

Social Media & Text Analysis

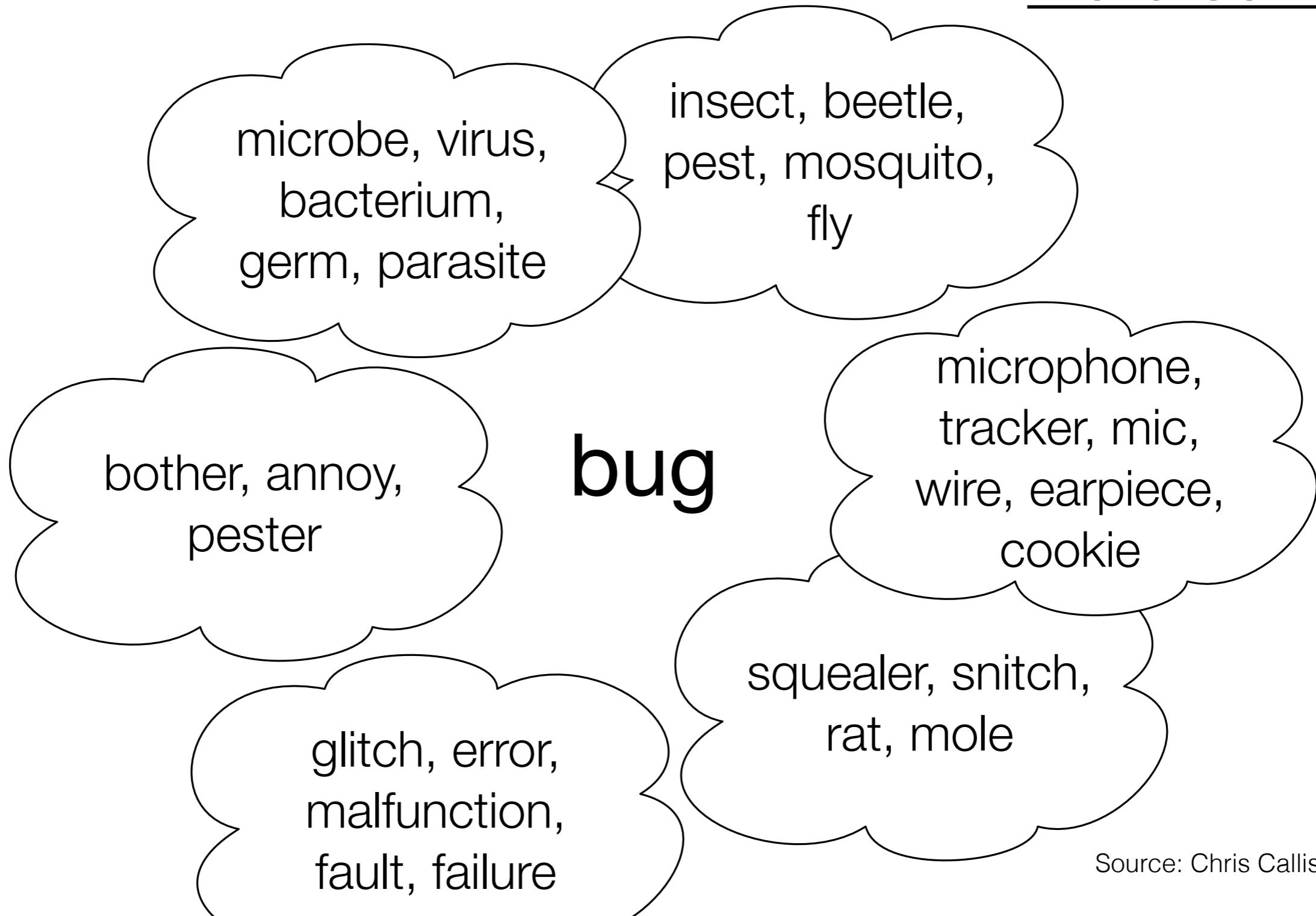
lecture 7 - Paraphrase Identification
and Linear Regression

CSE 5539-0010 Ohio State University
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Website: socialmedia-class.org

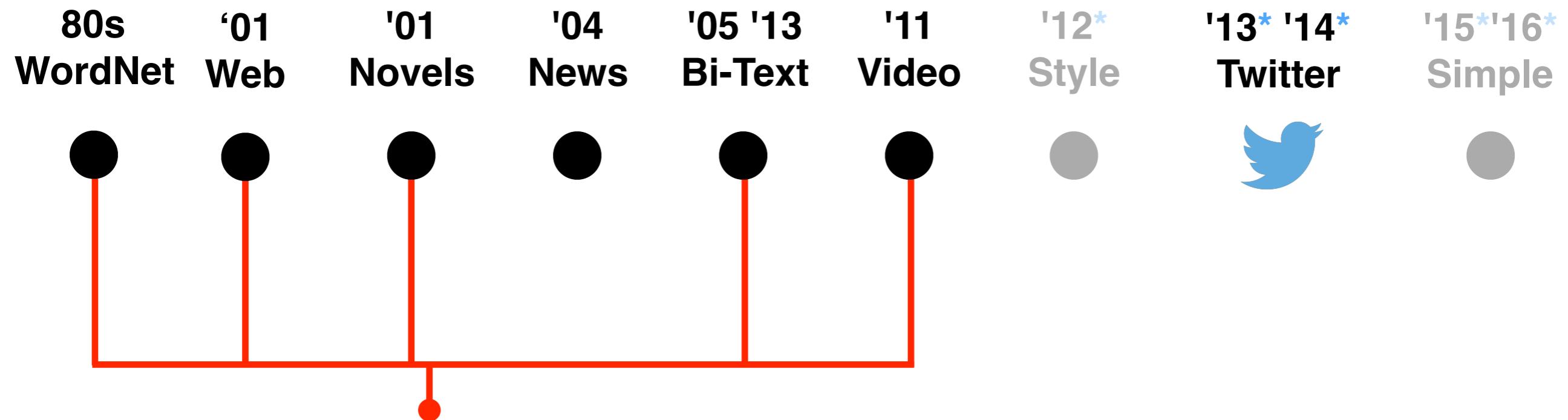
Key Limitations of PPDB?

Key Limitations of PPDB?

word sense



Another Key Limitation



only paraphrases, no non-paraphrases

Paraphrase Identification

obtain sentential paraphrases automatically

Mancini has been sacked by Manchester City

Yes!

Mancini gets the boot from Man City

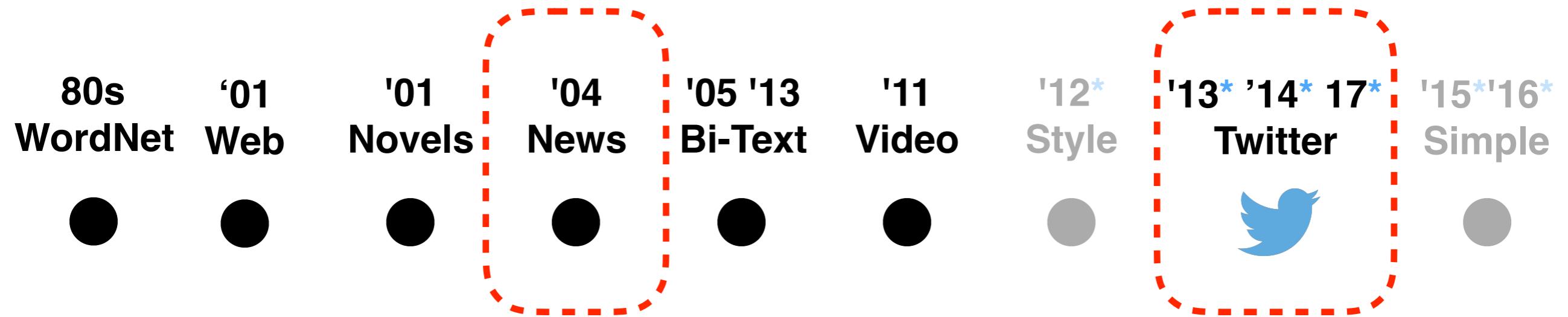
WORLD OF JENKS IS ON AT 11

No!

World of Jenks is my favorite show on tv

(meaningful) non-paraphrases are needed to train classifiers!

Also Non-Paraphrases



(meaningful) non-paraphrases are needed to train classifiers!

News Paraphrase Corpus



Microsoft Research Paraphrase Corpus

also contains some non-paraphrases

Twitter Paraphrase Corpus



Rep. Stacey Newman @staceynewman · 5h

So sad to hear today of former WH Press Sec **James Brady's** passing.
@bradybuzz & family will carry on his legacy of #gunsense.



Jim Sciutto @jimsciutto · 4h

Breaking: Fmr. WH Press Sec. **James Brady** has died at 73, crusader for gun control after wounded in '81 Reagan assassination attempt



NBC News @NBCNews · 2h

James Brady, President Reagan's press secretary shot in 1981 assassination attempt, dead at 73 nbcnews.to/WX1Btq pic.twitter.com/1ZtuEakRd9



also contains a lot of non-paraphrases

Paraphrase Identification:

A Binary Classification Problem

- Input:
 - a sentence pair \mathbf{x}
 - a fixed set of binary classes $Y = \{0, 1\}$
 - Output:
 - a predicted class $y \in Y$ ($y = 0$ or $y = 1$)
- negative (non-paraphrases)**
- positive (paraphrases)**
-
- ```
graph TD; A["negative (non-paraphrases)"] --> B["Y = {0, 1}"]; C["positive (paraphrases)"] --> B;
```

Paraphrase Identification:

# A Binary Classification Problem

- Input:
  - a sentence pair  $\mathbf{x}$
  - a fixed set of binary classes  $\mathbf{Y} = \{0, 1\}$
- Output:
  - a predicted class  $y \in \mathbf{Y}$  ( $y = 0$  or  $y = 1$ )

Classification Method:

# Supervised Machine Learning

- Input:
  - a sentence pair  $\mathbf{x}$
  - a fixed set of binary classes  $\mathbf{Y} = \{0, 1\}$
  - a training set of  $m$  hand-labeled sentence pairs  
 $(\mathbf{x}^{(1)}, \mathbf{y}^{(1)}), \dots, (\mathbf{x}^{(m)}, \mathbf{y}^{(m)})$
- Output:
  - a learned classifier  $\gamma: \mathbf{x} \rightarrow \mathbf{y} \in \mathbf{Y}$  ( $\mathbf{y} = 0$  or  $\mathbf{y} = 1$ )

Classification Method:

# Supervised Machine Learning

- Input:
  - a sentence pair  **$x$  (represented by features)**
  - a fixed set of binary classes  **$Y = \{0, 1\}$**
  - a training set of  **$m$**  hand-labeled sentence pairs  
 **$(x^{(1)}, y^{(1)}), \dots, (x^{(m)}, y^{(m)})$**
- Output:
  - a learned classifier  **$\gamma: x \rightarrow y \in Y$  ( $y = 0$  or  $y = 1$ )**

# (Recap) Classification Method: Supervised Machine Learning

- **Naïve Bayes**
- Logistic Regression
- Support Vector Machines (SVM)
- ...

(Recap)

# Naïve Bayes

- ***Cons:***

features  $t_i$  are assumed independent given the class  $y$

$$P(t_1, t_2, \dots, t_n | y) = P(t_1 | y) \cdot P(t_2 | y) \cdot \dots \cdot P(t_n | y)$$

- ***This will cause problems:***

- correlated features → double-counted evidence
- while parameters are estimated independently
- hurt classifier's accuracy

# Classification Method: Supervised Machine Learning

- Naïve Bayes
- **Logistic Regression**
- Support Vector Machines (SVM)
- ...

# Logistic Regression

- One of the most useful **supervised machine learning algorithm** for classification!
- Generally high performance for a lot of problems.
- Much more robust than Naïve Bayes (better performance on various datasets).

# Before Logistic Regression

**Let's start with  
something simpler!**

# Paraphrase Identification: Simplified Features

- We use only one feature:
  - number of words that two sentences share in common

A very related problem of Paraphrase Identification:  
**Semantic Textual Similarity**

- How similar (close in meaning) two sentences are?

5: completely equivalent in meaning

4: mostly equivalent, but some unimportant details differ

3: roughly equivalent, some important information differs/missing

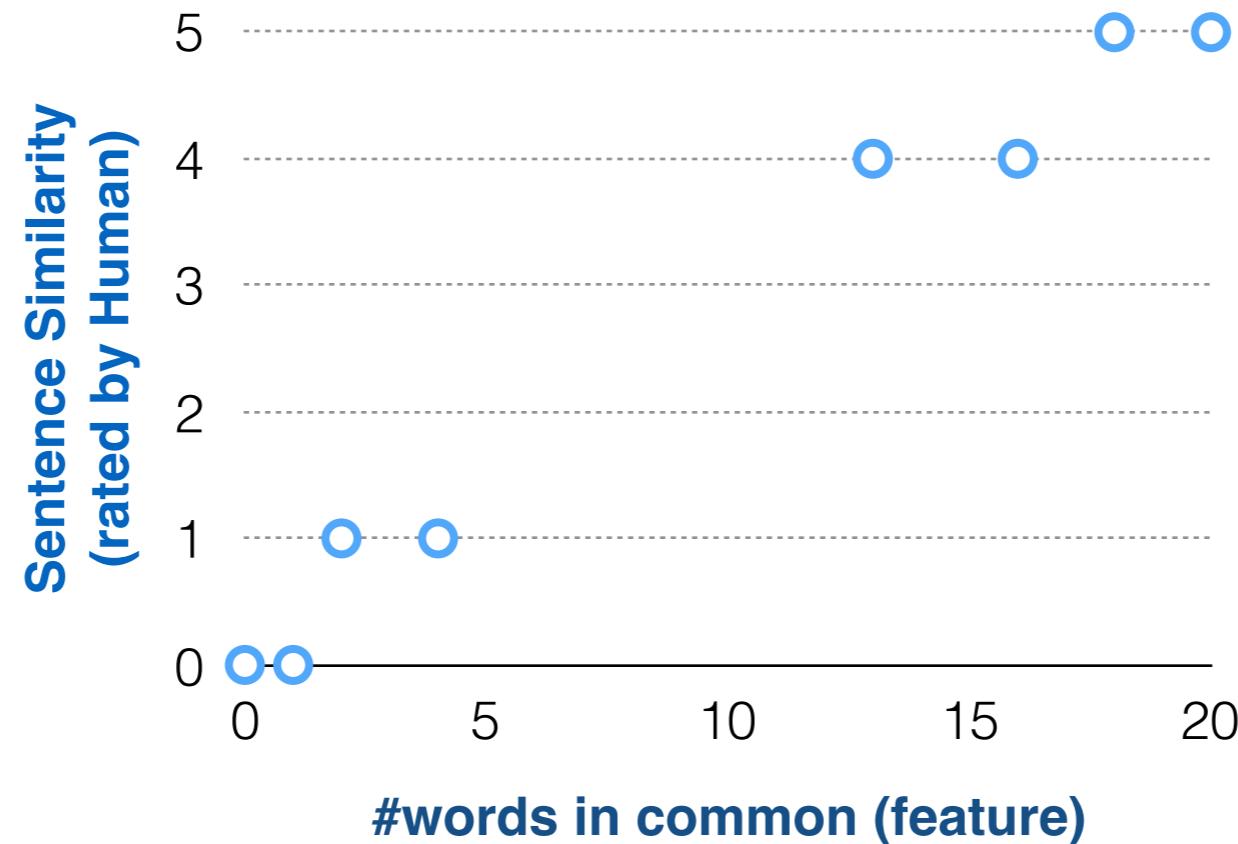
2: not equivalent, but share some details

