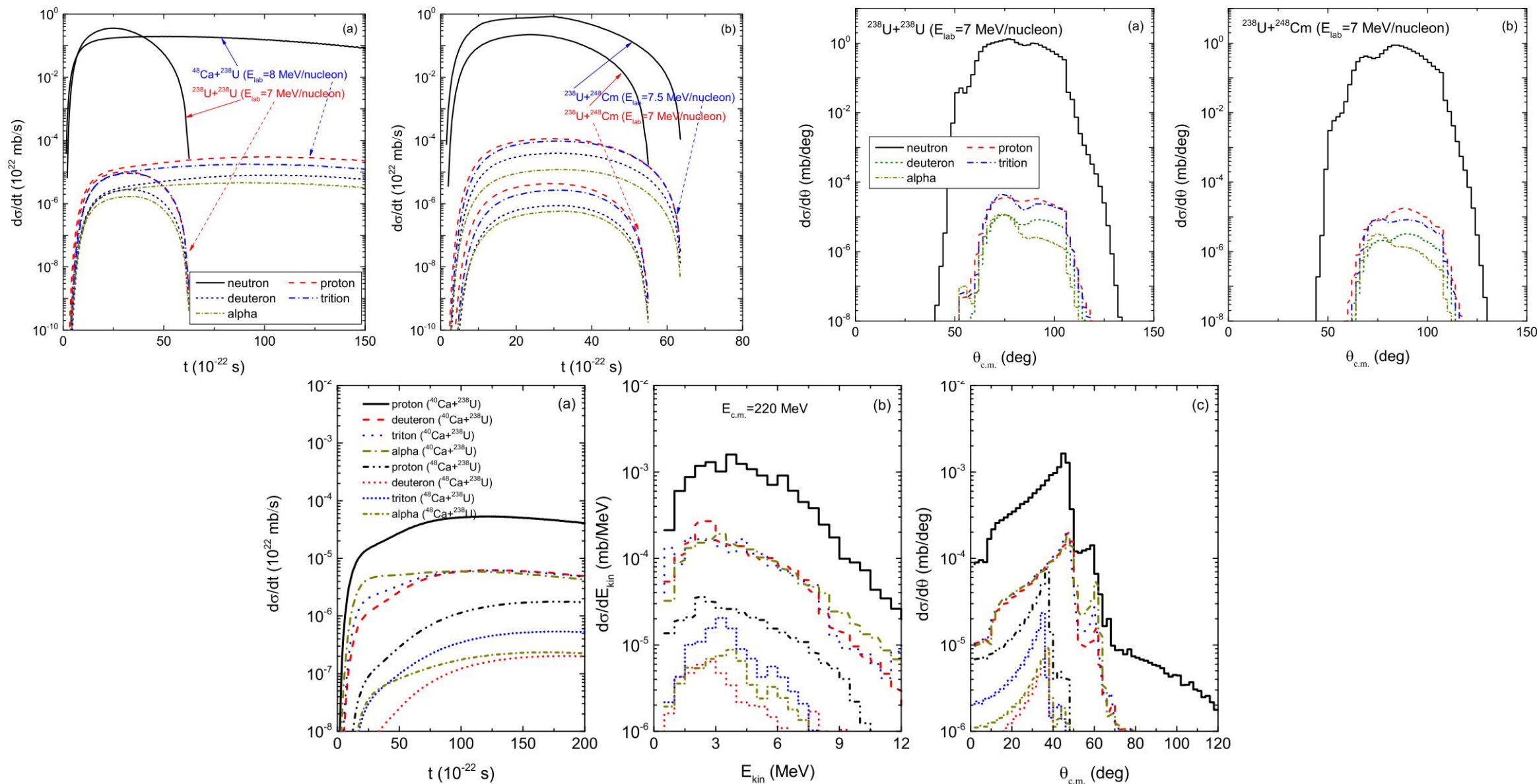
2.核偏转  $\Theta(J_i)_N = -\beta \Theta_C^{gr}(J_i) \frac{J_i}{J_{gr}} \left( \frac{\delta}{\beta} \right)^{J_i/J_{gr}}$

➤ *Z. Phys. A* 284, 209 (1978) ➤ *Eur. Phys. J. A* 58, 162 (2022)





