

Social Media & Text Analysis

lecture 5 - Paraphrase Identification
and Logistic Regression



CSE 5539-0010 Ohio State University
Instructor: Wei Xu
Website: socialmedia-class.org

In-class Presentation

- pick your topic and sign up
- a 10 minute presentation (20 points)
 - A Social Media Platform
 - Or a NLP Researcher

Reading #6 & Quiz #3

Identifying Products in Online Cybercrime Marketplaces: A Dataset for Fine-grained Domain Adaptation

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Abstract

One weakness of machine-learned NLP models is that they typically perform poorly on out-of-domain data. In this work, we study the task of identifying products being bought and sold in online cybercrime forums, which exhibits particularly challenging cross-domain effects. We formulate a task that represents a hybrid of slot-filling information extraction and named entity recognition and annotate data from four different forums. Each of these forums constitutes its own “fine-grained domain” in that the forums

TITLE: [buy] Backconnect bot

BODY: Looking for a solid backconnect bot.

If you know of anyone who codes them please let me know

(a) File 0-initiator4856

TITLE: Exploit cleaning ?

BODY: Have some Exploits i need fud .

(b) File 0-initiator10815

Figure 1: Example posts and annotations from Darkode, with annotated product tokens underlined. The second example exhibits jargon (*fud* means “fully undetectable”), nouns that could be a product in other contexts (*Exploit*), and multiple lexically-distinct descriptions of a single service.

Mini Research Proposal

- propose/explore NLP problems in GitHub dataset



<https://github.com>

GitHub Bootcamp If you are still new to things, we've provided a few walkthroughs to get you started. ✖

Set up Git
A quick guide to help you get started with Git.

Create repositories
Repositories are where you'll work and collaborate on projects.

Fork repositories
Forking creates a new, unique project from an existing one.

Be social
Send pull requests, follow friends. Star and watch projects.

Mini Research Proposal

- propose/explore NLP problems in GitHub dataset
- GitHub:
 - a social network for programmers (sharing, collaboration, bug tracking, etc.)
 - hosting Git repositories (a version control system that tracks changes to files, usually source code)
 - containing potentially interesting text fields in natural language (comments, issues, etc.)

(Recap)

what is Paraphrase?

“sentences or phrases that convey approximately the same meaning using different words” — (Bhagat & Hovy, 2012)

(Recap)

what is Paraphrase?

“sentences or phrases that convey approximately the same meaning using different words” — (Bhagat & Hovy, 2012)

wealthy

word

rich

(Recap)

what is Paraphrase?

“sentences or phrases that convey approximately the same meaning using different words” — (Bhagat & Hovy, 2012)

wealthy

word

rich

the king's speech

phrase

His Majesty's address

(Recap)

what is Paraphrase?

“sentences or phrases that convey approximately the same meaning using different words” — (Bhagat & Hovy, 2012)

wealthy

word

rich

the king's speech

phrase

His Majesty's address

*... the forced resignation
of the CEO of Boeing,
Harry Stonecipher, for ...*

sentence

*... after Boeing Co. Chief
Executive Harry Stonecipher
was ousted from ...*

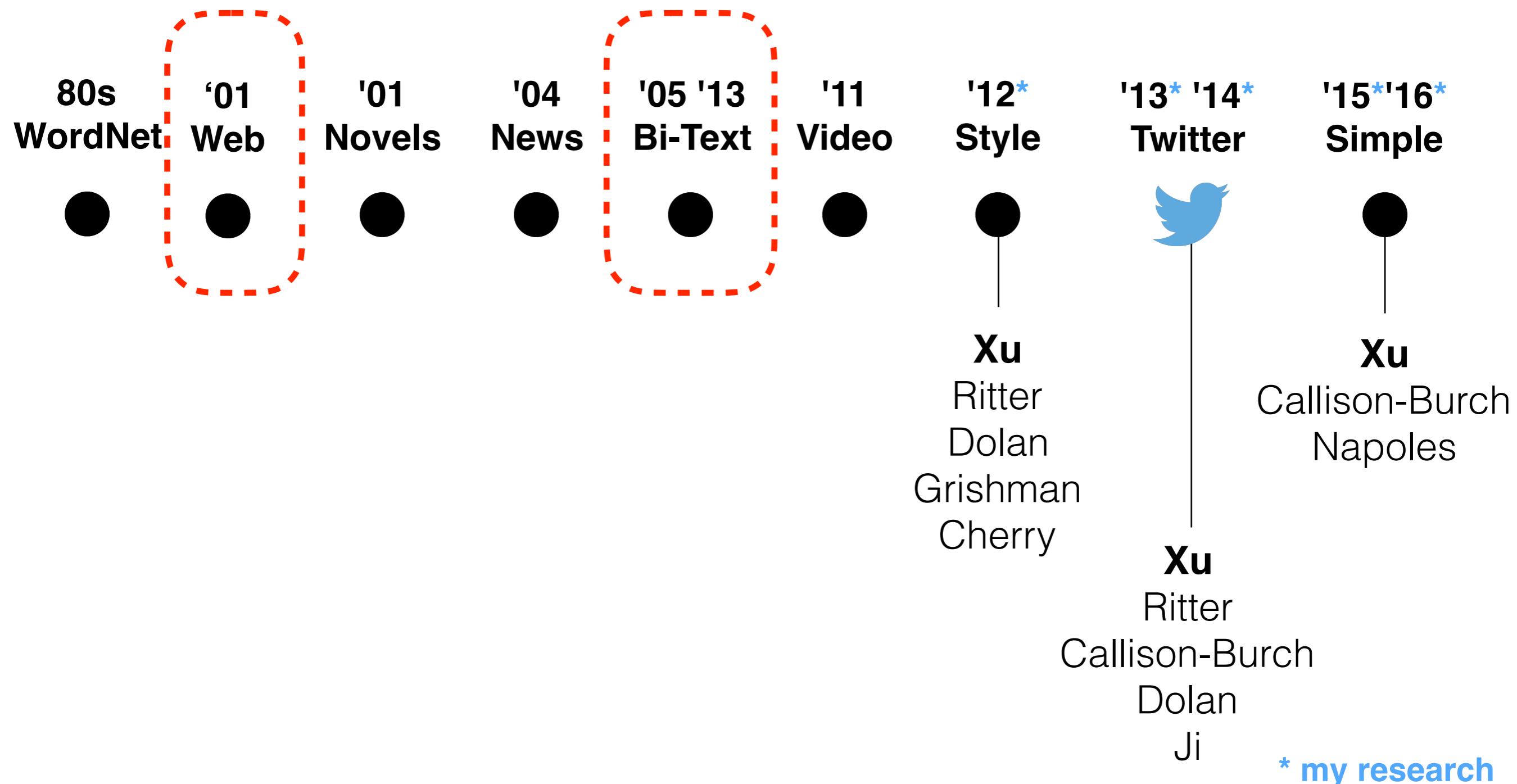
The Ideal



Translation: "You have a bruised rib."

(Recap)

Paraphrase Research



DIRT

(Discovery of Inference Rules from Text)

Lin and Pantel (2001) operationalize the Distributional Hypothesis using dependency relationships to define similar environments.

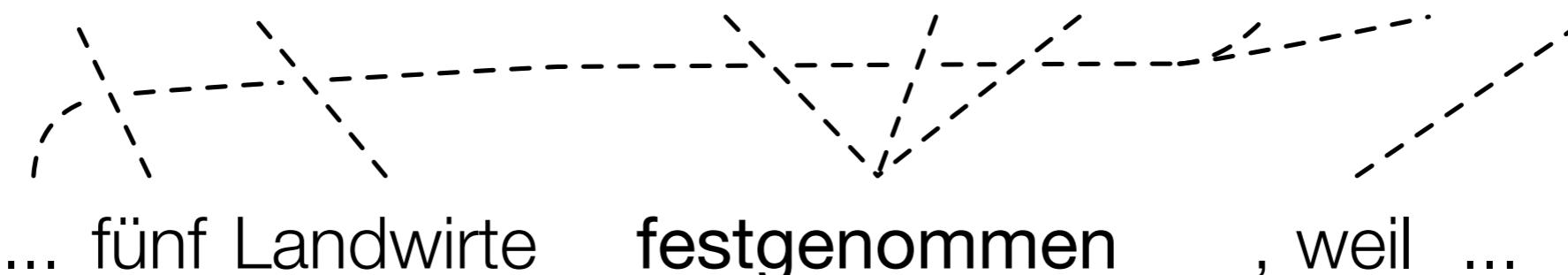
Duty and responsibility share a similar set of dependency contexts in large volumes of text:

modified by adjectives	objects of verbs
additional, administrative, assigned, assumed, collective, congressional, constitutional ...	assert, assign, assume, attend to, avoid, become, breach ...

Bilingual Pivoting

word alignment

... 5 farmers were thrown into jail in Ireland ...



Bilingual Pivoting

word alignment

... 5 farmers were thrown into jail in Ireland ...
... fünf Landwirte festgenommen , weil ...

The diagram illustrates the concept of bilingual pivoting. It shows two parallel sentences in English and German. A blue box highlights the verb 'thrown/festgenommen'. Dashed arrows point from 'thrown' to 'festgenommen' and from 'jail' to 'weil', indicating the pivot word used for alignment.

Bilingual Pivoting

word alignment

... 5 farmers were thrown into jail in Ireland ...

... fünf Landwirte , weil ...

... oder wurden , gefoltert ...

... or have been imprisoned , tortured ...

The diagram illustrates the concept of bilingual pivoting and word alignment. It shows two parallel sentences, one in English and one in German, with dashed lines connecting corresponding words. A blue box highlights the German words 'festgenommen', which are aligned with the English words 'thrown' and 'imprisoned'.

Bilingual Pivoting

word alignment

... 5 farmers were thrown into jail in Ireland ...

... fünf Landwirte festgenommen , weil ...

... oder wurden

... or have been

festgenommen

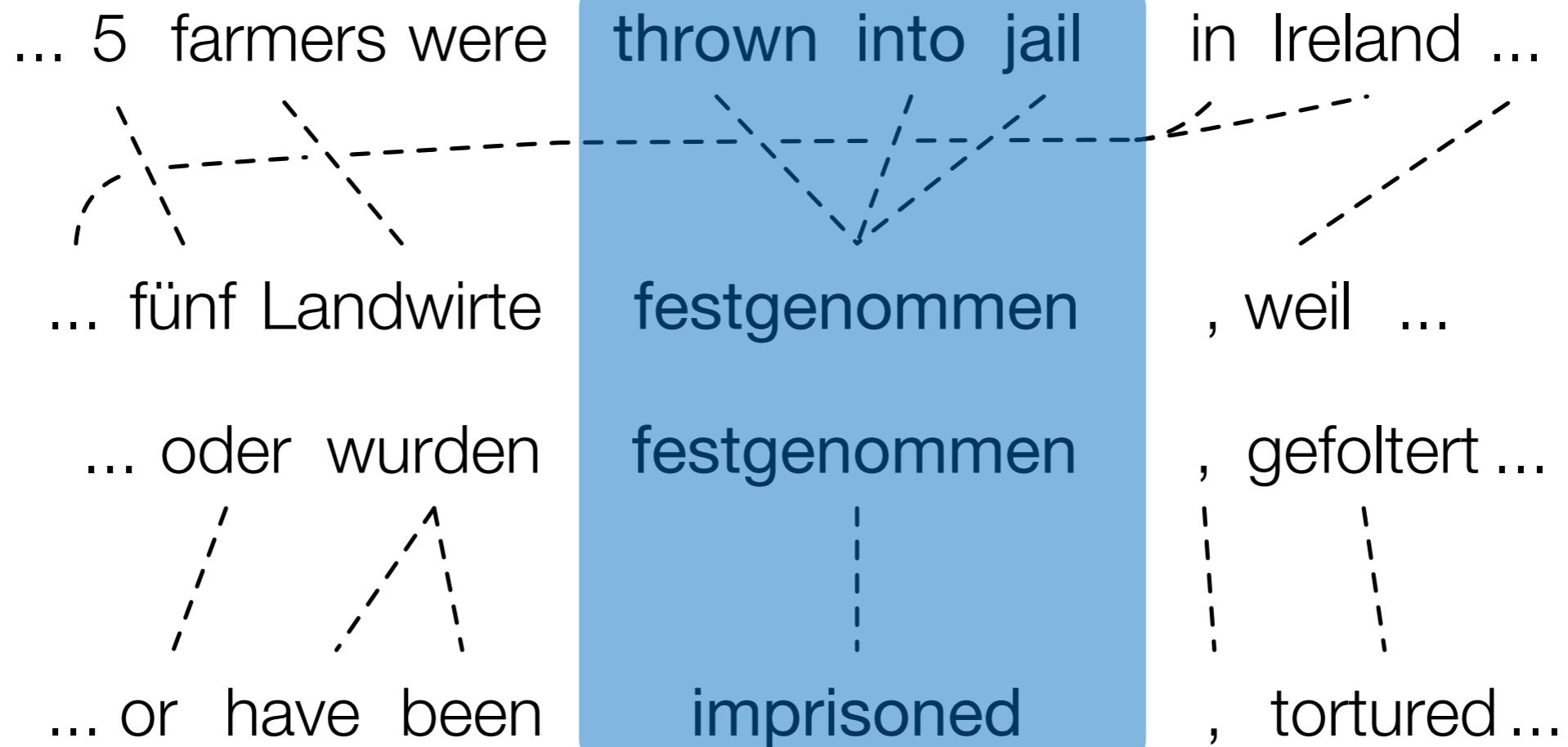
imprisoned

, gefoltert ...

, tortured ...

Bilingual Pivoting

word alignment



Quiz #2

Key Limitations of PPDB?

Quiz #2

word sense

bug

microbe, virus,
bacterium,
germ, parasite

insect, beetle,
pest, mosquito,
fly

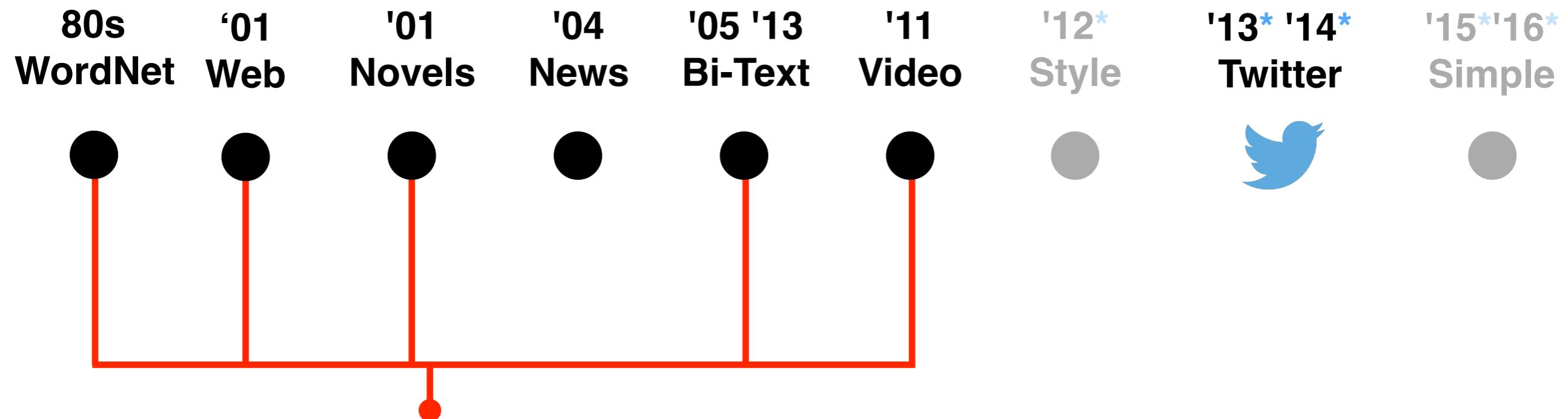
bother, annoy,
pester

microphone,
tracker, mic,
wire, earpiece,
cookie

glitch, error,
malfunction,
fault, failure

squealer, snitch,
rat, mole

Another Key Limitation



only paraphrases, no non-paraphrases

* my research

Paraphrase Identification

obtain sentential paraphrases automatically

Mancini has been sacked by Manchester City

Yes!

Mancini gets the boot from Man City

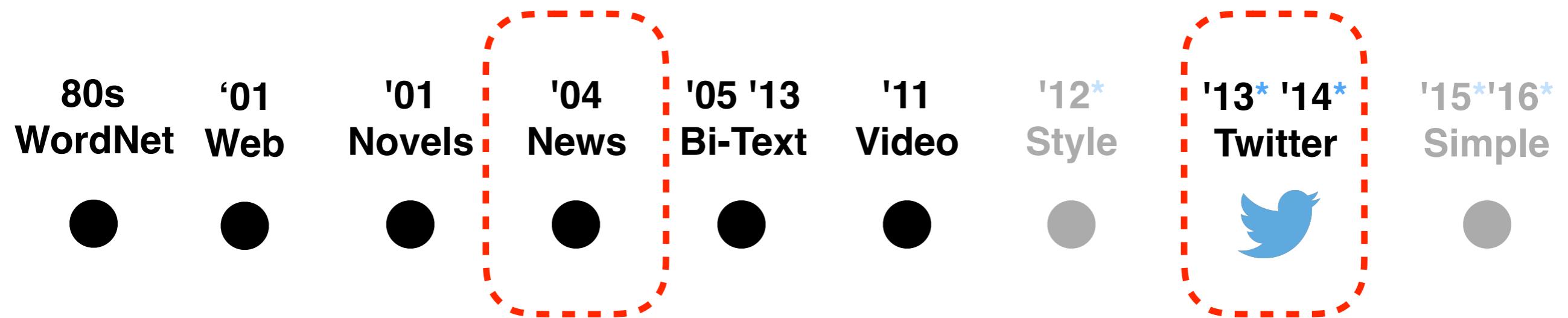
WORLD OF JENKS IS ON AT 11

No!

World of Jenks is my favorite show on tv

(meaningful) non-paraphrases are needed to train classifiers!

Also Non-Paraphrases



(meaningful) non-paraphrases are needed to train classifiers!

* my research

News Paraphrase Corpus



Microsoft Research Paraphrase Corpus

also contains some non-paraphrases

Twitter Paraphrase Corpus



Rep. Stacey Newman @staceynewman · 5h

So sad to hear today of former WH Press Sec **James Brady's passing**.
@bradybuzz & family will carry on his legacy of #gunsense.



Jim Sciutto @jimsciutto · 4h

Breaking: Fmr. WH Press Sec. **James Brady** has died at 73, crusader for gun control after wounded in '81 Reagan assassination attempt



NBC News @NBCNews · 2h

James Brady, President Reagan's press secretary shot in 1981 assassination attempt, dead at 73 nbcnews.to/WX1Btq pic.twitter.com/1ZtuEakRd9



also contains a lot of non-paraphrases

Paraphrase Identification:

A Binary Classification Problem

- Input:
 - a sentence pair \mathbf{x}
 - a fixed set of binary classes $\mathbf{Y} = \{0, 1\}$
- Output:
 - a predicted class $y \in \mathbf{Y}$ ($y = 0$ or $y = 1$)

Paraphrase Identification:

A Binary Classification Problem

- Input:
 - a sentence pair \mathbf{x}
 - a fixed set of binary classes $\mathbf{Y} = \{0, 1\}$
 - Output:
 - a predicted class $y \in \mathbf{Y}$ ($y = 0$ or $y = 1$)
- negative (non-paraphrases)**
- 

Paraphrase Identification:

A Binary Classification Problem

- Input:
 - a sentence pair \mathbf{x}
 - a fixed set of binary classes $Y = \{0, 1\}$
 - Output:
 - a predicted class $y \in Y$ ($y = 0$ or $y = 1$)
- negative (non-paraphrases)**

positive (paraphrases)

Paraphrase Identification:

A Binary Classification Problem

- Input:
 - a sentence pair \mathbf{x}
 - a fixed set of binary classes $\mathbf{Y} = \{0, 1\}$
- Output:
 - a predicted class $y \in \mathbf{Y}$ ($y = 0$ or $y = 1$)

Classification Method:

Supervised Machine Learning

- Input:
 - a sentence pair \mathbf{x}
 - a fixed set of binary classes $\mathbf{Y} = \{0, 1\}$
 - a training set of m hand-labeled sentence pairs
 $(\mathbf{x}^{(1)}, \mathbf{y}^{(1)}), \dots, (\mathbf{x}^{(m)}, \mathbf{y}^{(m)})$
- Output:
 - a learned classifier $\gamma: \mathbf{x} \rightarrow \mathbf{y} \in \mathbf{Y}$ ($\mathbf{y} = 0$ or $\mathbf{y} = 1$)

Classification Method:

Supervised Machine Learning

- Input:
 - a sentence pair **x (represented by features)**
 - a fixed set of binary classes **$Y = \{0, 1\}$**
 - a training set of **m** hand-labeled sentence pairs
 $(x^{(1)}, y^{(1)}), \dots, (x^{(m)}, y^{(m)})$
- Output:
 - a learned classifier **$\gamma: x \rightarrow y \in Y$ ($y = 0$ or $y = 1$)**

(Recap Week #3) Classification Method: Supervised Machine Learning

- **Naïve Bayes**
- Logistic Regression
- Support Vector Machines (SVM)
- ...

(Recap Week#3)

Naïve Bayes

- ***Cons:***

features t_i are assumed independent given the class y

$$P(t_1, t_2, \dots, t_n | y) = P(t_1 | y) \cdot P(t_2 | y) \cdot \dots \cdot P(t_n | y)$$

- ***This will cause problems:***

- correlated features → double-counted evidence
- while parameters are estimated independently
- hurt classifier's accuracy

Classification Method: Supervised Machine Learning

- Naïve Bayes
- **Logistic Regression**
- Support Vector Machines (SVM)
- ...

Logistic Regression

- One of the most useful **supervised machine learning algorithm** for classification!
- Generally high performance for a lot of problems.
- Much more robust than Naïve Bayes (better performance on various datasets).

Before Logistic Regression

**Let's start with
something simpler!**

Paraphrase Identification: Simplified Features

- We use only one feature:
 - number of words that two sentence shared in common

A very related problem of Paraphrase Identification:
Semantic Textual Similarity

- How similar (close in meaning) two sentences are?

5: completely equivalent in meaning

4: mostly equivalent, but some unimportant details differ

3: roughly equivalent, some important information differs/missing

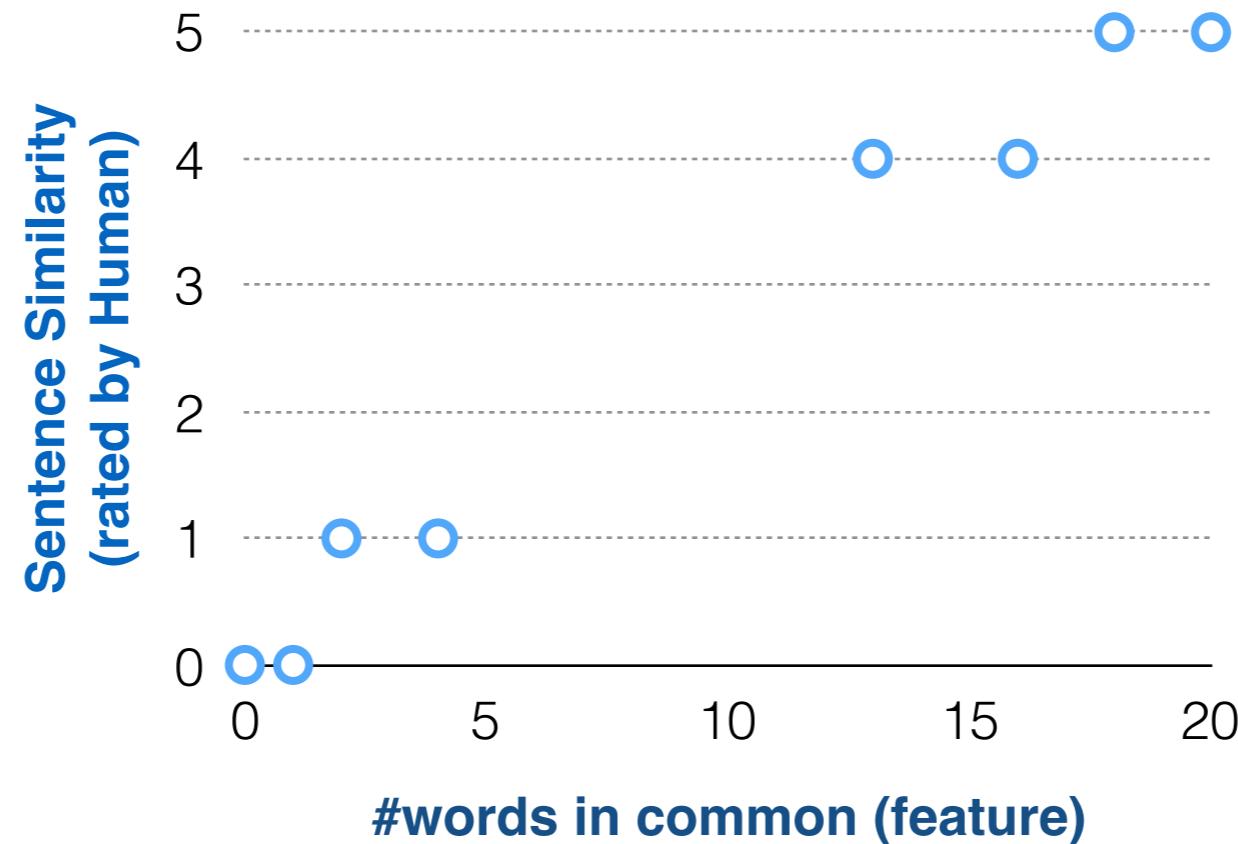
2: not equivalent, but share some details

1: not equivalent, but are on the same topic

0: completely dissimilar

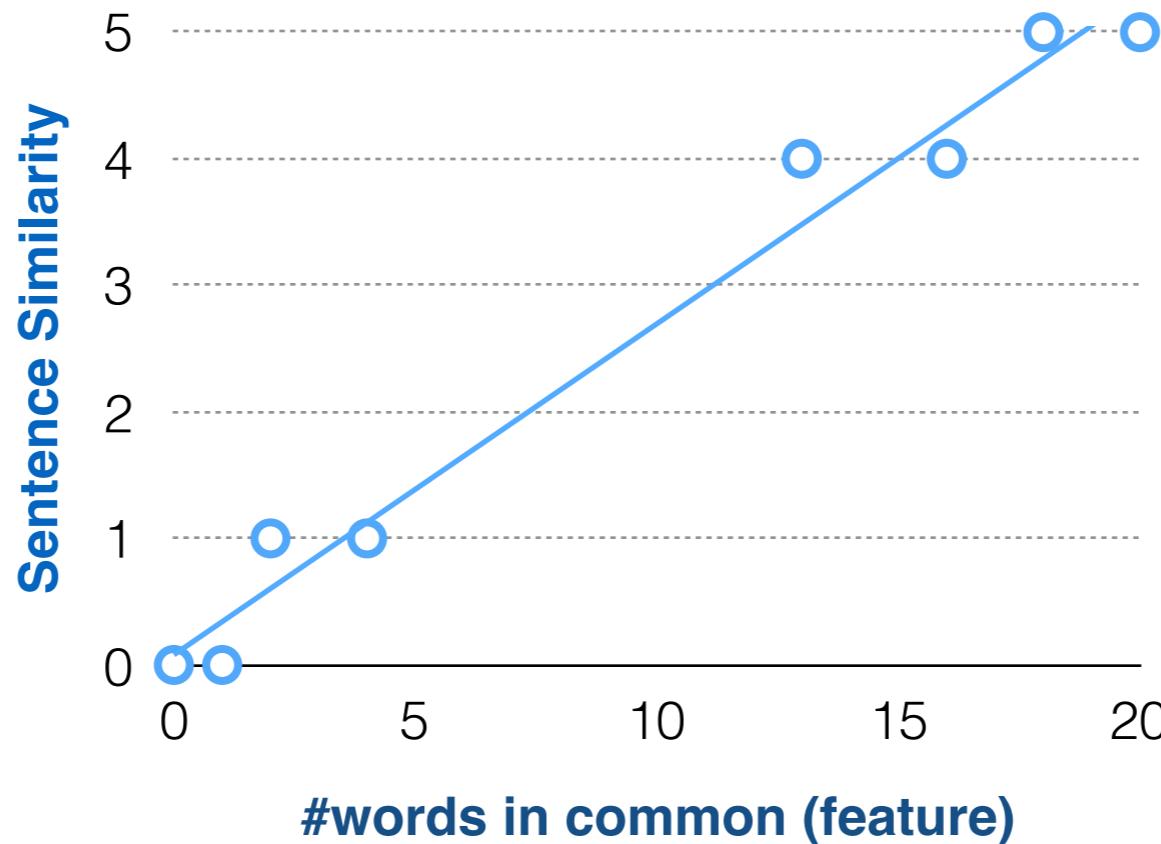
A Simpler Model:

Linear Regression



A Simpler Model:

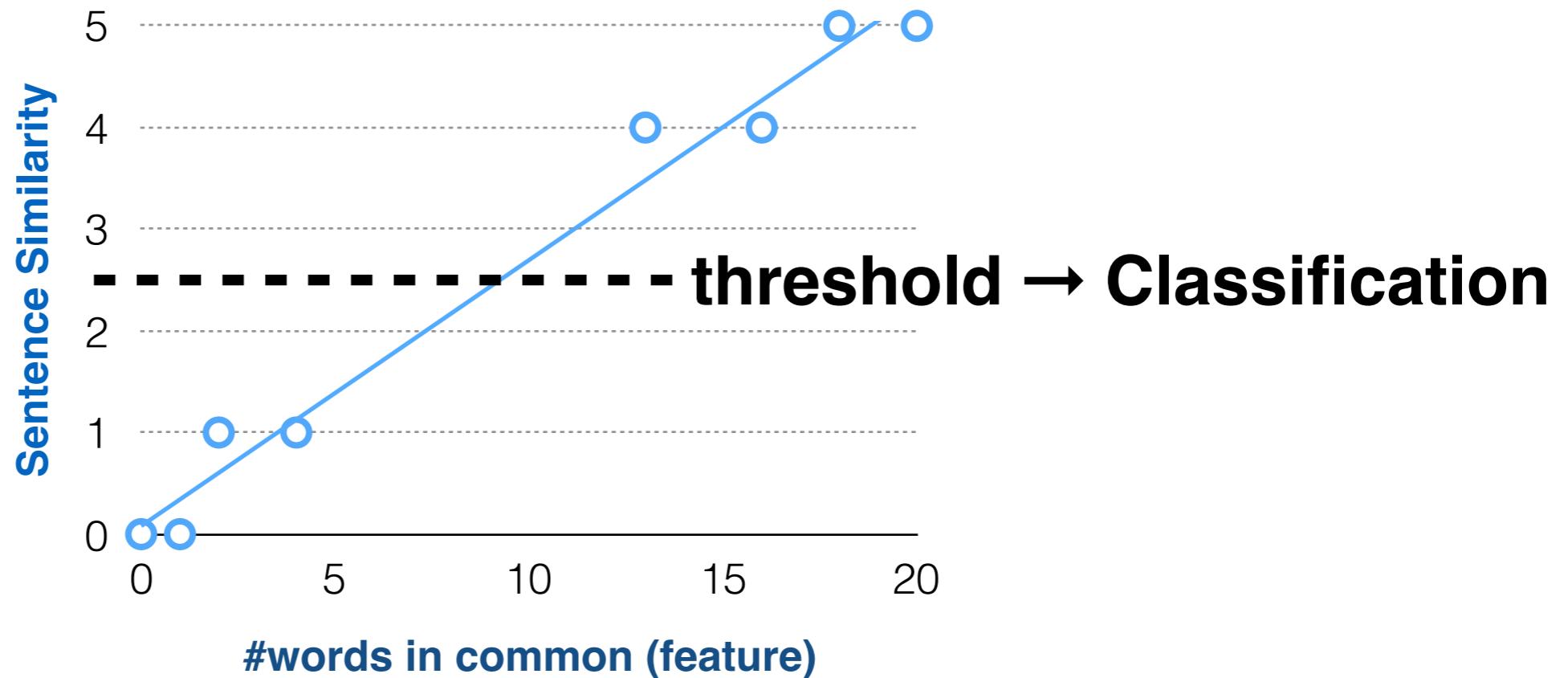
Linear Regression



- also supervised learning (learn from annotated data)
- but for **Regression**: predict **real-valued** output
(Classification: predict discrete-valued output)

A Simpler Model:

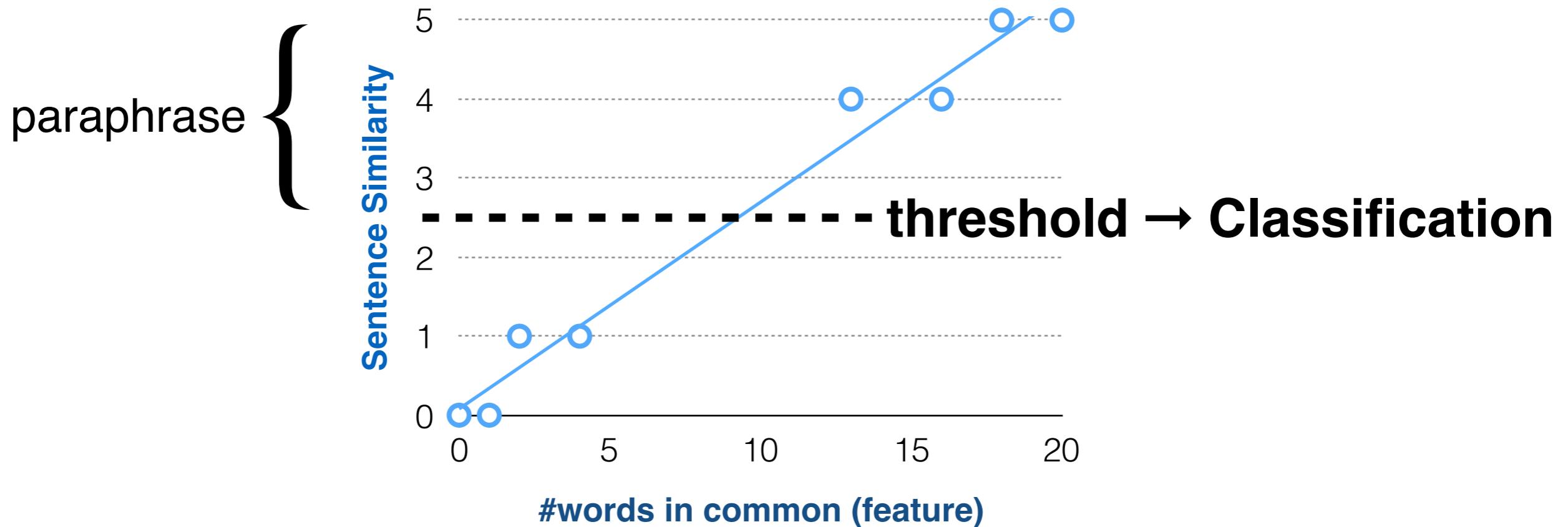
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A Simpler Model:

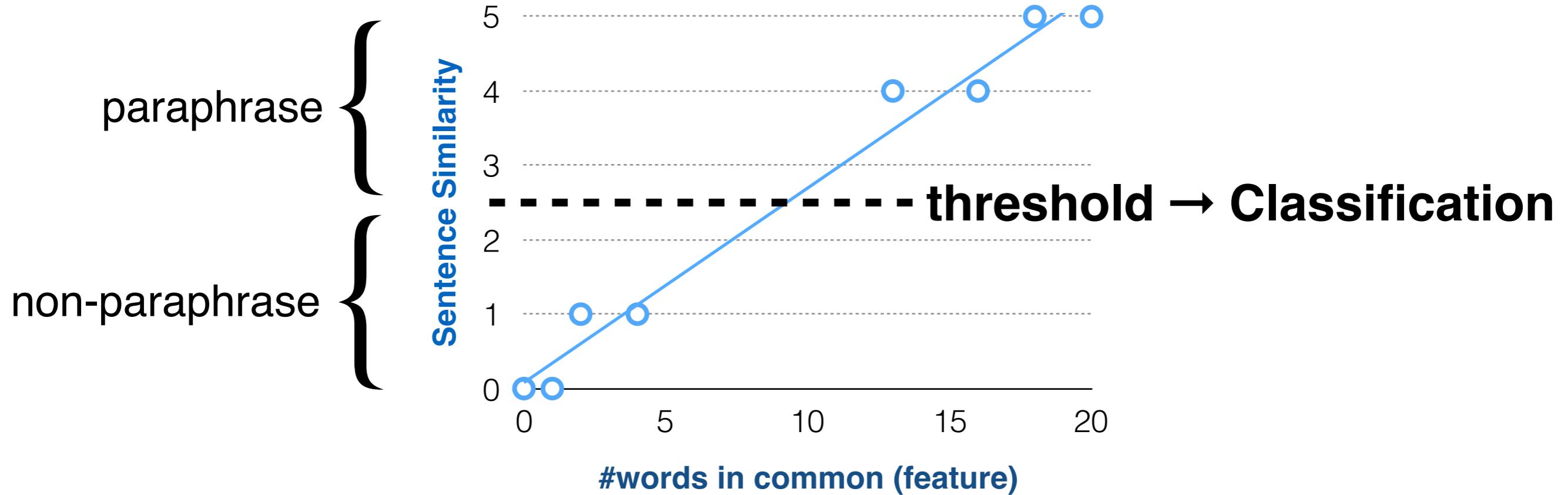
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A Simpler Model:

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- but for **Regression**: predict **real-valued** output
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Training Set

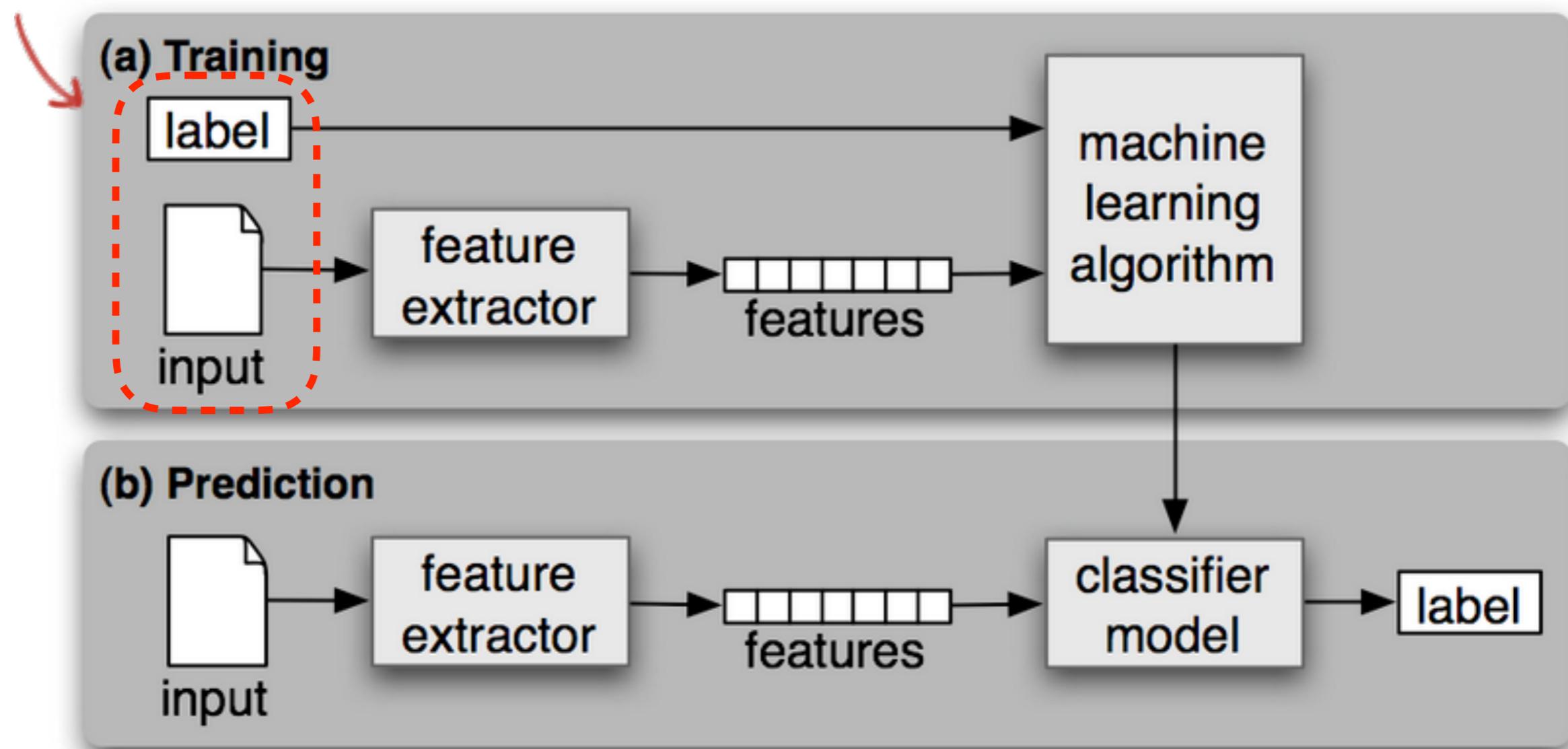
#words in common (x)	Sentence Similarity (y)
1	0
4	1
13	4
18	5
...	...

- m hand-labeled sentence pairs $(x^{(1)}, y^{(1)}), \dots, (x^{(m)}, y^{(m)})$
- x 's: “input” variable / features
- y 's: “output”/“target” variable

(Recap Week#3)

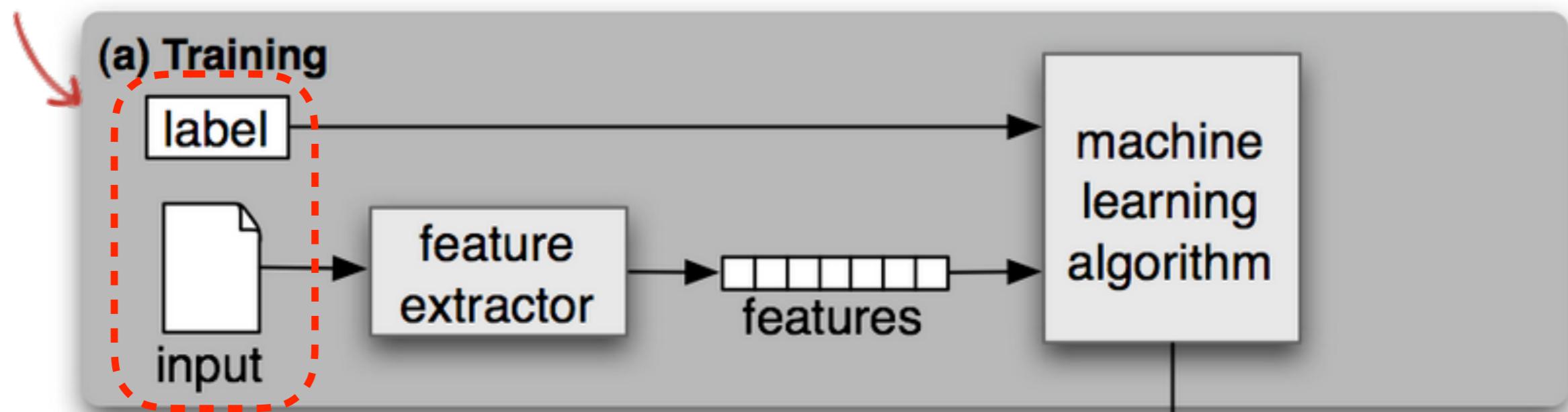
Supervised Machine Learning

training set

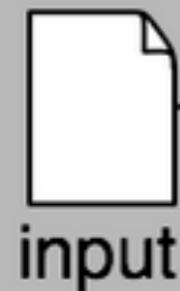


Supervised Machine Learning

training set



(b) Prediction



feature extractor

features

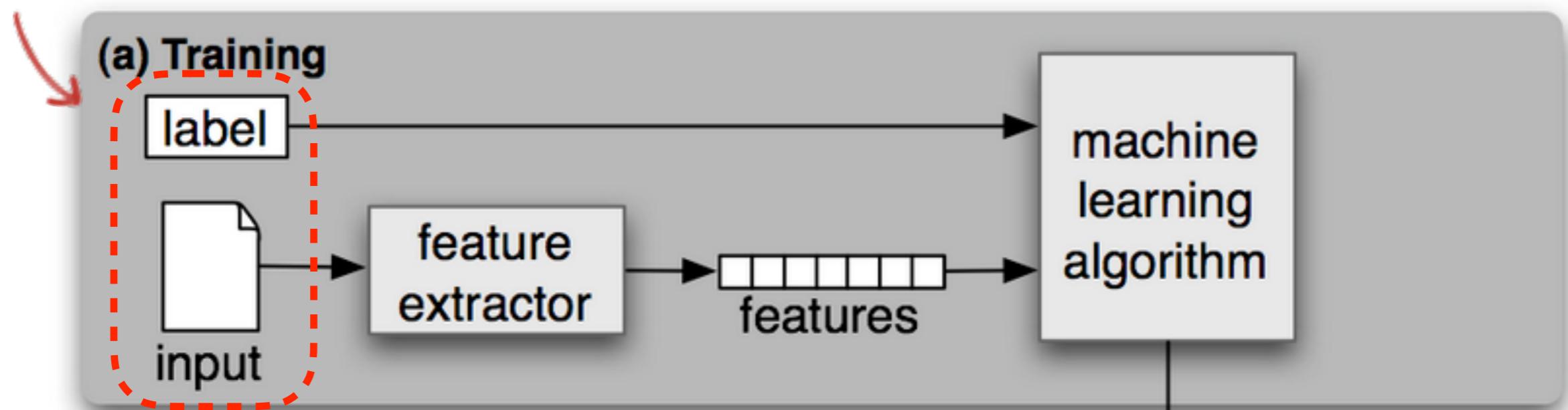
classifier model

label

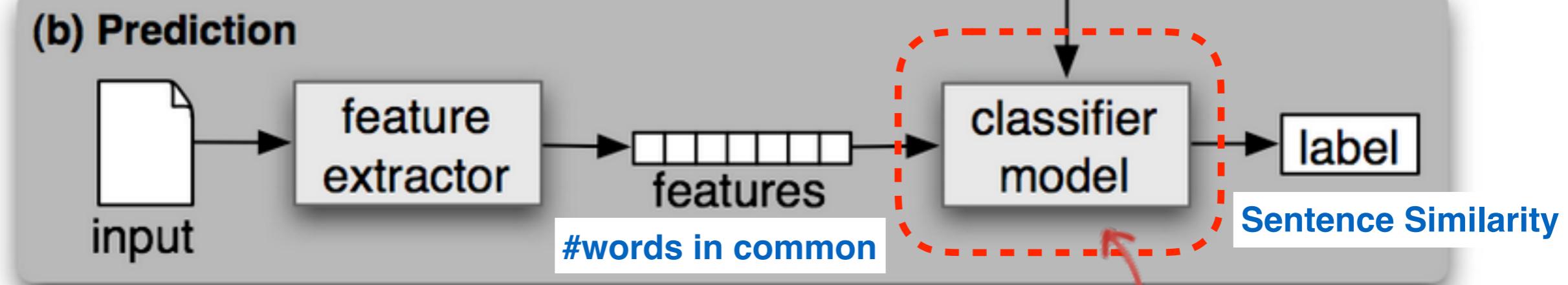
(also called) hypothesis

Supervised Machine Learning

training set



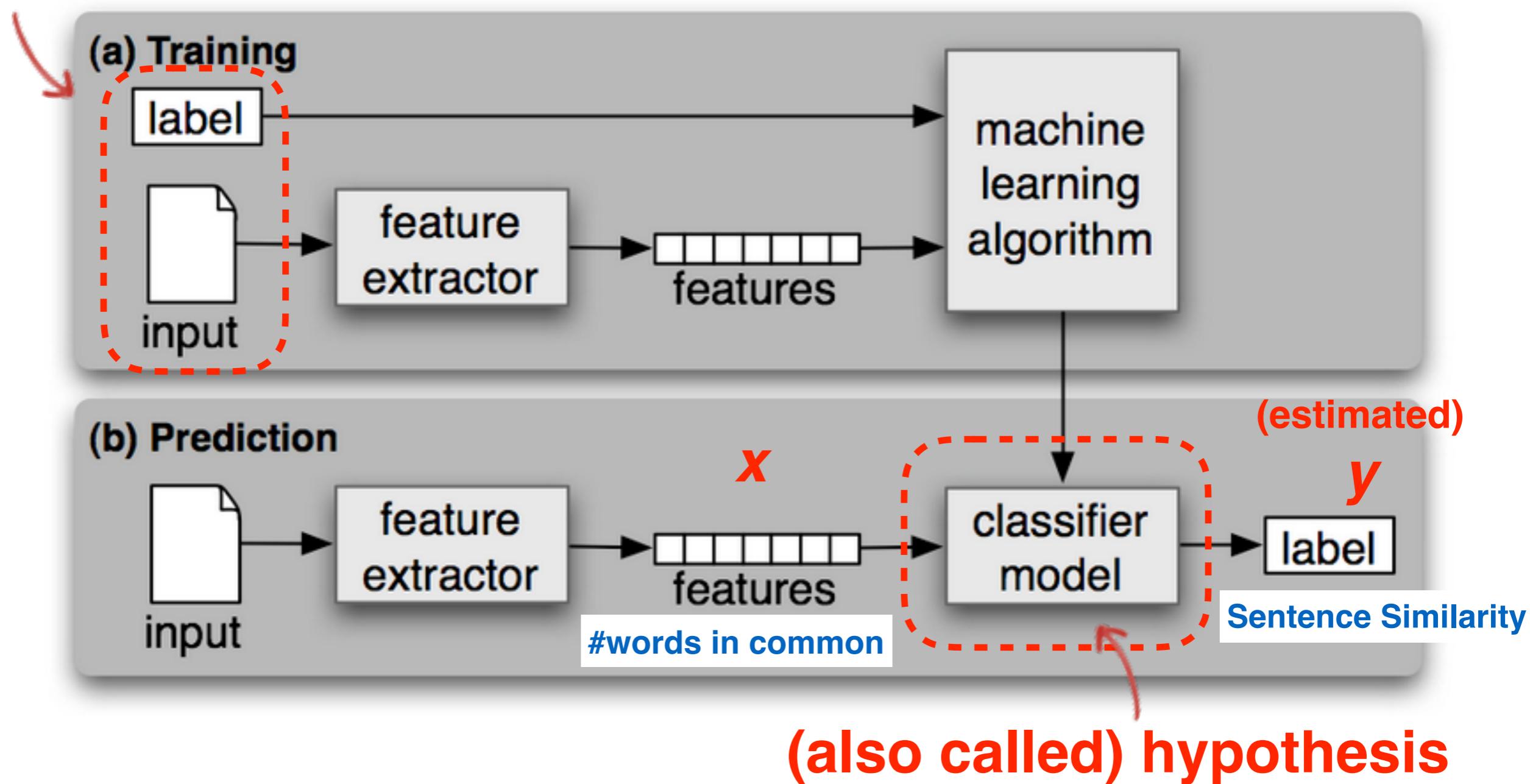
(b) Prediction



(also called) hypothesis

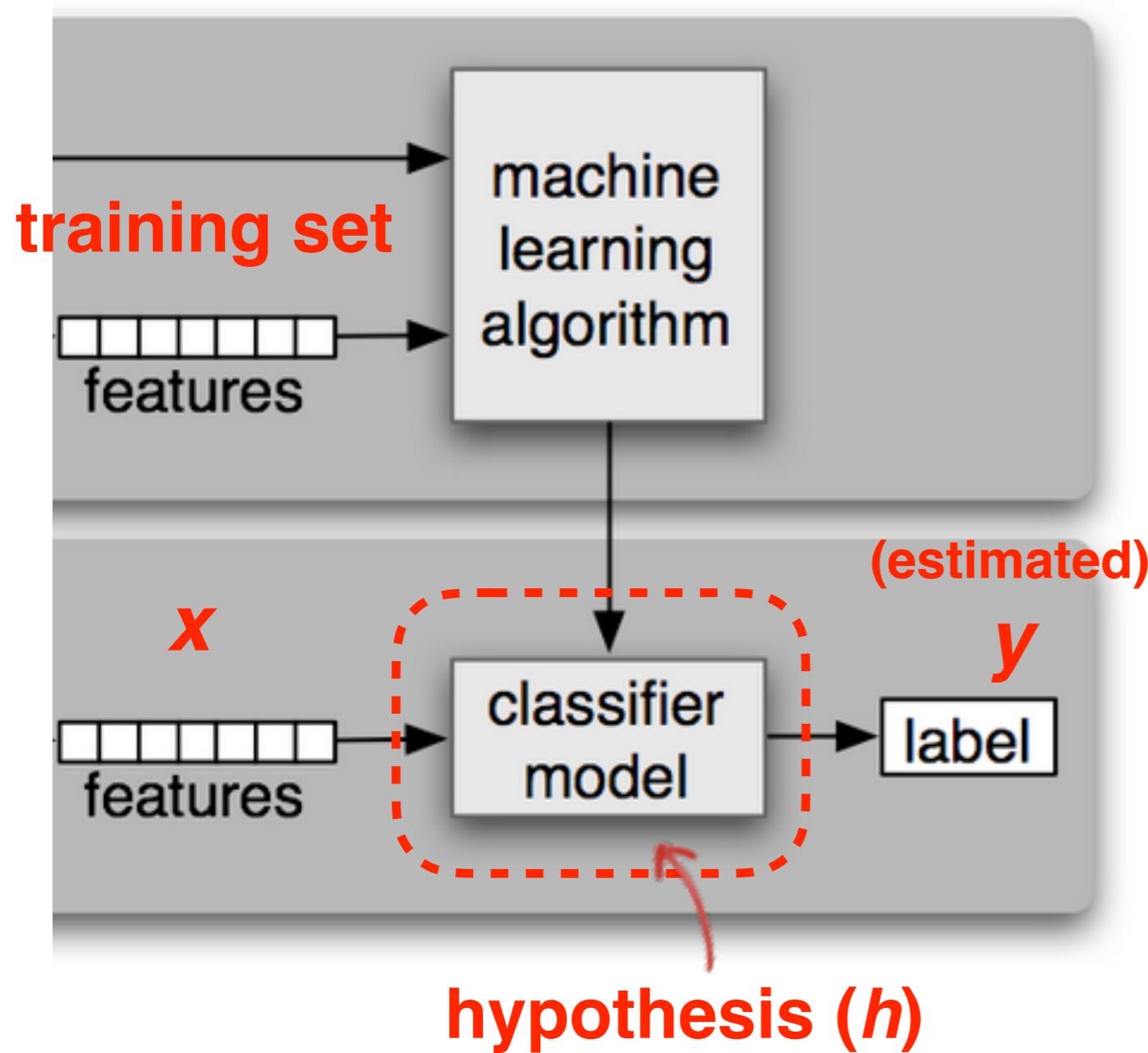
Supervised Machine Learning

training set



Linear Regression: Model Representation

- How to represent h ?



$$h_{\theta}(x) = \theta_0 + \theta_1 x$$

Linear Regression
w/ one variable

Linear Regression w/ one variable: Model Representation

#words in common (x)	Sentence Similarity (y)
1	0
4	1
13	4
18	5
...	...

$$h_{\theta}(x) = \theta_0 + \theta_1 x$$

- m hand-labeled sentence pairs $(\mathbf{x}^{(1)}, \mathbf{y}^{(1)}), \dots, (\mathbf{x}^{(m)}, \mathbf{y}^{(m)})$
- θ 's: parameters

Linear Regression w/ one variable: Model Representation

#words in common (x)	Sentence Similarity (y)
1	0
4	1
13	4
18	5
...	...

$$h_{\theta}(x) = \theta_0 + \theta_1 x$$

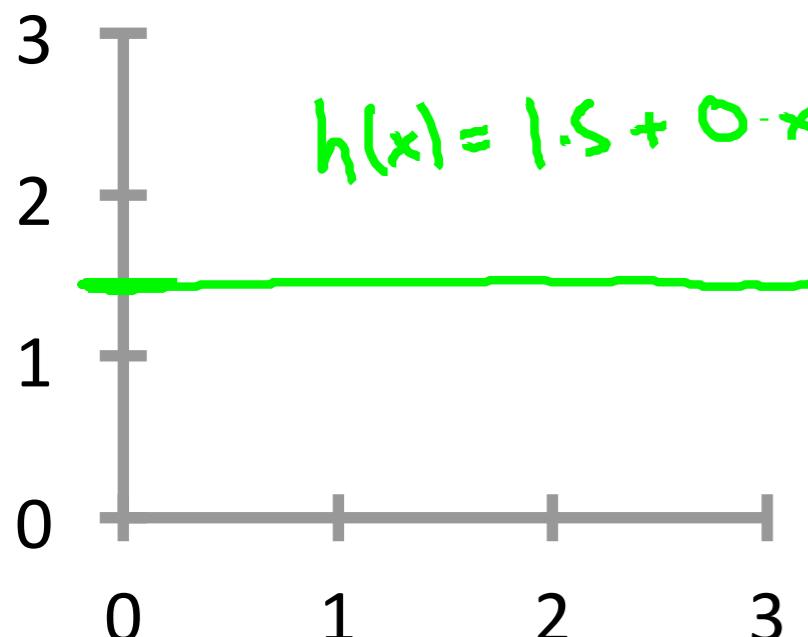
- m hand-labeled sentence pairs $(x^{(1)}, y^{(1)}), \dots, (x^{(m)}, y^{(m)})$
- θ 's: parameters



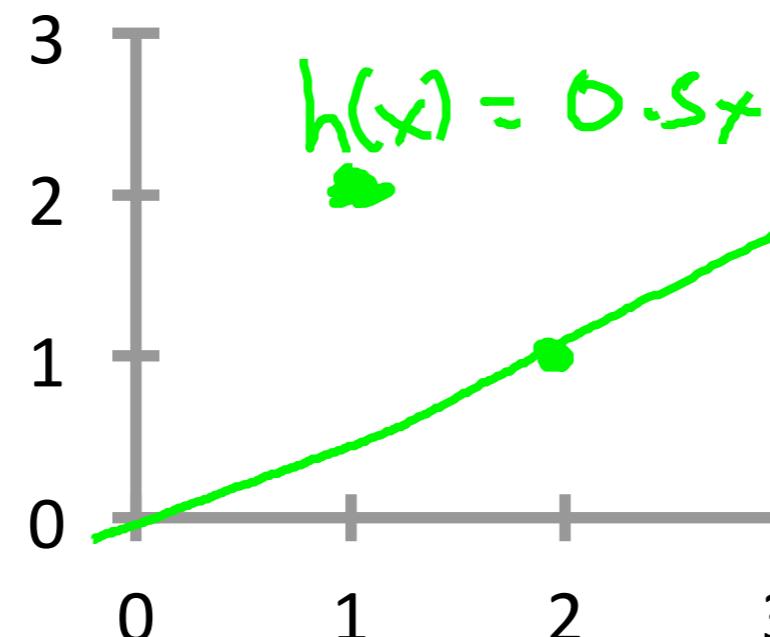
How to choose θ ?