1: not equivalent, but are on the same topic

0: completely dissimilar

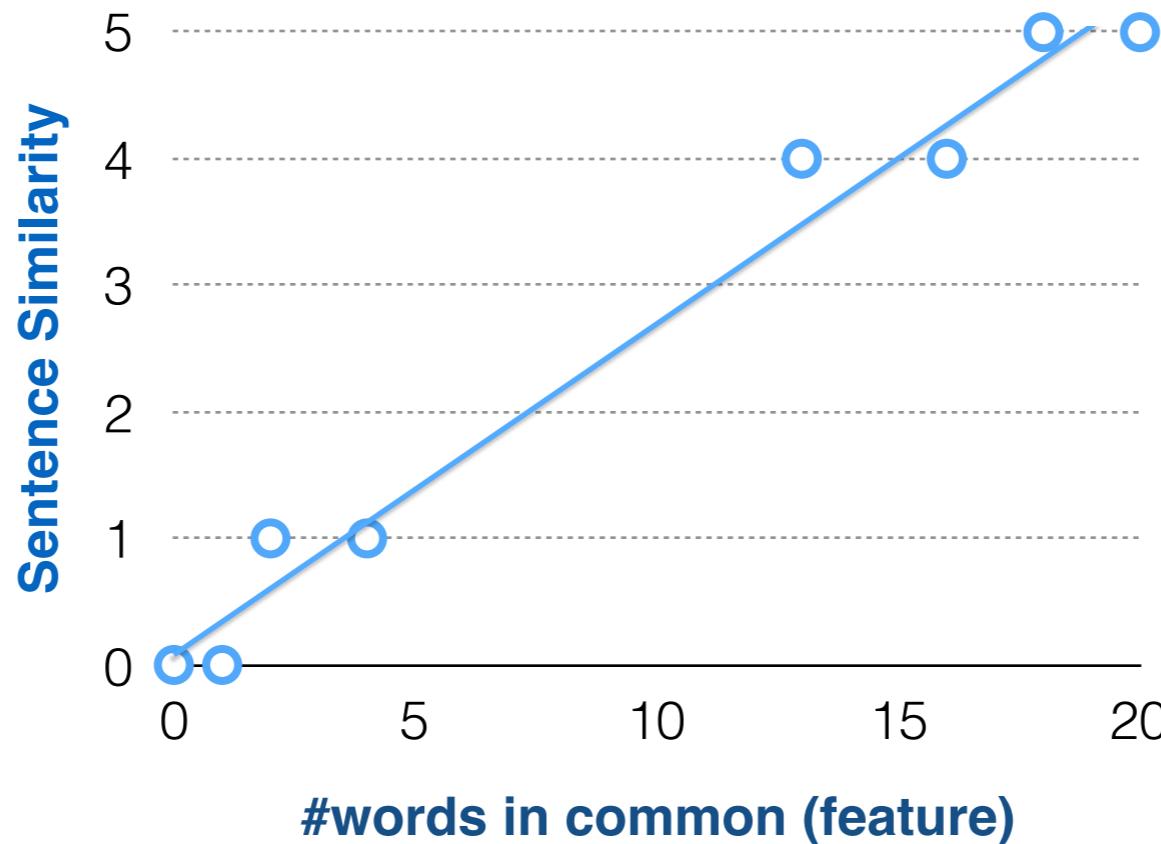
A Simpler Model:

# Linear Regression



A Simpler Model:

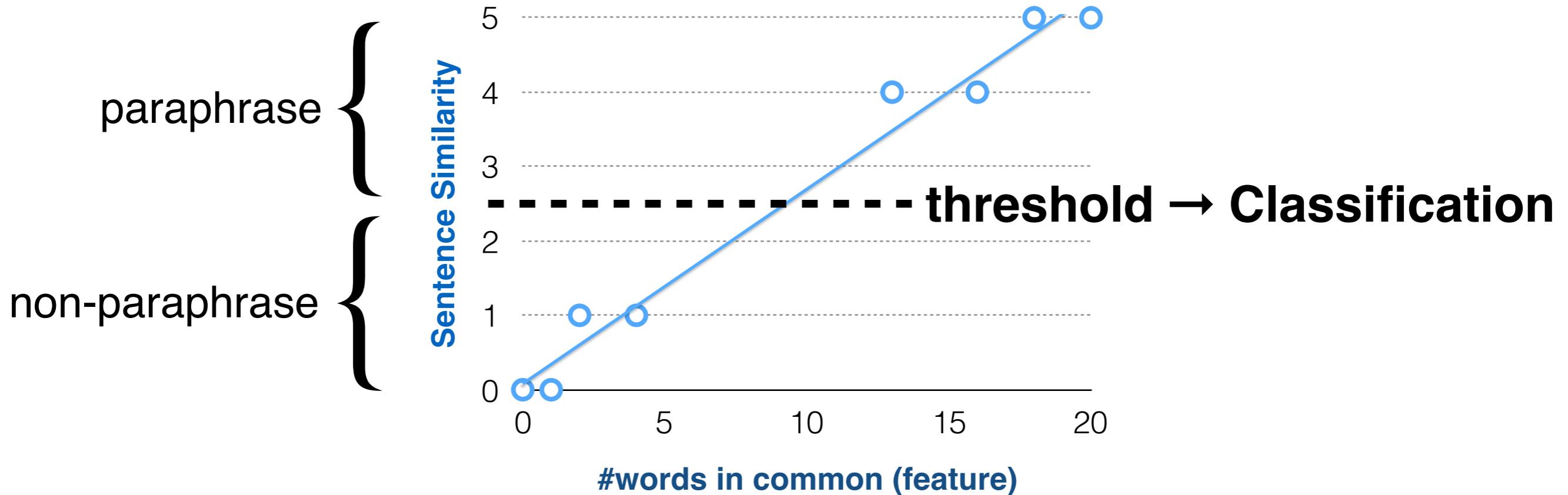
# Linear Regression



- also supervised learning (learn from annotated data)
- but for **Regression**: predict **real-valued** output  
(Classification: predict discrete-valued output)

A Simpler Model:

# Linear Regression



- also supervised learning (learn from labeled data)
- but for **Regression**: predict **real-valued** output  
(Classification: predict discrete-valued output)

# Training Set

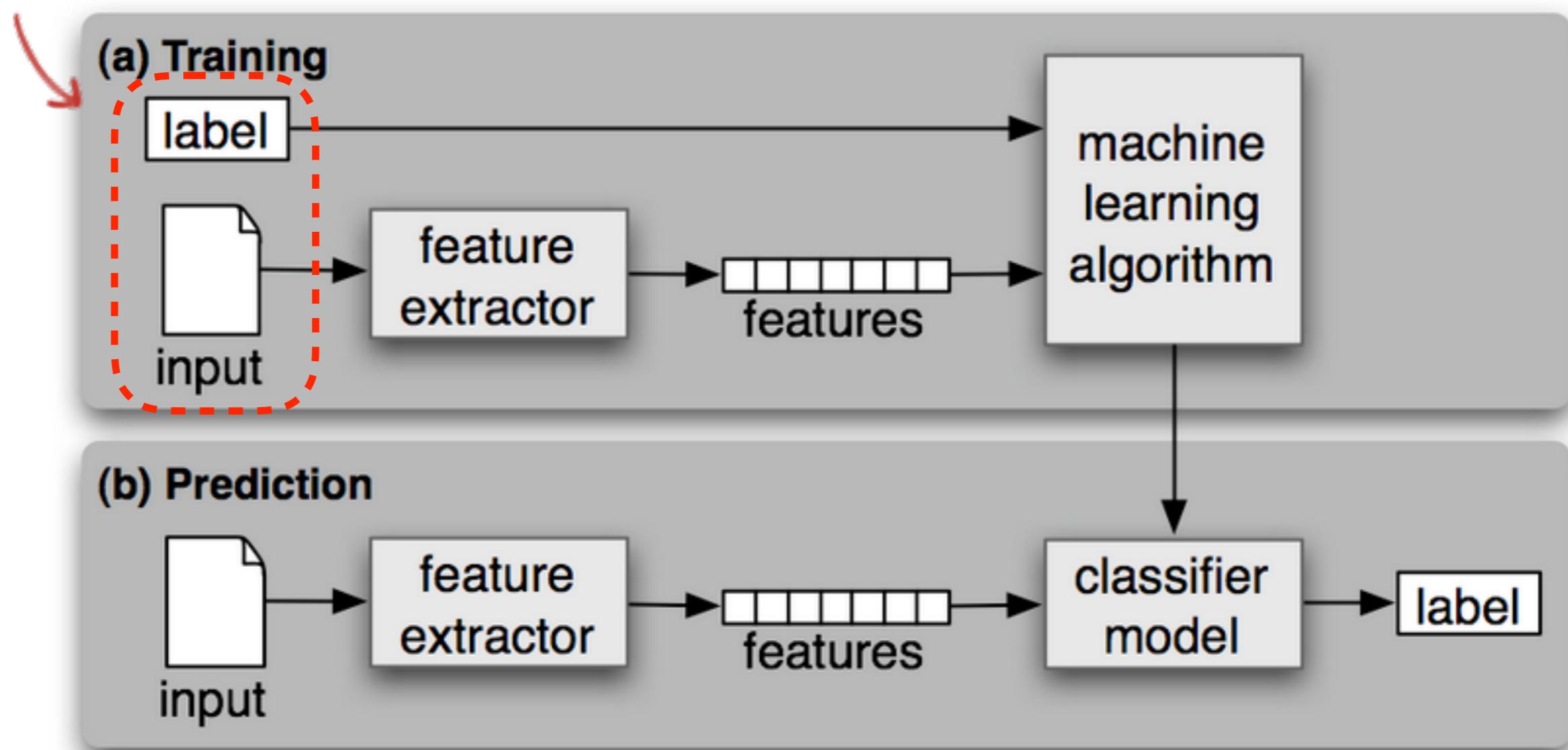
| #words in common<br>( $x$ ) | Sentence Similarity<br>( $y$ ) |
|-----------------------------|--------------------------------|
| 1                           | 0                              |
| 4                           | 1                              |
| 13                          | 4                              |
| 18                          | 5                              |
| ...                         | ...                            |

- $m$  hand-labeled sentence pairs  $(x^{(1)}, y^{(1)}), \dots, (x^{(m)}, y^{(m)})$
- $x$ 's: “input” variable / features
- $y$ 's: “output”/“target” variable

(Recap)

