Assignment 1

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1

1.1 Number of states visited

Game A:

Cutoff depth	3	4	5	6
Minmax	77,445	1,276,689		
α - β pruning	4,129	48,203		
Improvement	×18.76	×26.49		

Game B:

Cutoff depth	3	4	5	6
Minmax				
α - β pruning				
Improvement				

Game C:

Cutoff depth	3	4	5	6
Minmax				
α - β pruning				
Improvement				

1.2 Does state generation order matter?

My evaluation function iterates through the successor states in the order they were generated: left-to-right, top-to-bottom, with the directions generated in the (arbitrary) order north-east-south-west. I shuffled¹ the list of possible successors before evaluating their subtrees, which should indicate whether there were any serious discrepancies in the number of states visited.

1.3 Delaying defeat

2

- 2.1 Choice of evaluation function
- 2.2 Number of nodes visited
- 2.3 Tradeoff between evaluation function and game tree depth

¹I used the Python standard library's random. shuffle function, which shuffles a sequence (e.g., our list of successor states) in place.

A Appendix: Source code

A.1 Implementation comments

The code was written in Python, which is one of the languages I am most familiar with.

I consider the successors of the current state to be on cutoff level 0, and pass a depth parameter to the alpha-beta and minmax algorithms. The depth parameter is incremented for each ply in the recursion tree until the given cutoff limit is hit, at which point the heuristic evaluation of that state is returned.