Linear Regression w/ one variable:: Model Representation

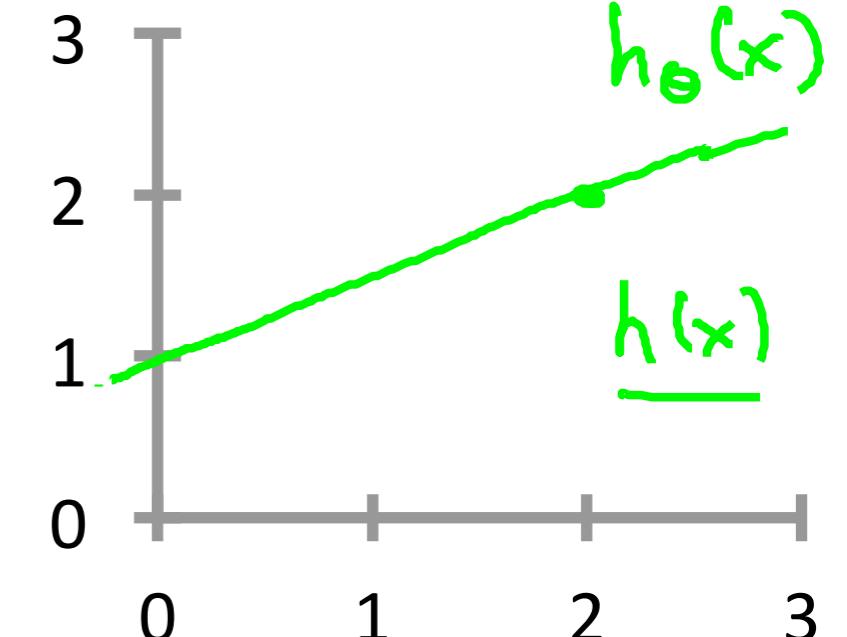
$$\underline{h_{\theta}(x) = \theta_0 + \theta_1 x}$$



$$\begin{aligned} \rightarrow \theta_0 &= 1.5 \\ \rightarrow \theta_1 &= 0 \end{aligned}$$

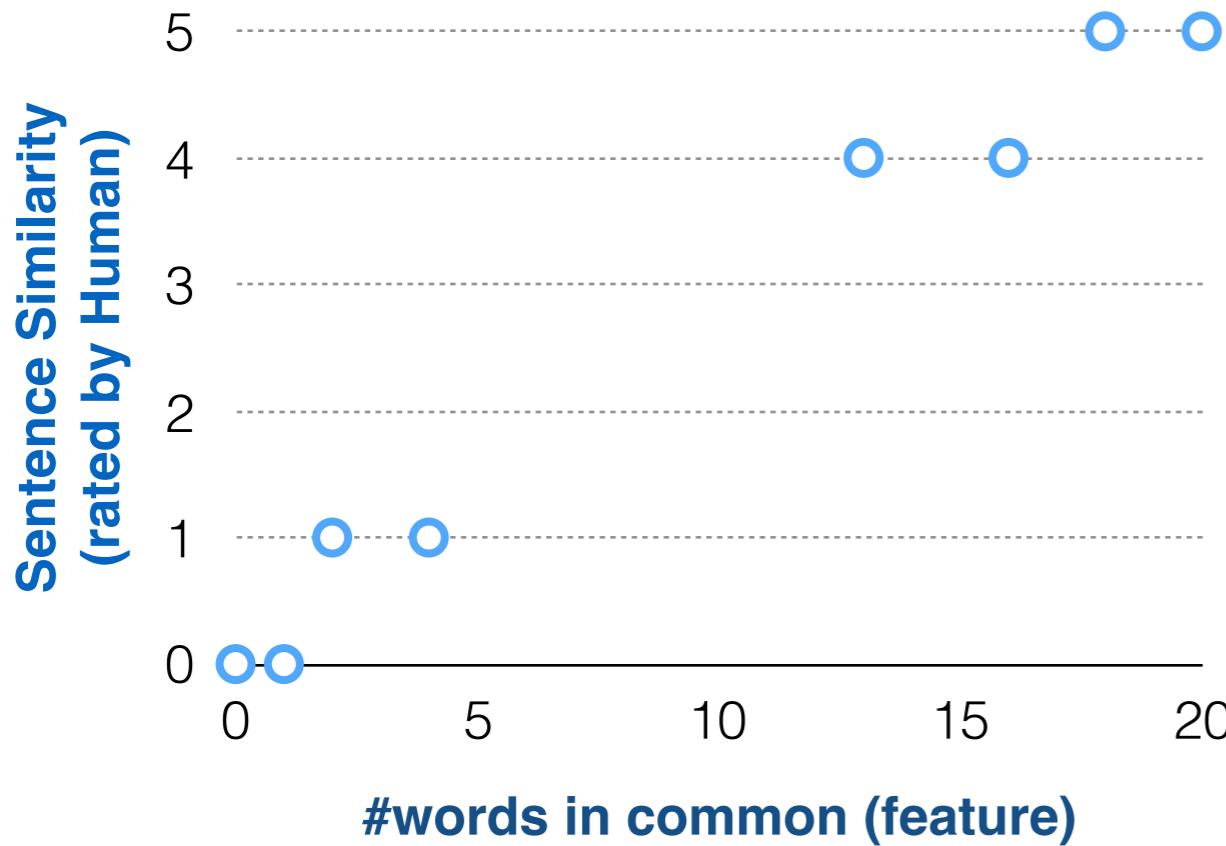


$$\begin{aligned} \rightarrow \theta_0 &= 0 \\ \rightarrow \theta_1 &= 0.5 \end{aligned}$$



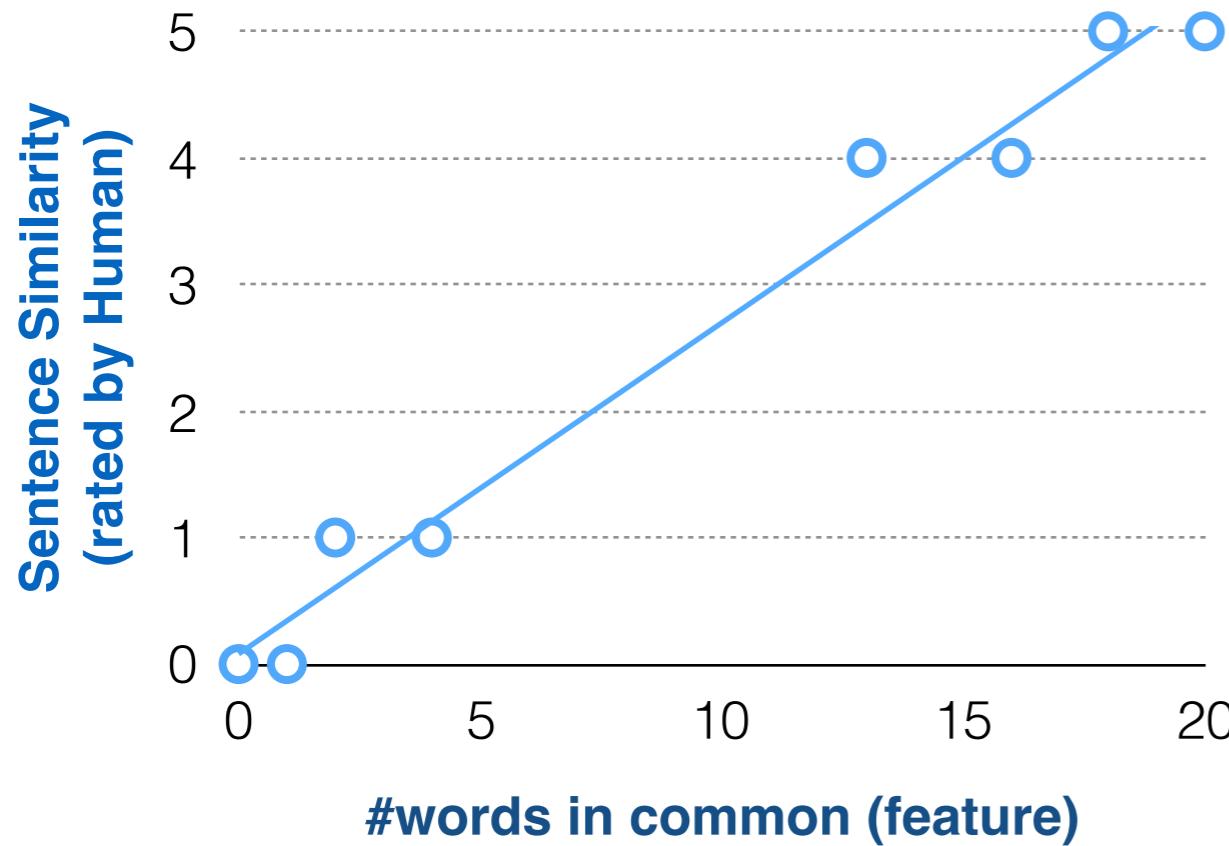
$$\begin{aligned} \rightarrow \theta_0 &= 1 \\ \rightarrow \theta_1 &= 0.5 \end{aligned}$$

Linear Regression w/ one variable: Cost Function



- **Idea:** choose θ_0, θ_1 so that $h_\theta(x)$ is close to y for training examples (x, y)

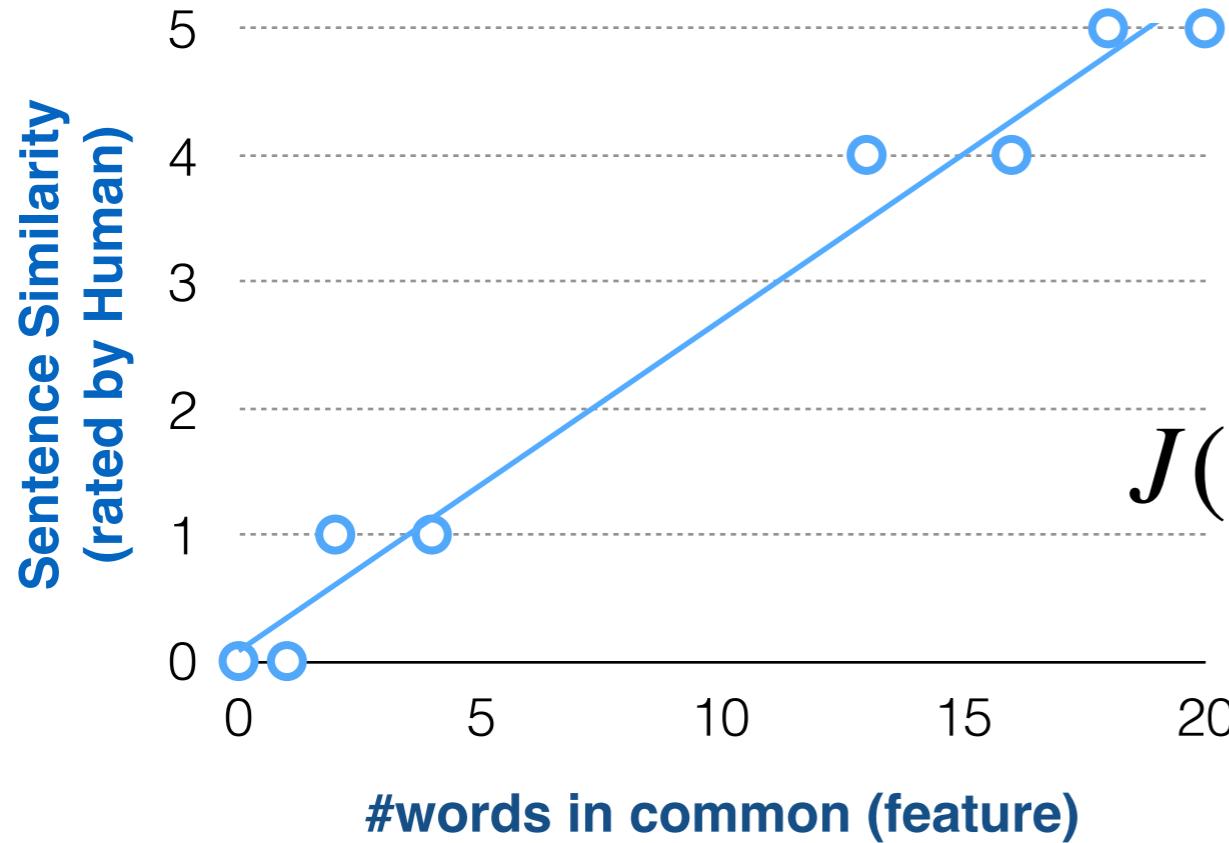
Linear Regression w/ one variable: Cost Function



- **Idea:** choose θ_0, θ_1 so that $h_\theta(x)$ is close to y for training examples (x, y)

Linear Regression w/ one variable:

Cost Function



squared error function:

$$J(\theta_0, \theta_1) = \frac{1}{2m} \sum_{i=1}^m (h_{\theta}(x^{(i)}) - y^{(i)})^2$$

- **Idea:** choose θ_0, θ_1 so that $h_{\theta}(x)$ is close to y for training examples (x, y)

$$\underset{\theta_0, \theta_1}{\text{minimize}} J(\theta_0, \theta_1)$$

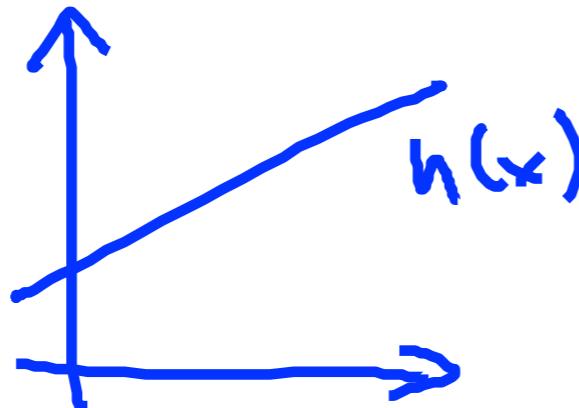
Linear Regression

- **Hypothesis:**

$$h_{\theta}(x) = \theta_0 + \theta_1 x$$

- **Parameters:**

$$\theta_0, \theta_1$$



- **Cost Function:**

$$J(\theta_0, \theta_1) = \frac{1}{2m} \sum_{i=1}^m (h_{\theta}(x^{(i)}) - y^{(i)})^2$$

- **Goal:** $\underset{\theta_0, \theta_1}{\text{minimize}} J(\theta_0, \theta_1)$

Linear Regression

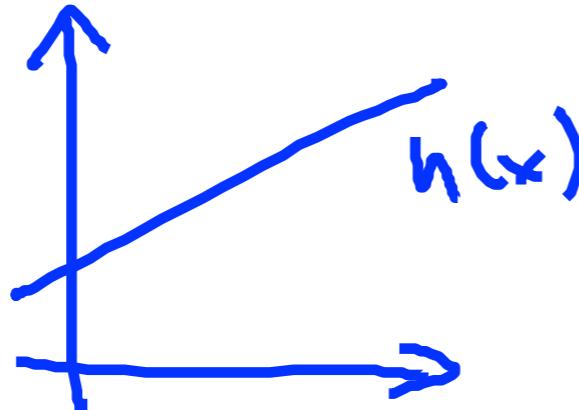
Simplified

- Hypothesis:

$$h_{\theta}(x) = \theta_0 + \theta_1 x$$

- Parameters:

$$\theta_0, \theta_1$$

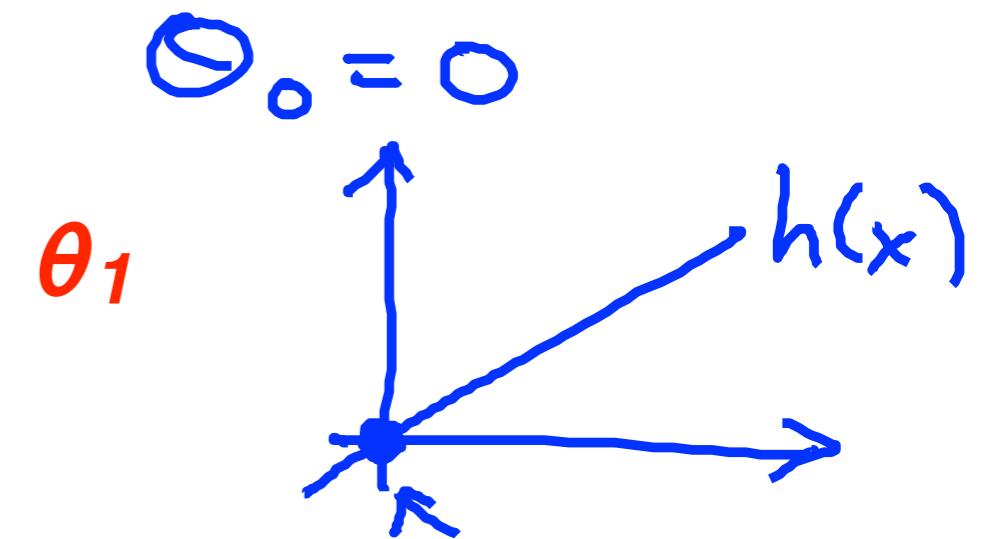


- Cost Function:

$$J(\theta_0, \theta_1) = \frac{1}{2m} \sum_{i=1}^m (h_{\theta}(x^{(i)}) - y^{(i)})^2$$

- Goal: $\underset{\theta_0, \theta_1}{\text{minimize}} J(\theta_0, \theta_1)$

$$h_{\theta}(x) = \theta_1 x$$

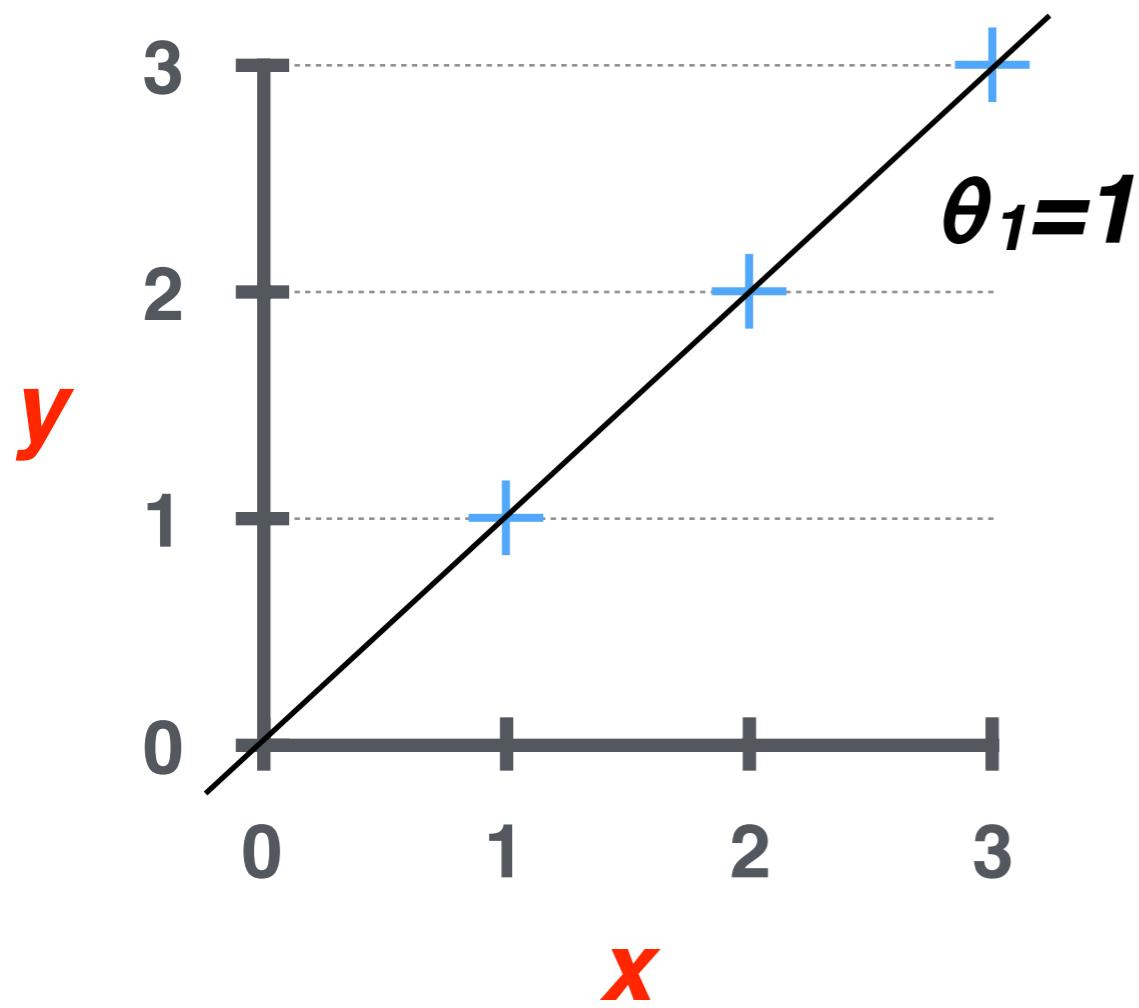


$$J(\theta_1) = \frac{1}{2m} \sum_{i=1}^m (h_{\theta}(x^{(i)}) - y^{(i)})^2$$

$$\underset{\theta_1}{\text{minimize}} J(\theta_1)$$

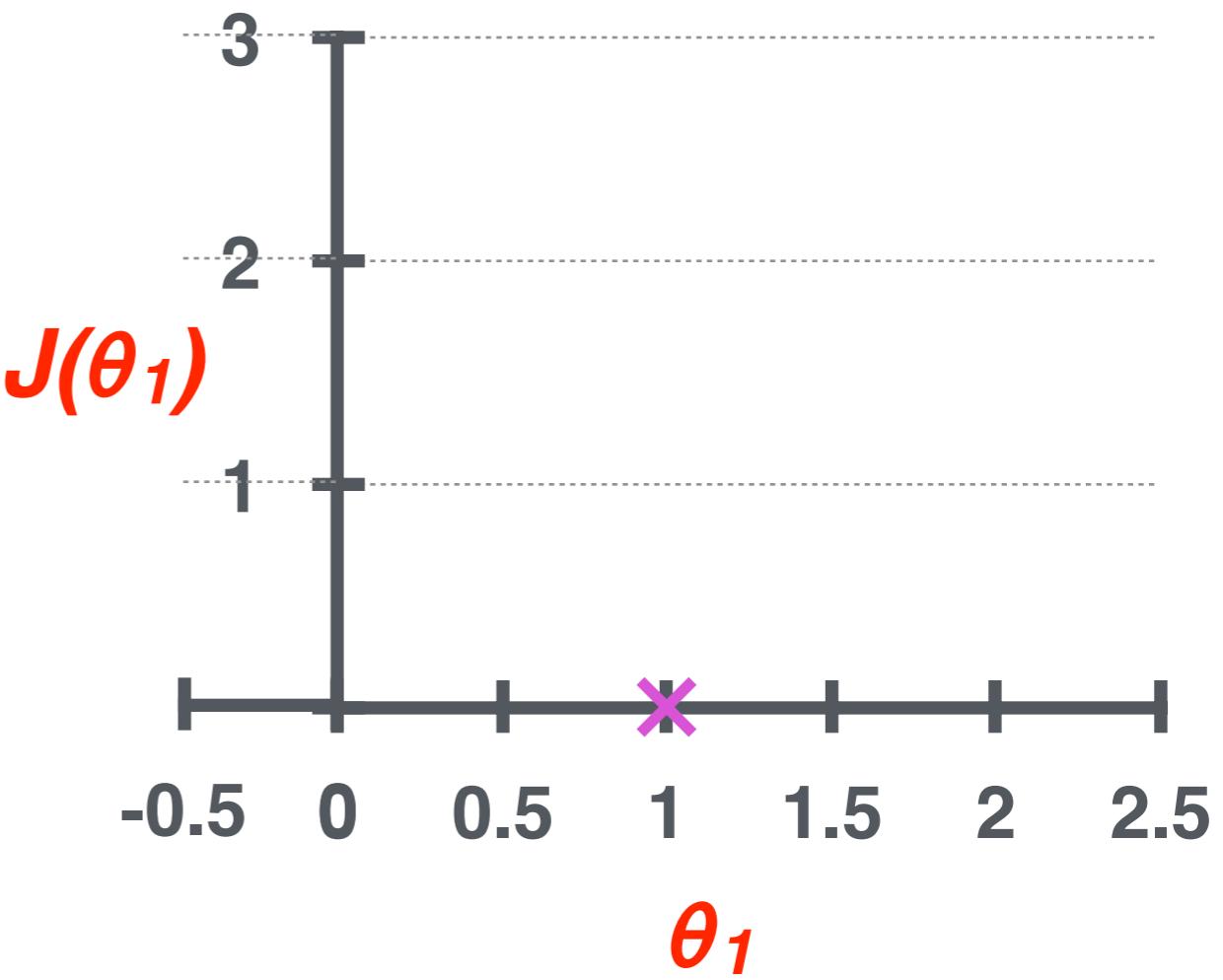
$h_{\theta}(x)$

(for fixed θ_1 , this is a function of x)