# 3. 结果讨论—— $^{48,40}\text{Ca}, ^{238}\text{U}+^{238}\text{U}, ^{248}\text{Cm}$

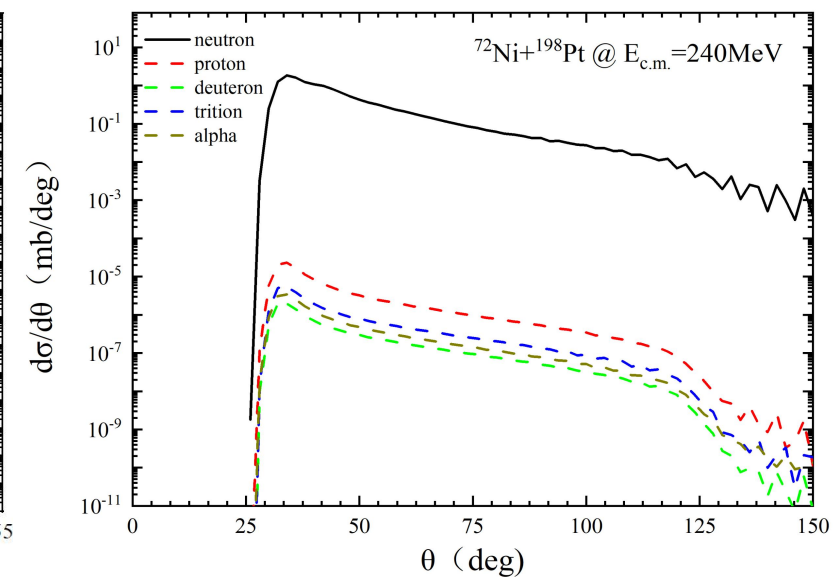
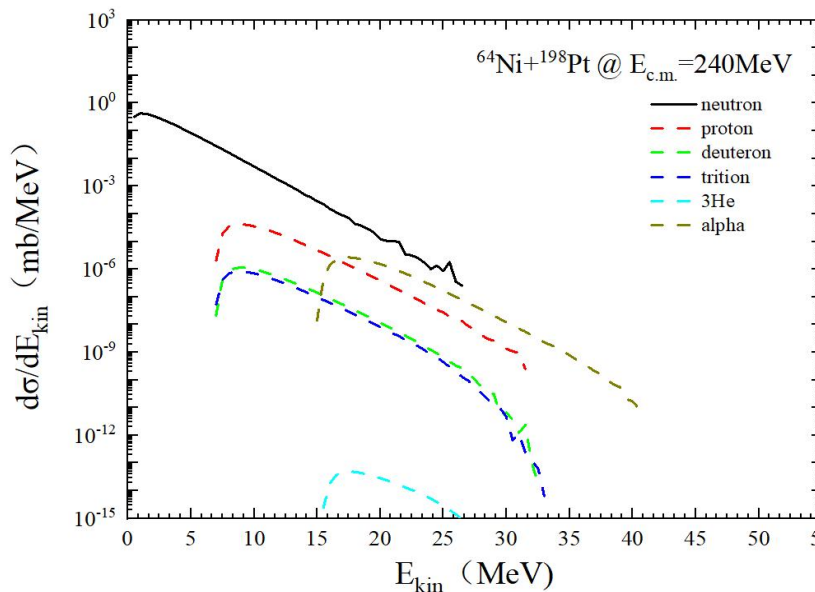
