

# Assignment 1

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ESCE 526 Artificial Intelligence

February 4, 2013

## 1

### 1.1 Number of states visited with simple heuristic

Game A:

Cutoff depth	3	4	5	6
Minmax	77,445	1,276,689	21,335,620	Unknown
$\alpha$ - $\beta$ pruning	4129	48,203	694,652	Unknown
Improvement	$\times 18.76$	$\times 26.49$	$\times 30.72$	Unknown

Game B:

Cutoff depth	3	4	5	6
Minmax	98,345	1,704,319	29,770,996	Unknown
$\alpha$ - $\beta$ pruning	6421	96,884	1,683,194	Unknown
Improvement	$\times 15.32$	$\times 17.59$	$\times 17.69$	Unknown

Game C:

Cutoff depth	3	4	5	6
Minmax	69,954	1,237,535	22,191,032	Unknown
$\alpha$ - $\beta$ pruning	3763	51,098	840,633	Unknown
Improvement	$\times 18.59$	$\times 24.22$	$\times 26.40$	Unknown

This game has a high branching factor, in the ballpark of about 16 possible moves for each round, which makes exploring the game tree to any significant depth a very time-consuming chore. I didn't have time to calculate the numbers for cutoff depth 6, but they should be at least one order of magnitude higher than for the previous depth.

An interesting observation is that alpha-beta pruning seems to be increasingly efficient at chopping off irrelevant branches of the game tree as the cutoff depth increases.<sup>1</sup> Observe, for example, that in game A the number of states visited by minmax with cutoff depth 3 was 18 times higher than the number visited by alpha-beta, while it was over 30 times higher when the cutoff depth was 5.

## 1.2 Does state generation order matter?

My evaluation function iterates through the successor states in the order they were generated: left-to-right, top-to-bottom, with the directions generated in the (arbitrary) order north-east-south-west. I considered the first move in game A and ran<sup>2</sup> alpha-beta pruning five times with a cutoff depth of 3, shuffling the list of successor states randomly every time one is generated. (Since the minmax algorithm does not prune the game tree at all, the order in which it evaluates successors is irrelevant.)

I found that evaluation order *did* matter, though not impressively so. Alpha-beta pruning with the non-shuffled evaluation order visited 4129 states, as per the table above. The sample runs with suffling visited 4480, 4338, 4324, 4114, and 4376 states, respectively, for an average of 4326 states, which is 4.77% more than the non-shuffled case. The maximum deviations were 8.5% more and 0.36% fewer states visited than the original order. I also tried evaluating states in the reverse order; the difference was negligible. This suggests that there is no significant benefit to be gained by shuffling; in fact, we see that more states were visited with alternative evaluation orders than with the original sequence. I don't know if this is a coincidence or if the order I picked is somehow optimal; alpha-beta pruning should perform best when the best branches of the game tree are explored early, and most of the subsequent branches are pruned.

# 2

## 2.1 Choice of evaluation function

The fancyheuristic function calculates a heuristic value for a given player in a given board state. Let  $n_i$  be the number of  $i$ -in-a-row instances the player has on the board; for example, if the player has 3 pieces in a row at two different spots on the board, then  $n_3 = 2$ . This number is multiplied by a corresponding power of 10, so that more weight is given to board states with more pieces

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<sup>1</sup>In my code I consider the children of the current state to be in ply 0; their children, i.e., the grandchildren of the current state, are in ply 1, and so on. If this interpretation is incorrect and the current state's children should instead be regarded as being on ply 1, the values in the tables above should be shifted one column to the right.

