SPCS Cryptography Class Lecture 1 Introduction

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Course Logistics

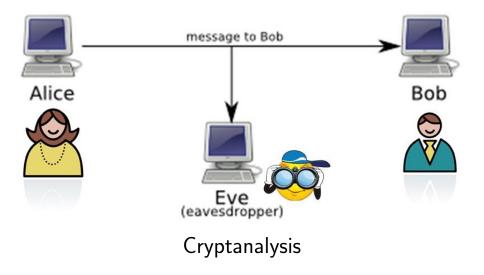
- Textbook: Cryptography, by Simon-Rubinstein Salzedo
- Course webpage: http://web.stanford.edu/~soarer/cryptography.html
- Problem sets
- Presentations on last two days: Jul 8,9.

Setup of Cryptography

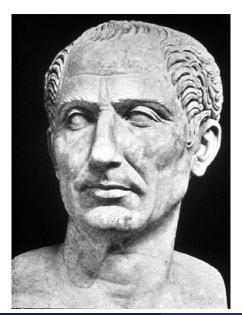


Cryptography

Setup of Cryptography



Caesar cipher



- Left shift by 3 alphabets.
- ullet For example, d o A, e o B.
- How would

cryptography

be encrypted?

ZOVMQLDOXMEV

- How to decrypt a message?
- For example,

OFDEQ

Shift cipher

- We can also do shifts other than -3 alphabets.
- For example, with a right shift of 10,

sleep

becomes

BUNNY

Shift cipher

- Let's say Alice and Bob agrees on a key (the shift). If Eve does not know the key, what can she do to crack a Caesar cipher?
- For example,

JRNGURE.

http://www.dcode.fr/caesar-cipher

• How can one make this harder to crack?

- Suppose Alice and Bob agrees on a substitution scheme instead where every letter would stand for another (perhaps random) letter.
- For example, if we have an encryption scheme

							<i>J</i> I					
а	b	С	d	е	f	g	h	i	j	k	ı	m
C	ı	S	Q	V	N	F	Ο	W	Α	Х	М	Т
n	0	р	q	r	S	t	u	V	W	×	у	z
G	U	Н	Р	В	K	L	R	Е	Υ	D	Z	J

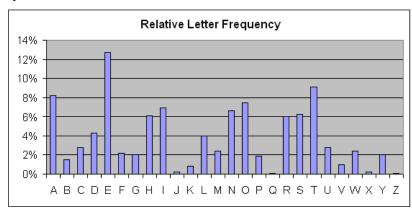
How would Alice send Bob the message

weather

- How does Bob decipher?
- What can Eve do? Frequency Analysis.

Frequency Analysis

• Normal English has certain letter frequency. For example, e appears way more often than x.



• Same for bigrams (pair of letters). For example,

Bigrams Frequency							
th	1.52 %	en	0.55 %				
he	1.28 %	ed	0.53 %				
in	0.94 %	to	0.52 %				
er	0.94 %	it	0.50 %				
an	0.82 %	ou	0.50 %				
re	0.68 %	ea	0.47 %				
nd	0.63 %	hi	0.46 %				
at	0.59 %	is	0.46 %				
on	0.57 %	or	0.43 %				
nd	0.56 %	ti	0.34 %				
ha	0.56 %	as	0.33 %				
es	0.56 %	te	0.27 %				
st	0.55 %	et	0.19 %				

• Substitution ciphers do NOT change this profile!

Example

We wish to decrypt

```
JNRZR BNIGI BJRGZ IZLQR OTDNJ GRIHT USDKR
ZZWLG OIBTM NRGJN IJTZJ LZISJ NRSBL QVRSI
ORIQT QDEKJ JNRQW GLOFN IJTZX QLFQL WBIMJ
ITQXT HHTBL KUHQL JZKMM LZRNT OBIMI EURLW
BLQZJ GKBJT QDIQS LWJNR OLGRI EZJGK ZRBGS
MJLDG IMNZT OIHRK MOSOT QHIJL QBRJN IJJNT
ZFIZL WIZTO MURZM RBTRZ ZKBNN LFRVR GIZFL
KUHIM MRIGJ LJNRB GKHRT QJRUU RBJLW JNRZI
TULGI EZLUK JRUST QZLUK EURFT JNLKJ JNRXR S
```

http://scottbryce.com/cryptograms/index.htm

Solution

- The most common English letter is E, T and A.
- The most common English bigram is TH, HE, IN.
- H is in the two most frequent English bigrams! This would give us a hint about what letters are T,H,E.

Here is a frequency table of the text

	R	J	I	L	Z	Т	N	Q	В	G	K
Freq	33	30	27	25	24	20	19	16	15	15	13
	U	М	0	S	Н	W	F	Е	D	Χ	V
Freq	12	12	10	9	8	7	6	5	5	3	2

The most frequent bigrams are: JN (11 times), NR (8 times), TQ (6 times), and LW, RB, RZ, and JL (5 times each).

What should JN,NR be?

Half way through..

theZe BhIGI BteGZ IZLQe OTDht GeIHT USDKe ZZWLG OIBTM heGth ItTZt LZISt heSBL QVeSI OEIQT QDEKt theQW GLOFH ItTZX QLFQL WBIMT ITQXT HHTBL KUHQL tZKMM LZehT OBIMI EUELW BLQZt GKBtT QDIQS LWthe OLGEI EZtGK ZeBGS MtLDG IMhZT OIHEK MOSOT QHITL QBeth ItthT ZFIZL WIZTO MUEZM eBTeZ ZKBhh LFeVe GIZFL KUHIM MeIGt LtheB GKHET QteUU eBtLW theZI TULGI EZLUK teUST QZLUK EUEFT thLKt theXe S

	R	J	I	L	Z	Т	N	Q	В	G	K
Freq	33	30	27	25	24	20	19	16	15	15	13
	U	М	0	S	Н	W	F	Е	D	Χ	V
Freq	12	12	10	9	8	7	6	5	5	3	2

Frequent bigrams are: JN (11 times), NR (8 times), TQ (6 times), and LW, RB, RZ, and JL (5 times each).