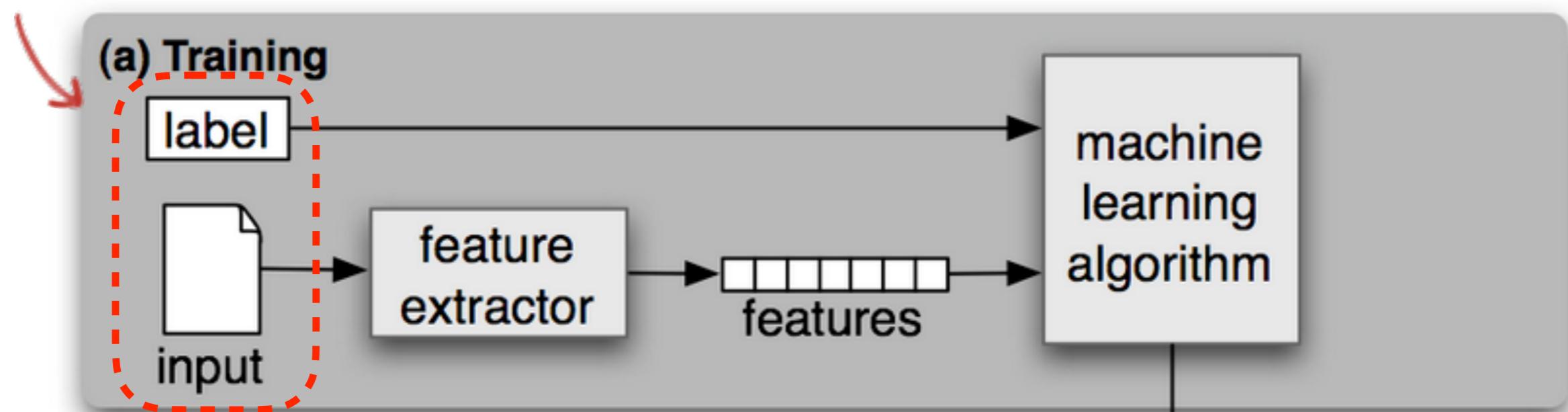
# Supervised Machine Learning

**training set**

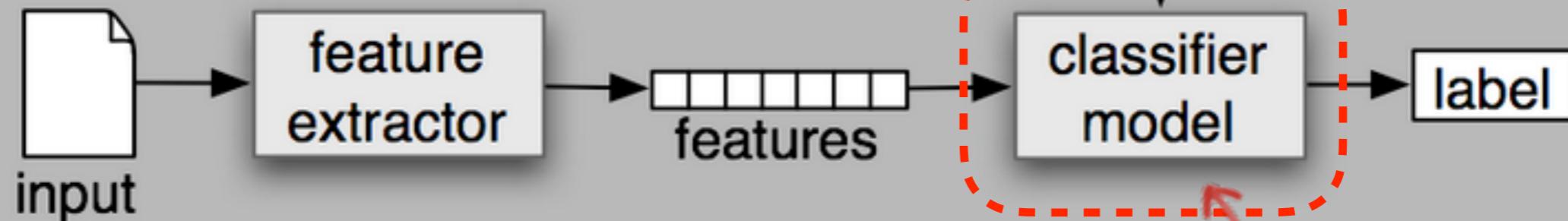


# Supervised Machine Learning

**training set**



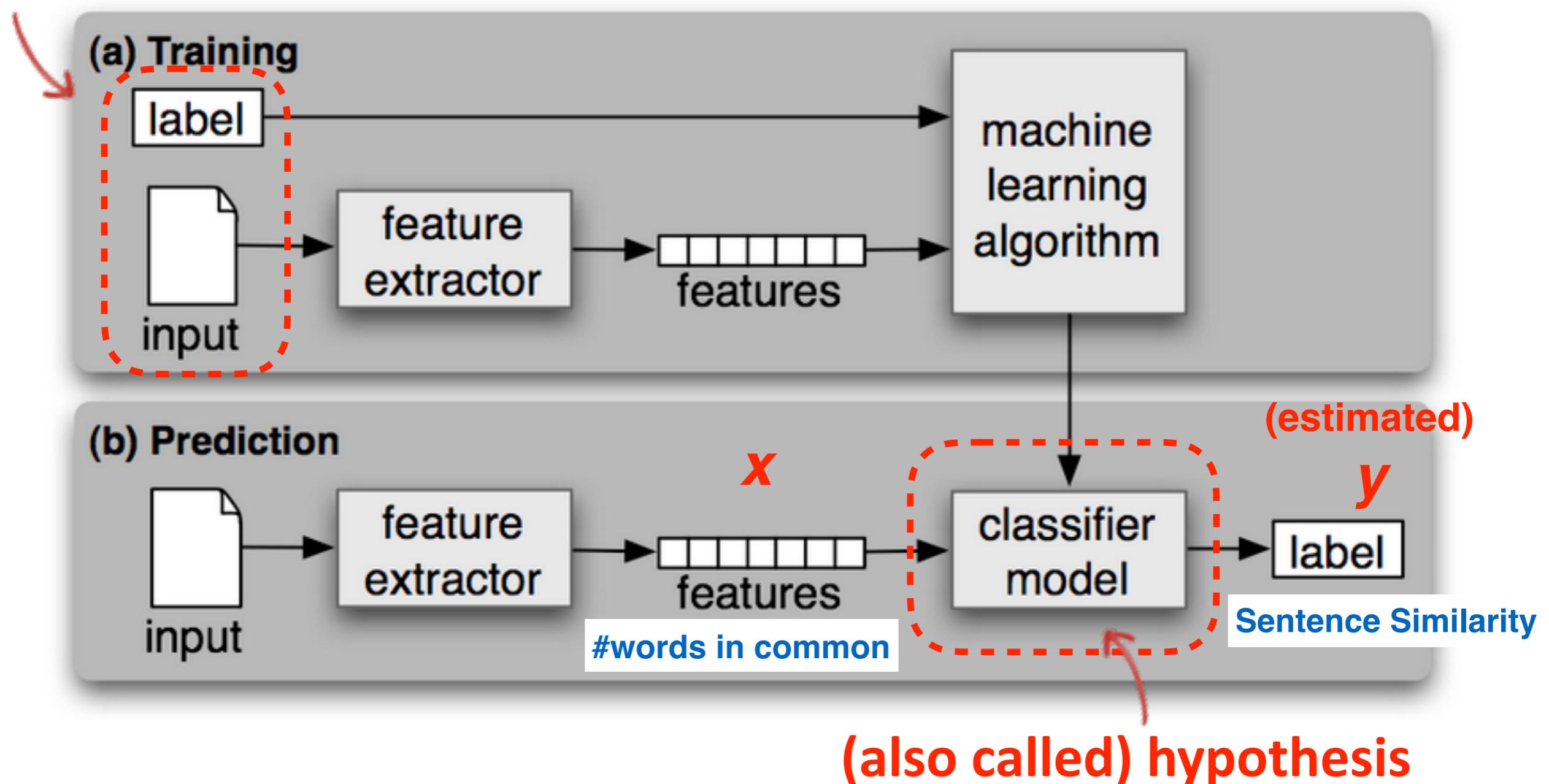
(b) Prediction



**(also called) hypothesis**

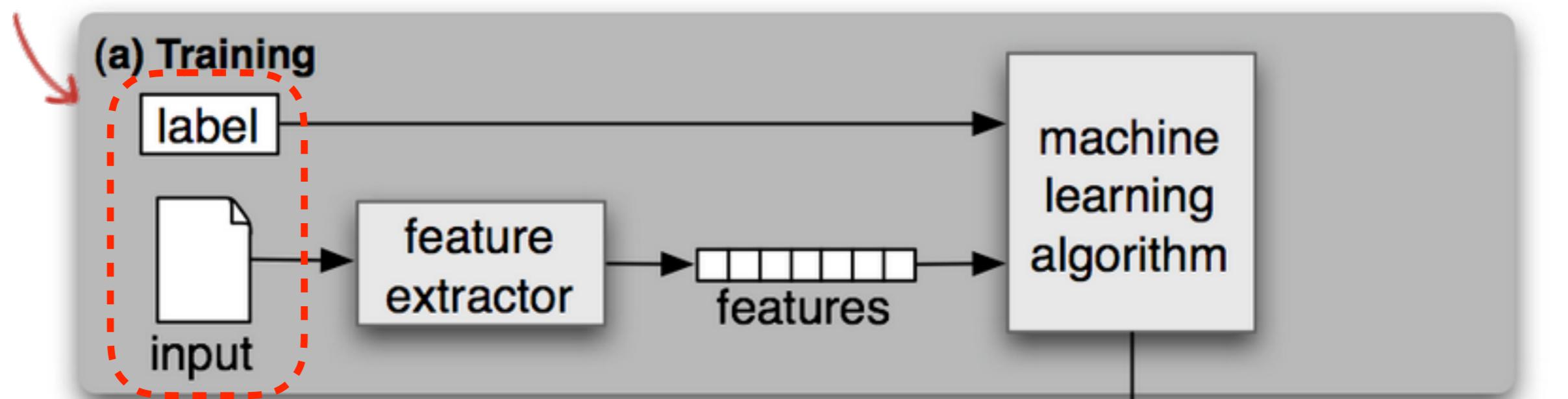
# Supervised Machine Learning

training set



# Supervised Machine Learning

training set



(b) Prediction



feature extractor

$x$   
features

classifier model

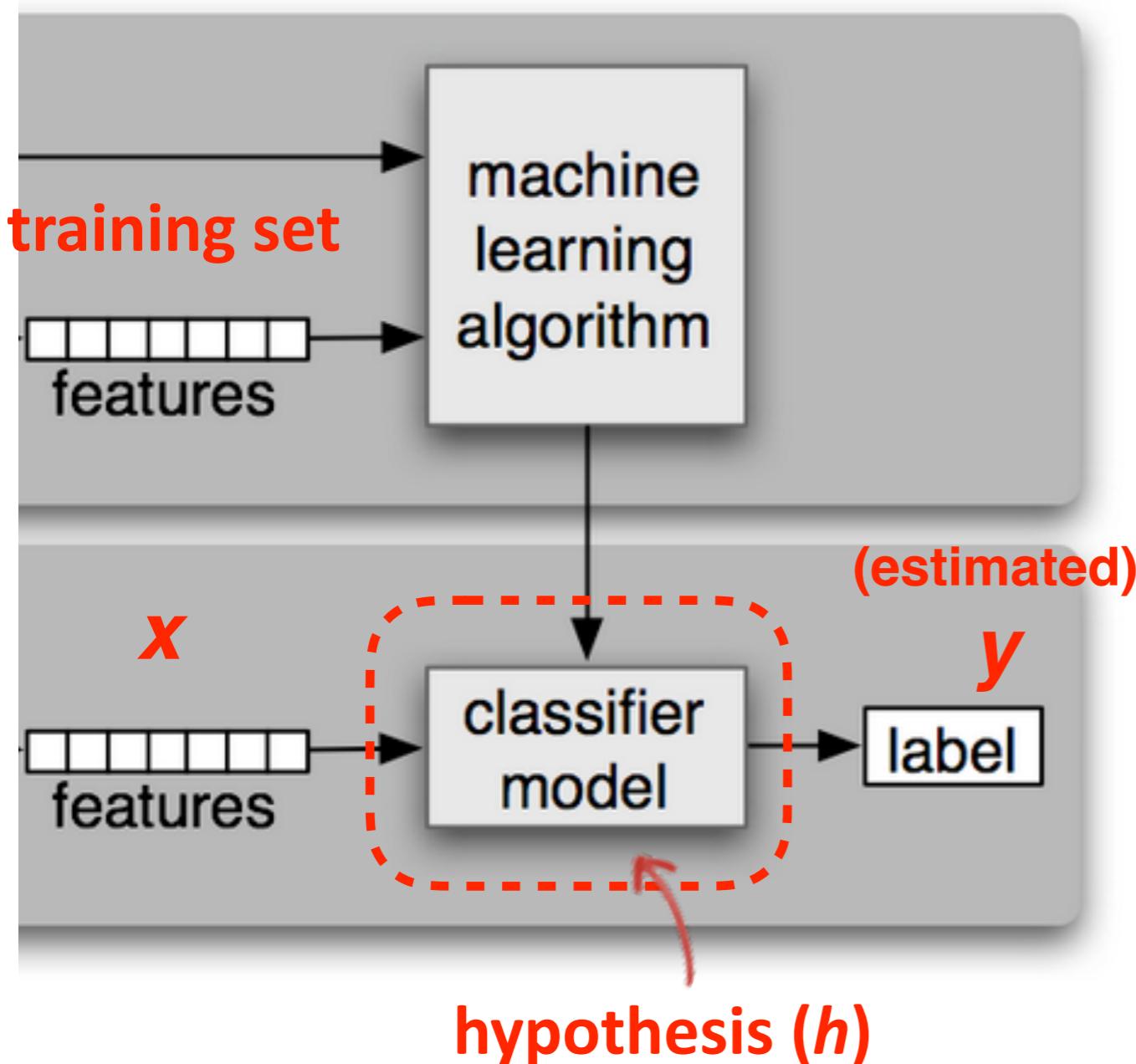
(estimated)  
 $y$

label

(also called) hypothesis

# Linear Regression: Model Representation

- How to represent  $h$  ?



$$h_{\theta}(x) = \theta_0 + \theta_1 x$$

Linear Regression  
w/ one variable

# Linear Regression w/ one variable: Model Representation

| #words in common<br>( $x$ ) | Sentence Similarity<br>( $y$ ) |
|-----------------------------|--------------------------------|
| 1                           | 0                              |
| 4                           | 1                              |
| 13                          | 4                              |
| 18                          | 5                              |
| ...                         | ...                            |

$$h_{\theta}(x) = \theta_0 + \theta_1 x$$

- $m$  hand-labeled sentence pairs  $(\mathbf{x}^{(1)}, \mathbf{y}^{(1)}), \dots, (\mathbf{x}^{(m)}, \mathbf{y}^{(m)})$
- $\theta$ 's: parameters

# Linear Regression w/ one variable: Model Representation

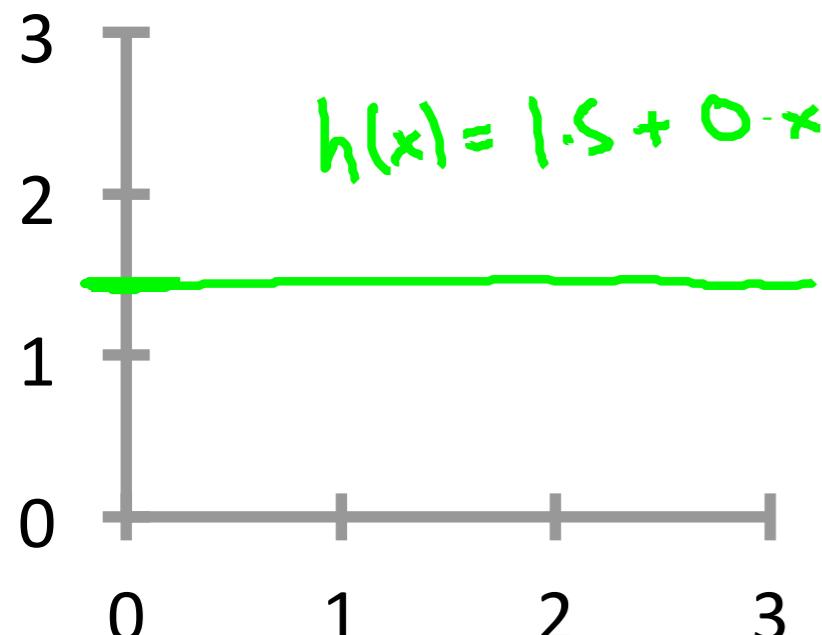
| #words in common<br>( $x$ ) | Sentence Similarity<br>( $y$ ) |
|-----------------------------|--------------------------------|
| 1                           | 0                              |
| 4                           | 1                              |
| 13                          | 4                              |
| 18                          | 5                              |
| ...                         | ...                            |

$$h_{\theta}(x) = \theta_0 + \theta_1 x$$

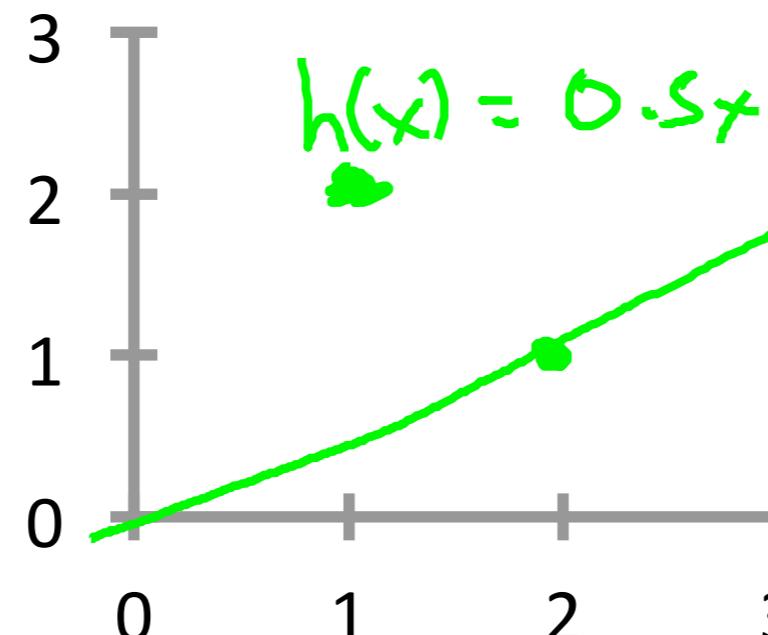
- $m$  hand-labeled sentence pairs  $(x^{(1)}, y^{(1)}), \dots, (x^{(m)}, y^{(m)})$
- $\theta$ 's: parameters

# Linear Regression w/ one variable:: Model Representation

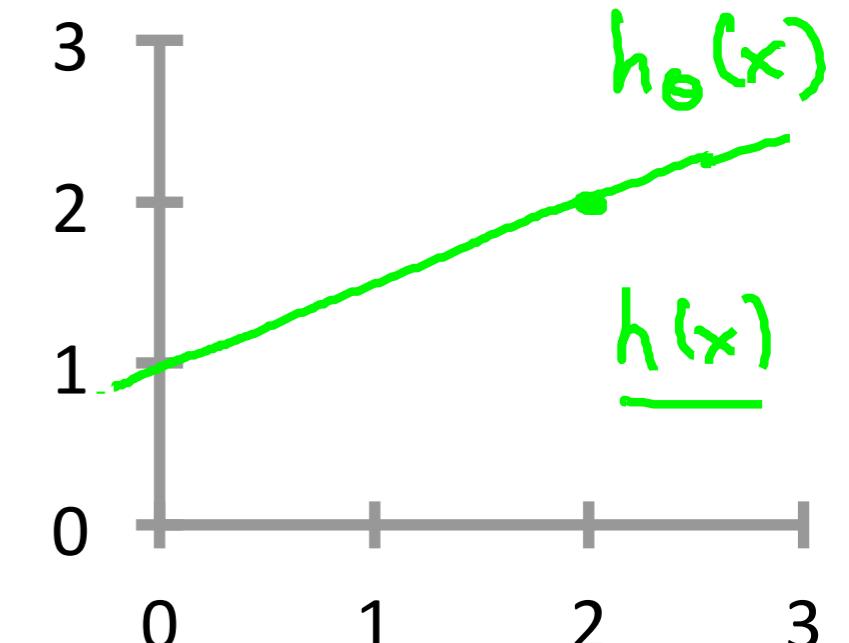
$$\underline{h_{\theta}(x) = \theta_0 + \theta_1 x}$$



$$\begin{aligned} \rightarrow \theta_0 &= 1.5 \\ \rightarrow \theta_1 &= 0 \end{aligned}$$

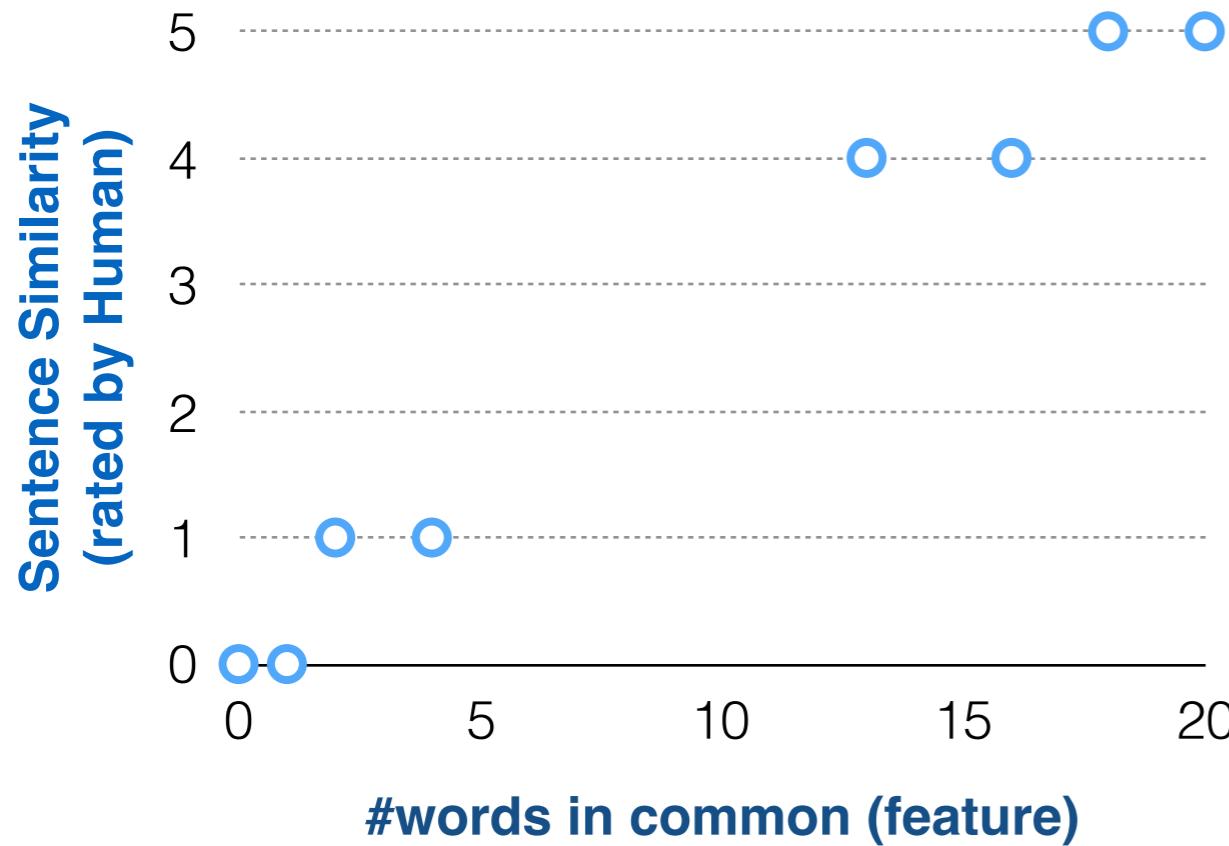


$$\begin{aligned} \rightarrow \theta_0 &= 0 \\ \rightarrow \theta_1 &= 0.5 \end{aligned}$$