$J(\theta_1)$

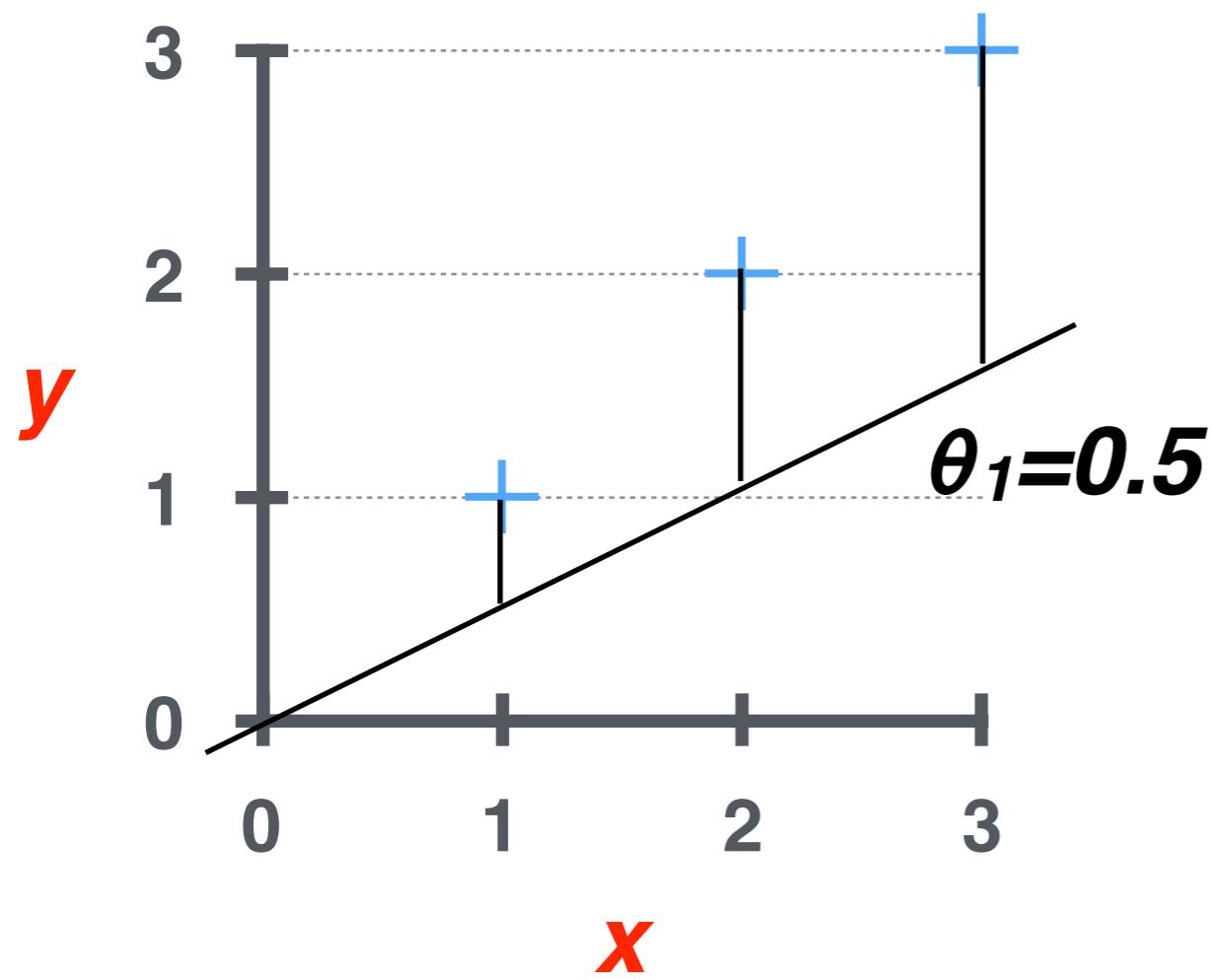
(function of the parameter θ_1)



$$J(1) = \frac{1}{2 \times 3} [(1-1)^2 + (2-2)^2 + (3-3)^2] = 0$$

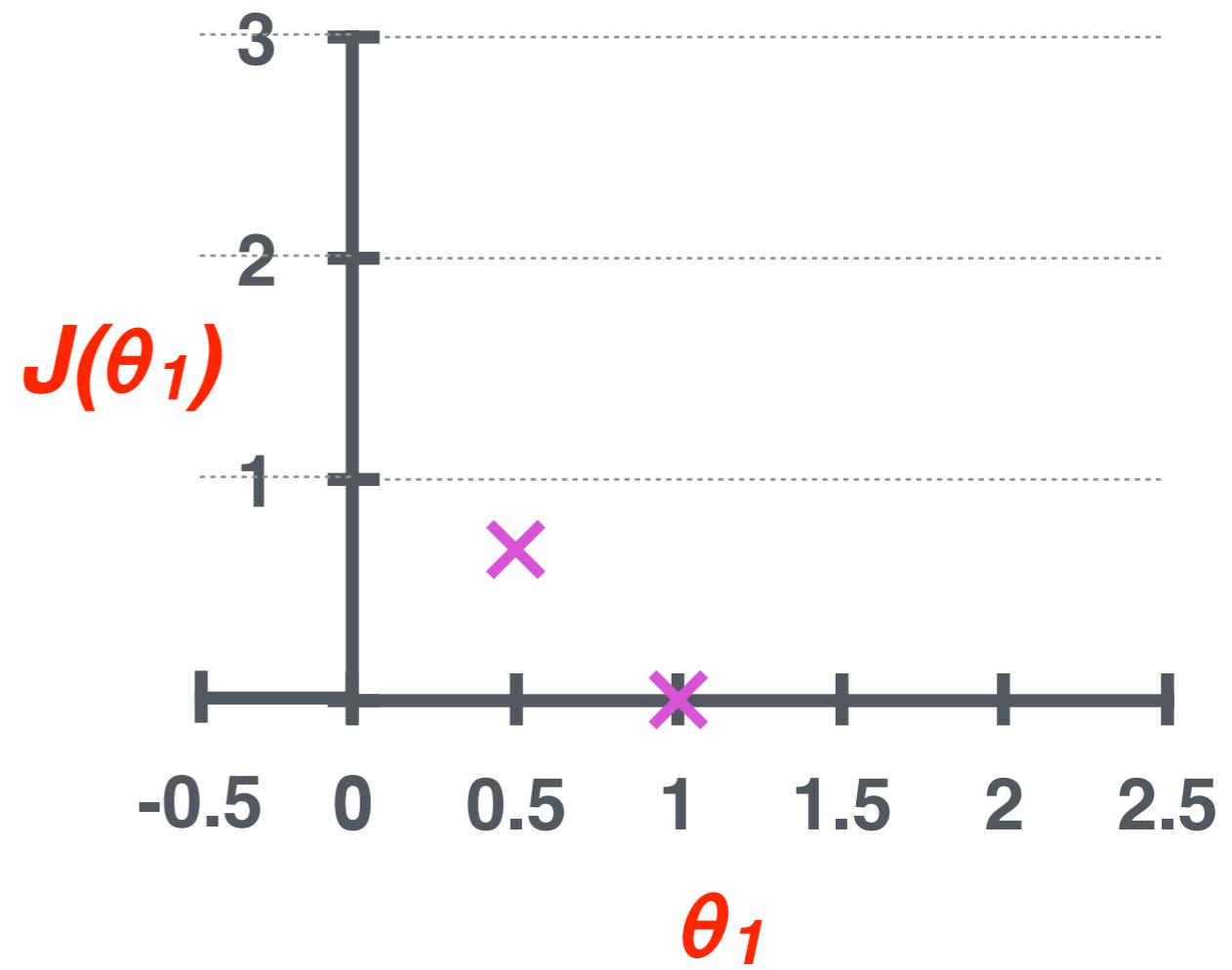
$h_{\theta}(x)$

(for fixed θ_1 , this is a function of x)



$J(\theta_1)$

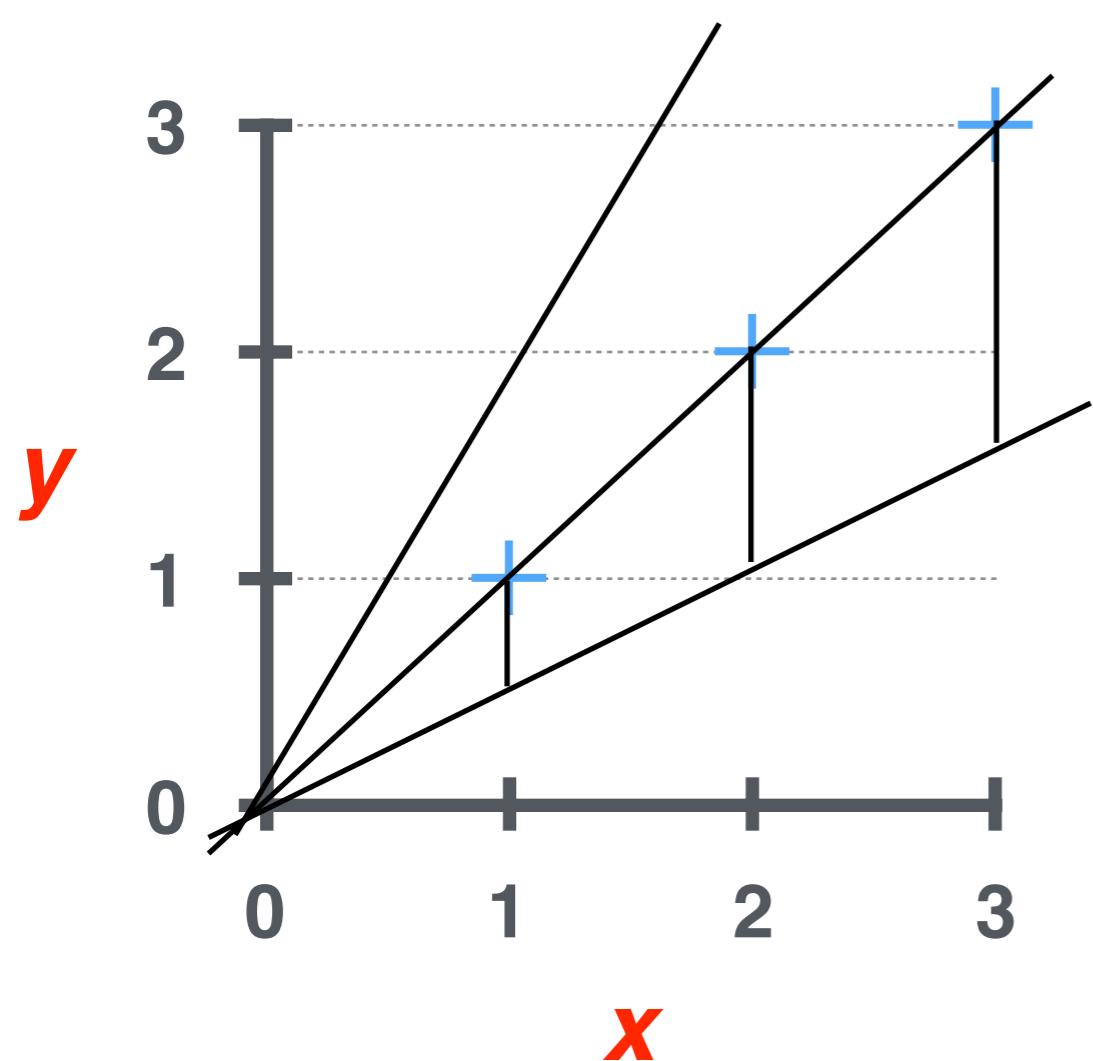
(function of the parameter θ_1)



$$J(1) = \frac{1}{2 \times 3} [(0.5 - 1)^2 + (1 - 2)^2 + (1.5 - 3)^2] = 0.68$$

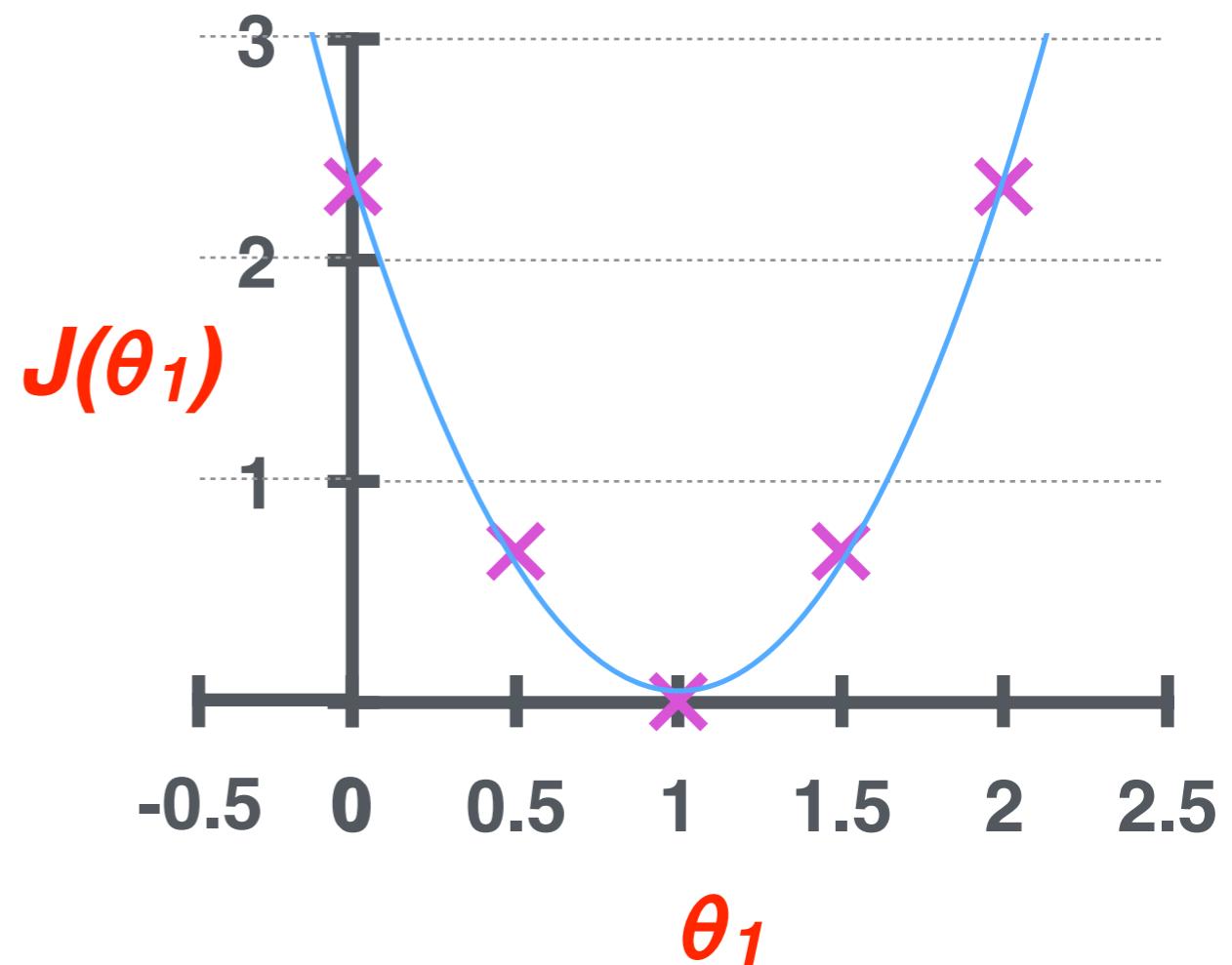
$h_{\theta}(x)$

(for fixed θ_1 , this is a function of x)



$J(\theta_1)$

(function of the parameter θ_1)



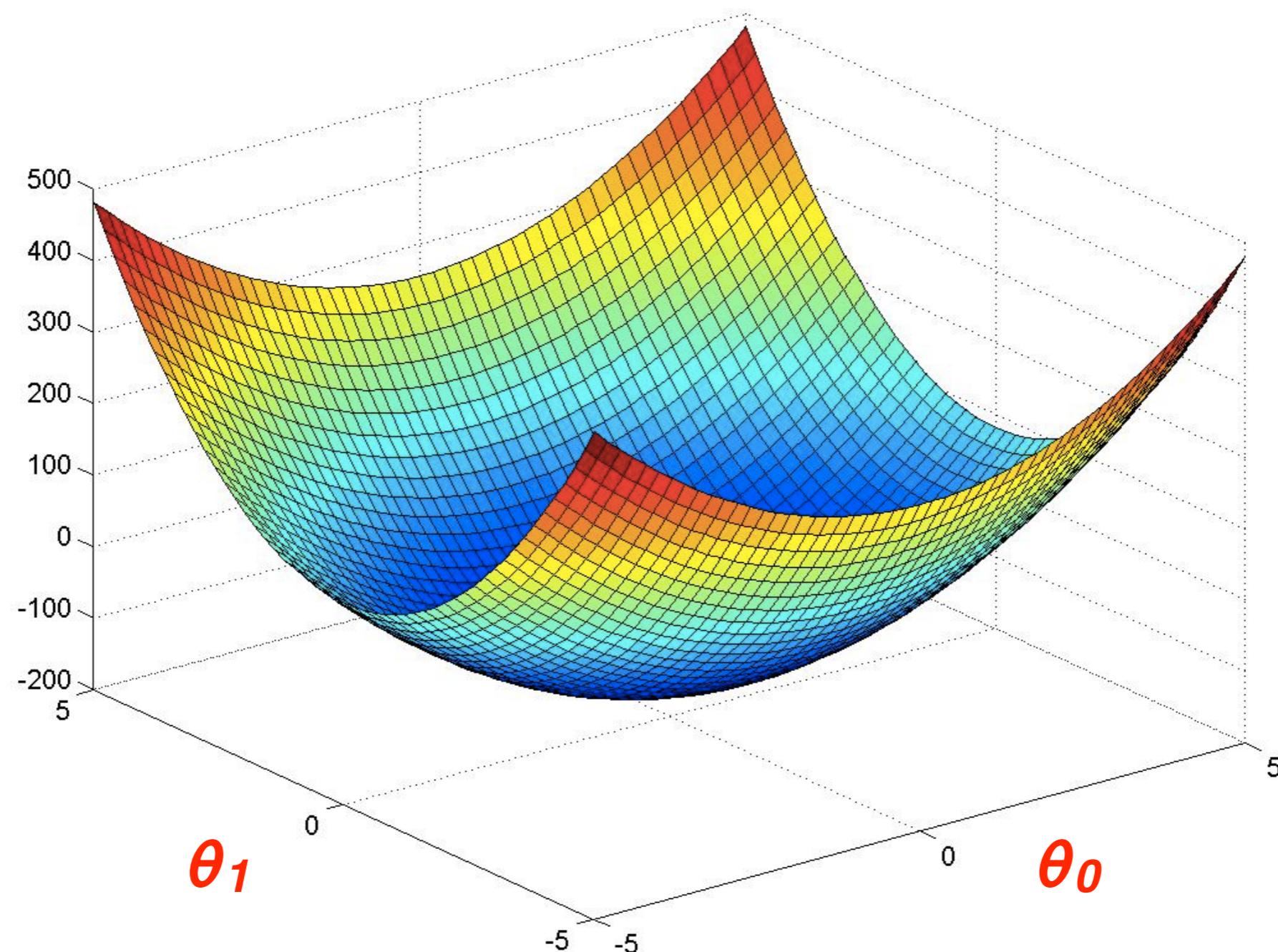
minimize $J(\theta_1)$
 θ_1

$$h_{\theta}(x)$$

(for fixed θ_0, θ_1 , this is a function of x)

$$J(\theta_0, \theta_1)$$

(function of the parameter θ_0, θ_1)

$$J(\theta_1, \theta_2)$$


Linear Regression

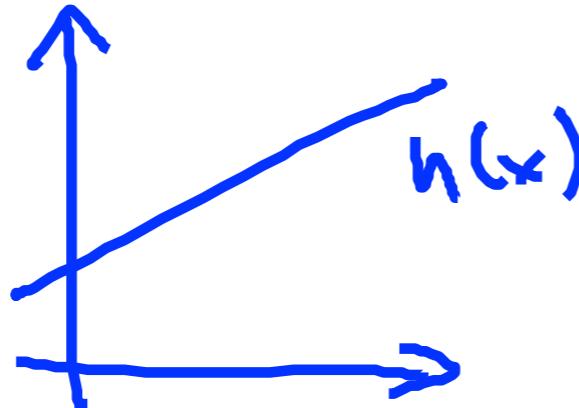
Simplified

- Hypothesis:

$$h_{\theta}(x) = \theta_0 + \theta_1 x$$

- Parameters:

$$\theta_0, \theta_1$$

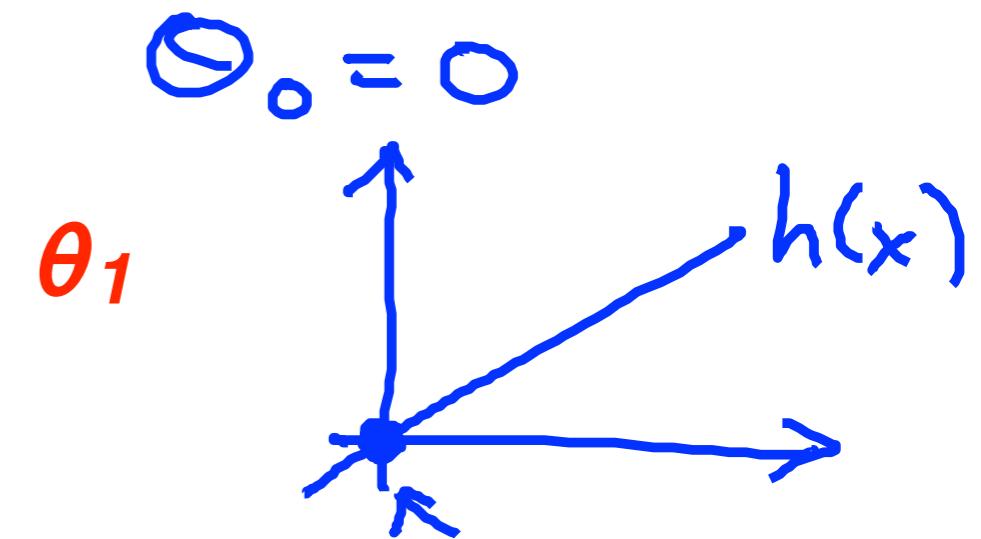


- Cost Function:

$$J(\theta_0, \theta_1) = \frac{1}{2m} \sum_{i=1}^m (h_{\theta}(x^{(i)}) - y^{(i)})^2$$

- Goal: $\underset{\theta_0, \theta_1}{\text{minimize}} J(\theta_0, \theta_1)$

$$h_{\theta}(x) = \theta_1 x$$



$$J(\theta_1) = \frac{1}{2m} \sum_{i=1}^m (h_{\theta}(x^{(i)}) - y^{(i)})^2$$

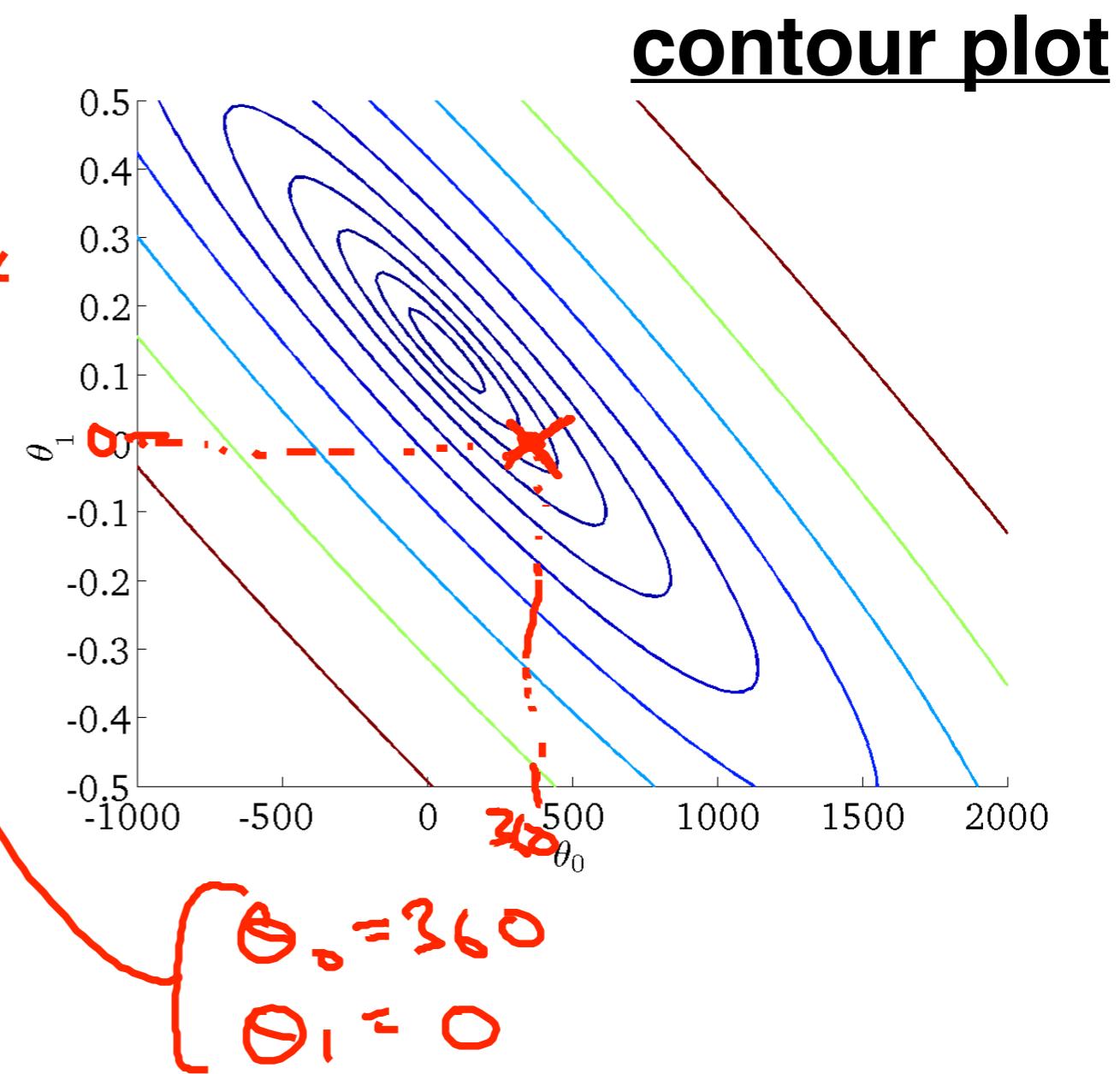
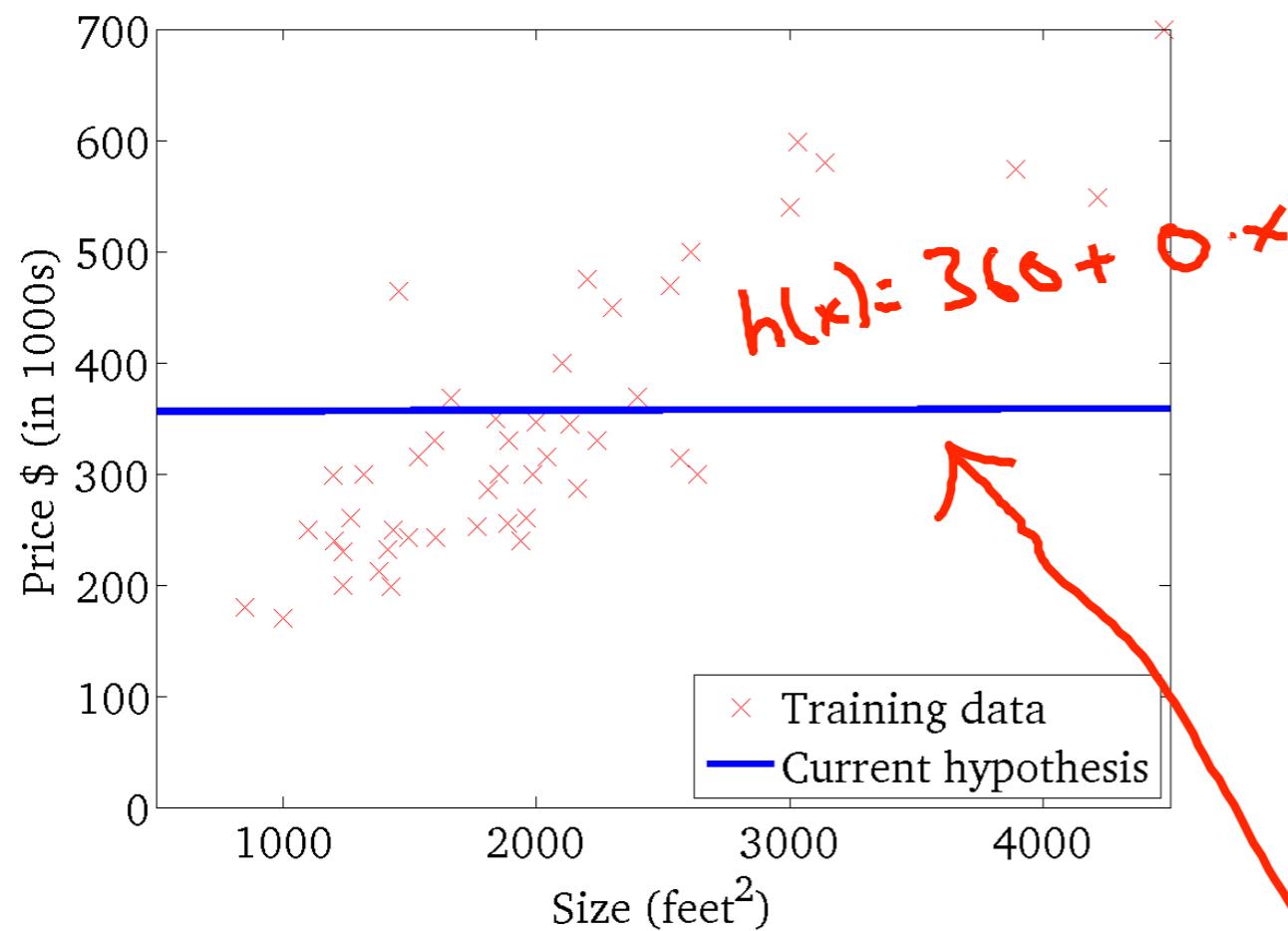
$$\underset{\theta_1}{\text{minimize}} J(\theta_1)$$

$$h_{\theta}(x)$$

(for fixed θ_0, θ_1 , this is a function of x)