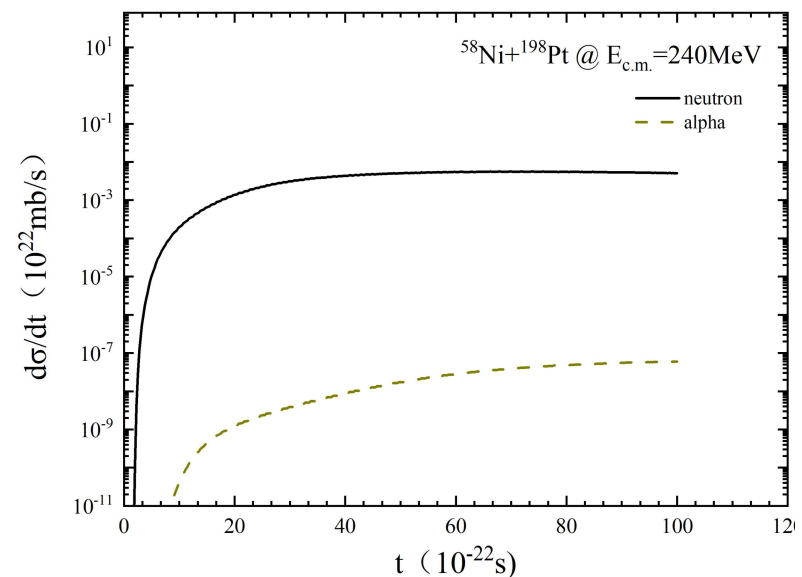
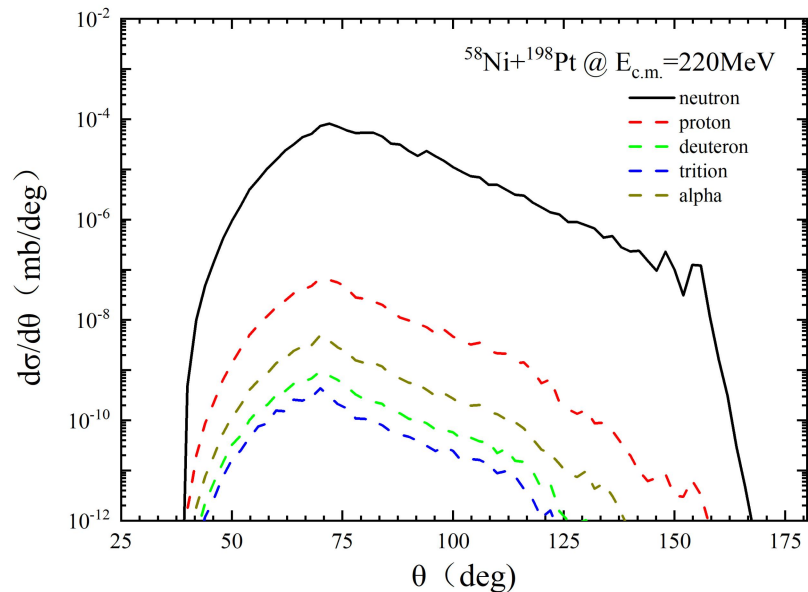
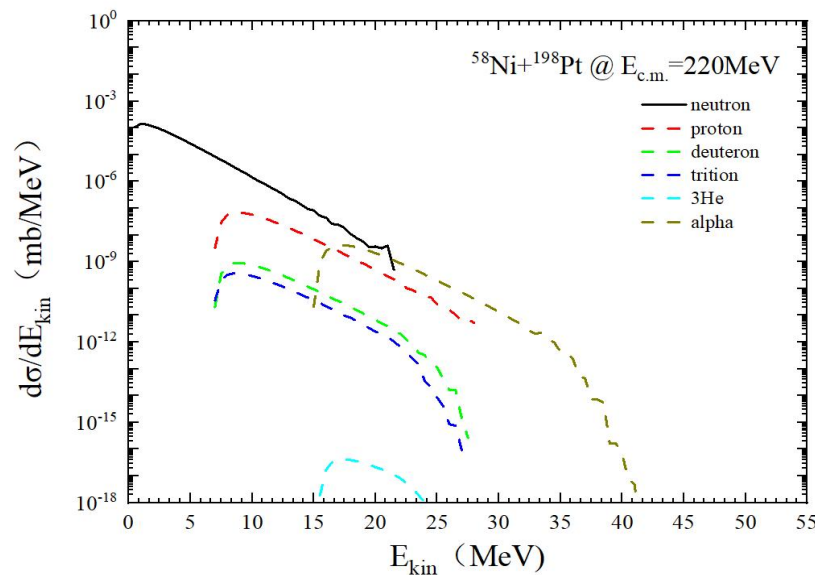
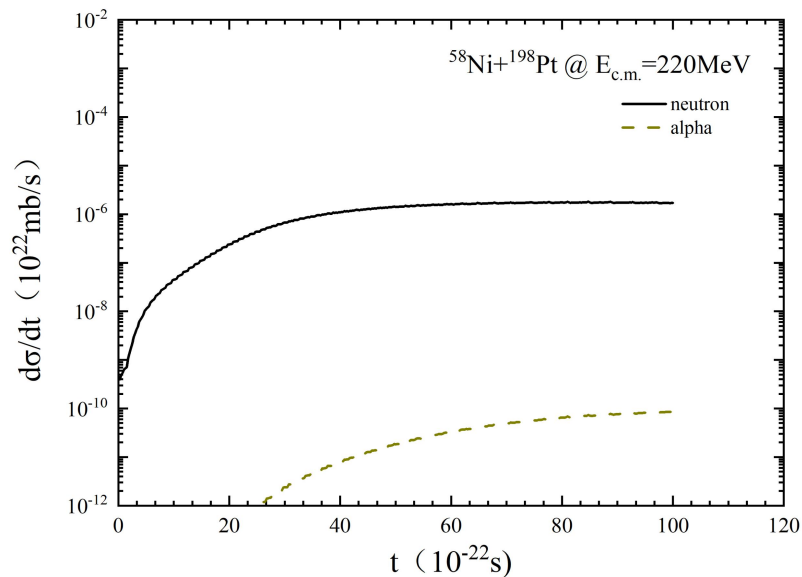