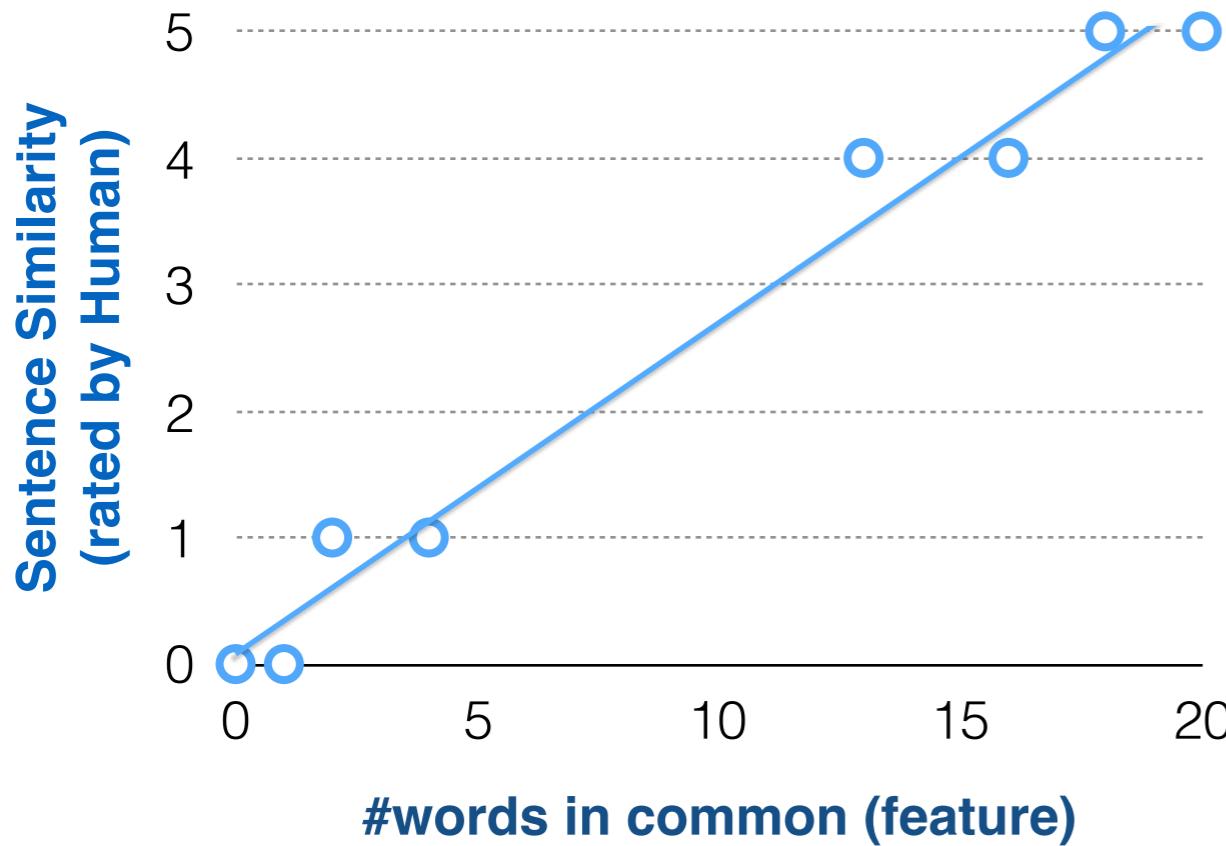
$$\begin{aligned} \rightarrow \theta_0 &= 1 \\ \rightarrow \theta_1 &= 0.5 \end{aligned}$$

# Linear Regression w/ one variable: Cost Function



- **Idea:** choose  $\theta_0, \theta_1$  so that  $h_{\theta}(x)$  is close to  $y$  for training examples  $(x, y)$

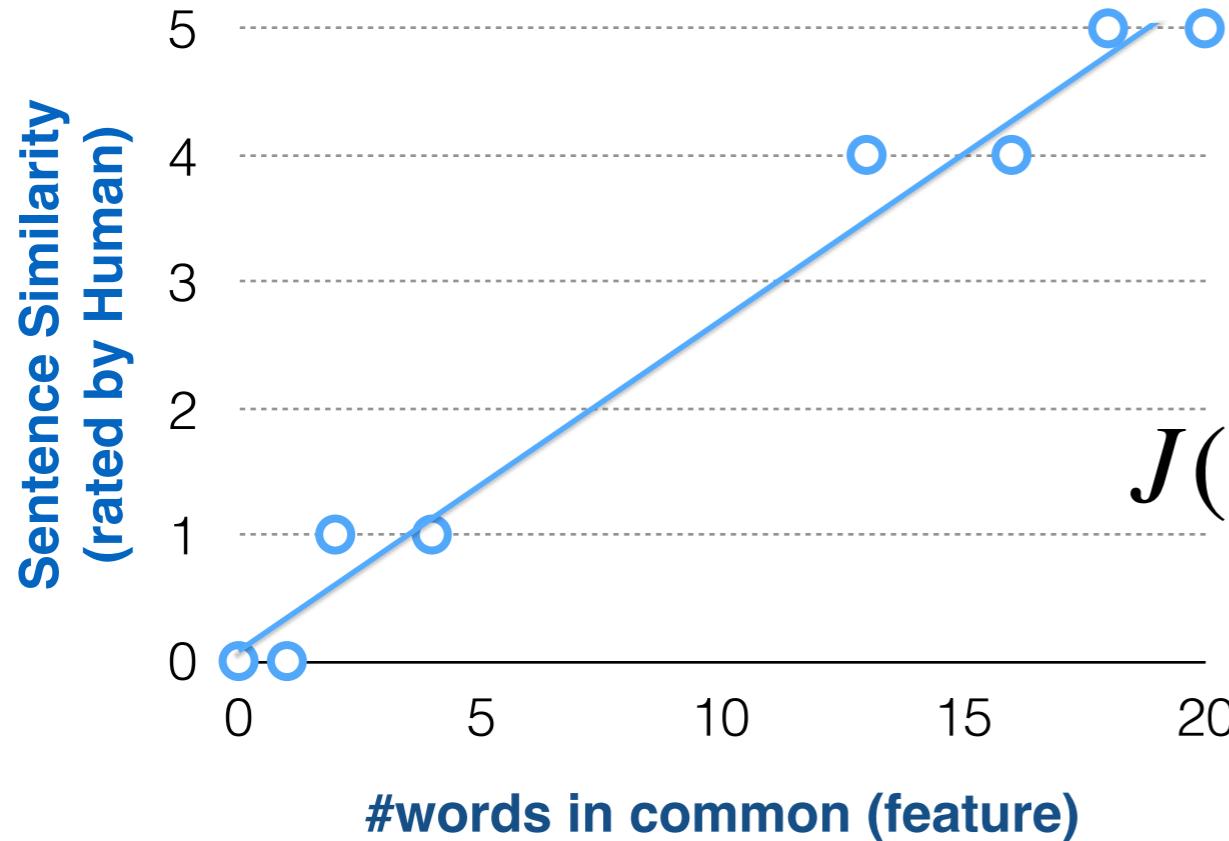
# Linear Regression w/ one variable: Cost Function



- **Idea:** choose  $\theta_0, \theta_1$  so that  $h_{\theta}(x)$  is close to  $y$  for training examples  $(x, y)$

Linear Regression w/ one variable:

# Cost Function



**squared error function:**

$$J(\theta_0, \theta_1) = \frac{1}{2m} \sum_{i=1}^m (h_{\theta}(x^{(i)}) - y^{(i)})^2$$

- **Idea:** choose  $\theta_0, \theta_1$  so that  $h_{\theta}(x)$  is close to  $y$  for training examples  $(x, y)$

$$\underset{\theta_0, \theta_1}{\text{minimize}} J(\theta_0, \theta_1)$$

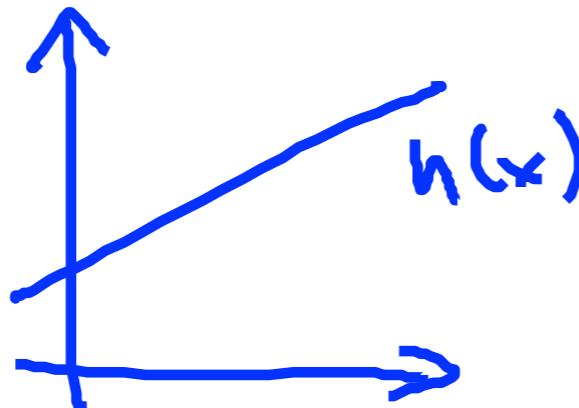
# Linear Regression

- **Hypothesis:**

$$h_{\theta}(x) = \theta_0 + \theta_1 x$$

- **Parameters:**

$$\theta_0, \theta_1$$



- **Cost Function:**

$$J(\theta_0, \theta_1) = \frac{1}{2m} \sum_{i=1}^m (h_{\theta}(x^{(i)}) - y^{(i)})^2$$

- **Goal:**  $\underset{\theta_0, \theta_1}{\text{minimize}} J(\theta_0, \theta_1)$

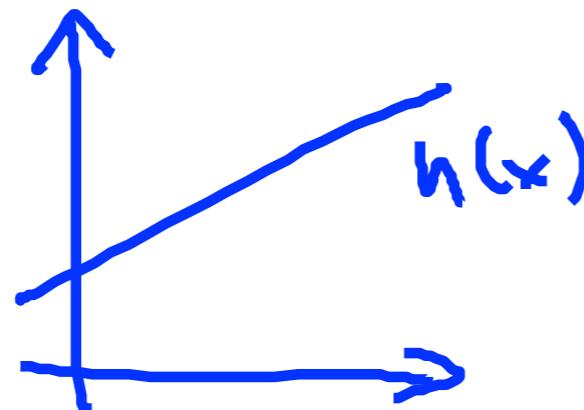
# Linear Regression

- Hypothesis:

$$h_{\theta}(x) = \theta_0 + \theta_1 x$$

- Parameters:

$$\theta_0, \theta_1$$



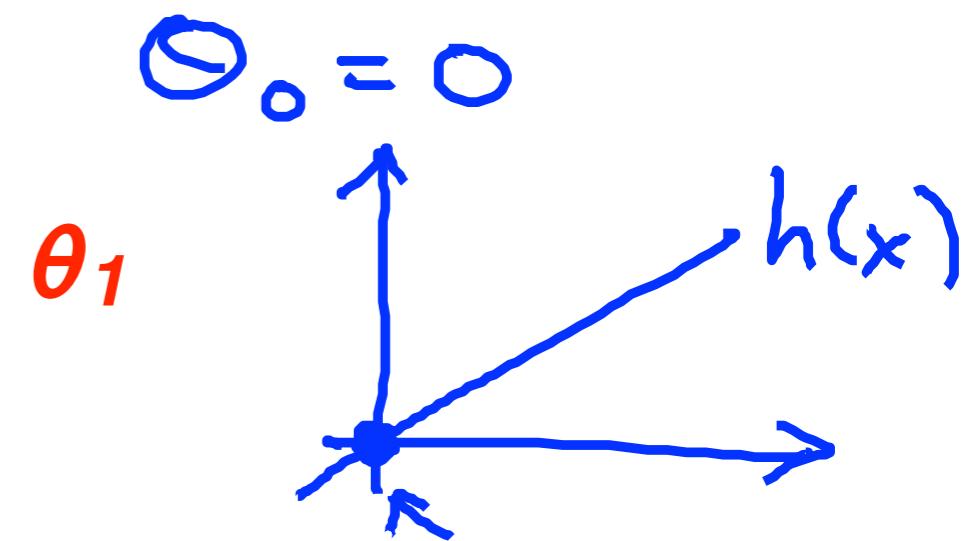
- Cost Function:

$$J(\theta_0, \theta_1) = \frac{1}{2m} \sum_{i=1}^m (h_{\theta}(x^{(i)}) - y^{(i)})^2$$

- Goal:  $\underset{\theta_0, \theta_1}{\text{minimize}} J(\theta_0, \theta_1)$

Simplified

$$h_{\theta}(x) = \theta_1 x$$



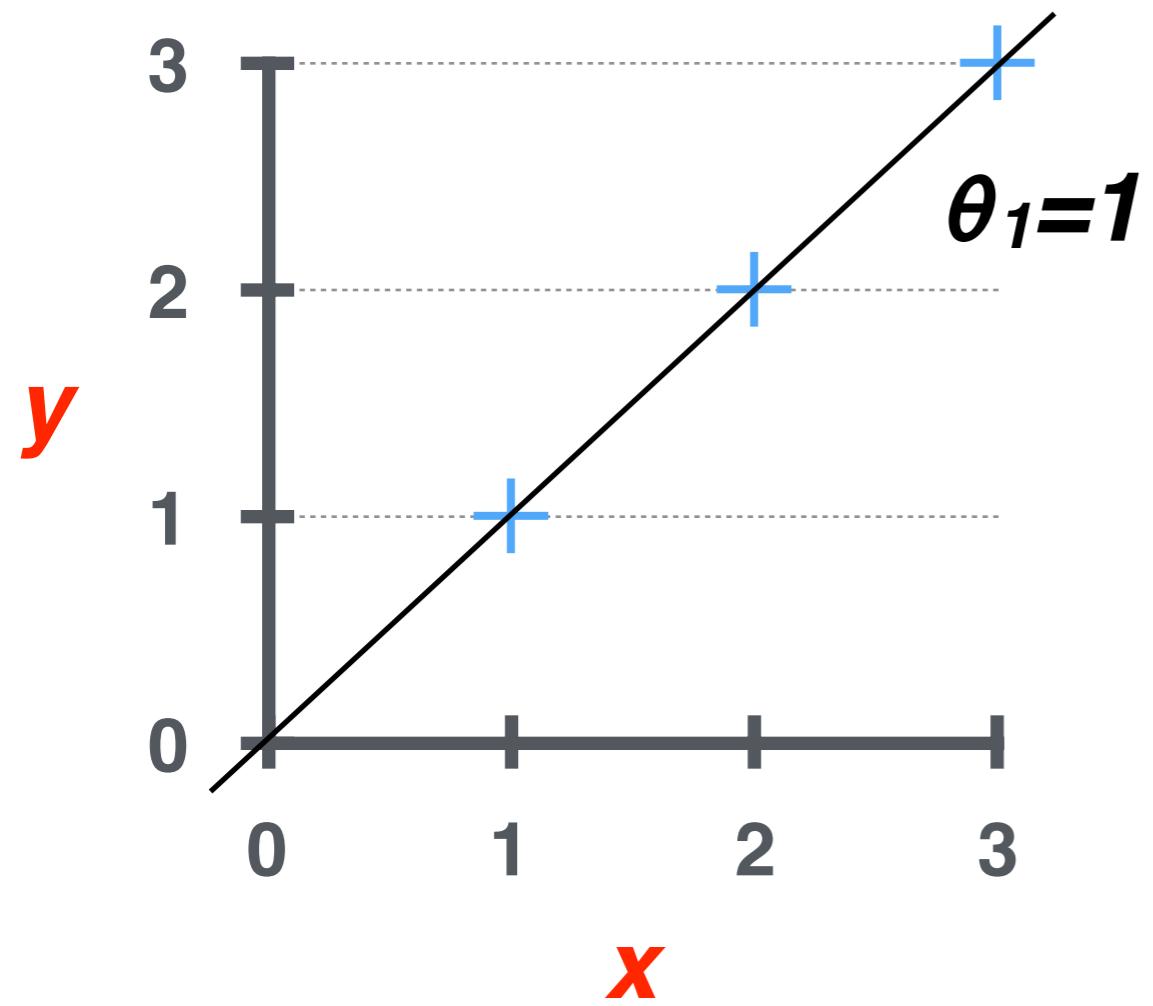
$$J(\theta_1) = \frac{1}{2m} \sum_{i=1}^m (h_{\theta}(x^{(i)}) - y^{(i)})^2$$

$$\underset{\theta_1}{\text{minimize}} J(\theta_1)$$

# Hypothesis

$$h_{\theta}(x)$$

(for fixed  $\theta_1$ , this is a function of  $x$ )



# Cost Function

$$J(\theta_1)$$

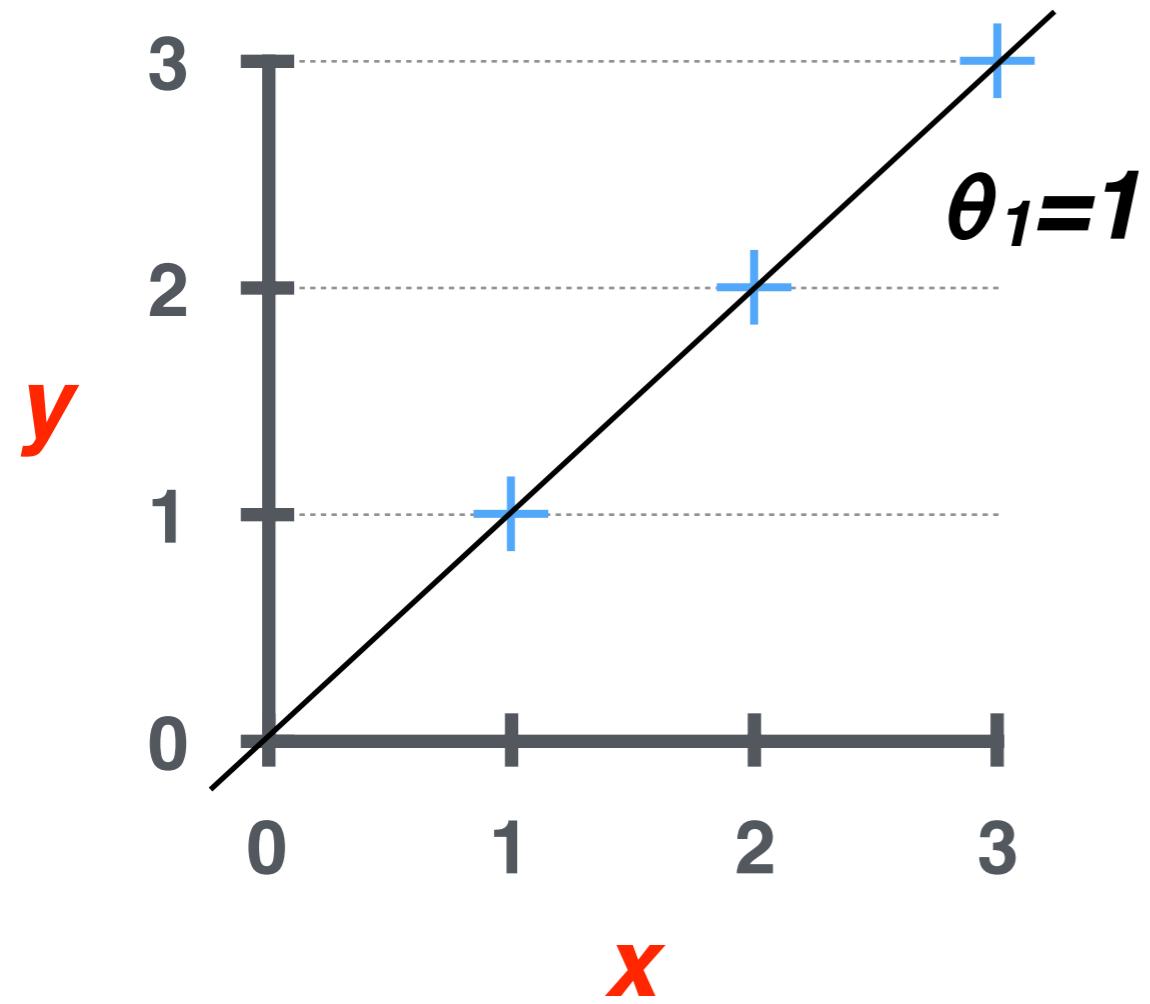
(function of the parameter  $\theta_1$ )