<sup>2</sup>The commands given were `python ass1.py --input starta.txt --cutoff 3 --alg ab --count --shuffle`. See the appendix for details on usage.

connected:

$$s = \sum_{i=2}^4 n_i \cdot 10^i$$

This ensures that the player gets a higher score

Suppose, for example, the

## 2.2 Number of states visited with advanced heuristic

The more advanced heuristic does *not* reduce the number of states visited, which I found surprising. Game A:

Cutoff depth	3	4	5	6
Minmax	77,445			
$\alpha$ - $\beta$ pruning	22,291			
Improvement	xx	xx	xx	Unknown

## 2.3 Tradeoff between evaluation function and game tree depth

### Other comments

Threading, improved heuristic, optimizing for speed

## A Appendix: Source code

### A.1 Usage

All arguments are optional:

- `-i` or `--input`: Specify an input file to be used as the initial game state. A plain-text file following the notation used in the assignment is expected. Defaults to the example illustrated in the “Introduction” part of the assignment text.
- `-u` or `--human`: The computer should play against a human adversary, not just against itself. May take values `w` or `b` to indicate that the human should be white or black, respectively. The user will be prompted for input when it is their turn to play.
- `-c` or `--cutoff`: Specify a cutoff depth. Defaults to 3.
- `-a` or `--alg`: Specify which of the minmax or alpha-beta pruning algorithms is to be used. May take values `mm` or `ab`. Defaults to alpha-beta pruning.
- `-l` or `--log`: A log file should be written on exit. May prove useful for the tournament.
- `-k` or `--count`: Count the number of states visited. Used for problem 1.1.
- `-s` or `--shuffle`: Shuffle the list of successor states before evaluating them. Used for problem 1.2.
- `-f` or `--fancy`: Indicate that the advanced heuristic should be used.

Example: `python ass1.py --input file.txt --alg ab --human w --fancy --log`

### A.2 Listing

The code is written in Python 2.7. I’ve expunged all logging statements and other debugging aids for the sake of readability.

```
1 #!/usr/bin/env python
2
3 import string, copy, time, logging, argparse, random
4
5 # debug < info < warning < error < critical?
6 logging.basicConfig(level=logging.DEBUG)
7
8 #withhuman = False # human vs. computer, or computer against itself
9 #fancy = False # simple or fancy heuristic
10
11 # tuples of (dy, dx) for all directions
```

```

12 directions = {
13     "N": (-1, 0),
14     "E": (0, 1),
15     "S": (1, 0),
16     "W": (0, -1)
17 }
18
19 # used for counting states, problem 1.1
20 statesvisited = 0
21
22 class Node:
23     def __init__(self, board, player, command):
24         self.board = board
25         self.player = player
26         self.value = fancyheuristic(board, player) if fancy else
27             simpleheuristic(board, player)
28         self.command = command # the move made to generate this state
29
30 class Black:
31     def __init__(self):
32         self.piece = "X"
33
34 class White:
35     def __init__(self):
36         self.piece = "O"
37
38 def successors(board, player):
39     logging.debug("Generating successors for player = " + player.__class__.__name__ +
40         ", board = " + str(board))
41     succs = []
42     for y, line in enumerate(board):
43         for x, char in enumerate(line):
44             if char == player.piece:
45                 # try all possible moves: xyN, xyE, xyS, xyW
46                 for cmd in (str(x + 1) + str(y + 1) + d for d in directions):
47                     try:
48                         candidate = move(cmd, board, player)
49                         succs.append(Node(candidate, player, cmd))
50                     except (ValueError, IndexError) as e:
51                         # ValueError: attempted move was illegal, e.g. trying to move
52                         # to an occupied square
53                         # IndexError: try to move outside of the board
54                         continue
55     logging.debug("There were " + str(len(succs)) + " successors")
56     if args.shuffle:
57         random.shuffle(succs)