前平衡粒子产生率

前平衡粒子动能谱

前平衡粒子角分布

# 3. 结果讨论—— $^{58,64,72}\text{Ni}+^{198}\text{Pt}$



前平衡粒子的时间演化过程

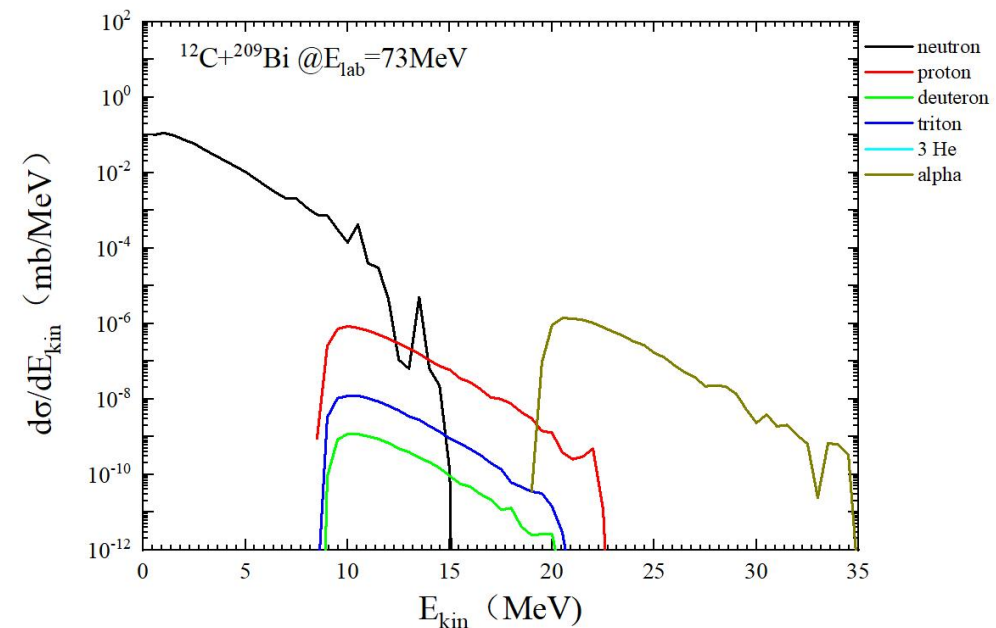
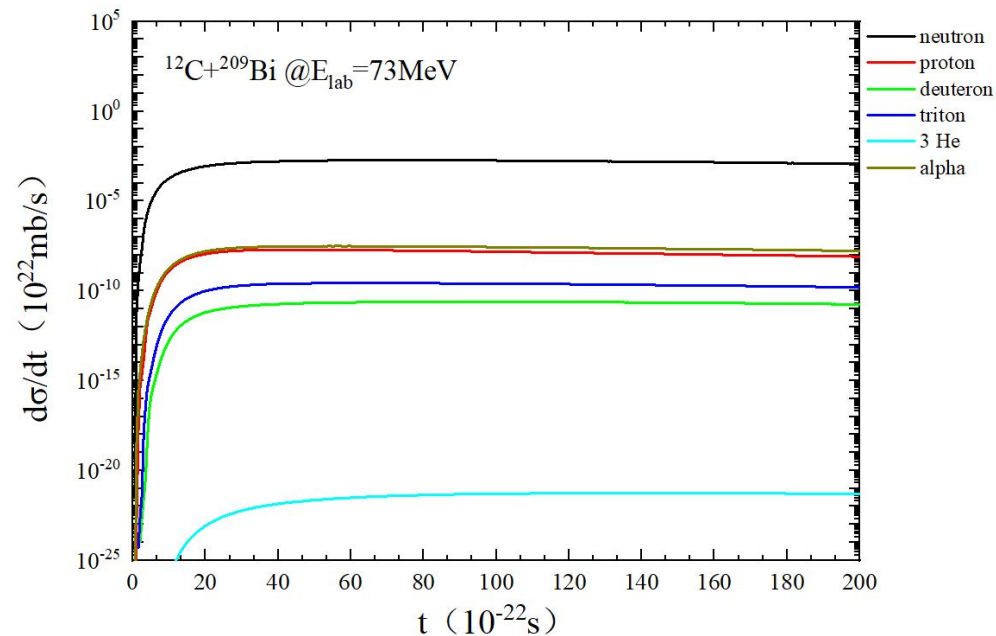
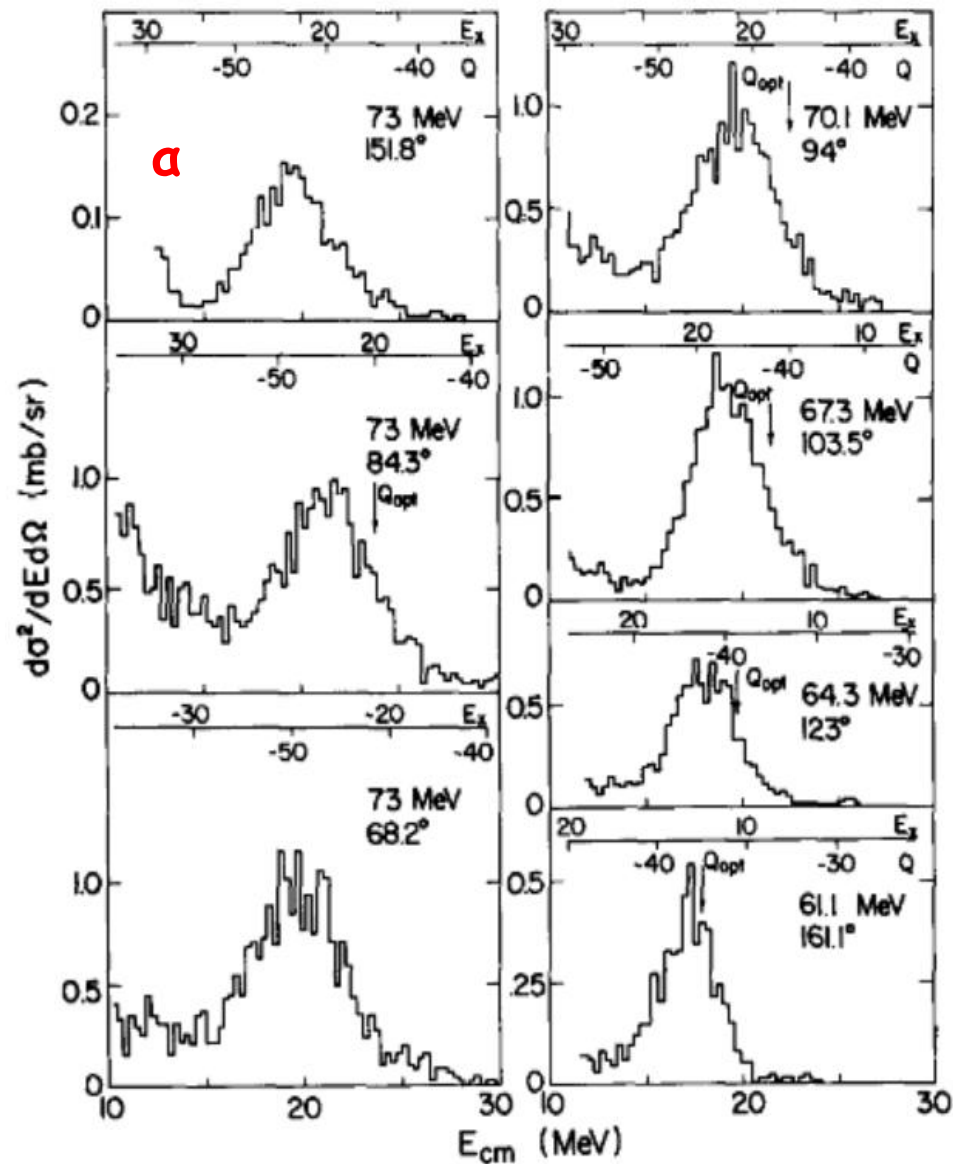
前平衡粒子动能谱