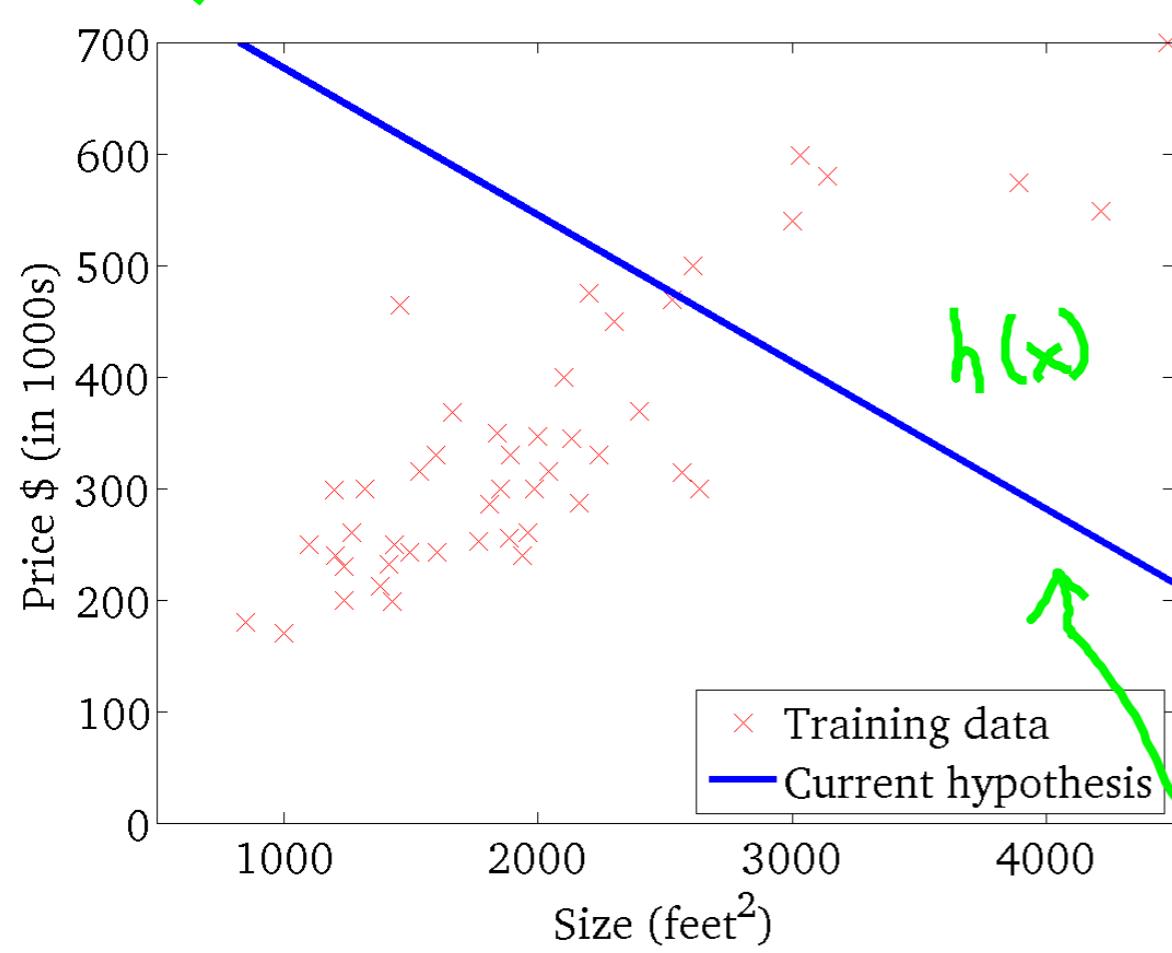
$$J(\theta_0, \theta_1)$$

(function of the parameter θ_0, θ_1)



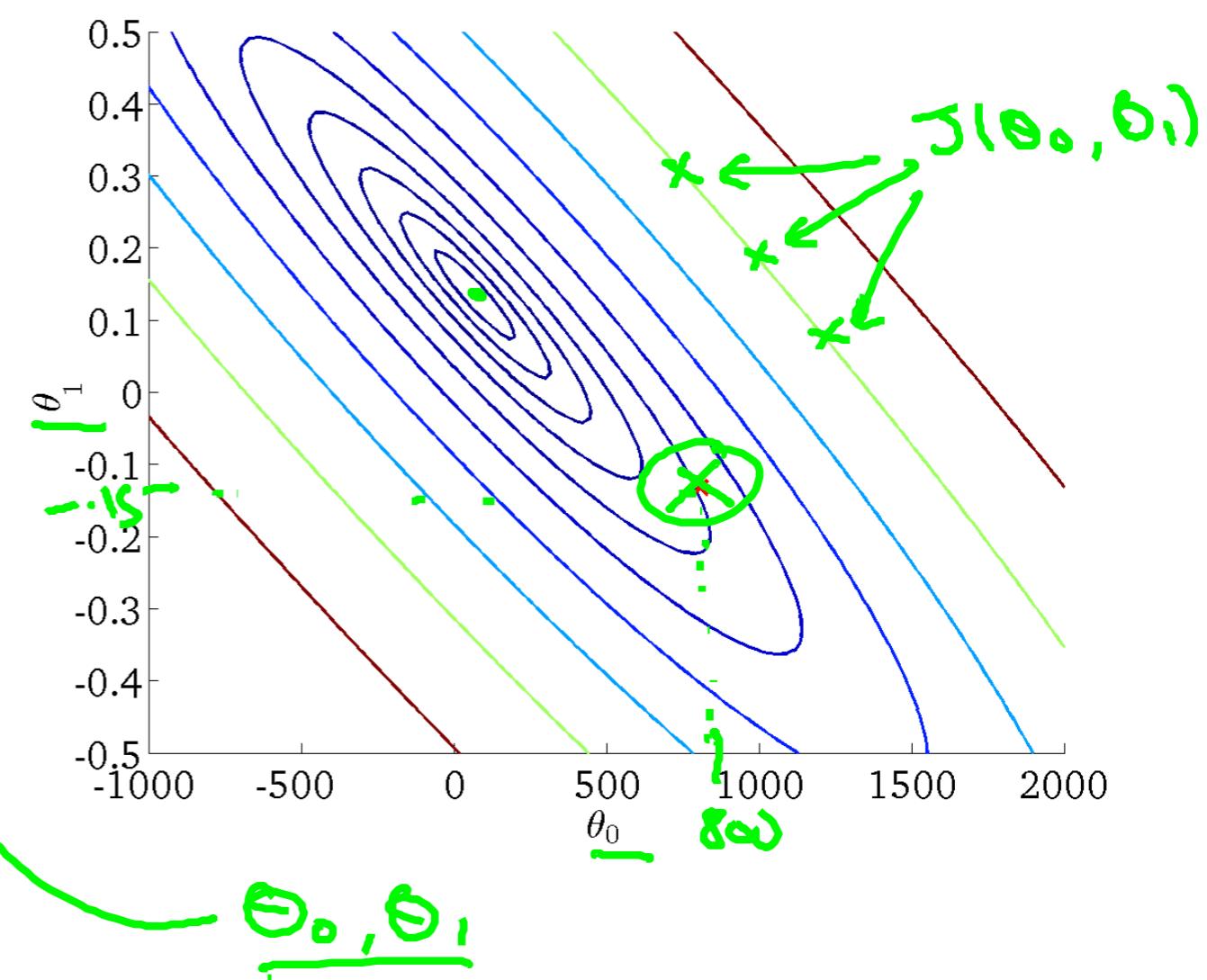
$$h_{\theta}(x)$$

(for fixed θ_0, θ_1 , this is a function of x)



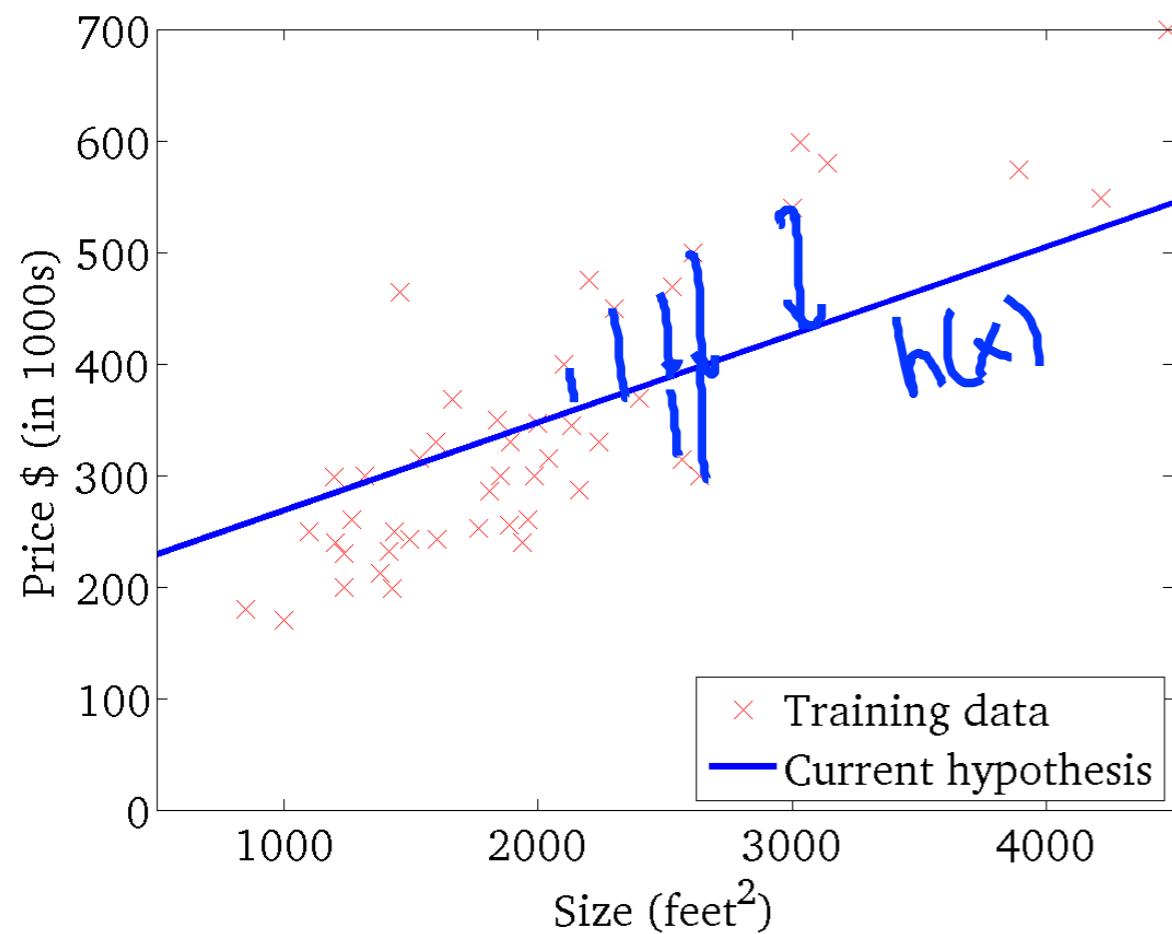
$$J(\theta_0, \theta_1)$$

(function of the parameter θ_0, θ_1)



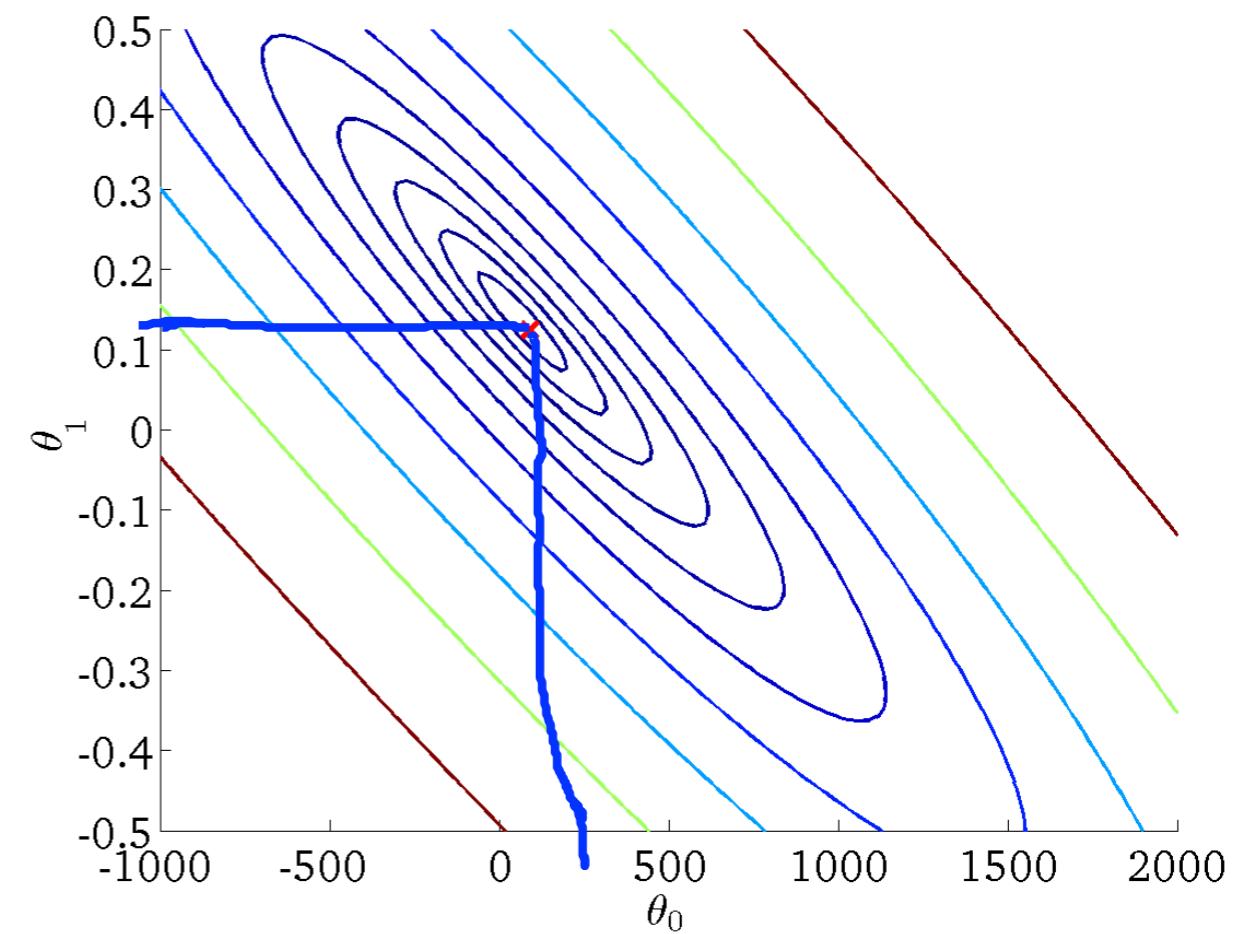
$$h_{\theta}(x)$$

(for fixed θ_0, θ_1 , this is a function of x)



$$J(\theta_0, \theta_1)$$

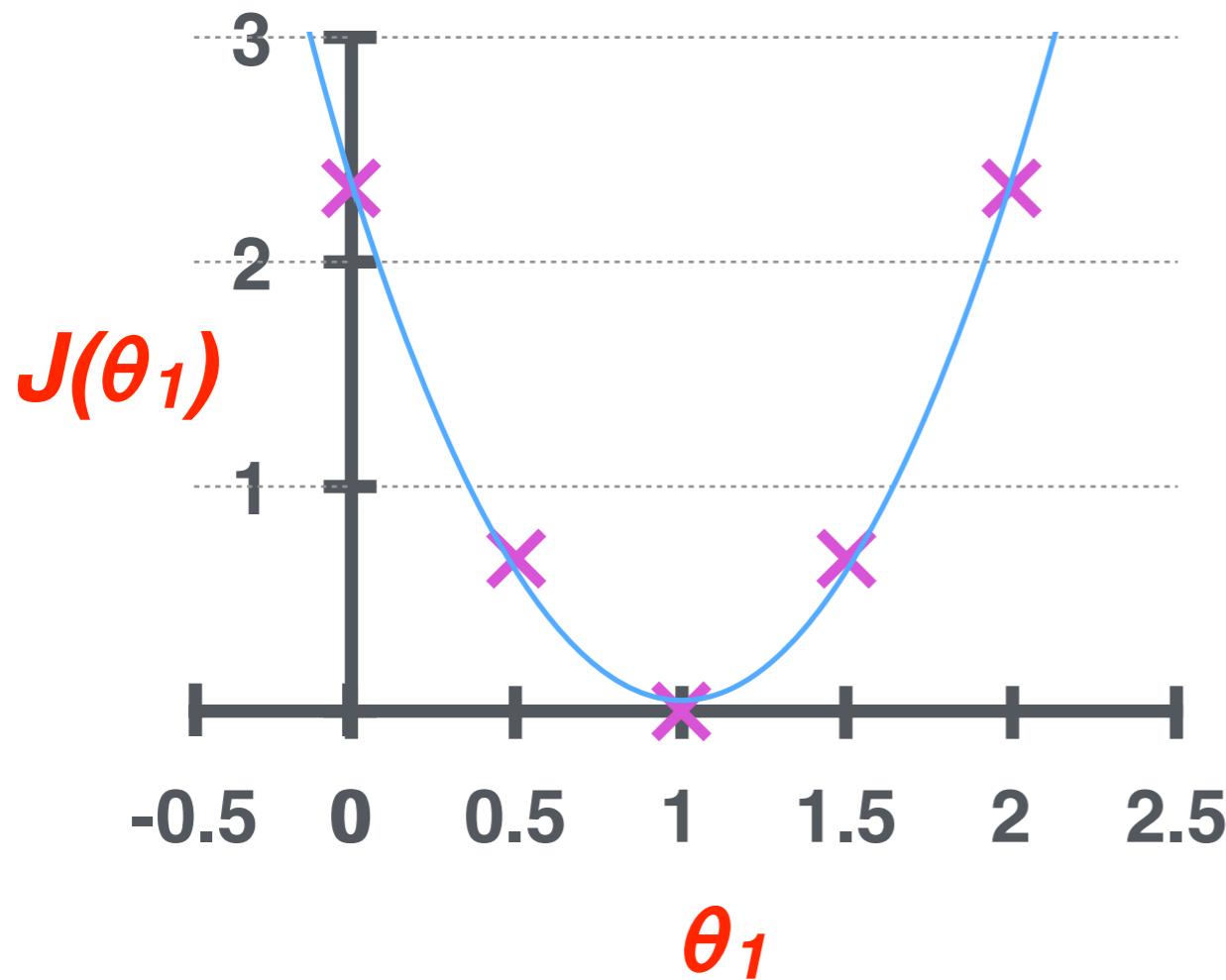
(function of the parameter θ_0, θ_1)



Parameter Learning

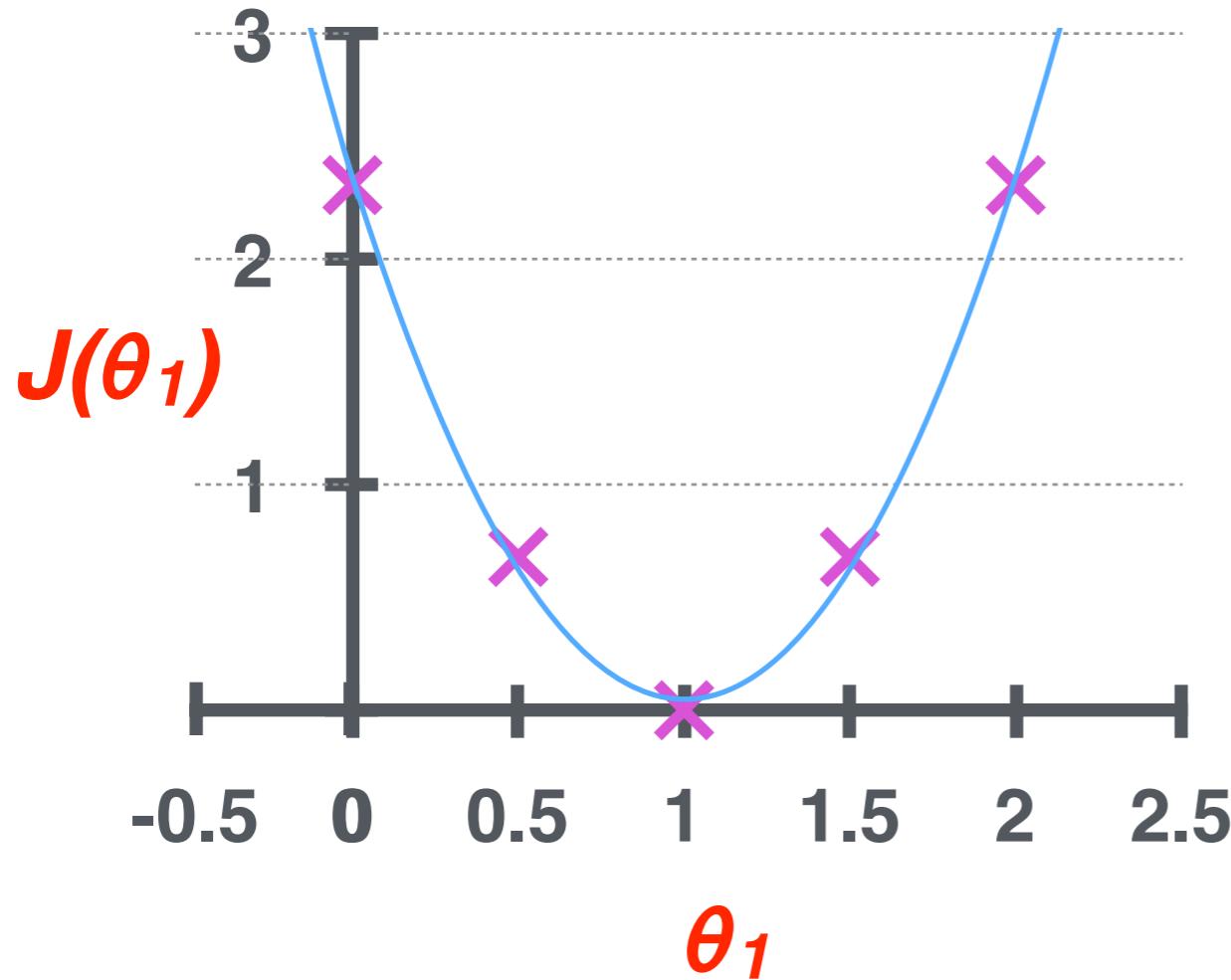
- Have some function $J(\theta_0, \theta_1)$
- Want $\min_{\theta_0, \theta_1} J(\theta_0, \theta_1)$
- **Outline:**
 - Start with some θ_0, θ_1
 - Keep changing θ_0, θ_1 to reduce $J(\theta_1, \theta_2)$ until we hopefully end up at a minimum

Gradient Descent



minimize $J(\theta_1)$
 θ_1

Gradient Descent

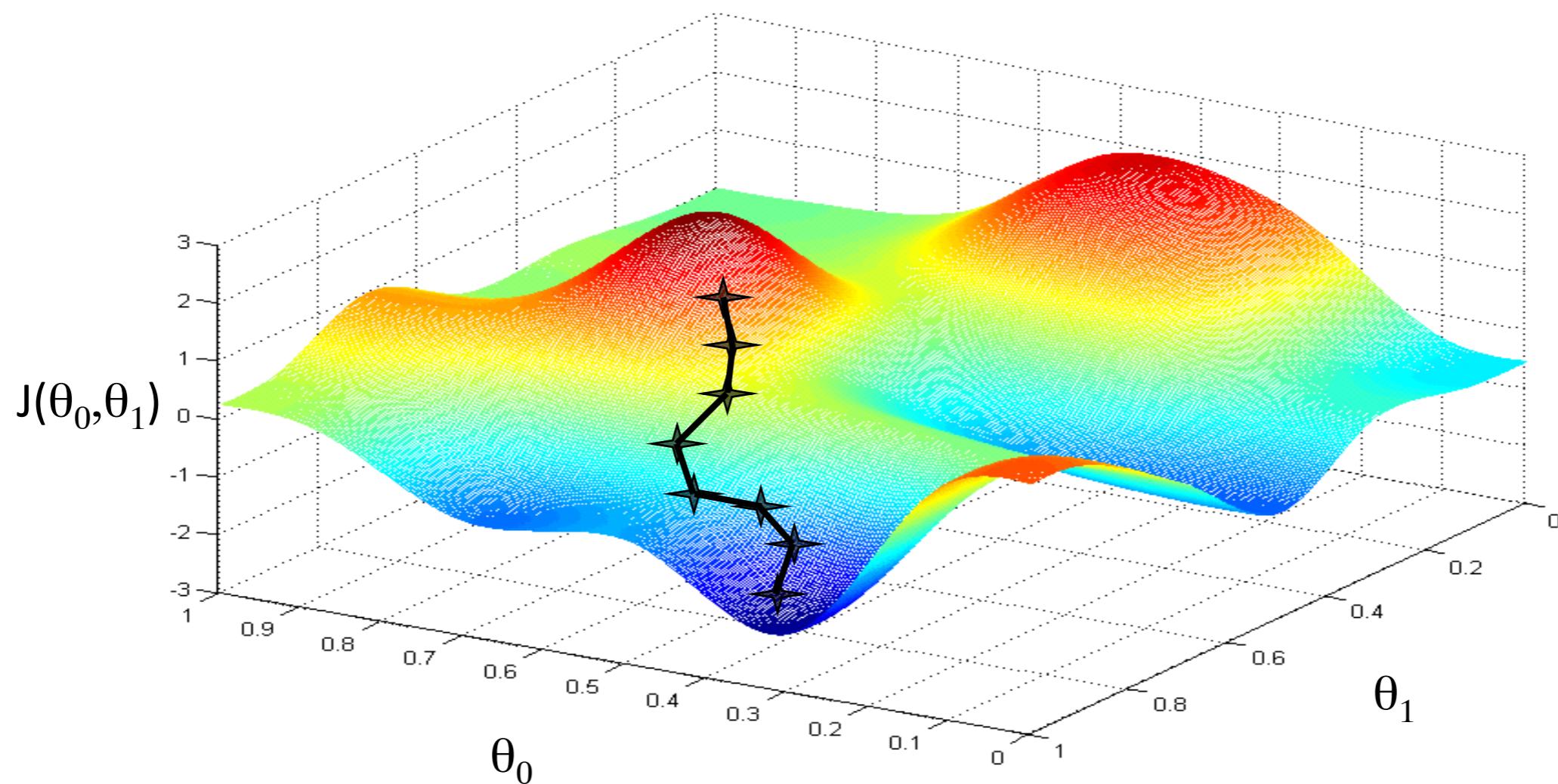


$$\theta_1 \doteq \theta_1 - \alpha \frac{\partial}{\partial \theta_1} J(\theta_1)$$

learning rate

minimize $J(\theta_1)$

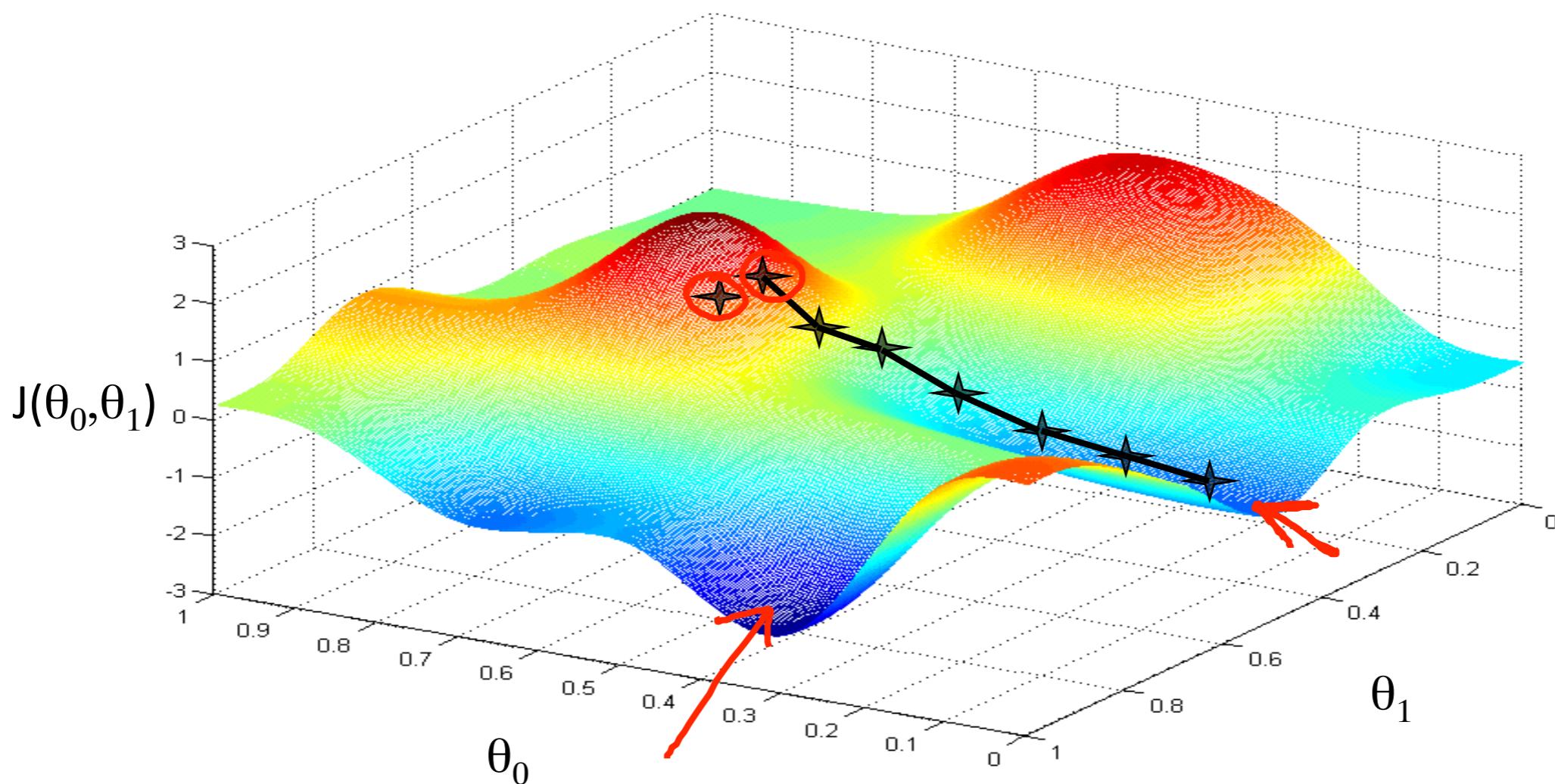
Gradient Descent



minimize $J(\theta_0, \theta_1)$
 θ_0, θ_1

Andrew Ng

Gradient Descent



minimize $J(\theta_0, \theta_1)$
 θ_0, θ_1

Andrew Ng

Gradient Descent

repeat until convergence {

$$\theta_j := \theta_j - \alpha \frac{\partial}{\partial \theta_j} J(\theta_0, \theta_1)$$

learning rate

(simultaneous update
for j=0 and j=1)