- Next frequent characters we don't know are I,L,Z,T.
- *RZ* appears often, and there is theZe in the beginning. This suggests that *Z* should be either *r* or *s*.
- TQ appears 6 times, and LQ appears 4 times, and they are among the characters we don't know yet. Looking at the bigram table,

	Bigrams I	requ	ency
th	1.52 %	en	0.55 %
he	1.28 %	ed	0.53 %
in	0.94 %	to	0.52 %
er	0.94 %	it	0.50 %
an	0.82 %	ou	0.50 %
re	0.68 %	ea	0.47 %
nd	0.63 %	hi	0.46 %
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ha	0.56 %	as	0.33 %
es	0.56 %	te	0.27 %
st	0.55 %	et	0.19 %

- This suggests that they are an, in or on. In particular, Q should be n, and T, L would be among {a, i, o}.
- IJ = It appears 4 times as well

 this would suggest that I is
 likely a, although it may also
 be s.

So far we know,

$$J = t$$
, $N = h$, $R = e$, $Q = n$, $I = a/s$, T , $L = a/i/o$, $Z = r/s$.

Back to the ciphertext for a moment,

```
theZe BhIGI BteGZ IZLQe OTDht GeIHT USDKe ZZWLG OIBTM heGth ItTZt LZISt heSBL QVeSI OEIQT QDEKt theQW GLOFH ItTZX QLFQL WBIMT ITQXT HHTBL KUHQL tZKMM LZehT OBIMI EUELW BLQZt GKBtT QDIQS LWthe OLGEI EZtGK ZeBGS MtLDG IMhZT OIHEK MOSOT QHITL QBeth ItthT ZFIZL WIZTO MUeZM eBTeZ ZKBhh LFeVe GIZFL KUHIM MeIGt LtheB GKHeT QteUU eBtLW theZI TULGI EZLUK teUST QZLUK EUEFT thLKt theXe S
```

This suggests,

$$J = t$$
, $N = h$, $R = e$, $Q = n$, $I = a$, $T = i$, $L = o$, $Z = s$.

Putting them in,

these BhaGa BteGs asone OiDht GeaHi USDKe ssWoG OaBiM heGth atist osaSt heSBo nVeSa Oeani nDEKt thenW GoOFh atisX noFno WBaMt ainXi HHiBo KUHno tsKMM osehi OBaMa EUeoW Bonst GKBti nDanS oWthe OoGea EstGK seBGS MtoDG aMhsi OaHeK MOSOi nHato nBeth atthi sFaso WasiO MUesM eBies sKBhh oFeVe GasFo KUHaM MeaGt otheB GKHei nteUU eBtoW thesa iUoGa EsoUK teUSi nsoUK EUeFi thoKt theXe S

First line almost decrypted!

- The beginning of message should look like
 these BhaGaBteGs as one OiDht...
- Bha is probably start of a word, and there is also an aBt part. One is led to guess that B = c, which leads to G = r.
- Moreover, OiDht strongly hints that D is g.

these chara cters asone Oight reaHi USgKe ssWor OaciM her that is to sa S theSco nVeSa Oeani ngEKt thenW roOFh atisX noFno WcaMt ainXi HHico KUHno tsKMM osehi OcaMa EUeoW const rKcti nganS oWthe Oorea EstrK secrS Mtogr aMhsi OaHeK MOSOi nHato nceth atthi sFaso WasiO MUesM ecies sKchh oFeVe rasFo KUHaM Meart othec rKHei nteUU ectoW thesa iUora EsoUK teUSi nsoUK EUeFi thoKt theXe S

- One can keep going for example, Oight suggests that O = m.
- The deciphered text is,

These characters, as one may readily guess, form a cipher; that is to say, they convey a meaning. But then from what is known of Captain Kidd, I could not suppose him capable of constructing any of the more abtruse cryptographs. I made up my mind at once that this was of a simple species. Such however as would appear to the crude intellect of the sailor absolutely insoluble without the key.

What next?

- So substitution cipher is cracked. What next?
- The reason substitution cipher is prone to frequency analysis, is because it is *monoalphabetic*, i.e. same letter always gets encrypted to the same thing.
- We can make it polyalphabetic!
- For example, g may get encoded by x at some point, but by m later in the message.

Vigenere cipher

Vigenere cipher is an example of a polyalphabetic cipher.

Example

Encrypt cryptography using the key lemon.

Solution

Plaintext	cryptography
Key	lemonlemonle
Ciphertext	NVKDGZKDOCSC

French calls it le chiffre indéchiffrable.

What can we do to crack this cipher?

Terminologies

Some terminologies: Alice wants to send Bob a message.

- The unencrypted message is the *plaintext*. The encrypted message is the *ciphertext*. Alice and Bob are doing *cryptography* in this process.
- A cryptosystem consists of a pair of algorithms, encryption (plaintext to ciphertext), and decryption (ciphertext to plaintext).
- For the encryption part, there are two components the *protocol* for encoding the message, and a specific *key*.

Kerckhoff's principle

A good cryptosystem should remain secure even if Eve knows the protocol, but not the key.

• What Eve does is *cryptanalysis*, the analysis of encrypted messages.