A.2 Listing

```
#!/usr/bin/env python
2
   import string, copy, time, logging
4
   # debug < info < warning < error < critical?</pre>
   logging.basicConfig(level=logging.CRITICAL)
 6
7
   withhuman = False # human vs. computer, or computer against itself
   logthegame = False # write a log file on exit
   useab = True # alphabeta or minmax
10
   fancy = False # simple or fancy heuristic
12
   statesvisited = 0
13
14
   # we store the board as a matrix, i.e., a list of lists
15
   # initialstate = [
17
       ["O", None, None, None, None, "X"],
       ["X", None, None, None, None, "O"],
18
       ["O", None, None, None, None, "X"],
19
20
       ["X", None, None, None, None, "0"],
       ["O", None, None, None, None, "X"],
21
       ["X", None, None, None, None, "0"],
22
       ["O", None, None, None, None, "X"]
23
24
   # ]
25
26 class Node:
27
       def __init__(self, board, player, command):
           self.board = board
28
```

```
29
            self.player = player
            self.value = fancyheuristic(board, player) if fancy else
30
               simpleheuristic(board, player)
31
            self.command = command # the move made to generate this state
32
33 class Black:
34
       def __init__(self):
35
            self.piece = "X"
36
   class White:
37
38
       def __init__(self):
           self.piece = "0"
39
40
   def successors(board, player):
41
42
       logging.debug("Generating successors for player = " +
           player.__class__.__name__ + ", board = " + str(board))
43
       succs = []
44
       for y, line in enumerate(board):
45
            for x, char in enumerate(line):
               if char == player.piece:
46
47
                    # try all possible moves: xyN, xyE, xyS, xyW
48
                    for cmd in (str(x + 1) + str(y + 1) + d for d in directions):
49
                        #print player.__class__._name__, cmd,
50
                        try:
                            candidate = move(cmd, board, player)
51
                            succs.append(Node(candidate, player, cmd))
52
                            #print "works ->", len(succs)
53
54
                        except (ValueError, IndexError) as e:
55
                            # ValueError: attempted move was illegal, e.g. trying
                                to move to an occupied square
56
                            # IndexError: try to move outside of the board
                            #print "".join(e)
57
58
                            continue
59
       logging.debug("There were " + str(len(succs)) + " successors")
60
       return succs
61
62
   def alphabeta(player, node, depth, alpha, beta):
       global statesvisited
63
64
       statesvisited += 1
65
       succs = successors(node.board, player)
66
       otherplayer = black if player is white else black
```

```
67
       logging.info("Inside alphabeta on node " + str(hash(node)) + " obtained
           by " + node.command)
       logging.info(str(hash(node)) + " looks like\n" + prettyprint(node.board))
68
       logging.info(str(hash(node)) + " has depth = " + str(depth) + ", children
69
           = " + str(len(succs)))
70
       logging.debug("They are (" + player.__class__.__name__ + "): ")
71
       logging.debug("\n".join([c.command + " -> node " + str(hash(c))) for c in
           succs]))
72
       if depth == cutoff or len(succs) == 0:
           logging.info("Bottom reached, return utility " + str(node.value) + "
73
               from " + str(hash(node)))
74
           if node.value > 0:
75
                logging.info("Win found:\n" + prettyprint(node.board))
76
           return node.value
77
       elif player is white: #maxplayer, arbitrary
78
           logging.debug("State is \n" + prettyprint(node.board))
79
           for childnode in succs:
80
                logging.debug("Entering examination of child " +
                   str(hash(childnode)) + " by " + childnode.command + " from "
                   + str(hash(node)))
81
                alpha = max(alpha, alphabeta(otherplayer, childnode, depth + 1,
                   alpha, beta))
               if alpha >= beta:
82
83
                    logging.info("Pruning: returning beta = " + str(beta) + "
                       from " + str(hash(childnode)))
                    return beta
84
           logging.info("No pruning: returning alpha = " + str(alpha) + " from "
85
               + str(hash(node)))
86
           return alpha
       else: #black minplayer
87
88
           logging.debug("State is \n" + prettyprint(node.board))
           for childnode in succs:
89
                logging.debug("Entering examination of child " +
90
                   str(hash(childnode)) + " by " + childnode.command + " from "
                   + str(hash(node)))
               beta = min(beta, alphabeta(otherplayer, childnode, depth + 1,
91
                   alpha, beta))
               if alpha >= beta:
92
93
                    logging.info("Pruning: returning alpha = " + str(alpha) + "
                       from " + str(hash(childnode)))
94
                   return alpha
```

```
95
            logging.info("No pruning: returning beta = " + str(beta) + " from " +
                str(hash(node)))
            return beta
96
97
    def minmax(player, node, depth):
98
        global statesvisited
99
100
        statesvisited += 1
101
        logging.debug("Inside minmax on node " + str(hash(node)) + " depth = " +
            str(depth))
        #otherplayer = white if player is black else black
102
103
        minplayer = black # arbitrary
        if depth == cutoff or not successors(node.board, player):
104
105
            logging.debug("Bottom reached, return utility " + str(node.value))
106
            if node.value > 0:
107
                logging.debug("Win found:\n" + prettyprint(node.board))
108
            return node.value
109
        elif node.player is minplayer:
110
            logging.debug("Recursive minmax: player " + str(player) + ", depth =
                " + str(depth) + ", node = " + str(hash(node)))
            return min(minmax(player, child, depth + 1) for child in
111
                successors(node.board, player))
        else:
112
            logging.debug("Recursive minmax: player " + str(player) + ", depth =
113
                " + str(depth) + ", node = " + str(hash(node)))
            return max(minmax(player, child, depth + 1) for child in
114
                successors(node.board, player))
115
    def prettyprint(board):
116
117
        b = "\n".join(",".join(map(str, row)) for row in board)
        return b.replace("None", " ")
118
119
    def winner(board):
120
        # indicate the winner (if any) in the given board state
121
122
        def horizontal(board):
            # check if any consecutive four entries in a row are X-es or O-s
123
124
            for line in board:
125
                for i, char in enumerate(line):
                     if line[i : i + 4] == ["0"] * 4:
126
127
                         return white
                     elif line[i : i + 4] == ["X"] * 4:
128
129