}

Linear Regression w/ one variable:

Gradient Descent

$$h_{\theta}(x) = \theta_0 + \theta_1 x$$

Cost Function



$$J(\theta_0, \theta_1) = \frac{1}{2m} \sum_{i=1}^m (h_{\theta}(x^{(i)}) - y^{(i)})^2$$

$$\frac{\partial}{\partial \theta_0} J(\theta_0, \theta_1) = ?$$

$$\frac{\partial}{\partial \theta_1} J(\theta_0, \theta_1) = ?$$

Linear Regression w/ one variable:

Gradient Descent

repeat until convergence {

$$\theta_0 \leftarrow \theta_0 - \alpha \frac{1}{m} \sum_{i=1}^m (h_\theta(x^{(i)}) - y^{(i)})$$

simultaneous
update θ_0, θ_1

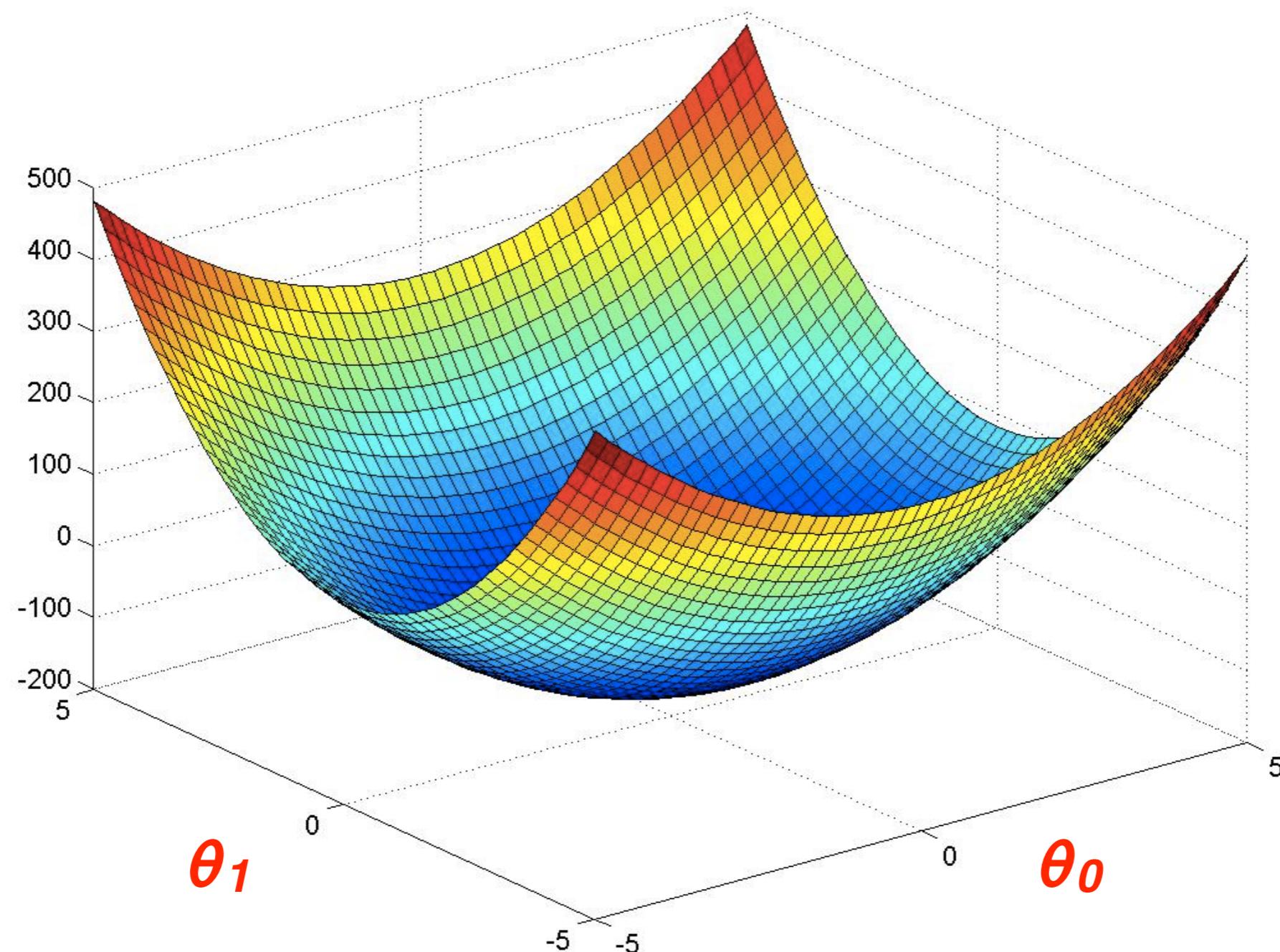
$$\theta_1 \leftarrow \theta_1 - \alpha \frac{1}{m} \sum_{i=1}^m (h_\theta(x^{(i)}) - y^{(i)}) \cdot x^{(i)}$$

}

Linear Regression

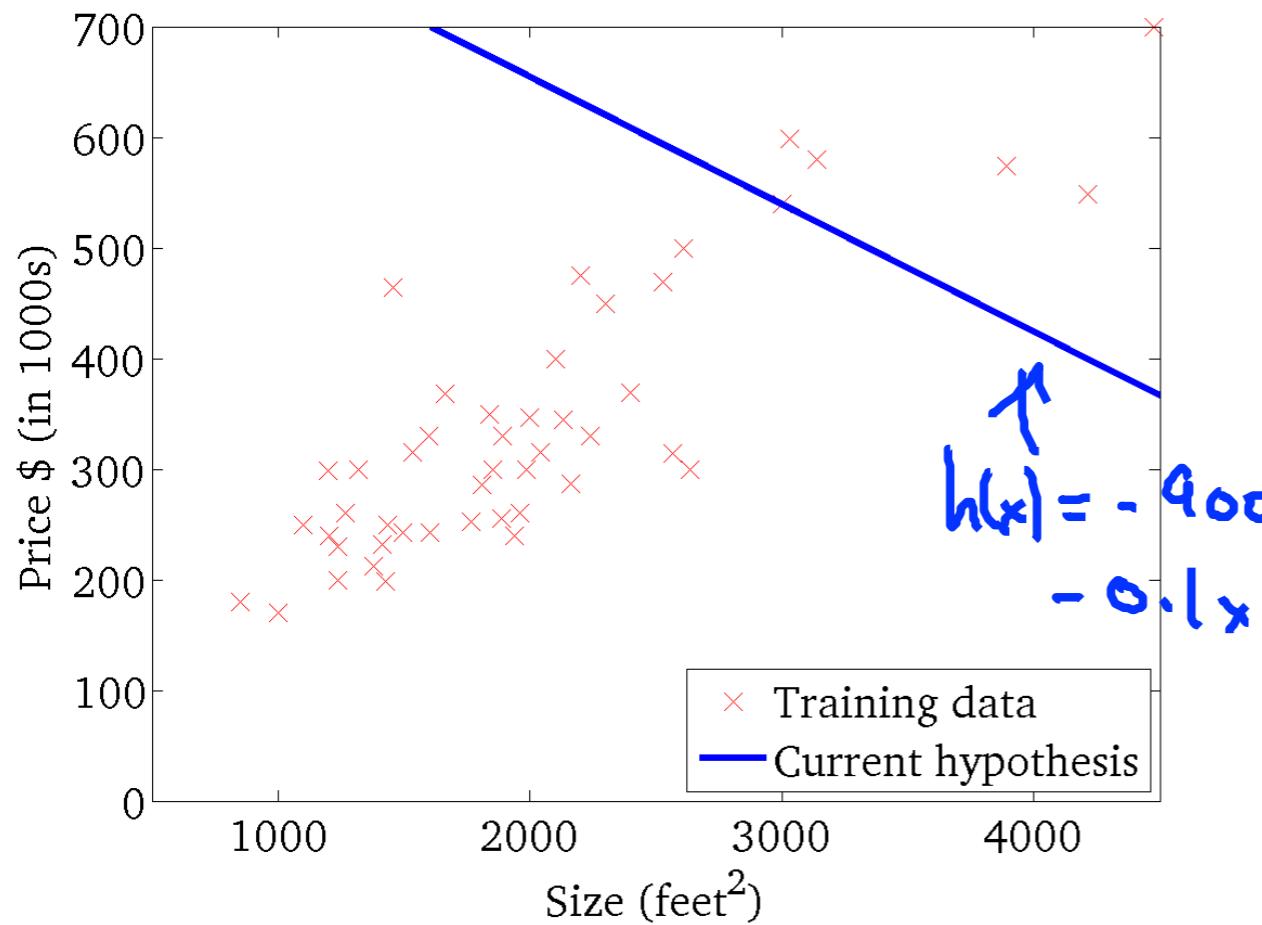
cost function is convex

$J(\theta_1, \theta_2)$



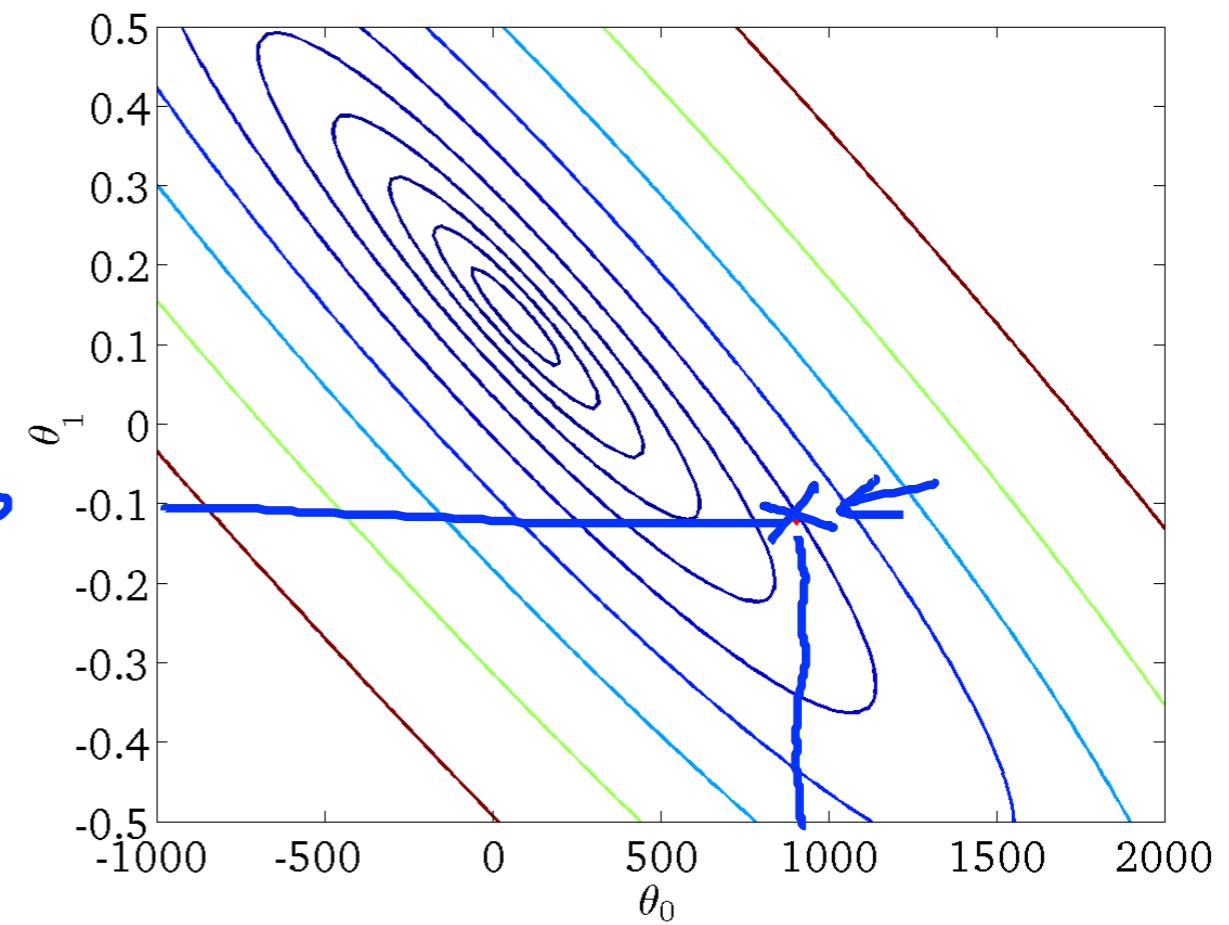
$$h_{\theta}(x)$$

(for fixed θ_0, θ_1 , this is a function of x)



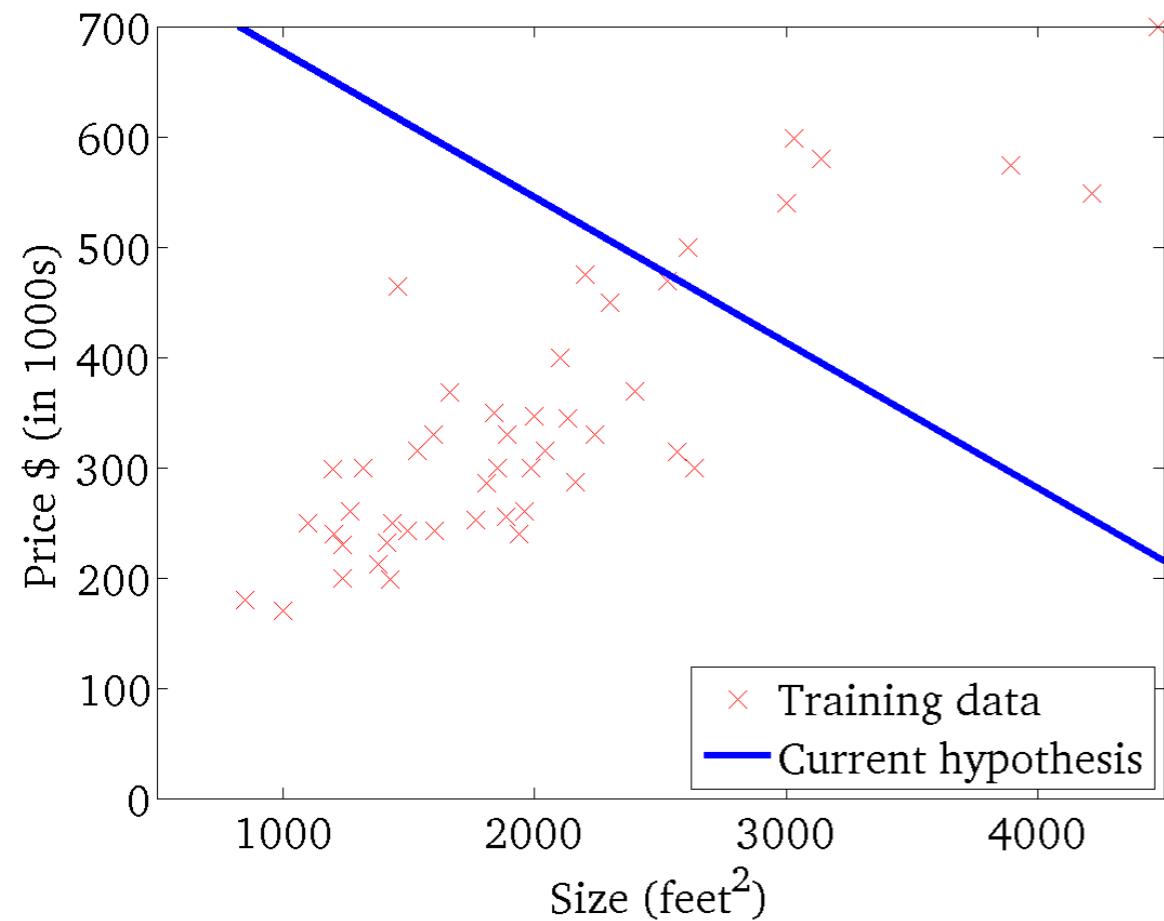
$$J(\theta_0, \theta_1)$$

(function of the parameter θ_0, θ_1)



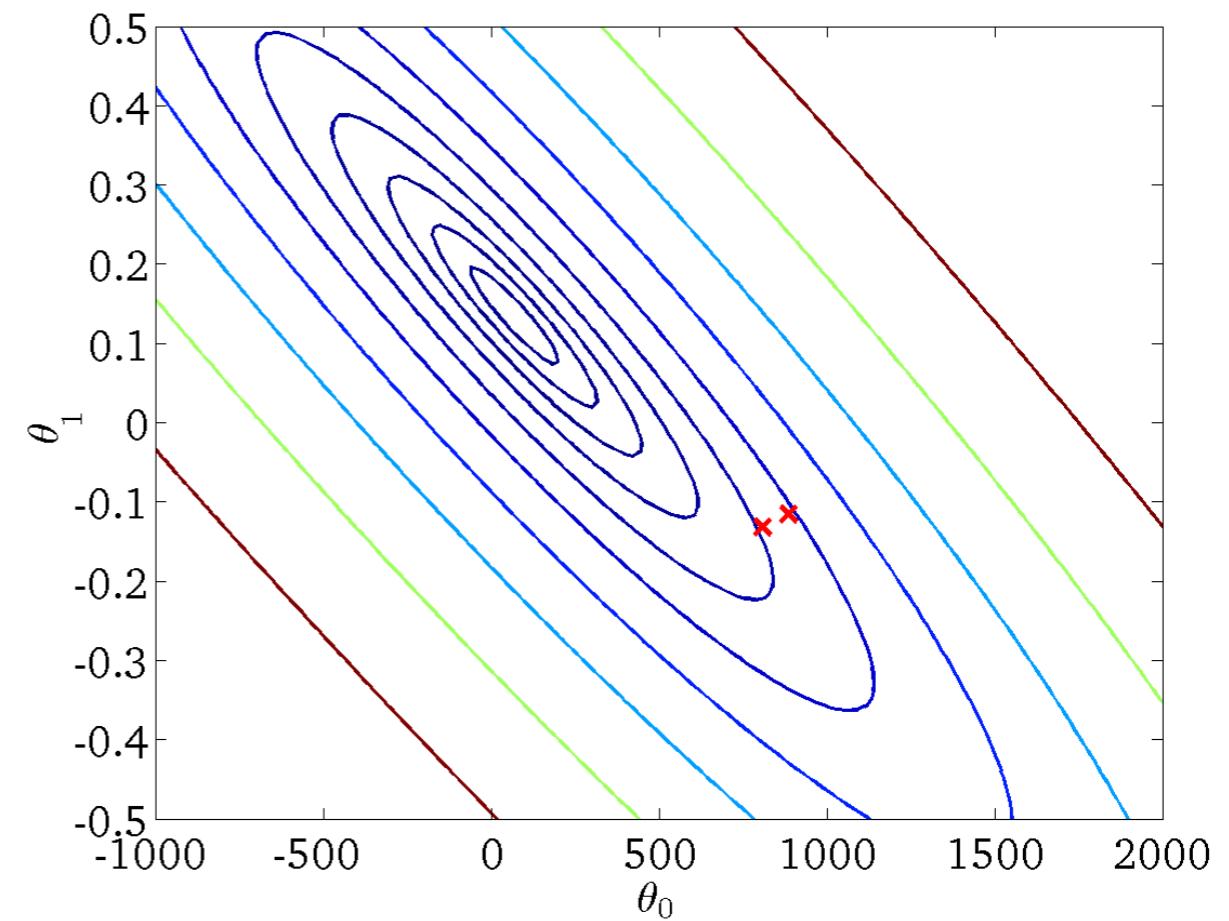
$$h_{\theta}(x)$$

(for fixed θ_0, θ_1 , this is a function of x)



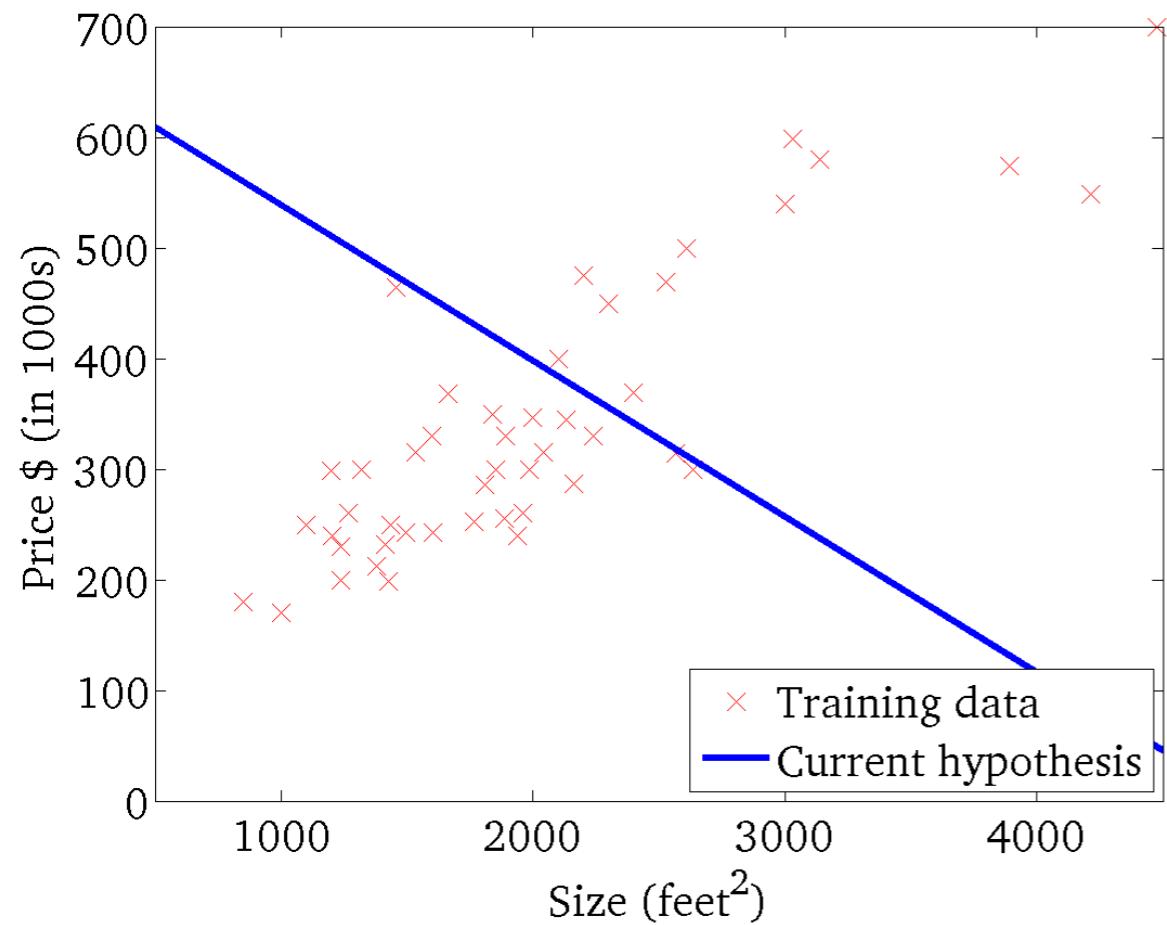
$$J(\theta_0, \theta_1)$$

(function of the parameter θ_0, θ_1)



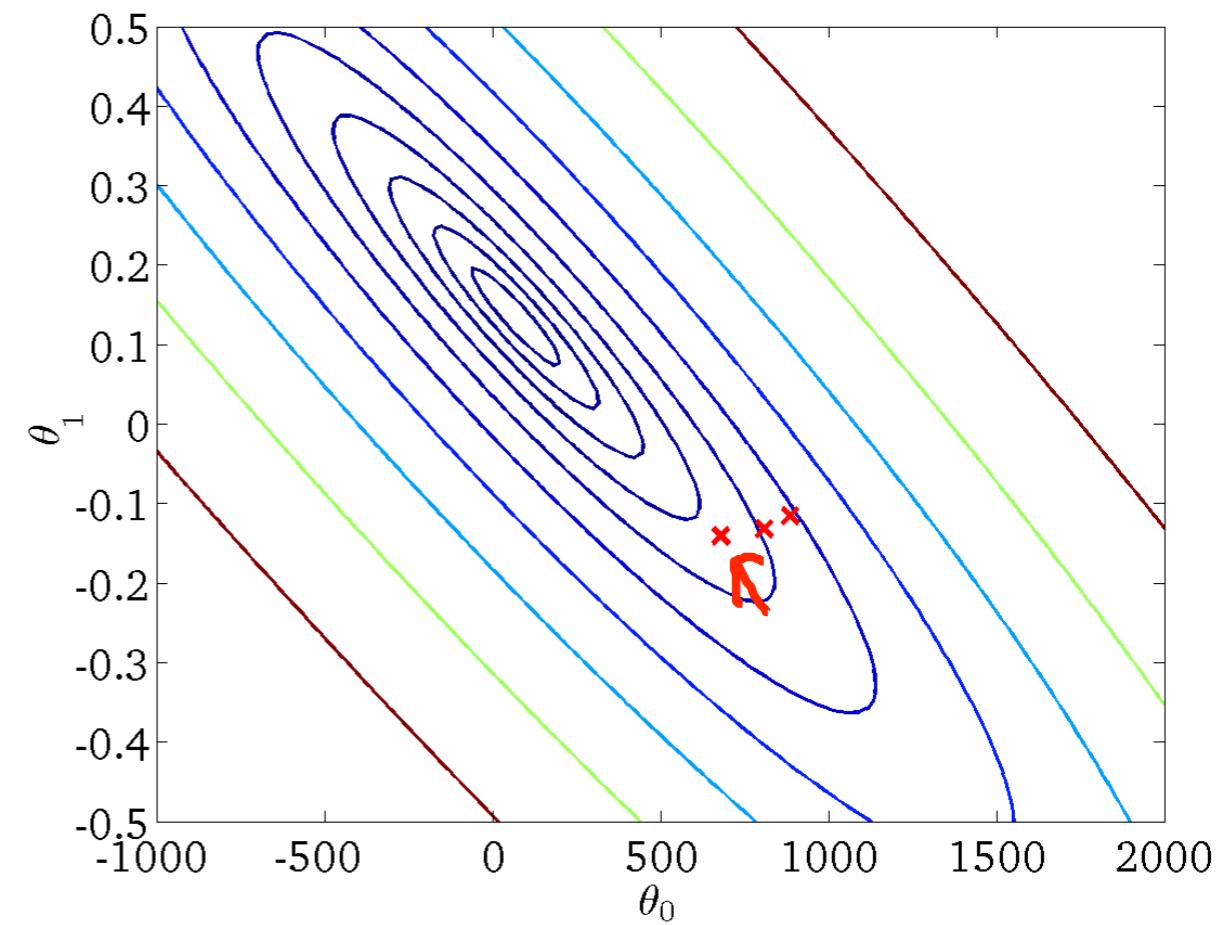
$$h_{\theta}(x)$$

(for fixed θ_0, θ_1 , this is a function of x)