Q:  $J(1) = ?$

# Hypothesis

$$h_{\theta}(x)$$

(for fixed  $\theta_1$ , this is a function of  $x$ )



# Cost Function

$$J(\theta_1)$$

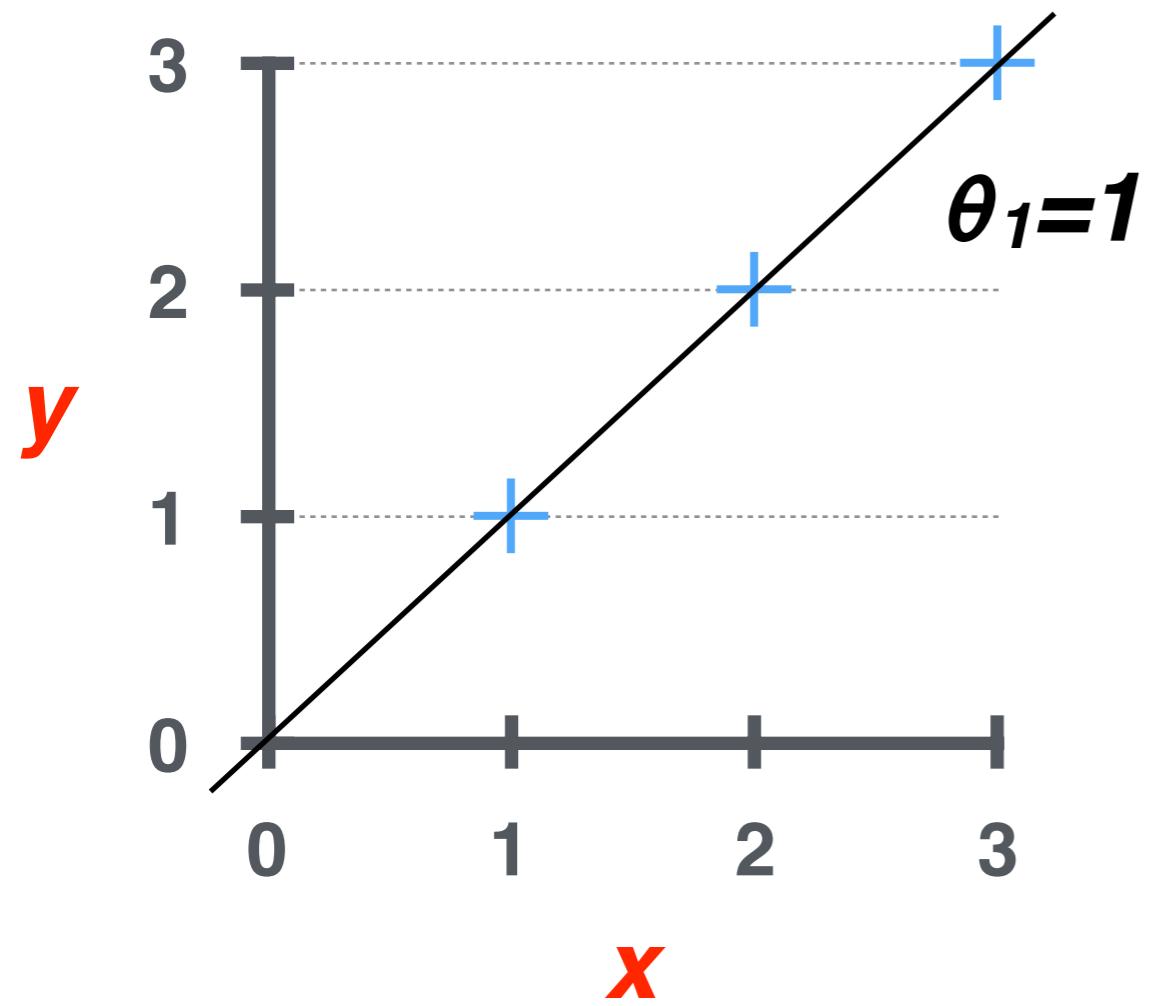
(function of the parameter  $\theta_1$ )

$$J(1) = \frac{1}{2 \times 3} [(1 - 1)^2 + (2 - 2)^2 + (3 - 3)^2] = 0$$

# Hypothesis

$$h_{\theta}(x)$$

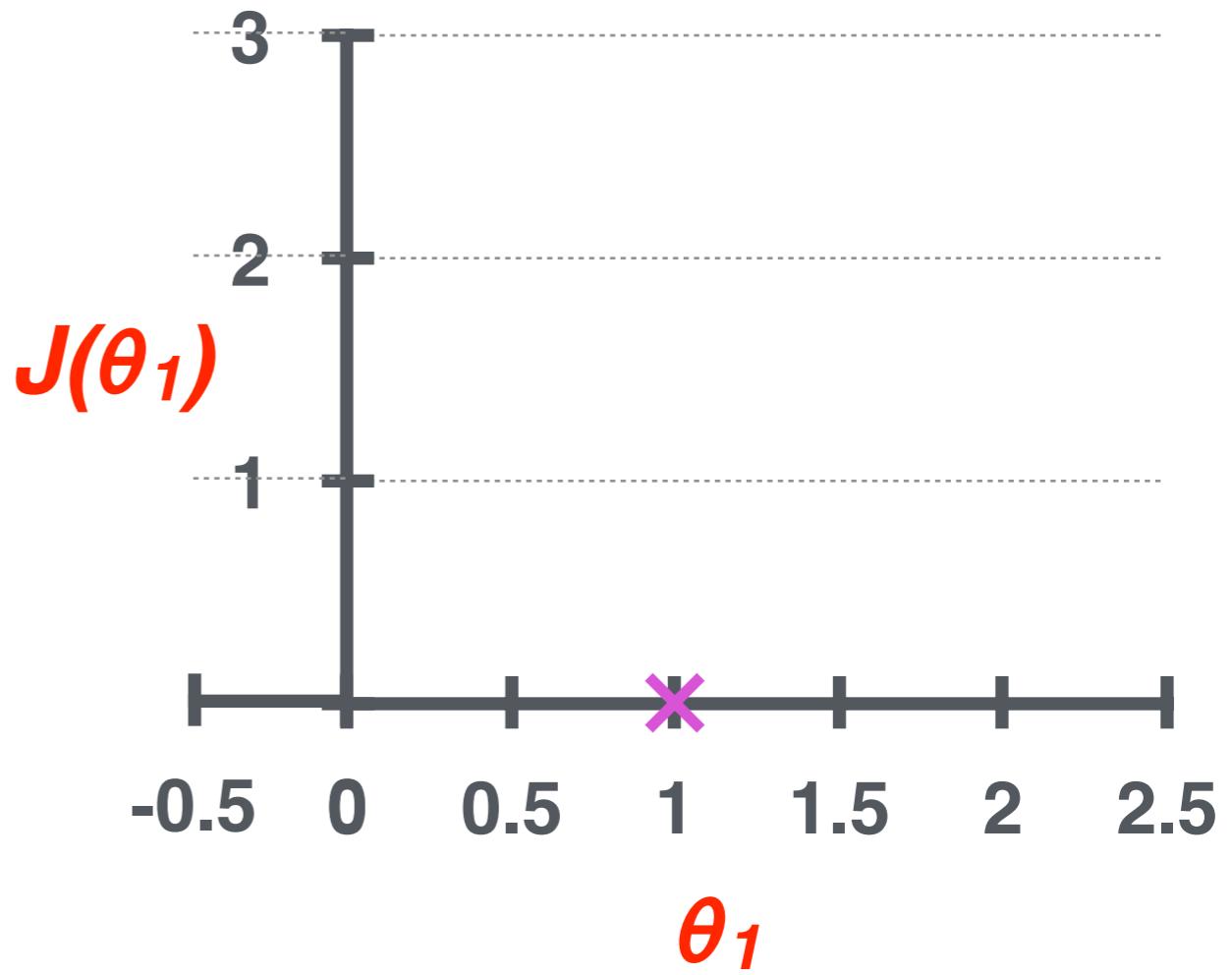
(for fixed  $\theta_1$ , this is a function of  $x$ )



# Cost Function

$$J(\theta_1)$$

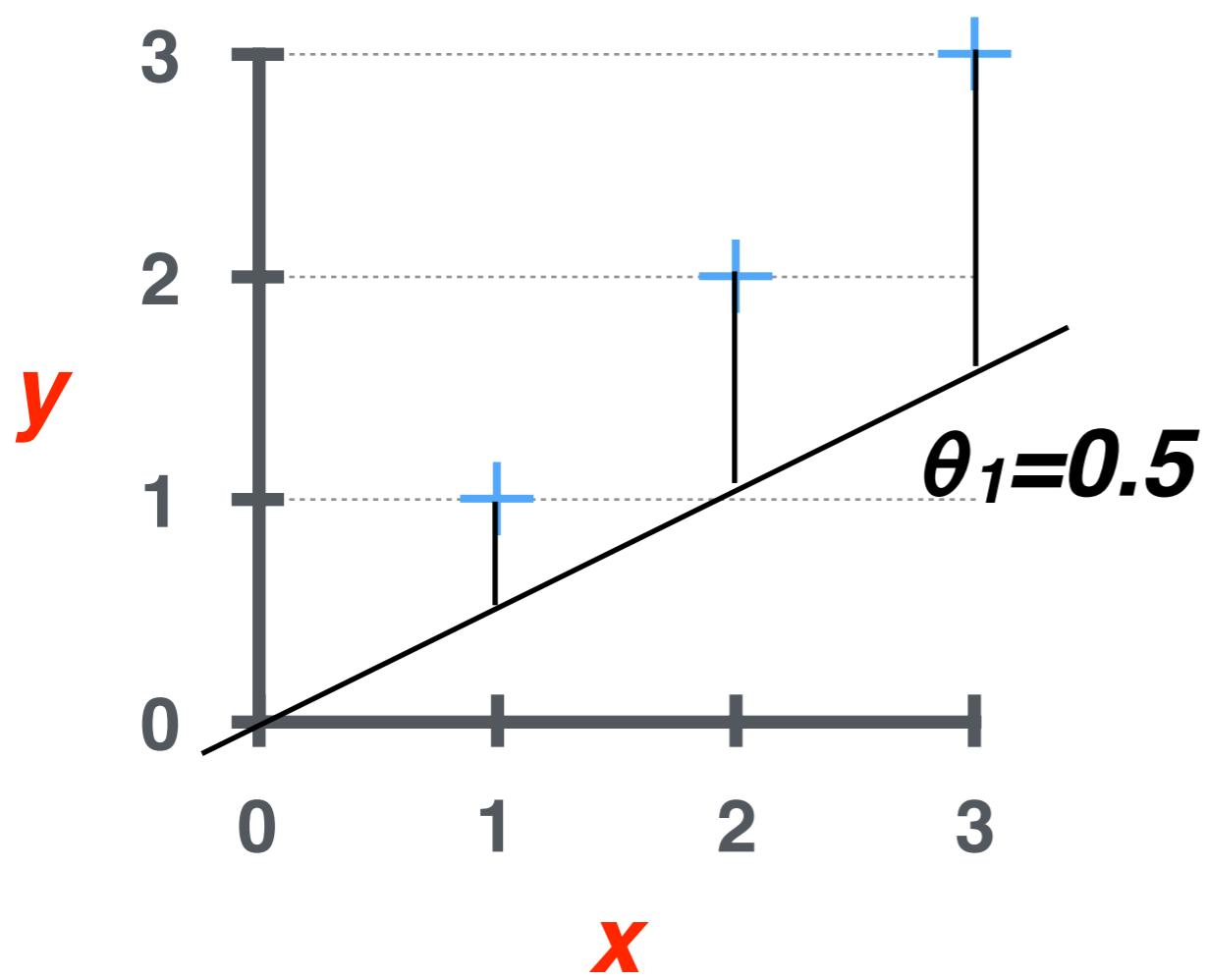
(function of the parameter  $\theta_1$ )



$$J(1) = \frac{1}{2 \times 3} [(1 - 1)^2 + (2 - 2)^2 + (3 - 3)^2] = 0$$

$$h_{\theta}(x)$$

(for fixed  $\theta_1$ , this is a function of  $x$ )

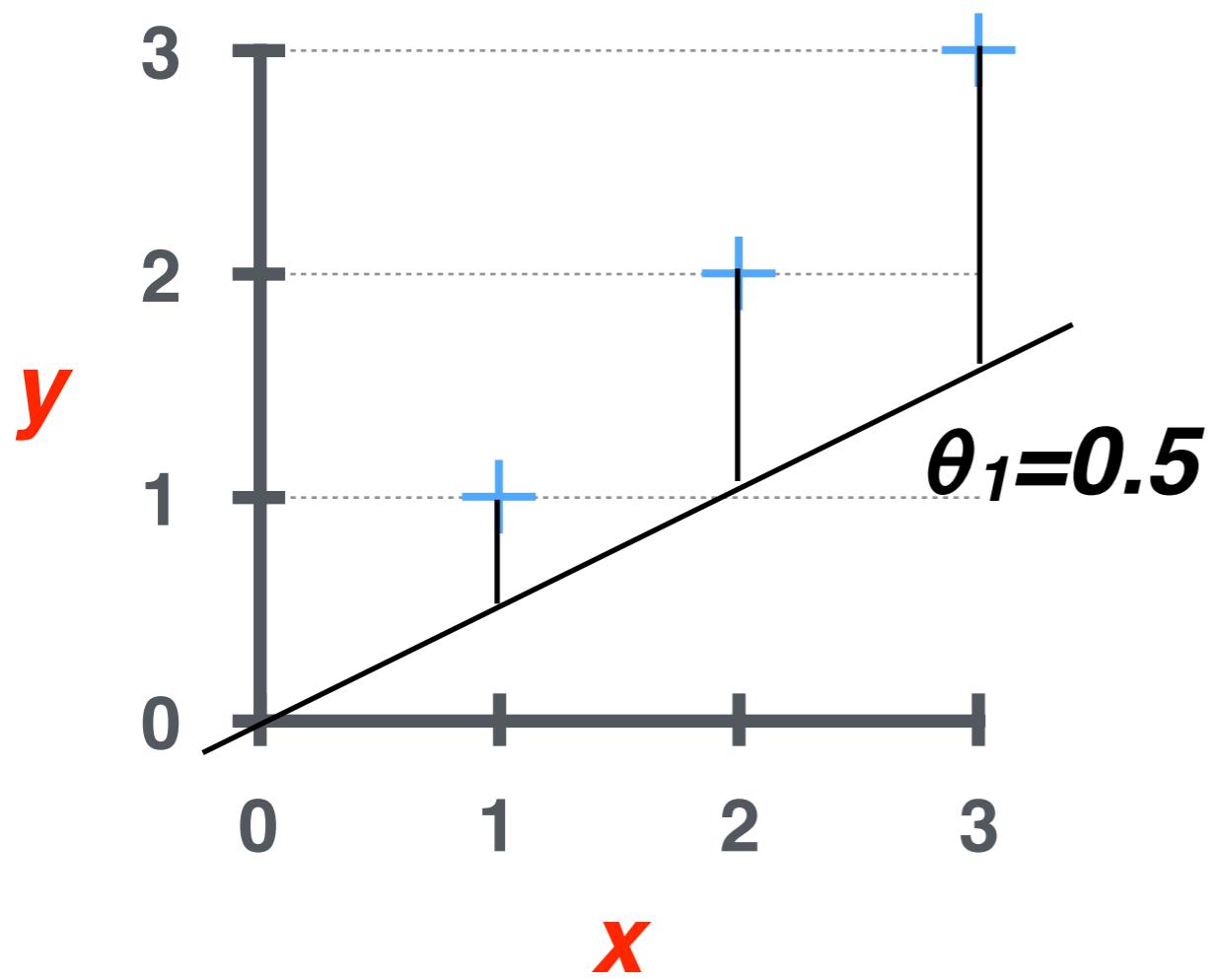

$$J(\theta_1)$$

(function of the parameter  $\theta_1$ )