前平衡粒子角分布



# 3. 结果讨论—— $^{12}\text{C}+^{209}\text{Bi}$

IMP:  $^{12}\text{C}+^{209}\text{Bi}$



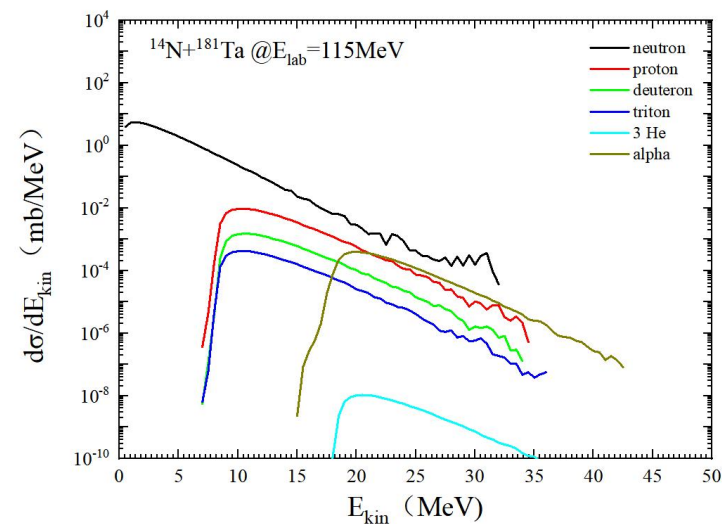