                         return black
```

```
130
        def vertical(board):
131
            # equivalent to the horizontal winner in the transposed matrix
            return horizontal(map(list, zip(*board)))
132
133
        def diagonal(board):
134
            # all downward diagonals must start in the upper-left 4x4 submatrix
            # similarly, all upward diagonals must start in the lower-left 4x4
135
                submatrix
            # somewhat inelegant, but it works
136
            for i in range(4):
137
138
                 for j in range(4):
139
                     if all(board[i + k][j + k] == "0" for k in range(4)) or
                        all(board[6 - i - k][j + k] == "0" for k in range(4)):
140
                         return white
141
                     elif all(board[i + k][j + k] == "X" for k in range(4)) or
                        all(board[6 - i - k][j + k] == "X" for k in range(4)):
142
                         return black
143
        return horizontal(board) or vertical(board) or diagonal(board)
144
145
    def simpleheuristic(board, player):
        otherplayer = white if player is black else black
146
147
        if winner(board) is player:
148
            return 1
        elif winner(board) is otherplayer:
149
150
            return -1
        else:
151
152
            return 0
153
154
    def fancyheuristic(board, player):
155
        pass
156
157
    def parse(boardstring):
        # build a matrix from a string describing the board layout
158
        boardstring = string.replace(boardstring, ",", "")
159
160
        board, line = [], []
        for char in boardstring:
161
162
            if char == " ":
163
                 line.append(None)
            elif char == "\n":
164
165
                 board.append(line)
166
                 line = []
167
            else:
```

```
168
                 line.append(char)
169
        if line:
             board.append(line) # last line, if there is no newline at the end
170
171
        return board
172
173
174
    def move(command, board, player):
        # takes indices and a direction, e.g. "43W" or "26N"
175
176
        x, y, d = tuple(command)
177
        # the board is a zero-indexed array, adjust accordingly
178
        x, y = int(x) - 1, int(y) - 1
179
        dy, dx = directions[d.upper()]
180
        # does the piece fall within the bounds?
181
        if ((0 \le x + dx \le 7) \text{ and } (0 \le y + dy \le 7)
        # and is it our piece?
182
183
        and board[y][x] == player.piece
184
        # and is the destination square empty?
185
        and not board[y + dy][x + dx]):
             # then it's okay
186
187
             # we don't want to update in place
188
             successor = copy.deepcopy(board)
             successor[y + dy][x + dx] = successor[y][x]
189
190
             successor[y][x] = None
191
             return successor
        else:
192
             raise ValueError#("The move " + command + " is not legal")
193
194
195 white = White()
196 black = Black()
197 human = white if withhuman else None
198 computer = black
199 currentplayer = white
200 \text{ cutoff} = 5
201
202 # tuples of (dy, dx) for all directions
    directions = {
203
204
        "N": (-1, 0),
        "E": (0, 1),
205
206
        "S": (1, 0),
        "W": (0, -1)
207
208 }
```

```
209
210 with open("./starta.txt", "r") as f:
211
        initstatestr = f.read()
212 board = parse(initstatestr)
213
214 #board = initialstate
215 log = ["Initial state:"]
216 \quad movenumber = 1
217
218 while winner(board) is None:
        playername = currentplayer.__class__.__name__
219
220
        p = prettyprint(board)
221
        print p
222
        log.append(p)
223
        print "\nMove #%s:" % movenumber
224
        log.append("\nMove #%s:" % movenumber)
225
        cmd = ""
226
        print "It's %s's turn." % playername
227
228
            if currentplayer is human:
                 print "Possible moves:"
229
230
                 for s in successors(board, currentplayer):
                     print s.command
231
232
                 cmd = raw_input()
233
            else: #let the computer play against itself
234
                 succs = successors(board, currentplayer)
                 # take the possible move now, pick something better later on if
235
                    we can find it
                 bestmove = succs[0].command
236
237
                 bestutility = 0
                 if useab: #alphabeta
238
                     logging.warning("Player " + playername + " thinking about
239
                        what to do.")
                     logging.warning("Using alphabeta with cutoff " + str(cutoff))
240
                     for succboard in succs:
241
242
                         #init with alpha = -\inf, beta = \inf
243
                         u = alphabeta(currentplayer, succboard, 0, float("-inf"),
                             float("inf"))
244
                         if u > bestutility:
245
                             bestutility = u
                             bestmove = succboard.command
246
```

```
247
                else: #minmax
                     logging.warning("Player " + playername + " thinking about
248
                        what to do.")
249
                     logging.warning("Using minmax with cutoff " + str(cutoff))
                     for succboard in succs:
250
                         u = minmax(currentplayer, succboard, 0)
251
252
                         if u > bestutility:
                             logging.critical("Utility improved: " + str(u) + "
253
                                 from " + succboard.command)
254
                             bestutility = u
255
                             bestmove = succboard.command
256
                cmd = bestmove
                 print "The computer makes the move", cmd
257
258
259
            print "cutoff", cutoff, "states", statesvisited, "with", "alphabeta"
                if useab else "minmax"
260
            raise Exception("Counting states visited")
261
            board = move(cmd, board, currentplayer)
            log.append("%s plays %s." % (playername, cmd))
262
            currentplayer = white if currentplayer is black else black
263
            playername = currentplayer.__class__.__name__
264
265
            movenumber += 1
        #except ValueError:
266
            print "Illegal move."
267
            #raise
268
        except KeyboardInterrupt:
269
            log.append("Game cancelled.")
270
271
            logging.critical("Game cancelled.")
272
            break
273
274 # post-game cleanup
275 print prettyprint(board)
276 log.append(prettyprint(board))
277
278 if winner(board):
279
        s = "%s won the match" % winner(board).__class__.__name__
280
        print s
281
        log.append(s)
282 else:
        print "It's a draw"
283
284
        log.append("It's a draw")
```

```
285
286 if logthegame:
287    logname = time.strftime("/Users/hakon/Desktop/con4-%Hh%M-%S.log")
288    with open(logname, "w+") as logfile:
289    logfile.write("\n".join(log))
```