```

```

55     return succs
56
57 def alphabeta(player, node, depth, alpha, beta):
58     if countingstates:
59         global statesvisited
60         statesvisited += 1
61     succs = successors(node.board, player)
62     otherplayer = black if player is white else black
63     logging.info("Inside alphabeta on node " + str(hash(node)) + " obtained by " +
64                 node.command)
65     logging.info(str(hash(node)) + " looks like\n" + prettyprint(node.board))
66     logging.info(str(hash(node)) + " has depth = " + str(depth) + ", children = " +
67                 str(len(succs)))
68     logging.debug("They are (" + player.__class__.__name__ + "): ")
69     logging.debug("\n".join([c.command + " -> node " + str(hash(c)) for c in succs]))
70     # cut off and return heuristic value if we are too deep down
71     if depth == cutoff or len(succs) == 0:
72         logging.info("Bottom reached, return utility " + str(node.value) + " from " +
73                     str(hash(node)))
74         return node.value
75     # return immediately if we win by making this move
76     # elif winner(node.board) is player:
77     #     return float("inf")
78     elif player is white: # white is maxplayer (arbitrary pick)
79         logging.debug("State is \n" + prettyprint(node.board))
80         for childnode in succs:
81             logging.debug("Entering examination of child " + str(hash(childnode)) + "
82                             by " + childnode.command + " from " + str(hash(node)))
83             alpha = max(alpha, alphabeta(otherplayer, childnode, depth + 1, alpha,
84                                         beta))
85             if alpha >= beta:
86                 logging.info("Pruning: returning beta = " + str(beta) + " from " +
87                             str(hash(childnode)))
88                 return beta
89             logging.info("No pruning: returning alpha = " + str(alpha) + " from " +
90                         str(hash(node)))
91         return alpha
92     else: # black is minplayer
93         logging.debug("State is \n" + prettyprint(node.board))
94         for childnode in succs:
95             logging.debug("Entering examination of child " + str(hash(childnode)) + "
96                             by " + childnode.command + " from " + str(hash(node)))
97             beta = min(beta, alphabeta(otherplayer, childnode, depth + 1, alpha,
98                                       beta))
99             if alpha >= beta:

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91         logging.info("Pruning: returning alpha = " + str(alpha) + " from " +
92                        str(hash(childnode)))
93         return alpha
94     logging.info("No pruning: returning beta = " + str(beta) + " from " +
95                  str(hash(node)))
96     return beta
97
98 def minmax(player, node, depth):
99     if countingstates:
100         global statesvisited
101         statesvisited += 1
102     logging.debug("Inside minmax on node " + str(hash(node)) + " depth = " +
103                  str(depth))
104     minplayer = black # arbitrary
105     if depth == cutoff or not successors(node.board, player):
106         logging.debug("Bottom reached, return utility " + str(node.value))
107         if node.value > 0:
108             logging.debug("Win found:\n" + prettyprint(node.board))
109             return node.value
110     elif node.player is minplayer:
111         logging.debug("Recursive minmax: player " + str(player) + ", depth = " +
112                      str(depth) + ", node = " + str(hash(node)))
113         return min(minmax(player, child, depth + 1) for child in
114                   successors(node.board, player))
115     else:
116         logging.debug("Recursive minmax: player " + str(player) + ", depth = " +
117                      str(depth) + ", node = " + str(hash(node)))
118         return max(minmax(player, child, depth + 1) for child in
119                   successors(node.board, player))
120
121 def prettyprint(board):
122     b = "\n".join(", ".join(map(str, row)) for row in board)
123     return b.replace("None", " ")
124
125 def horizontal(board, n, player):
126     # check if any consecutive n entries in a row are X-es or O-s
127     # return the number of n-in-a-row instances on the board
128     piece = player.piece
129     connected = 0
130     for line in board:
131         for i, char in enumerate(line):
132             if line[i : i + n] == [piece] * n:
133                 connected += 1
134     return connected
135
136 def vertical(board, n, player):