Q:  $J(0.5) = ?$

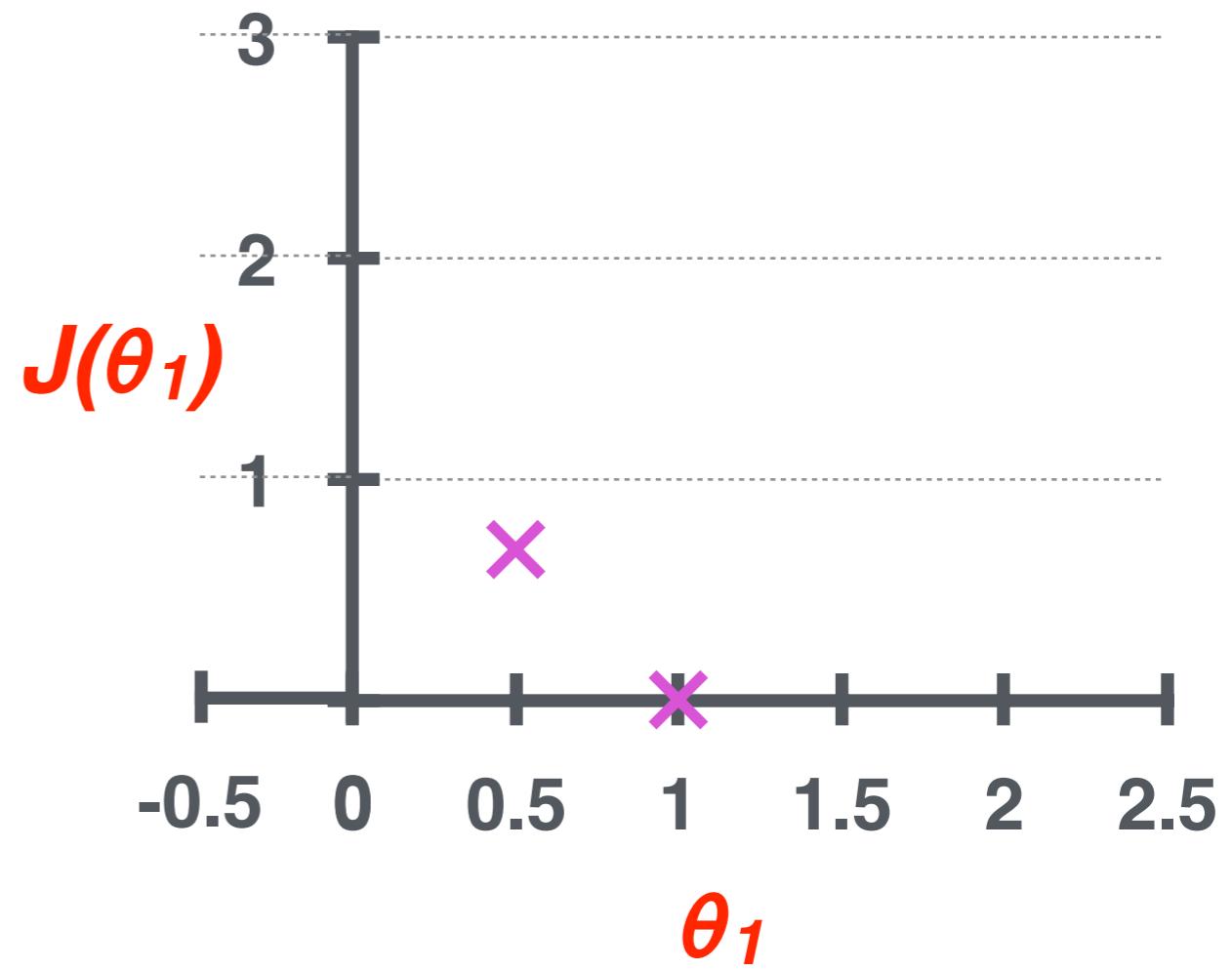
$h_{\theta}(x)$

(for fixed  $\theta_1$ , this is a function of  $x$ )



$J(\theta_1)$

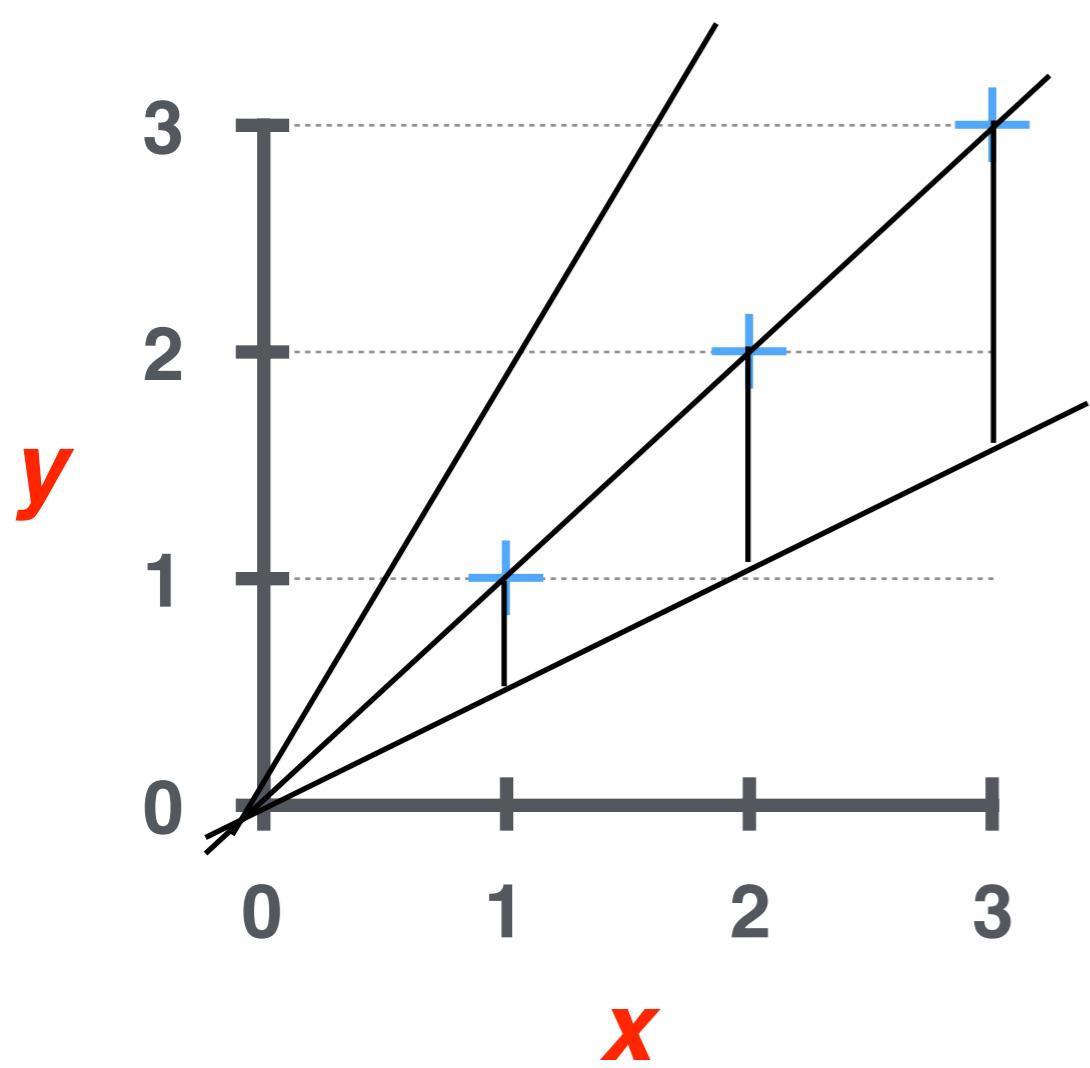
(function of the parameter  $\theta_1$ )



$$J(0.5) = \frac{1}{2 \times 3} [(0.5 - 1)^2 + (1 - 2)^2 + (1.5 - 3)^2] = 0.68$$

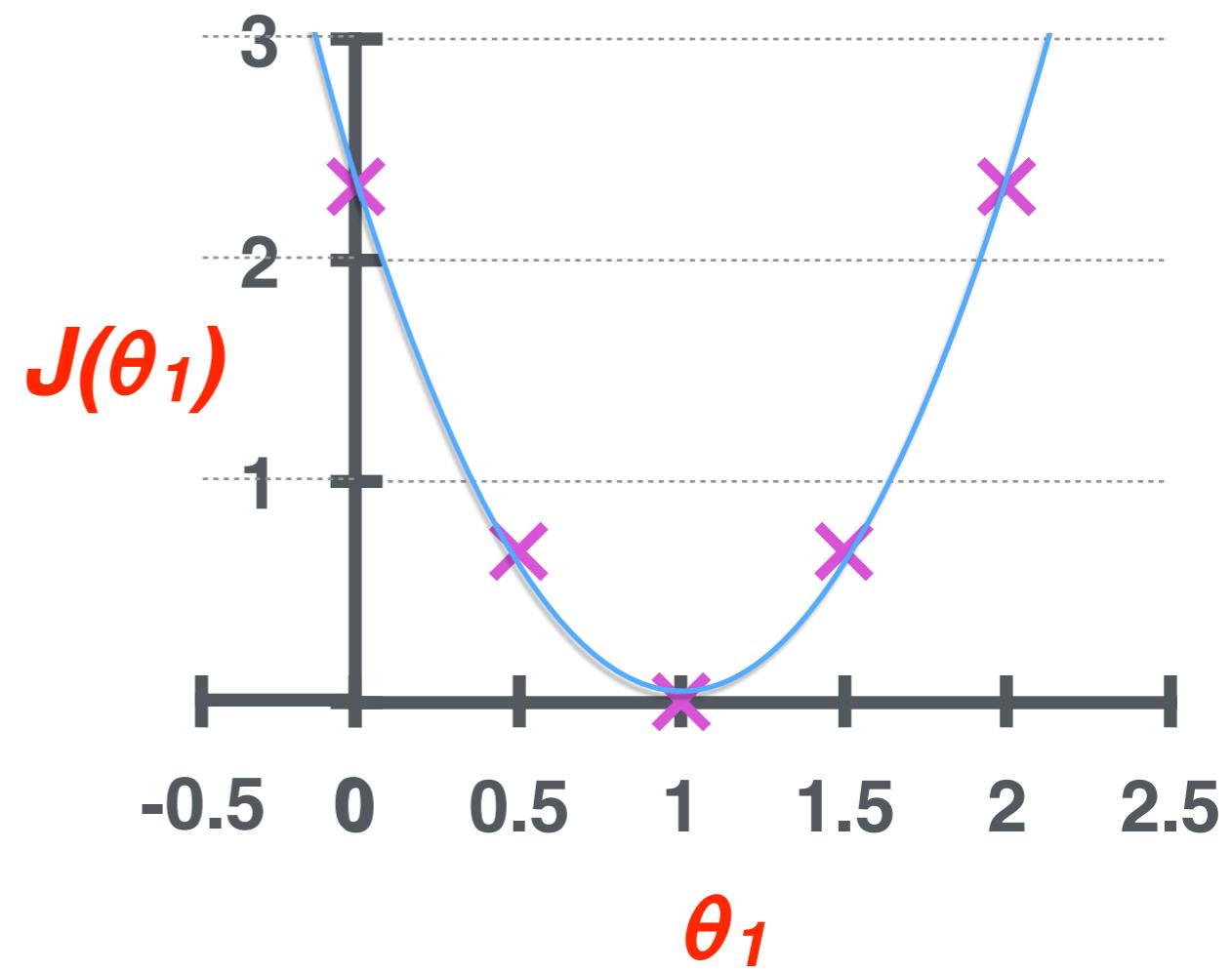
$h_{\theta}(x)$

(for fixed  $\theta_1$ , this is a function of  $x$ )



$J(\theta_1)$

(function of the parameter  $\theta_1$ )



minimize  $J(\theta_1)$   
 $\theta_1$

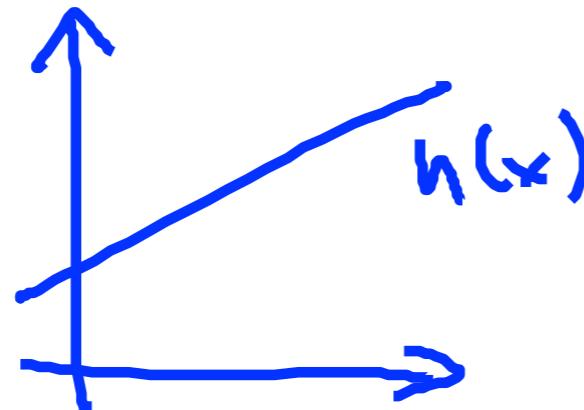
# Linear Regression

- Hypothesis:

$$h_{\theta}(x) = \theta_0 + \theta_1 x$$

- Parameters:

$$\theta_0, \theta_1$$



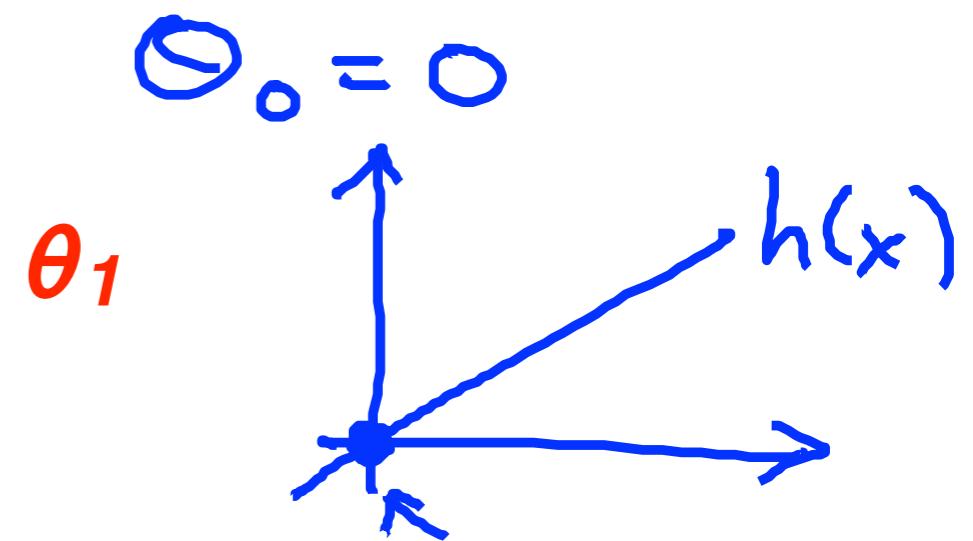
- Cost Function:

$$J(\theta_0, \theta_1) = \frac{1}{2m} \sum_{i=1}^m (h_{\theta}(x^{(i)}) - y^{(i)})^2$$