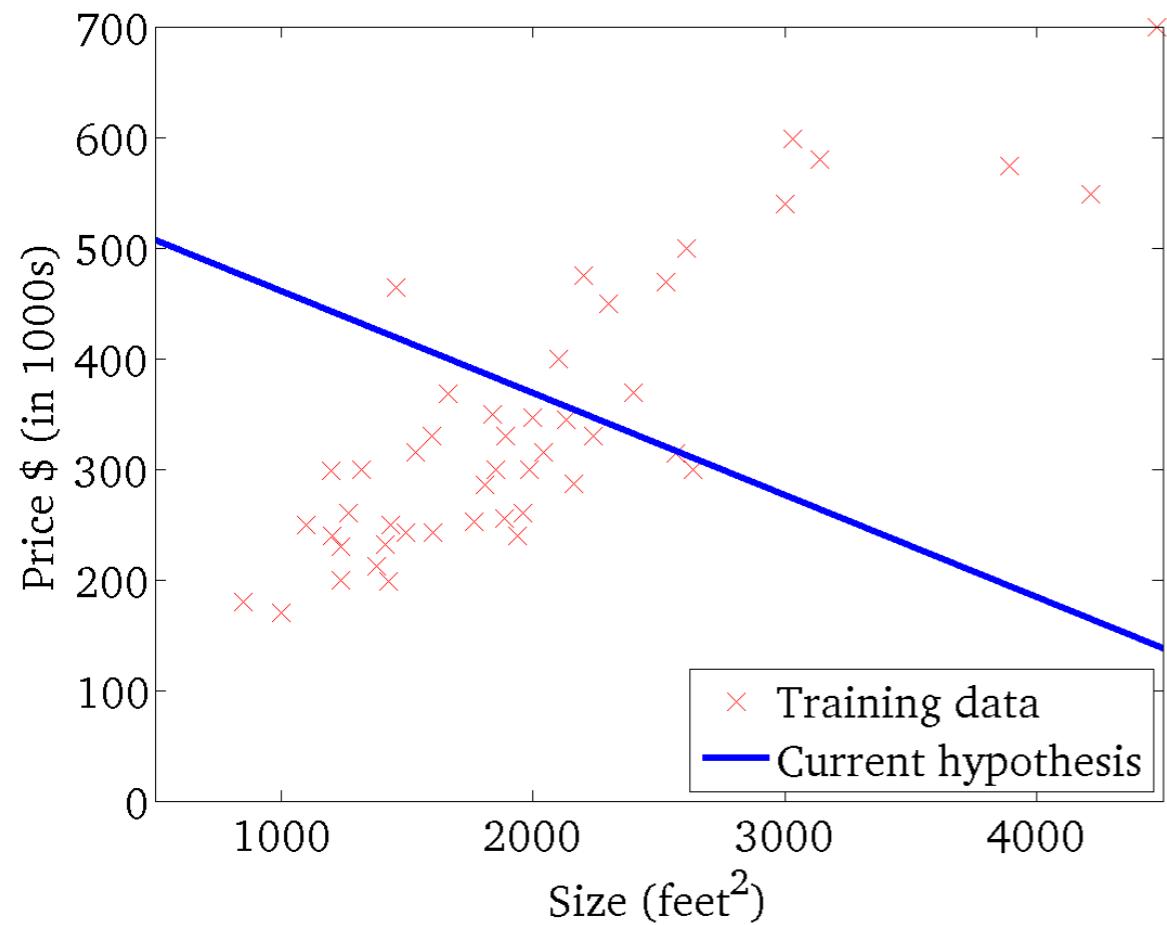
$$J(\theta_0, \theta_1)$$

(function of the parameter θ_0, θ_1)



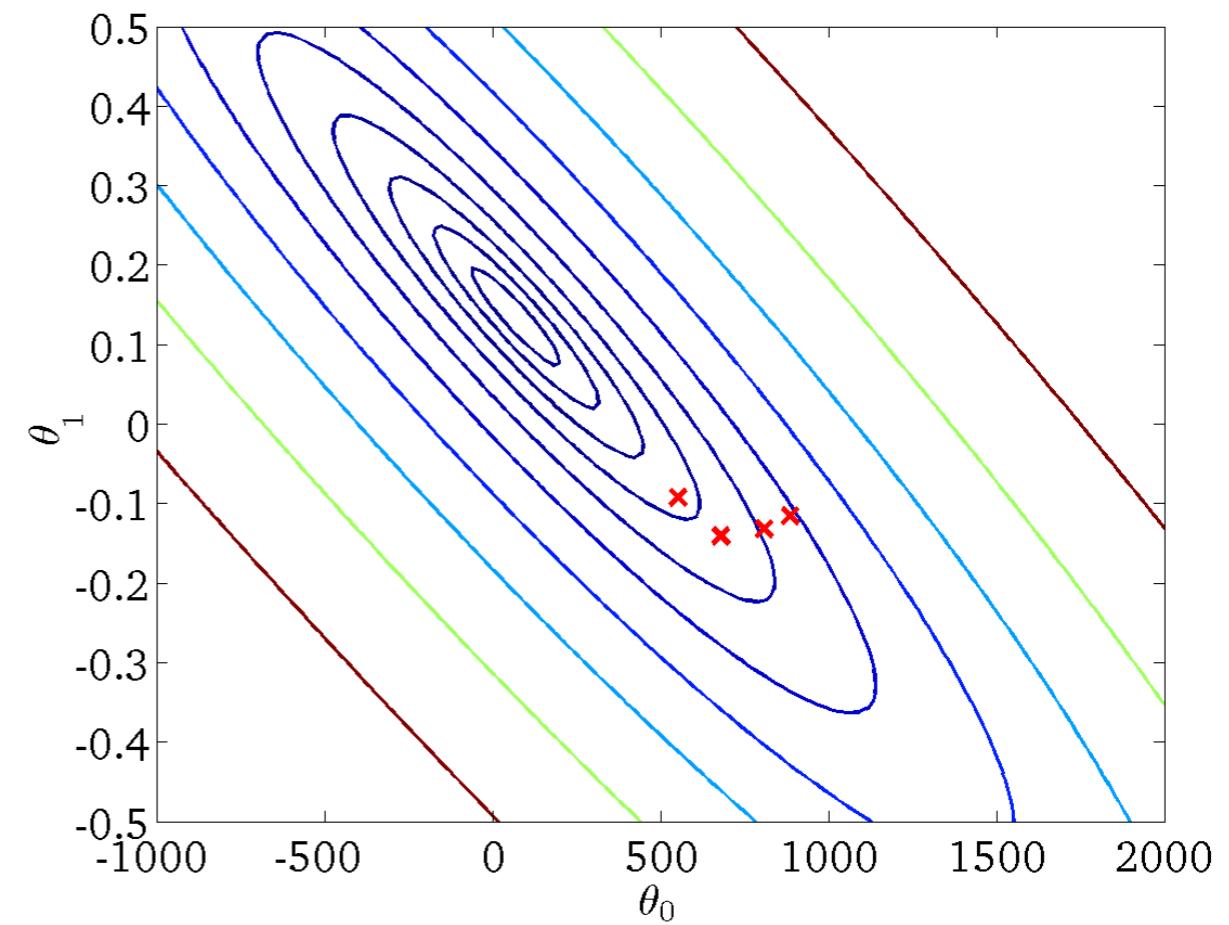
$$h_{\theta}(x)$$

(for fixed θ_0, θ_1 , this is a function of x)



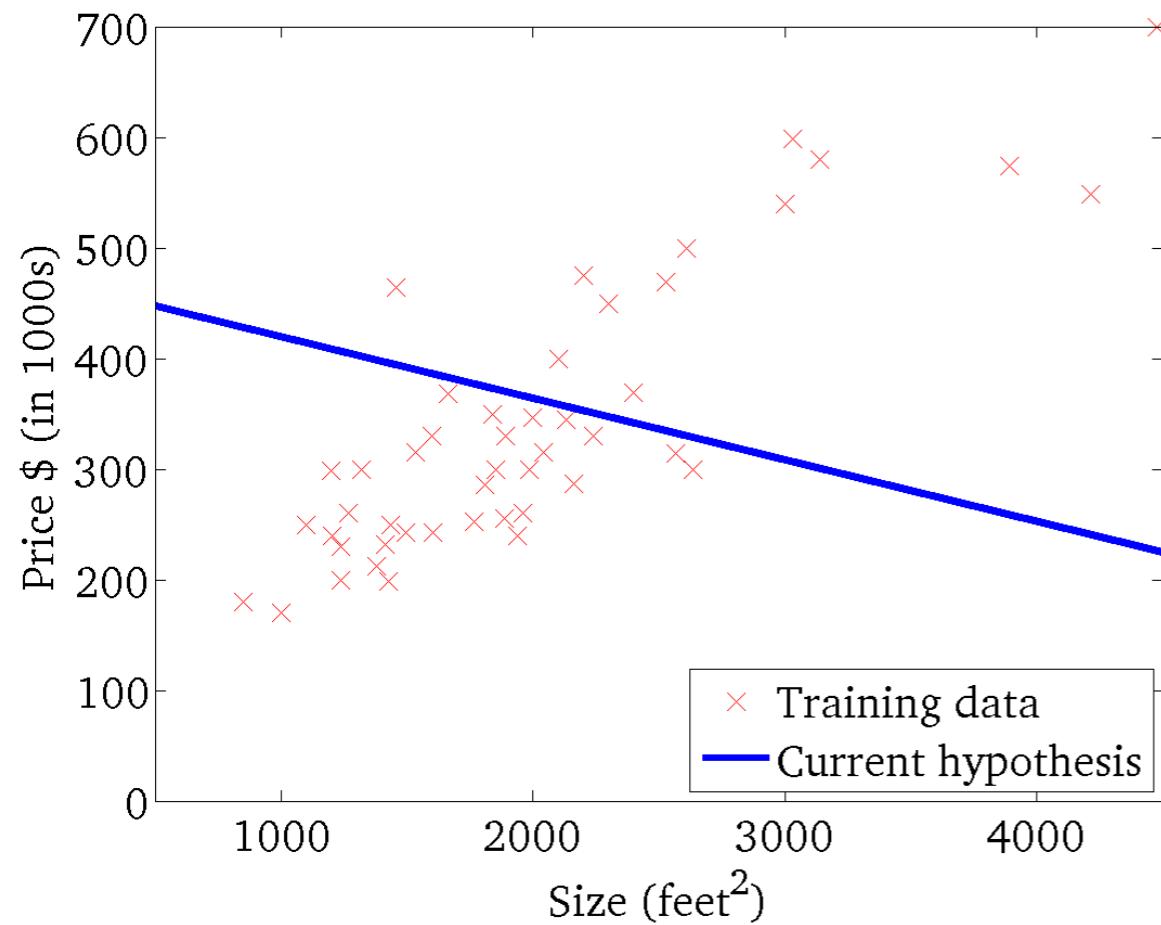
$$J(\theta_0, \theta_1)$$

(function of the parameter θ_0, θ_1)



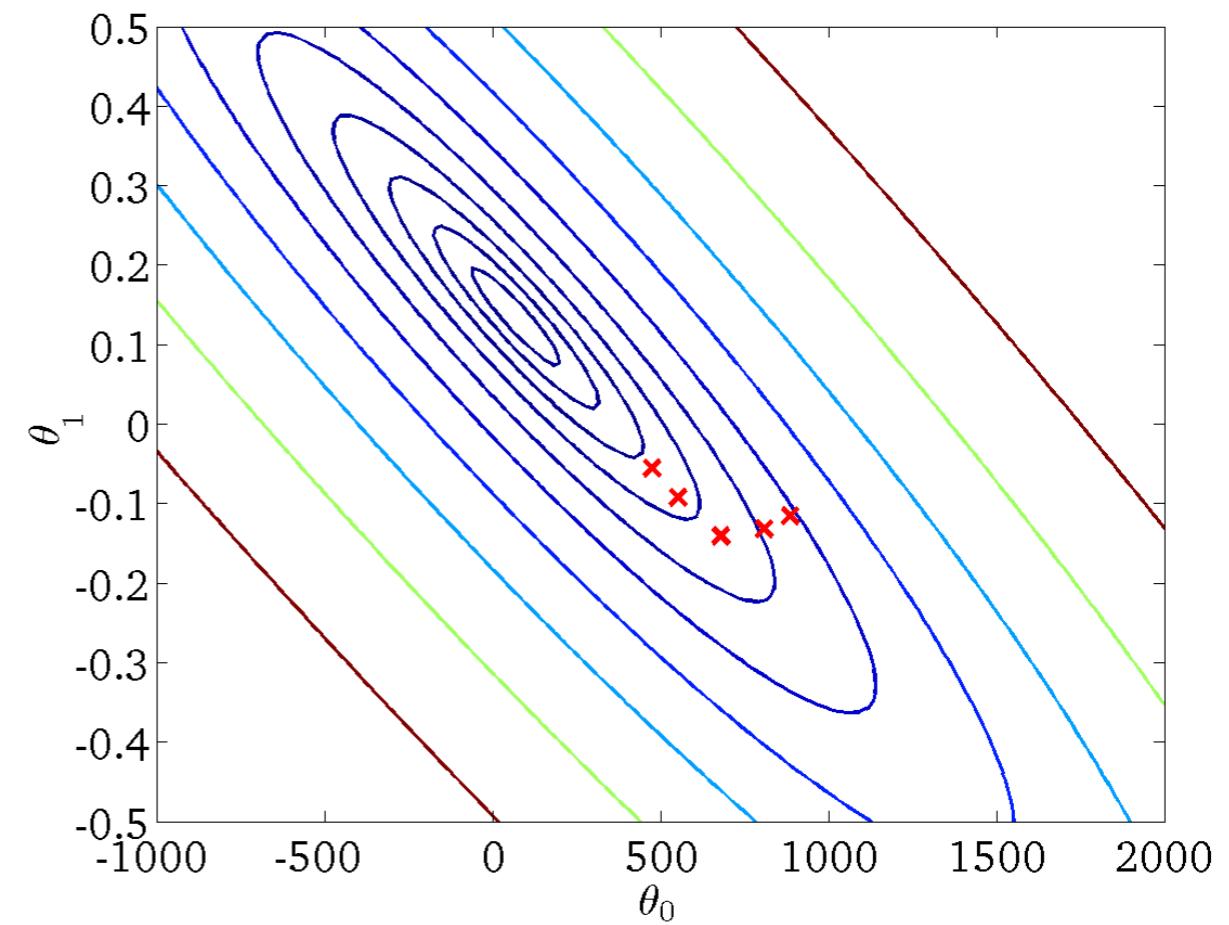
$$h_{\theta}(x)$$

(for fixed θ_0, θ_1 , this is a function of x)



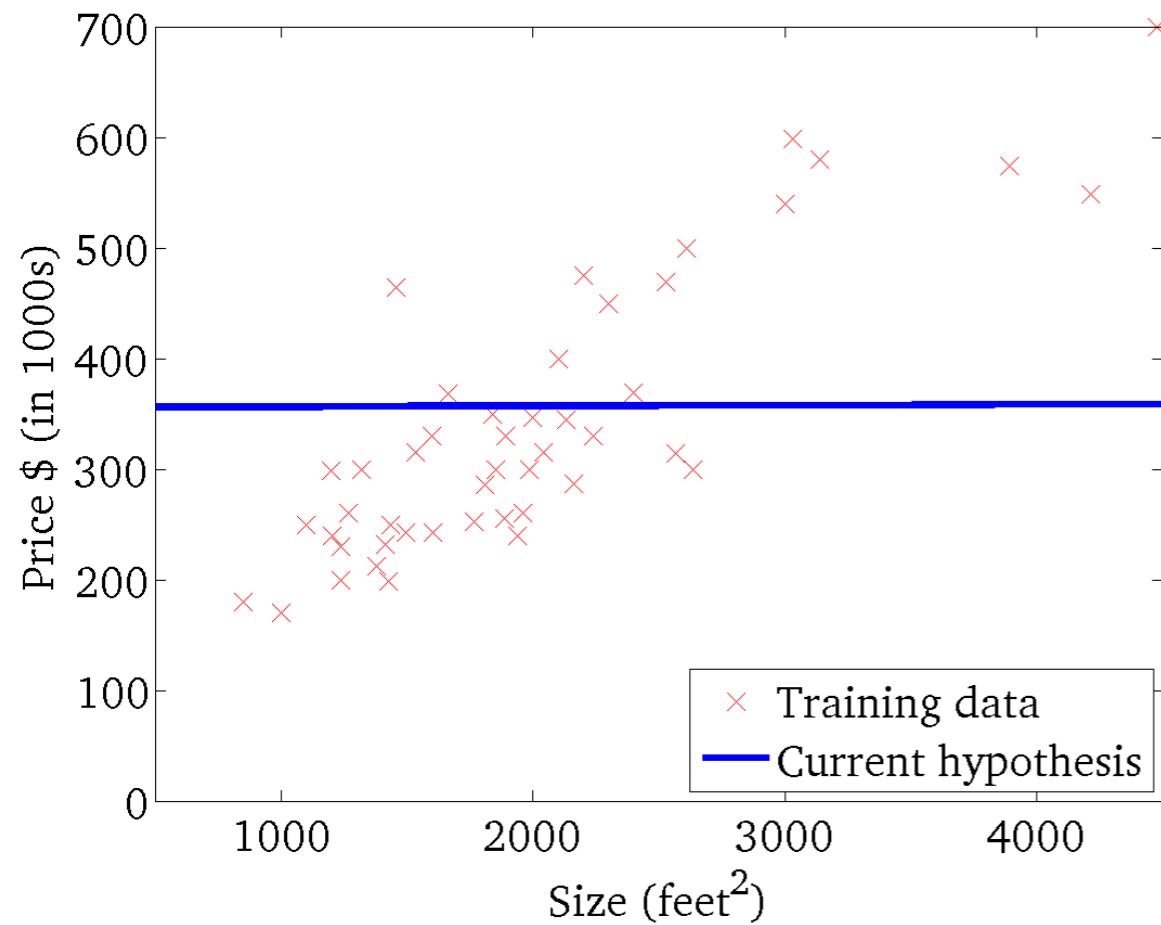
$$J(\theta_0, \theta_1)$$

(function of the parameter θ_0, θ_1)



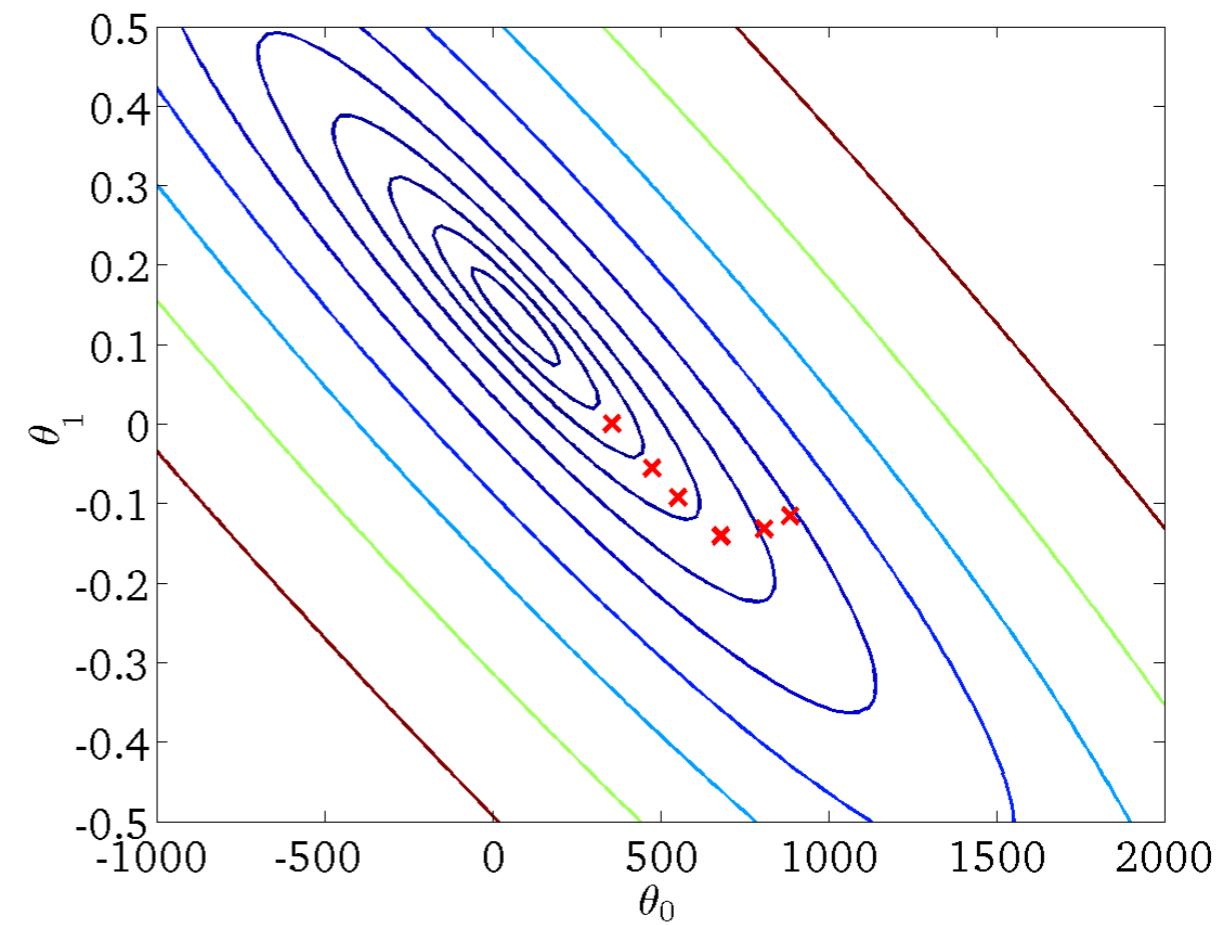
$$h_{\theta}(x)$$

(for fixed θ_0, θ_1 , this is a function of x)



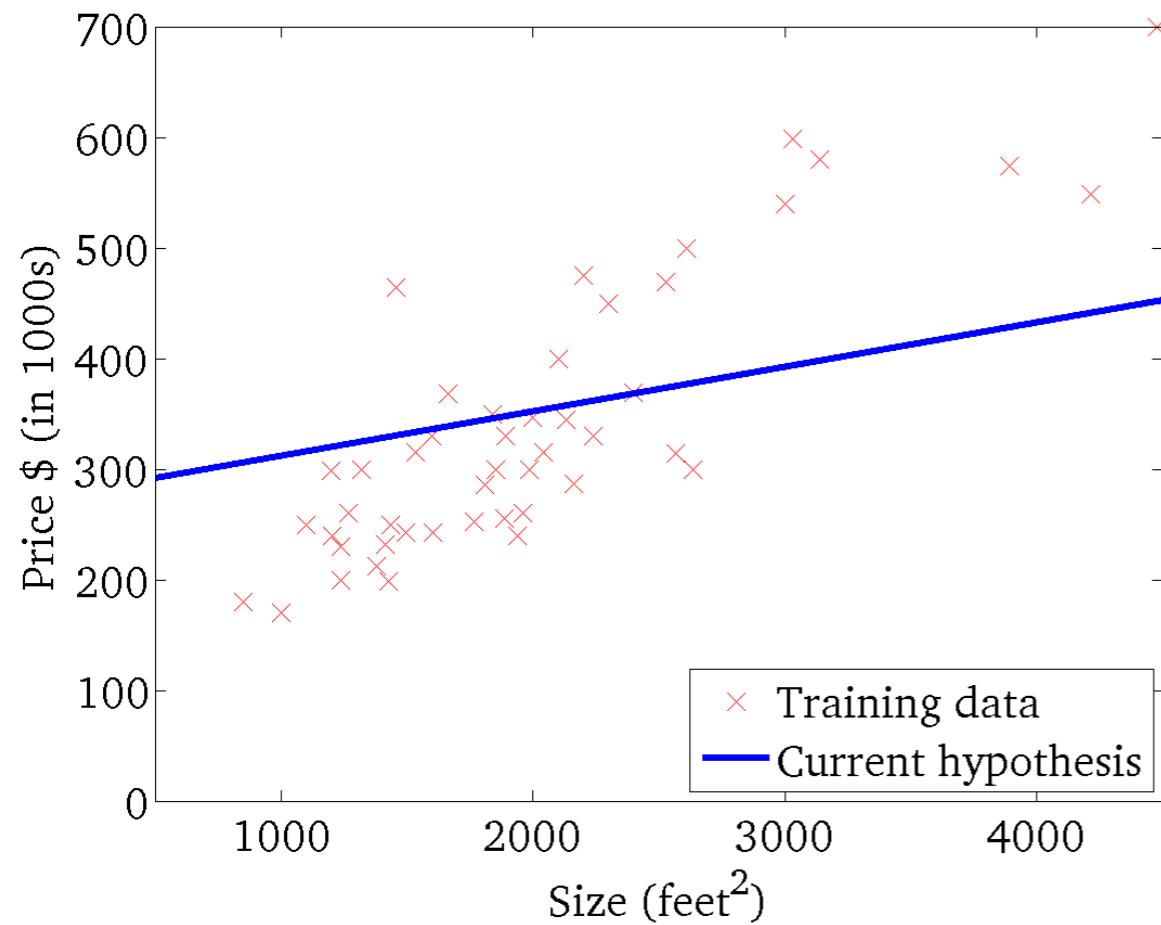
$$J(\theta_0, \theta_1)$$

(function of the parameter θ_0, θ_1)



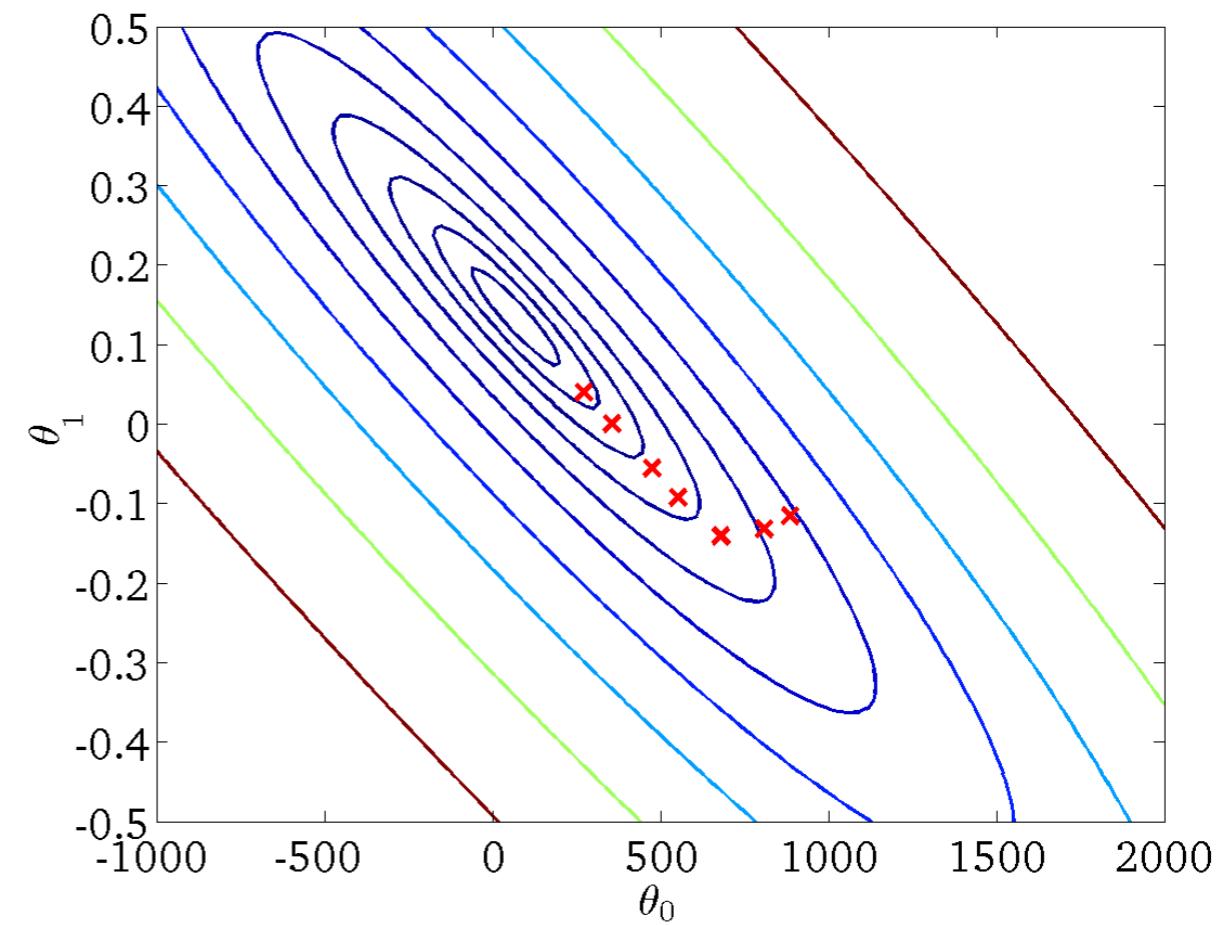
$$h_{\theta}(x)$$

(for fixed θ_0, θ_1 , this is a function of x)