```

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130     # equivalent to horizontal in the transposed matrix
131     return horizontal(map(list, zip(*board)), n, player)
132
133 def diagonal(board, n, player):
134     # all downward diagonals must start in the upper-left 4x4 submatrix
135     # similarly, all upward diagonals must start in the lower-left 4x4 submatrix
136     # somewhat inelegant, but it works
137     piece = player.piece
138     connected = 0
139     for i in range(n):
140         for j in range(n):
141             if all(board[i + k][j + k] == piece for k in range(n)) or all(board[6 - i
142                                     - k][j + k] == piece for k in range(n)):
143                 connected += 1
144     return connected
145
146 def winner(board):
147     # indicate the winner (if any) in the given board state
148     if horizontal(board, 4, white) or vertical(board, 4, white) or diagonal(board, 4,
149                                     white):
150         return white
151     elif horizontal(board, 4, black) or vertical(board, 4, black) or diagonal(board,
152                                     4, black):
153         return black
154     else:
155         return None
156
157 def sabotage(board, player):
158     pass
159
160 def simpleheuristic(board, player):
161     # as given in problem 1
162     otherplayer = white if player is black else black
163     if winner(board) is player:
164         return 1
165     elif winner(board) is otherplayer:
166         return -1
167     else:
168         return 0
169
170 def fancyheuristic(board, player):
171     otherplayer = white if player is black else white
172     score = 0
173     for i in [4, 3, 2]:
174         h = horizontal(board, i, player)
175         v = vertical(board, i, player)

```



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173         d = diagonal(board, i, player)
174         score += (10 ** i) * (h + v + d)
175     return score
176
177 def parseboard(boardstring):
178     # in case we want to specify an initial board layout,
179     # build a matrix from the given string (notation as in assignment)
180     boardstring = string.replace(boardstring, ",", "")
181     board, line = [], []
182     for char in boardstring:
183         if char == " ":
184             line.append(None)
185         elif char == "\n":
186             board.append(line)
187             line = []
188         else:
189             line.append(char)
190     if line:
191         board.append(line) # last line, if there is no newline at the end
192     return board
193
194
195 def move(command, board, player):
196     # takes indices and a direction, e.g. "43W" or "26N"
197     x, y, d = tuple(command)
198     # the board is a zero-indexed array, adjust accordingly
199     x, y = int(x) - 1, int(y) - 1
200     dy, dx = directions[d.upper()]
201     # does the piece fall within the bounds?
202     if ((0 <= x + dx <= 7) and (0 <= y + dy <= 7)
203         # and is it our piece?
204         and board[y][x] == player.piece
205         # and is the destination square empty?
206         and not board[y + dy][x + dx]):
207         # then it's okay
208         successor = copy.deepcopy(board)
209         successor[y + dy][x + dx] = successor[y][x]
210         successor[y][x] = None
211         return successor
212     else:
213         raise ValueError("The move " + command + " by " + player.__class__.__name__ +
214             " is not legal")
215
216 parser = argparse.ArgumentParser()
217 parser.add_argument("-c", "--cutoff", help="Cutoff depth")

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218 parser.add_argument("-i", "--input", help="Input game board")
219 parser.add_argument("-u", "--human", choices=["w", "b"], help="Play with a human
    opponent")
220 parser.add_argument("-a", "--alg", choices=["mm", "ab"], help="Minmax or alpha-beta
    algorithm")
221 parser.add_argument("-l", "--log", help="Write a game log on exit",
    action="store_true")
222 parser.add_argument("-s", "--shuffle", help="Shuffle successor list",
    action="store_true")
223 parser.add_argument("-k", "--count", help="Count states visited", action="store_true")
224 parser.add_argument("-f", "--fancy", help="Fancy heuristic function",
    action="store_true")
225 args = parser.parse_args()
226
227 cutoff = int(args.cutoff) if args.cutoff else 3
228 useab = not (args.alg == "mm") # alpha-beta by default
229 logthegame = args.log
230 countingstates = args.count
231 fancy = args.fancy
232
233 if args.input:
234     with open(args.input, "r") as inputfile:
235         initstr = inputfile.read()
236         board = parseboard(initstr)
237 else:
238     board = [
239         ["O", None, None, None, None, None, "X"],
240         ["X", None, None, None, None, None, "O"],
241         ["O", None, None, None, None, None, "X"],
242         ["X", None, None, None, None, None, "O"],
243         ["O", None, None, None, None, None, "X"],
244         ["X", None, None, None, None, None, "O"],
245         ["O", None, None, None, None, None, "X"]
246     ]
247
248 white = White()
249 black = Black()
250
251 if args.human == "w":
252     human = white
253     computer = black
254 elif args.human == "b":
255     human = black
256     computer = white
257 else:
258     human = None