- Goal:  $\underset{\theta_0, \theta_1}{\text{minimize}} J(\theta_0, \theta_1)$

Simplified

$$h_{\theta}(x) = \theta_1 x$$



$$J(\theta_1) = \frac{1}{2m} \sum_{i=1}^m (h_{\theta}(x^{(i)}) - y^{(i)})^2$$

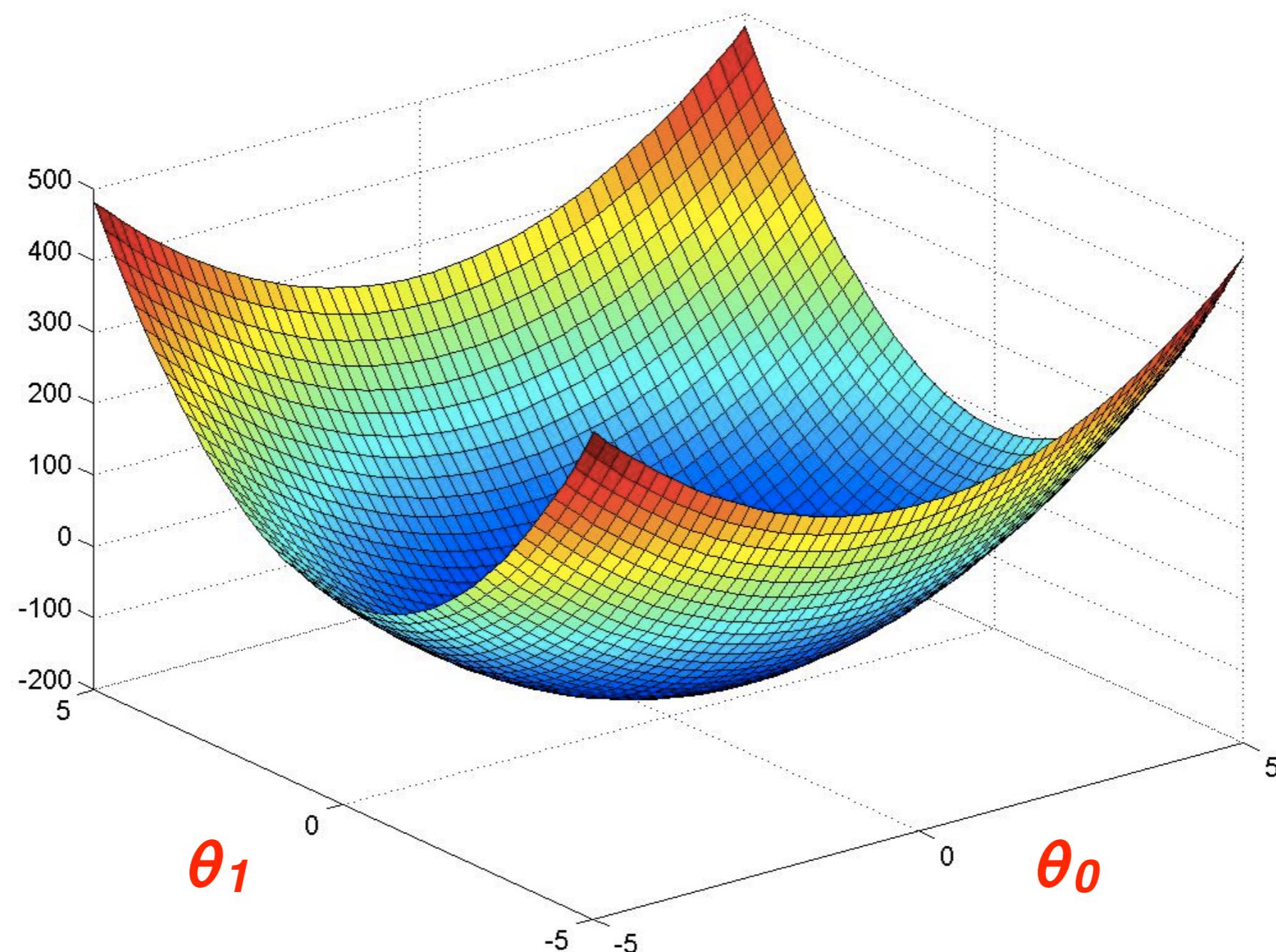
$\underset{\theta_1}{\text{minimize}} J(\theta_1)$

$$h_{\theta}(x)$$

(for fixed  $\theta_0, \theta_1$ , this is a function of  $x$ )

$$J(\theta_0, \theta_1)$$

(function of the parameter  $\theta_0, \theta_1$ )

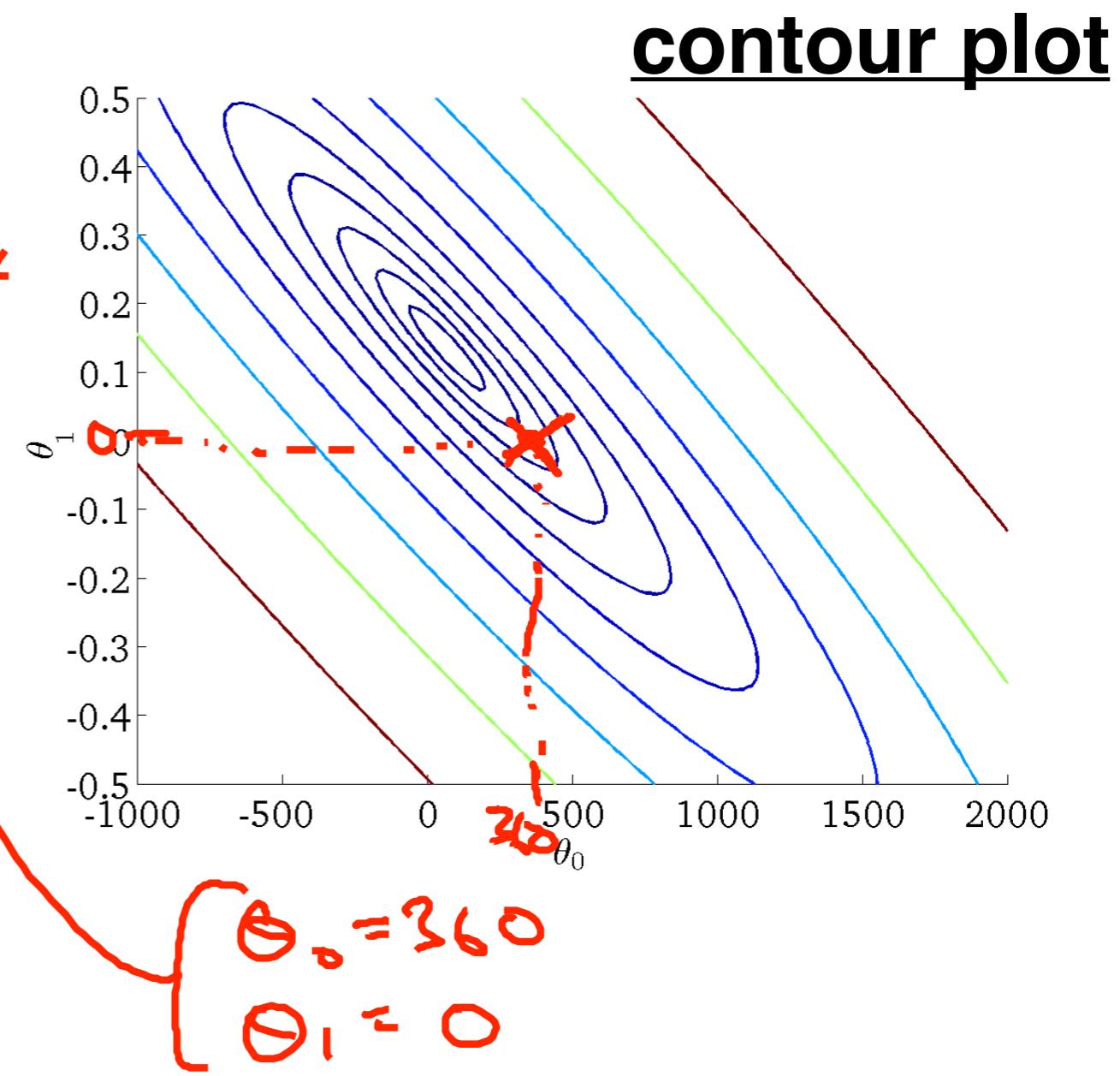
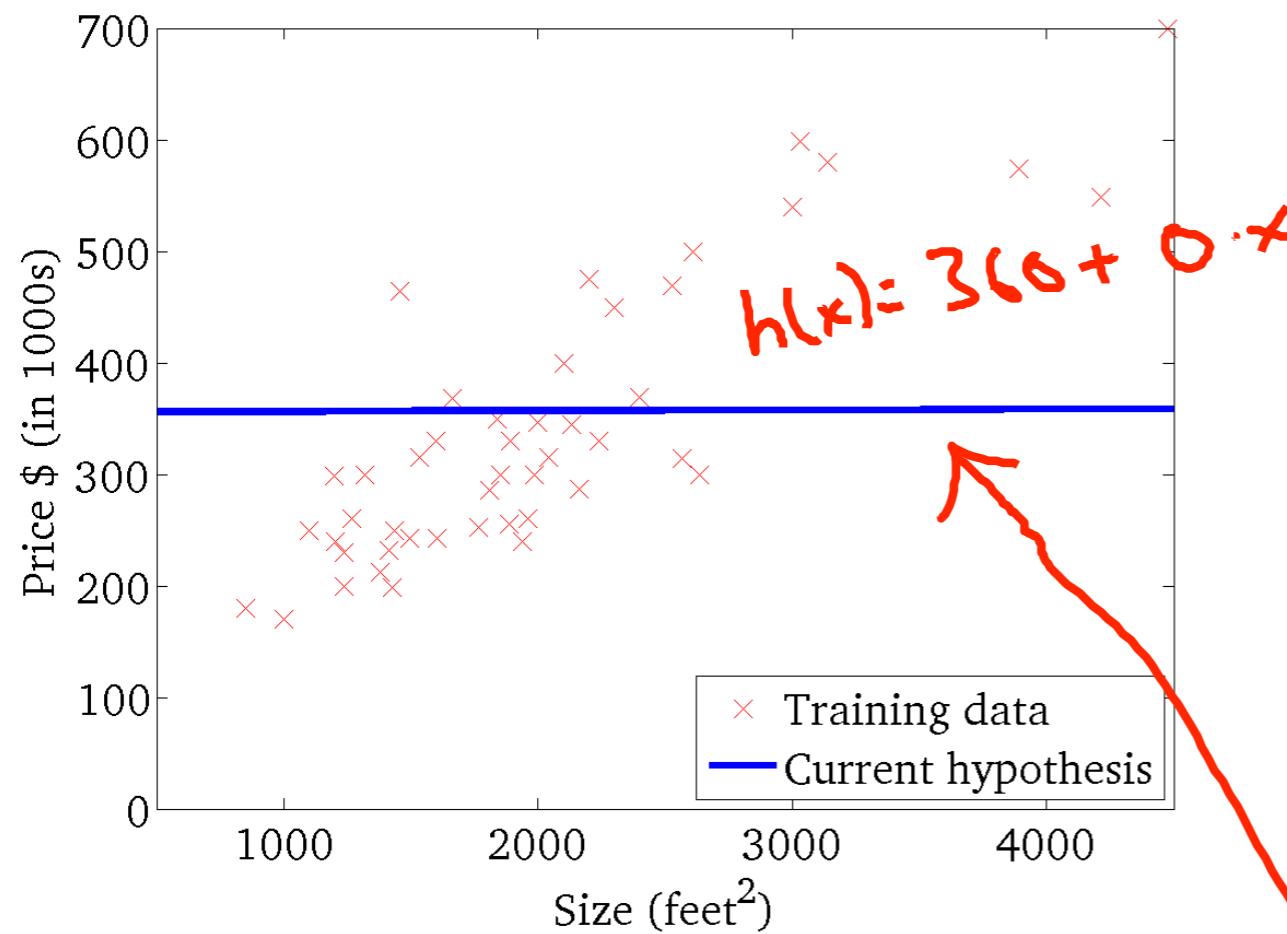
$$J(\theta_1, \theta_2)$$


$$h_{\theta}(x)$$

(for fixed  $\theta_0, \theta_1$ , this is a function of  $x$ )

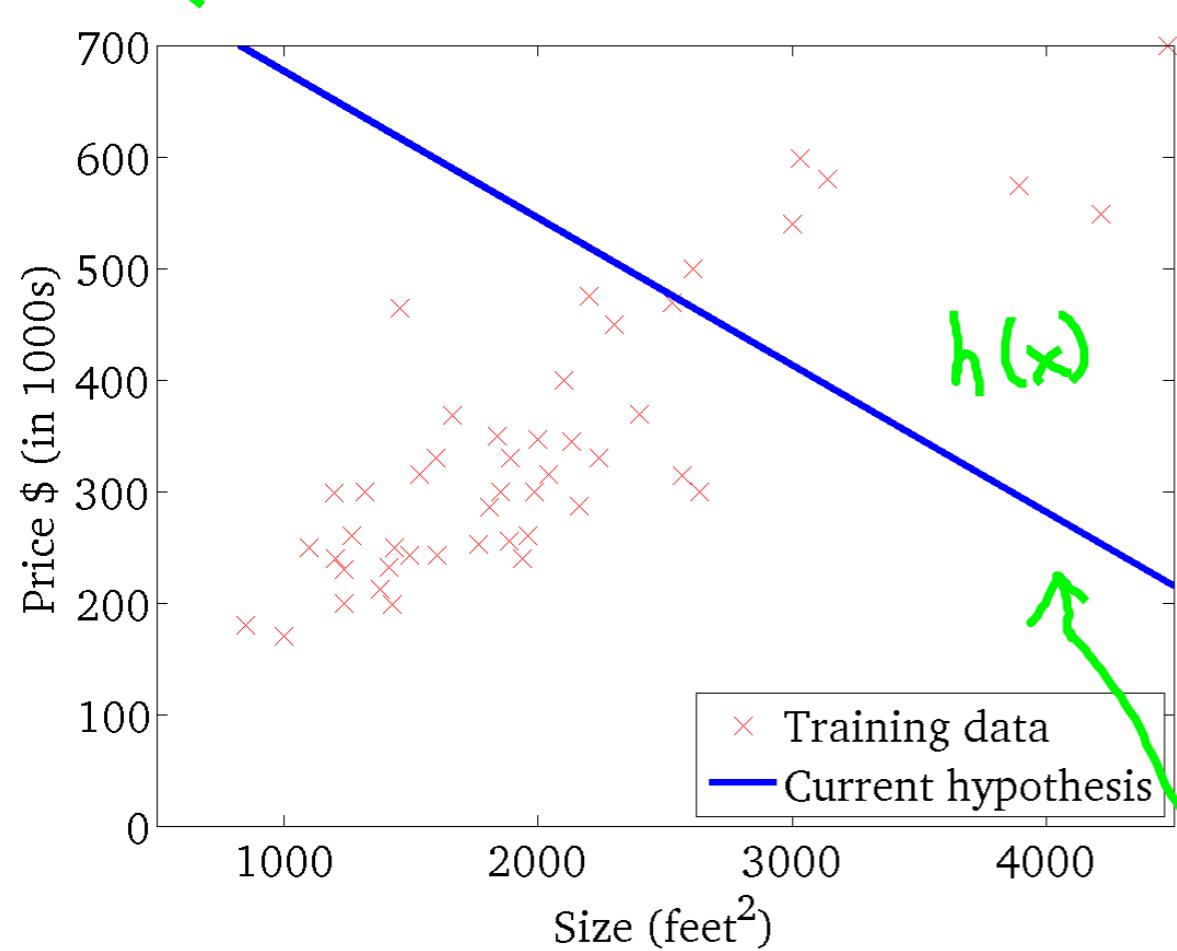
$$J(\theta_0, \theta_1)$$

(function of the parameter  $\theta_0, \theta_1$ )



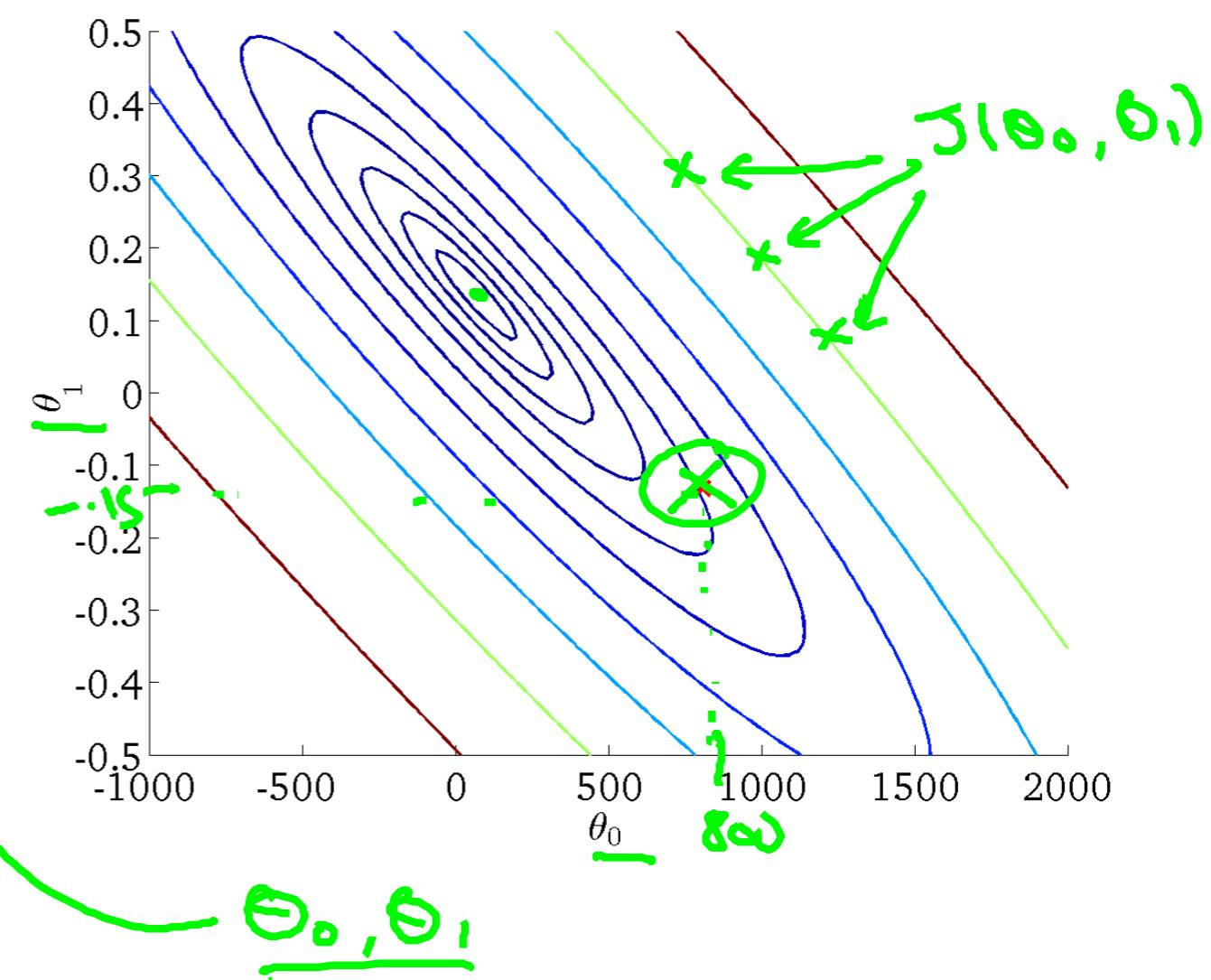
$$h_{\theta}(x)$$

(for fixed  $\theta_0, \theta_1$ , this is a function of  $x$ )