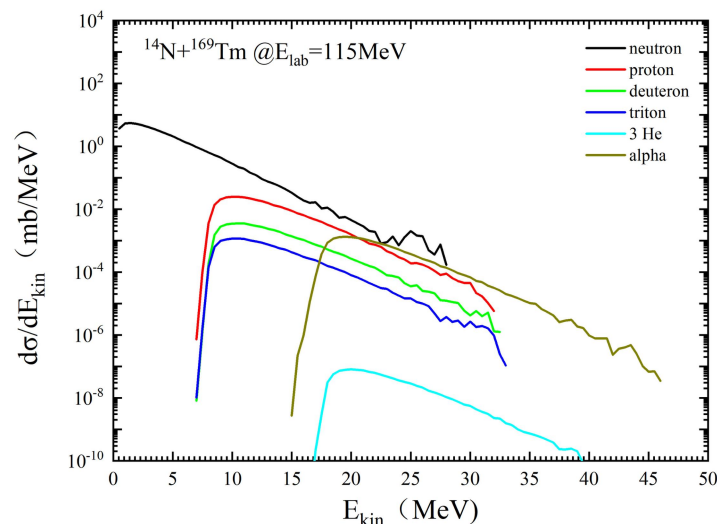
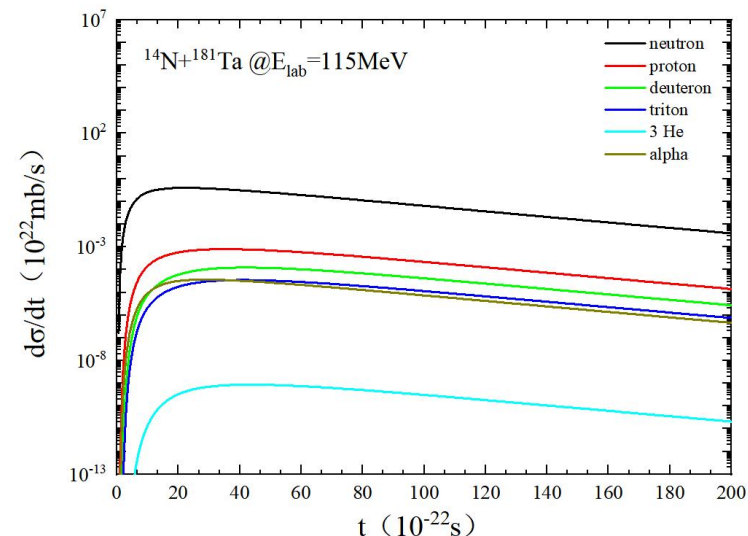
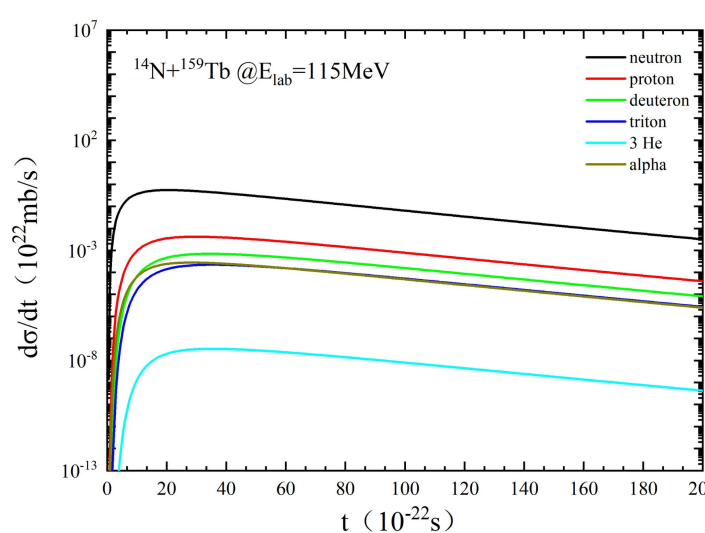
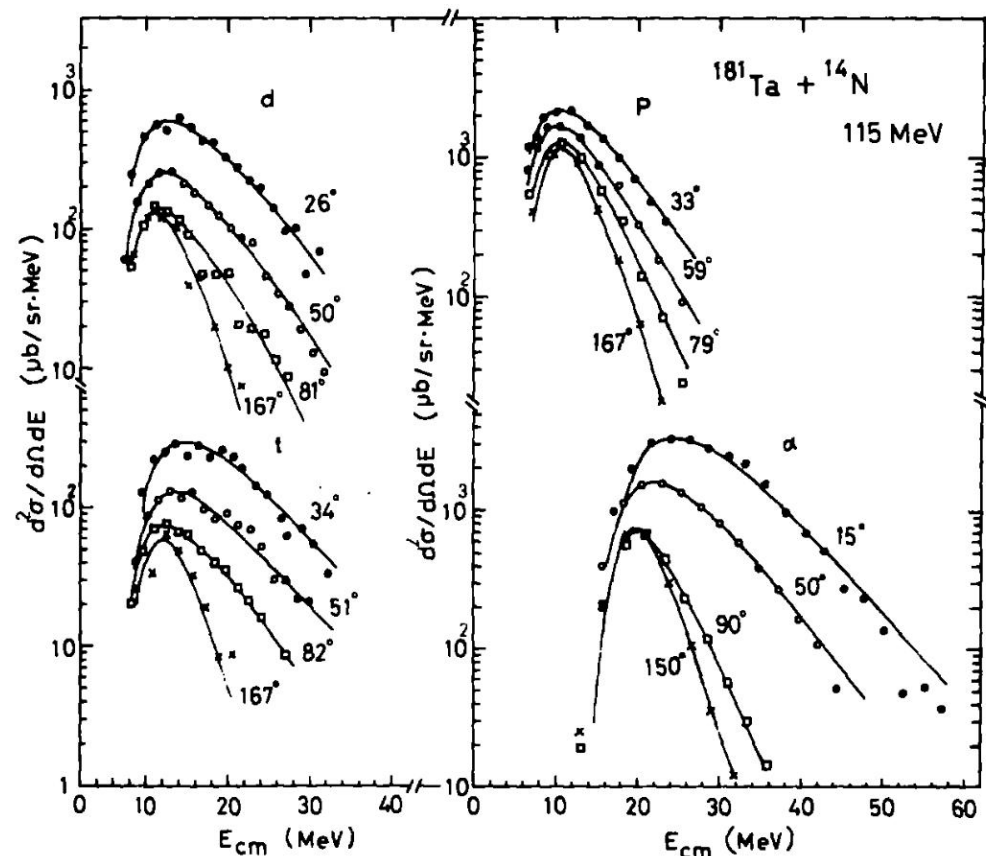