```

```

259     computer = black # arbitrary
260
261     currentplayer = white
262
263     log = ["Initial state:"]
264     movenumber = 1
265
266     while winner(board) is None:
267         playername = currentplayer.__class__.__name__
268         p = prettyprint(board)
269         print p
270         print "\nMove #s:" % movenumber
271         print "It's %s's turn." % playername
272         if logthegame:
273             log.append(p)
274             log.append("\nMove #s:" % movenumber)
275             log.append("It's %s's turn." % playername)
276         cmd = "" # command string, e.g. 11E or 54N
277         try:
278             if currentplayer is human:
279                 print "Possible moves:"
280                 for s in successors(board, currentplayer):
281                     print s.command
282                 cmd = raw_input()
283             else:
284                 t = time.time() # time limit is 20 seconds
285                 succs = successors(board, currentplayer)
286                 # take the first move, pick something better later on if we can find it
287                 bestmove = succs[0].command
288                 bestutility = 0
289                 if useab: # alpha-beta pruning
290                     logging.warning("Player " + playername + " thinking about what to
291                                     do.")
292                     logging.warning("Using alphabeta with cutoff " + str(cutoff))
293                     for succboard in succs:
294                         # init with alpha = -inf, beta = inf
295                         u = alphabeta(currentplayer, succboard, 0, float("-inf"),
296                                     float("inf"))
297                         if u > bestutility:
298                             bestutility = u
299                             bestmove = succboard.command
300                 else: # minmax
301                     logging.warning("Player " + playername + " thinking about what to
302                                     do.")
303                     logging.warning("Using minmax with cutoff " + str(cutoff))
304                     for succboard in succs:

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```

302         u = minmax(currentplayer, succboard, 0)
303         if u > bestutility:
304             logging.critical("Utility improved: " + str(u) + " from " +
                              succboard.command)
305             bestutility = u
306             bestmove = succboard.command
307         cmd = bestmove
308         print "The computer makes the move", cmd
309         print "Thinking took", time.time() - t, "seconds"
310         if logging:
311             log.append("Thinking took " + str(time.time() - t) + " seconds")
312     # may raise a ValueError if input is ill-formed:
313     board = move(cmd, board, currentplayer)
314     if countingstates:
315         print statesvisited
316         raise Exception("Counting states only, stopping here")
317     if logthegame:
318         log.append("%s plays %s" % (playername, cmd))
319     currentplayer = white if currentplayer is black else black
320     playername = currentplayer.__class__.__name__
321     movenumber += 1
322 except ValueError:
323     print "Illegal move."
324     #raise
325 except KeyboardInterrupt:
326     if logthegame:
327         log.append("Game cancelled.")
328     logging.critical("Game cancelled.")
329     break
330
331 # post-game formalities
332 print prettyprint(board)
333
334 if winner(board):
335     s = "%s won the match" % winner(board).__class__.__name__
336     print s
337     if logthegame:
338         log.append(s)
339 else:
340     print "It's a draw"
341     if logthegame:
342         log.append("It's a draw")
343
344 if logthegame:
345     log.append(prettyprint(board))
346     logname = time.strftime("./connect4-%H-%M-%S.log")

```

```
347     with open(logname, "w+") as logfile:
348         logfile.write("\n".join(log))
```