$$\begin{split} & \underset{z \in \mathcal{L}^n}{\text{minimize}} & \frac{-\left\|z \odot \Pi_1^\mathsf{T} s_1\right\|_1 - \left\|(1-z) \odot \Pi_2^\mathsf{T} s_2\right\|_1}{\sup_{(i,j) \in \mathcal{N}} \psi(z_i, z_j) + \gamma \sum_{(i,j) \in \mathcal{N}} \phi_{i,j}(z_i, z_j)} \\ & + \beta \sum_{(i,j) \in \mathcal{N}} \psi(z_i, z_j) + \gamma \sum_{(i,j) \in \mathcal{N}} \phi_{i,j}(z_i, z_j) \\ & \frac{-\eta \sum \log p(z_i) + \xi \sum \left\langle \Pi_k, C \right\rangle}{\end{split}} \\ & \text{smoothness} \end{split}$$

i mixing ratio k=1,2 transport

$$-\eta \sum_{i} \log p(z_i) + \xi \sum_{k=1,2} \langle \Pi_k, C \rangle$$

$$-\eta \sum_{i} \min_{mixing \ ratio} \frac{1}{k=1,2} \text{ transport}$$
 subject to $\Pi_k 1_n = 1_n$, $\Pi_k^\intercal 1_n = 1_n$ for $k=1,2$.