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Measure of Variability: Range, Variance & Standard Deviation

Math for Machine Learning



Measure of Variability

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graph TD; A[Measure of Variability] --> B[Range]; A --> C[Variance]; A --> D[Standard Deviation];
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Range

The **range** of a set of data is the difference between the largest and smallest values. It can give a rough idea about the distribution of our dataset.

$$\text{Range} = \text{Max value} - \text{Min Value}$$

Variance

Variance is a measure of how far each number in the set is from the mean and therefore from every other number in the dataset.

$$\sigma^2 = \frac{\sum (x - \mu)^2}{N}$$

Standard Deviation

Standard Deviation is the square root of Variance. Standard deviation looks at how spread out a group of numbers is from the mean.

$$SD = \sqrt{\sigma^2}$$

Range ; Variance ; Standard Deviation

-5, 0, 5, 10, 15,

$$\text{Mean} = \frac{-5 + 0 + 5 + 10 + 15}{5} = 5$$

$$\text{Range} = 15 - (-5) = 20$$

$$\text{Variance} = \frac{(-5 - 5)^2 + (0 - 5)^2 + (5 - 5)^2 + (10 - 5)^2 + (15 - 5)^2}{5}$$

$$\text{Variance} = 50$$

$$\text{Standard Deviation} = 7.1$$

3, 4, 5, 6, 7

$$\text{Mean} = \frac{3 + 4 + 5 + 6 + 7}{5} = 5$$

$$\text{Range} = 7 - 3 = 4$$

$$\text{Variance} = \frac{(3 - 5)^2 + (4 - 5)^2 + (5 - 5)^2 + (6 - 5)^2 + (7 - 5)^2}{5}$$

$$\text{Variance} = 2$$

$$\text{Standard Deviation} = 1.4$$