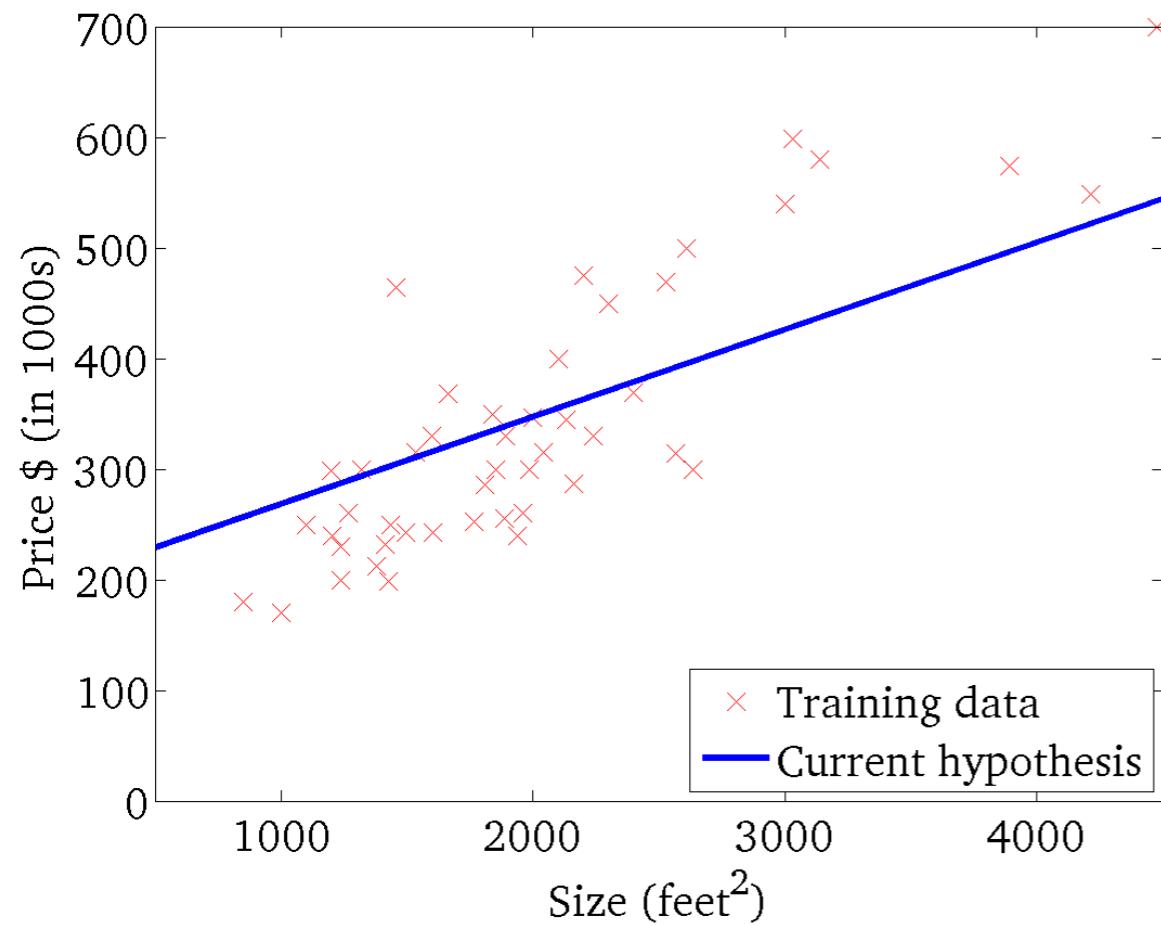
$$J(\theta_0, \theta_1)$$

(function of the parameter θ_0, θ_1)



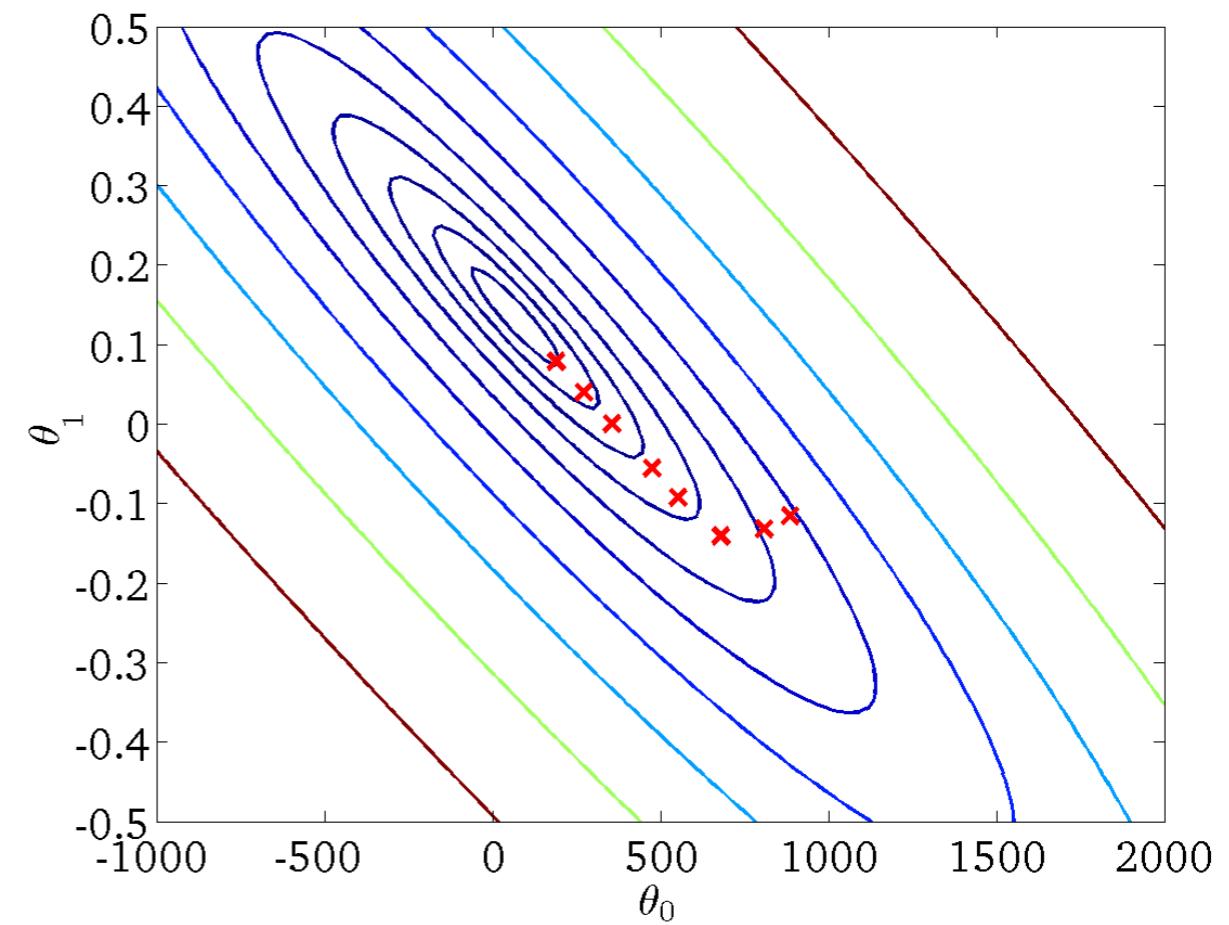
$$h_{\theta}(x)$$

(for fixed θ_0, θ_1 , this is a function of x)



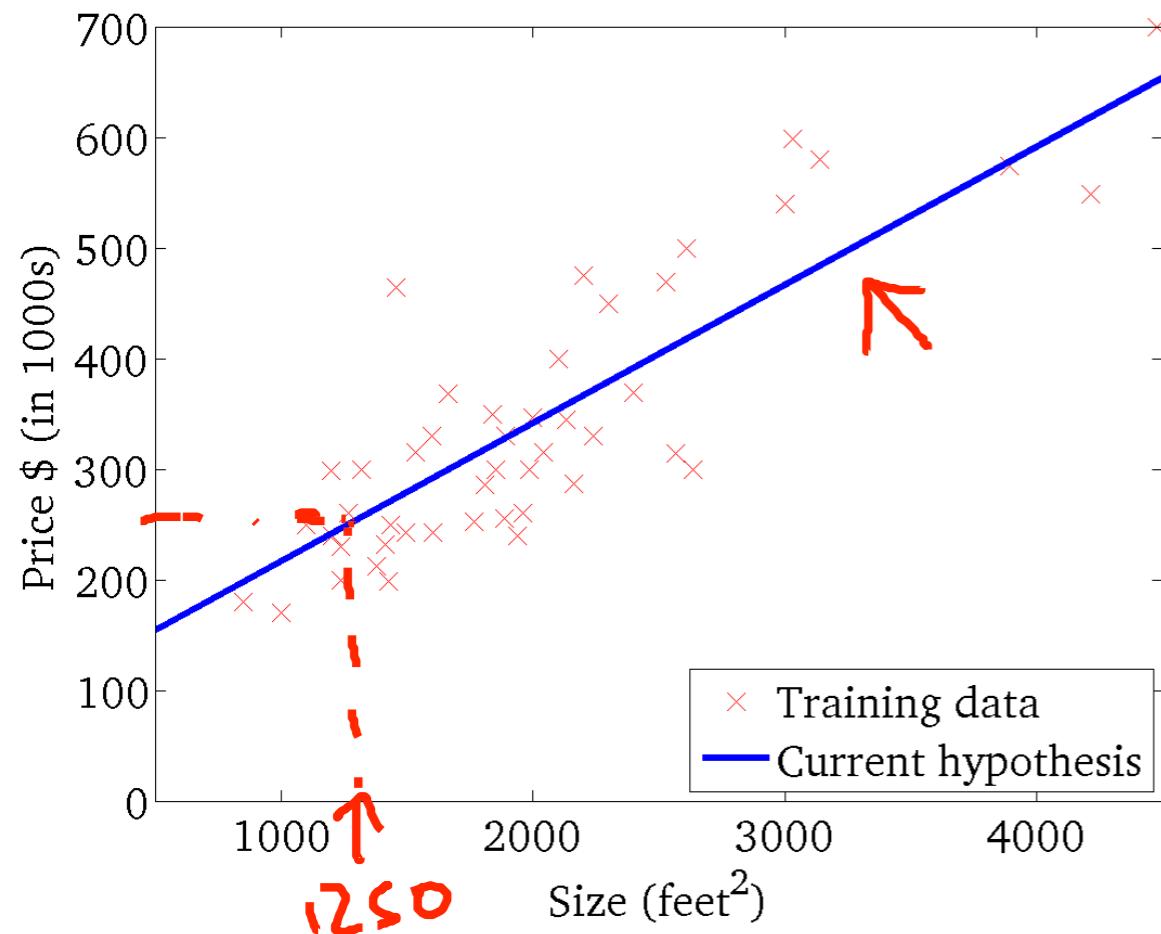
$$J(\theta_0, \theta_1)$$

(function of the parameter θ_0, θ_1)



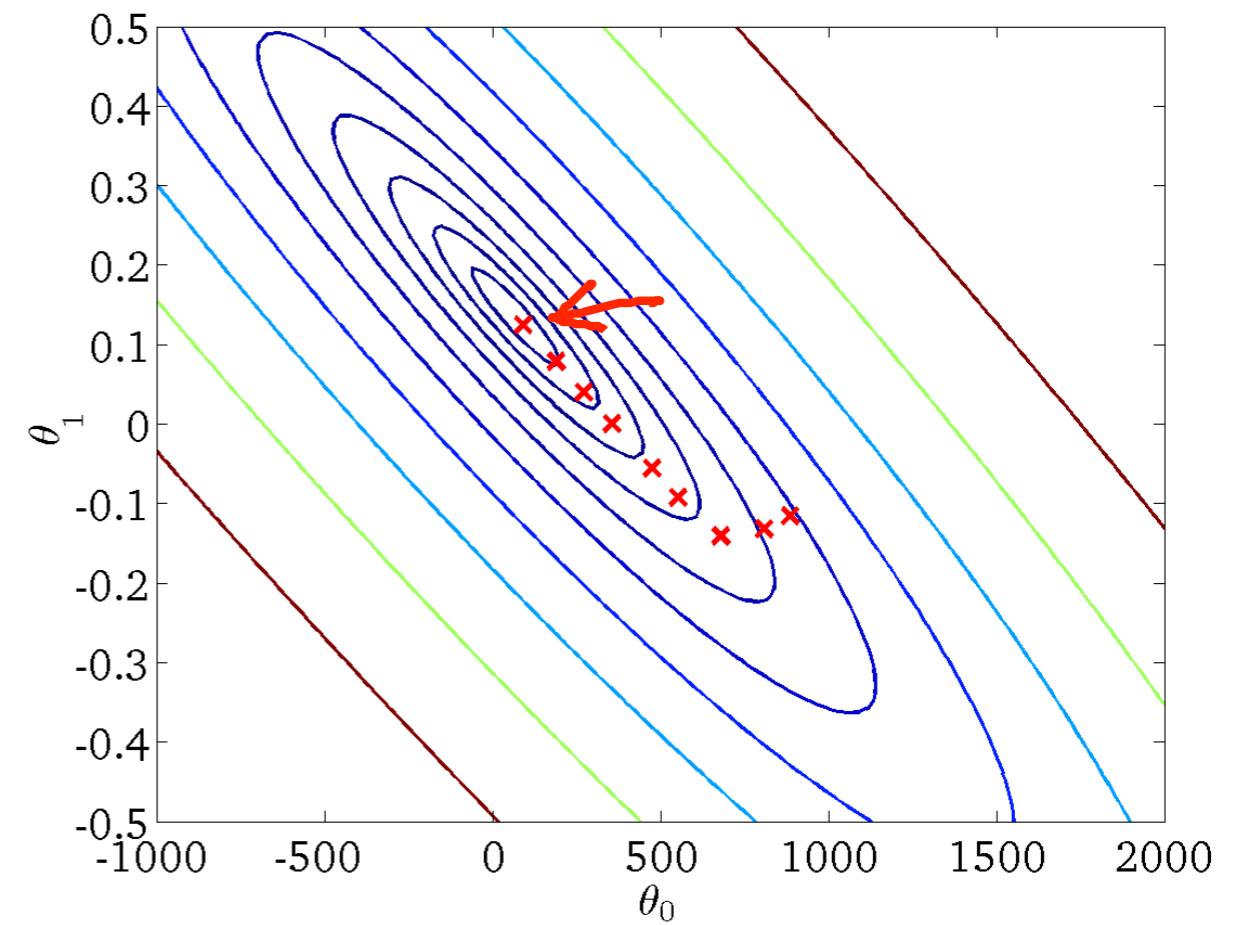
$$h_{\theta}(x)$$

(for fixed θ_0, θ_1 , this is a function of x)



$$J(\theta_0, \theta_1)$$

(function of the parameter θ_0, θ_1)

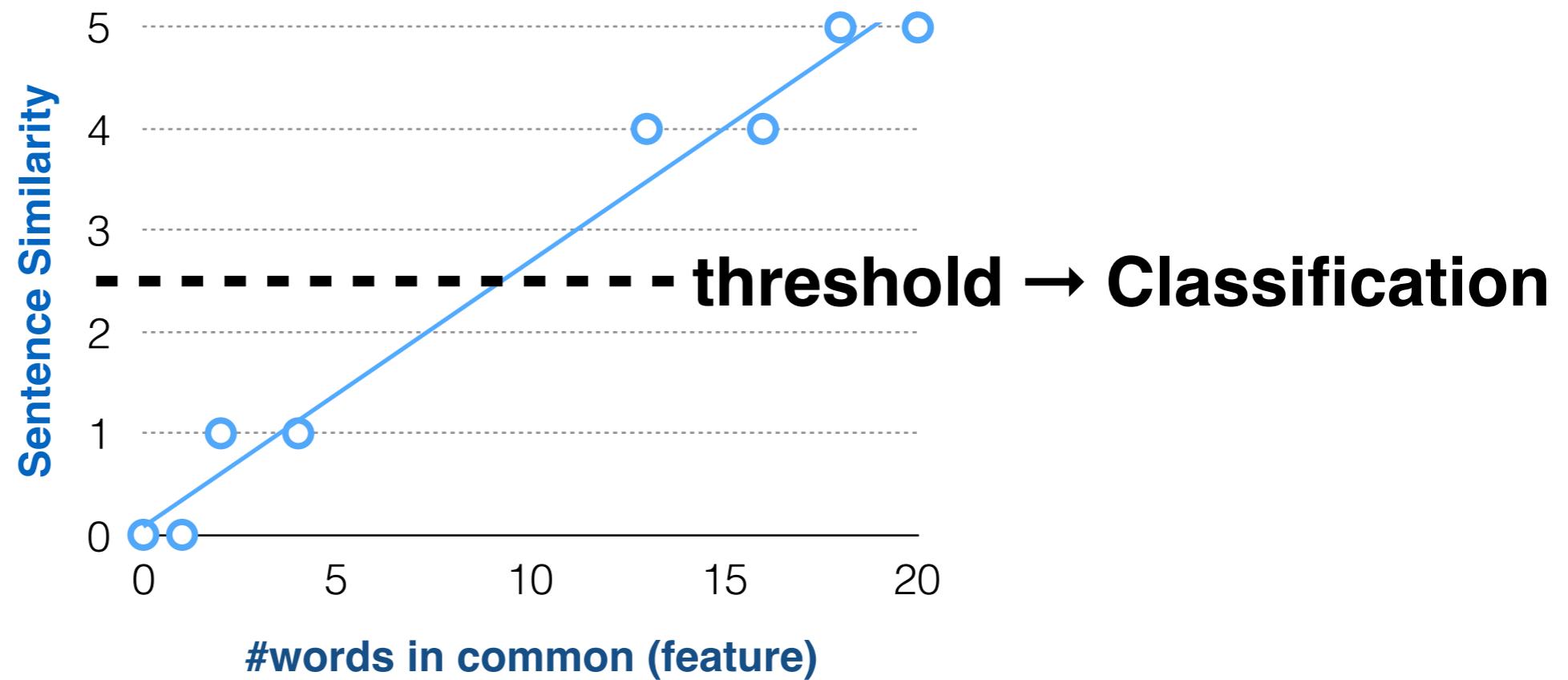


Batch Update

- Each step of gradient descent uses all the training examples

(Recap)

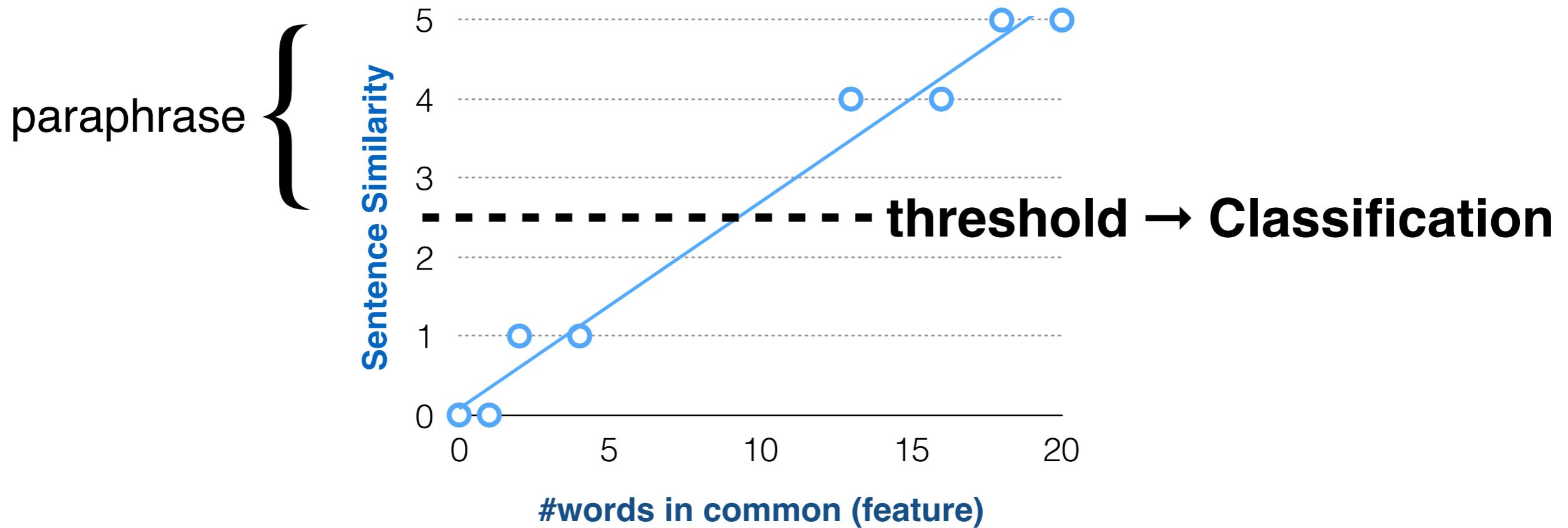
Linear Regression



- also supervised learning (learn from annotated data)
- but for **Regression**: predict **real-valued** output
(Classification: predict discrete-valued output)

(Recap)

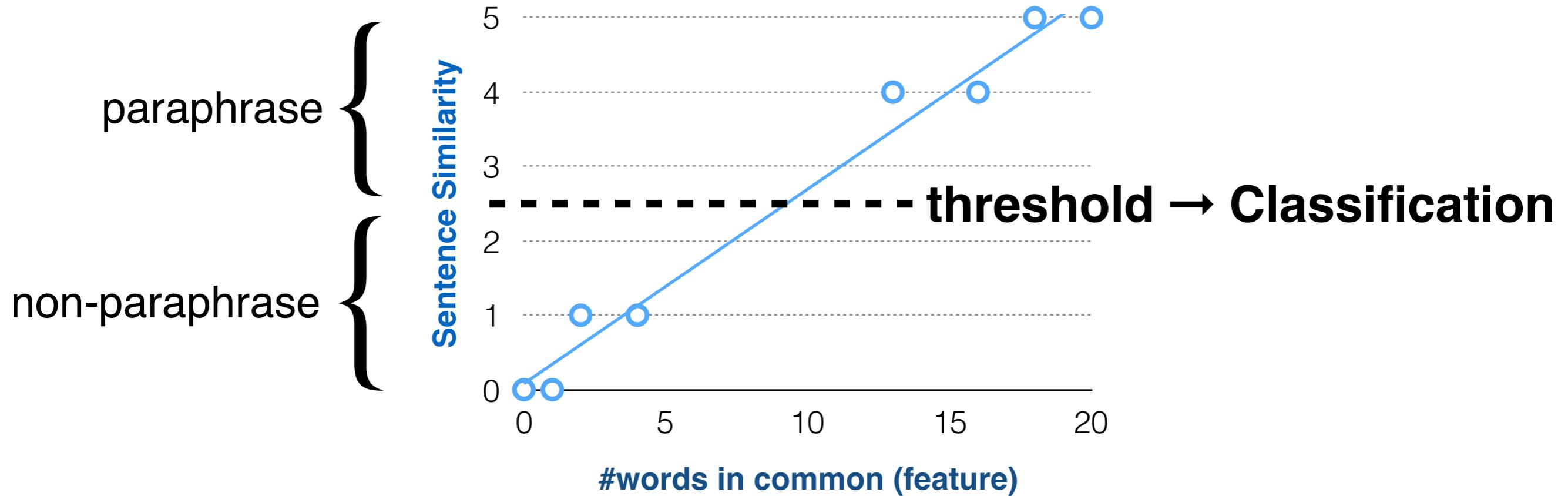
Linear Regression



- also supervised learning (learn from annotated data)
- but for **Regression**: predict **real-valued** output
(Classification: predict discrete-valued output)

(Recap)

Linear Regression



- also supervised learning (learn from annotated data)
- but for **Regression**: predict **real-valued** output
(Classification: predict discrete-valued output)

(Recap)

Linear Regression

- **Hypothesis:**

$$h_{\theta}(x) = \theta_0 + \theta_1 x$$

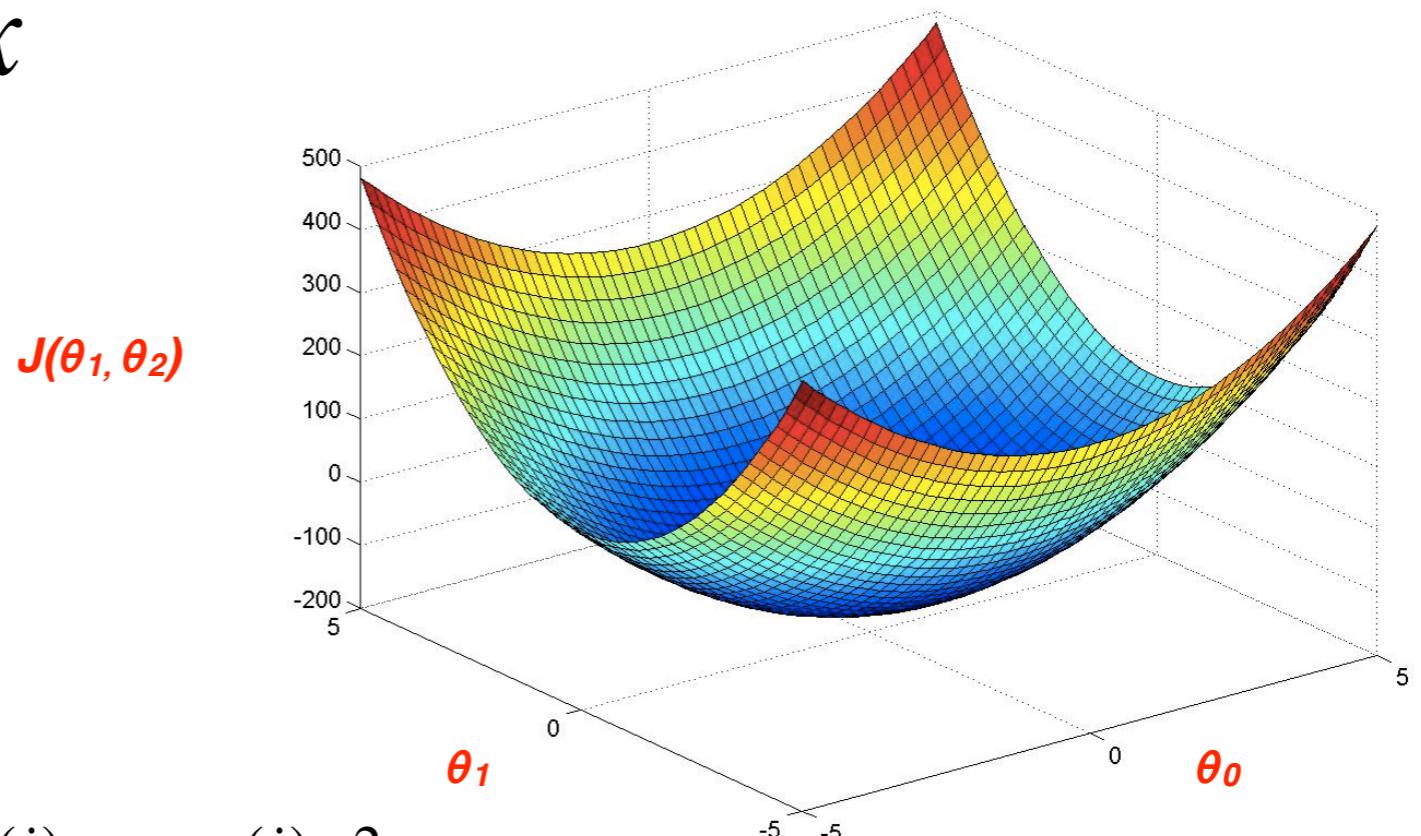
- **Parameters:**

$$\theta_0, \theta_1$$

- **Cost Function:**

$$J(\theta_0, \theta_1) = \frac{1}{2m} \sum_{i=1}^m (h_{\theta}(x^{(i)}) - y^{(i)})^2$$

- **Goal:** $\underset{\theta_0, \theta_1}{\text{minimize}} J(\theta_0, \theta_1)$



(Recap)

Gradient Descent

repeat until convergence {

$$\theta_j := \theta_j - \alpha \frac{\partial}{\partial \theta_j} J(\theta_0, \theta_1)$$

(simultaneous update
for j=0 and j=1)

learning rate

Next Class:

- Logistic Regression (cont')

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