# 3. 结果讨论—— $^{14}\text{N}+^{159}\text{Tb}, ^{169}\text{Tm}, ^{181}\text{Ta}$



RIKEN:  $^{14}\text{N}+^{181}\text{Ta}$

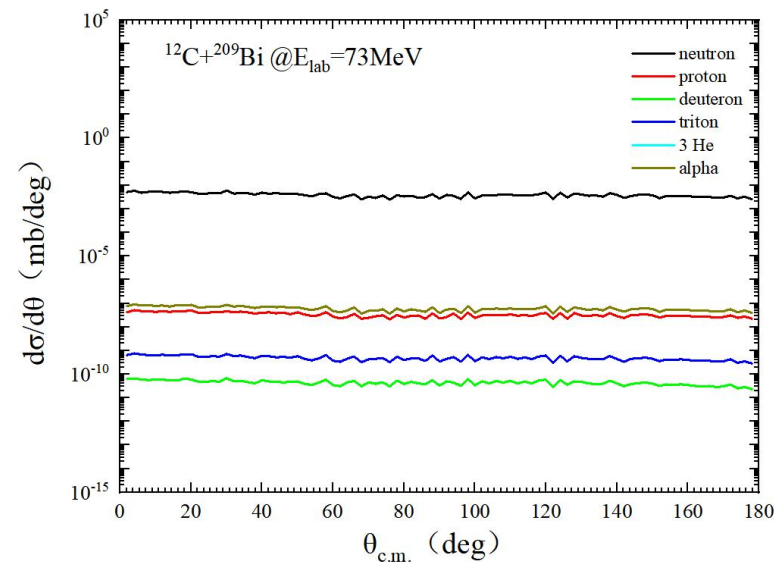
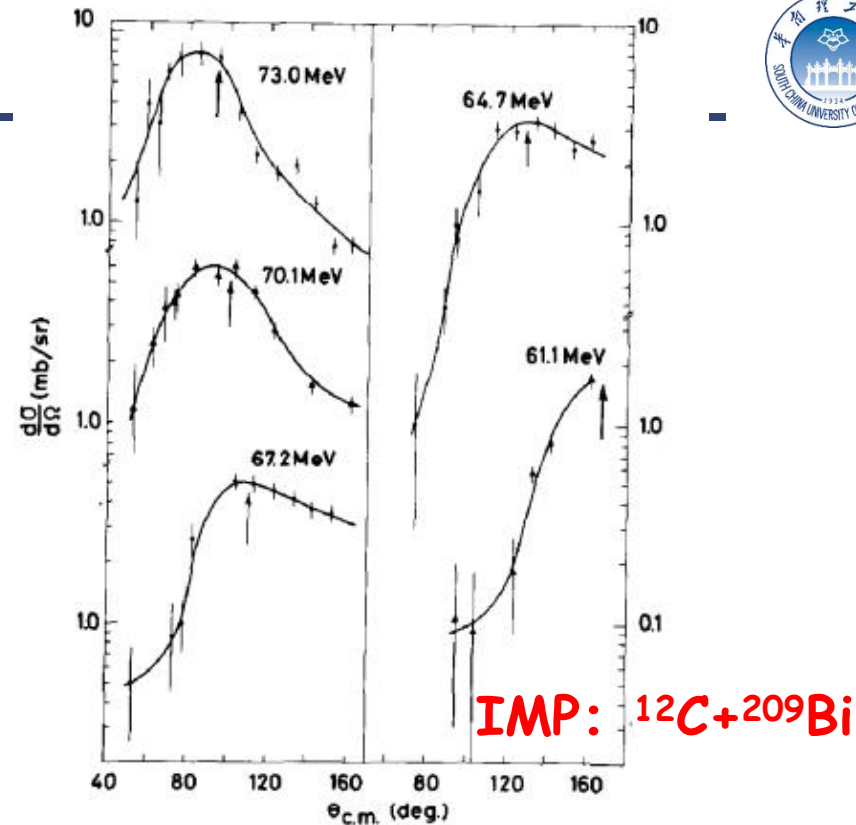




## 4. 总结展望



- 前平衡结团被认为是在核子转移过程中由初始DNS碎片衰变而发射出来的，它的发射一直持续到复合核的形成。
- 前平衡结团可以实现与转移片段相似的反应动力学，如角动量分布，它的发射蕴含着核反应中核子关联的重要信息。
- 前平衡结团的生成速率与反应体系和束流能量有关，其发射截面与分离能和库仑势垒密切相关。中子被发射的概率最大， $\alpha$ 和p，d，t的发射速率在大小上是相当的， $^3\text{He}$ 最小。
- 不足：模型中没有考虑反应系统的结构信息，较轻反应系统的角分布不能很好地描述实验结果。
- 展望：Consider the influence of cluster structure of projectile nuclides, such as  $^{12}\text{C}$ ,  $^{16}\text{O}$ , on the cluster emission, spectroscopic factor.



敬请各位专家、老师批评指正！

T H A N K   Y O U