

FEDERAL PUBLIC SERVICE COMMISSION COMPETITIVE EXAMINATION-2024 FOR RECRUITMENT TO POSTS IN BS-17 UNDER THE FEDERAL GOVERNMENT

Roll Number

APPLIED MATHEMATICS

TIME ALLOWED: THREE HOURS	PART-I (MCQS)	MAXIMUM MARKS = 20
PART-I(MCQS): MAXIMUM 30 MINUTES	PART-II	MAXIMUM MARKS = 80

NOTE: (i) Part-II is to be attempted on the separate Answer Book.

- (ii) Attempt ONLY FOUR questions from PART-II. ALL questions carry EQUAL marks.
- (iii) All the parts (if any) of each Question must be attempted at one place instead of at different places.
- (iv) Candidate must write Q. No. in the Answer Book in accordance with Q. No. in the Q. Paper.
- (v) No Page/Space be left blank between the answers. All the blank pages of Answer Book must be crossed.
- (vi) Extra attempt of any question or any part of the attempted question will not be considered.

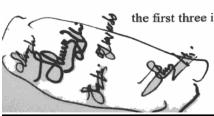


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Roll Number

APPLIED MATHEMATICS

TIME		OWED: THREE HOURS MAXIMUM MARKS = 100		
NOTE: (i) A ii) A pl iii) W iv) N	ttempt only FIVE questions in all. ALL questions carry EQUAL marks. If the parts (if any) of each Question must be attempted at one place instead of at eaces. Vrite Q. No. in the Answer Book in accordance with Q. No. in the Q.Paper. No Page/Space be left blank between the answers. All the blank pages of Answer Book.		
(v) E	e crossed. xtra attempt of any question or any part of the attempted question will not be consider se of Calculator is allowed.	ed.	
Q. No. 1	(a)	Expand a fourier series of $f(x) = x^2$, $1 < x < 2$	(10)	
	(b)	Find equation of integral surface of the differential equation $2y(z-3)p$ +	(10)	
		$(2x-z)q = y(2x-3)$ which passes through the circle $x^2 + y^2 = 2x$, $z = 0$.		
Q. No. 2	(a)	Solve the higher order differential equation $y'''' + y'' = 3x^2 + 4Sinx - 2Cosx$	(10)	
	(b)	Solve the initial value problem $y'' - 8y' + 15y = 9xe^{2x}$, $y(0) = 5$, $y'(0) = 10$	(10)	
Q. No. 3		Solve the equation $4u_{xx} + 5u_{xy} + u_{yy} + u_x + u_y = 2$, also find its canonical	(10)	
		form.		
	(p)	Prove that $\int_{-1}^{1} x^n P_n(x) dx = \frac{2^{n+1}(n!)^2}{(2n+1)!}$, where $P_n(x) = \frac{1}{2^n n!} \frac{d^n}{dx^n} (x^2 - 1)^n$ is	(10)	
		Legender polynomial of degree n.		
Q. No. 4	(a)	Verify the divergence theorem for $A = 4x\mathbf{i} - 2y^2\mathbf{j} + z^2\mathbf{k}$ taken over the region	(10)	
		bounded by $x^2 + y^2 = 4$, $z = 0$ and $z = 3$.		
	(b)	State and prove Stoke's theorem.	(10)	
Q. No. 5	(a)	Using the modified Euler's method, obtain the solution of the differential equation	(10)	
		$\frac{dy}{dt} = t + \sqrt{y} = f(t, y)$		
		with initial condition $y_0 = 1$ at $t_0 = 0$ for the range $0 \le t \le 0.6$ in step of 0.2.		
	(b)	Find the real roots of equation $4x + Cosx + 2 = 0$ by using Newton Raphson	(10)	
		method, correct to four decimal places.		
Q. No. 6	(a)	Solve the system of linear equations by Guass-Seidel iterative method and perform	(10)	
	3	the first three iterations of		



20x + y - 2z = 173x + 20y - z = -182x - 3y + 20z = 25

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- (b) Solve the following Van der Pol's equation y" (0.1)(1 y²)y' + y = 0, using fourth order Runge-Kutta method for x = 0.2, with the initial values y(0) = 1, y'(0) = 0.
- Q. No. 7 (a) Find the law of force for a particle moving in an orbit, $r = \frac{l}{1 eCos\theta'}$ where l is semi-latus rectum and e is ecentricity.
 - (b) Prove that the speed required to project a particle from a height h to fall a horizental distance a from the point of projection is at least $\sqrt{g(\sqrt{a^2 + h^2}) h}$.
- Q. No. 8 (a) Find the radial and transvers components of velocity moving along a curve $ax^2 + by^2 = 1 \text{ at any time t if the polar angle } \theta = ct^2.$ (10)
 - (b) Find the centroid of the surface formed by the revolution of the cardioide $r = a(1 + Cos\theta)$ about the initial line. (10)