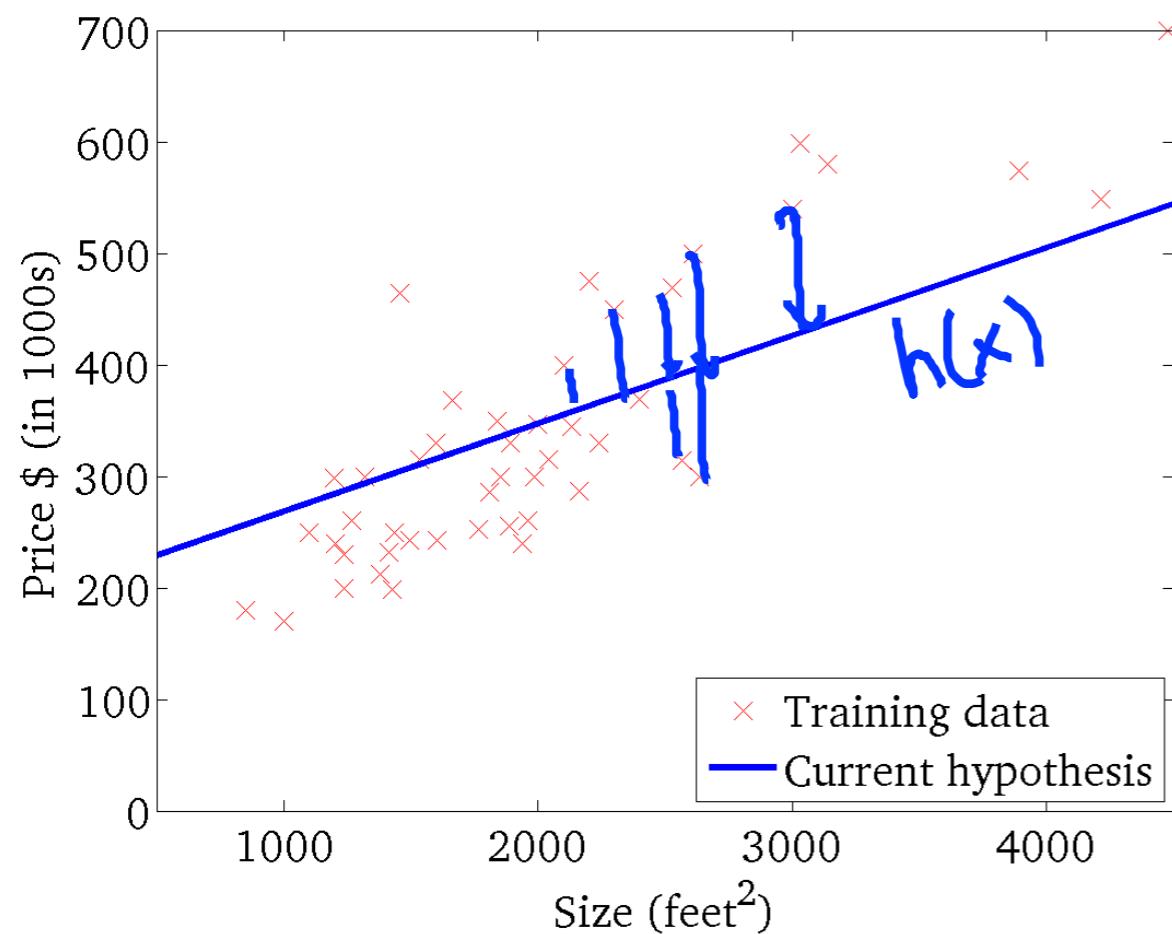
$$J(\theta_0, \theta_1)$$

(function of the parameter  $\theta_0, \theta_1$ )



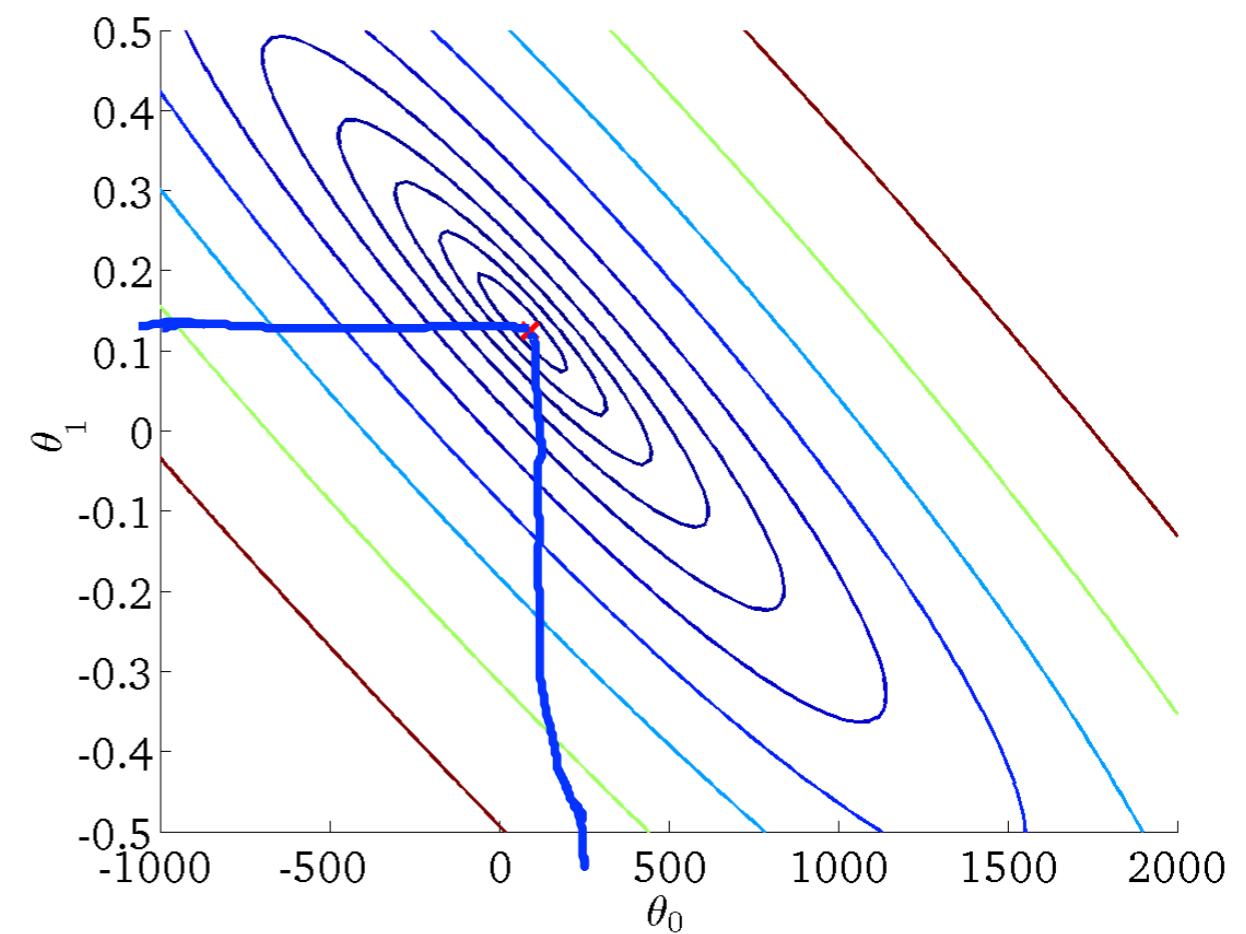
$$h_{\theta}(x)$$

(for fixed  $\theta_0, \theta_1$ , this is a function of  $x$ )



$$J(\theta_0, \theta_1)$$

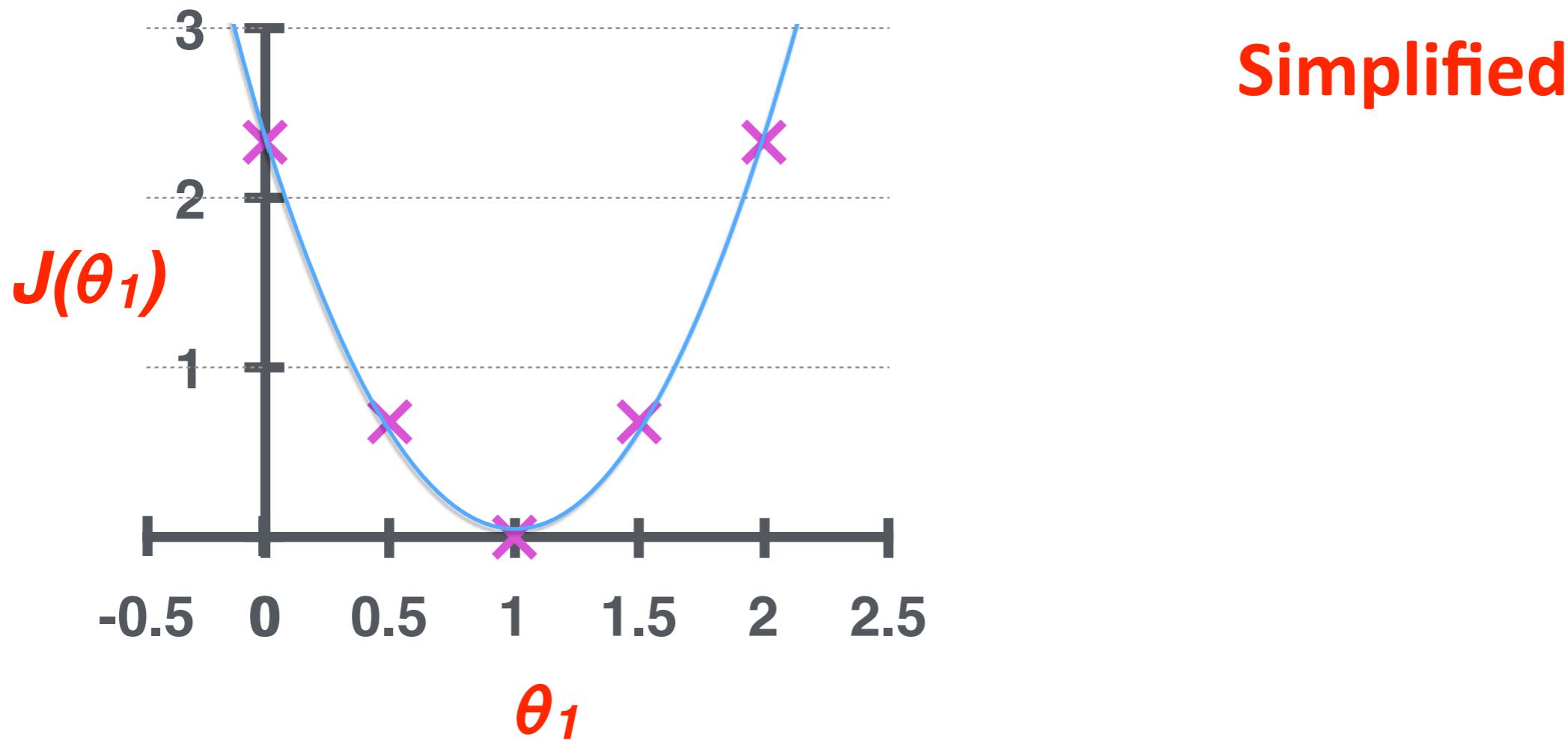
(function of the parameter  $\theta_0, \theta_1$ )



# Parameter Learning

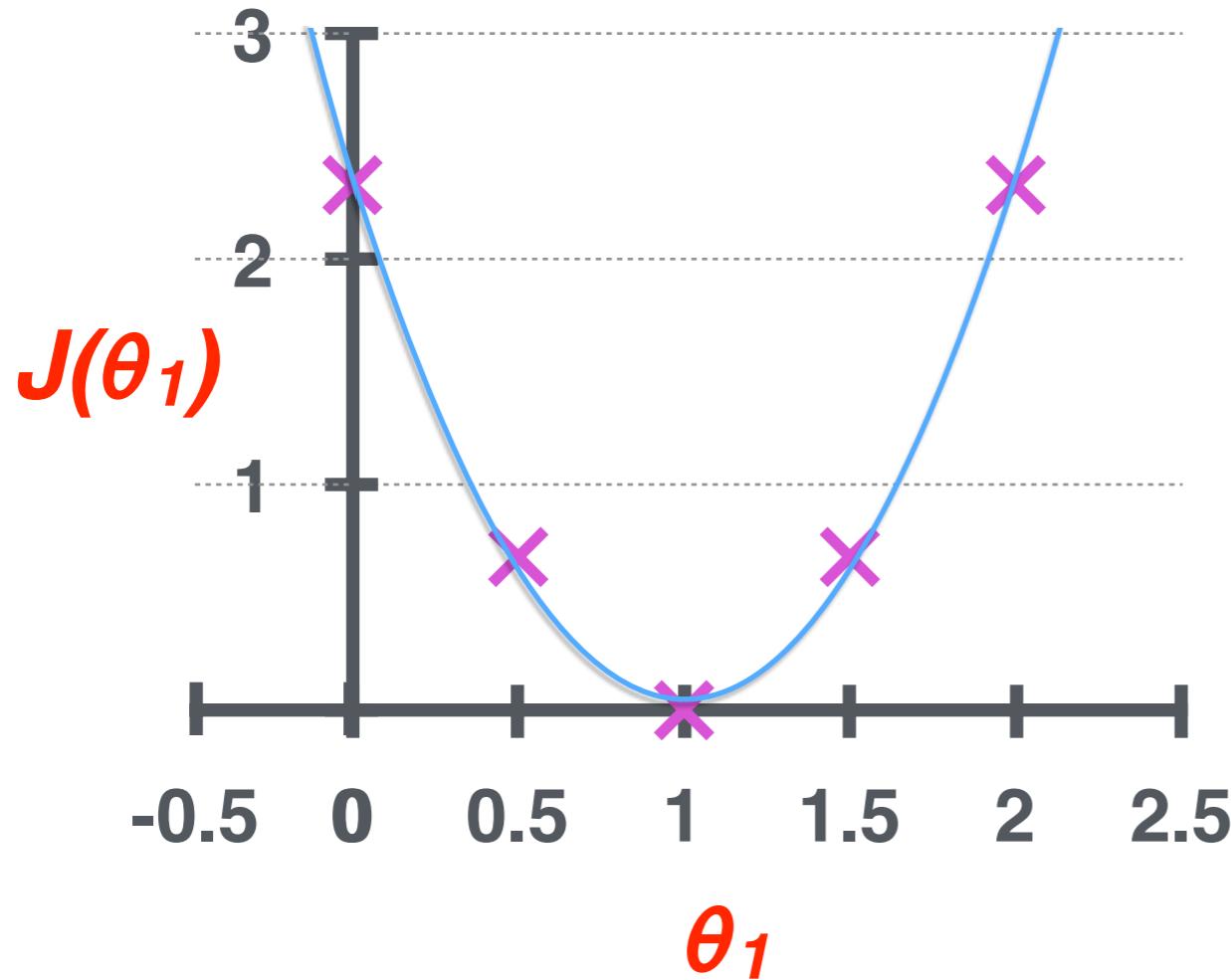
- Have some function  $J(\theta_0, \theta_1)$
- Want  $\min_{\theta_0, \theta_1} J(\theta_0, \theta_1)$
- **Outline:**
  - Start with some  $\theta_0, \theta_1$
  - Keep changing  $\theta_0, \theta_1$  to reduce  $J(\theta_1, \theta_2)$  until we hopefully end up at a minimum

# Gradient Descent



minimize  $J(\theta_1)$   
 $\theta_1$

# Gradient Descent



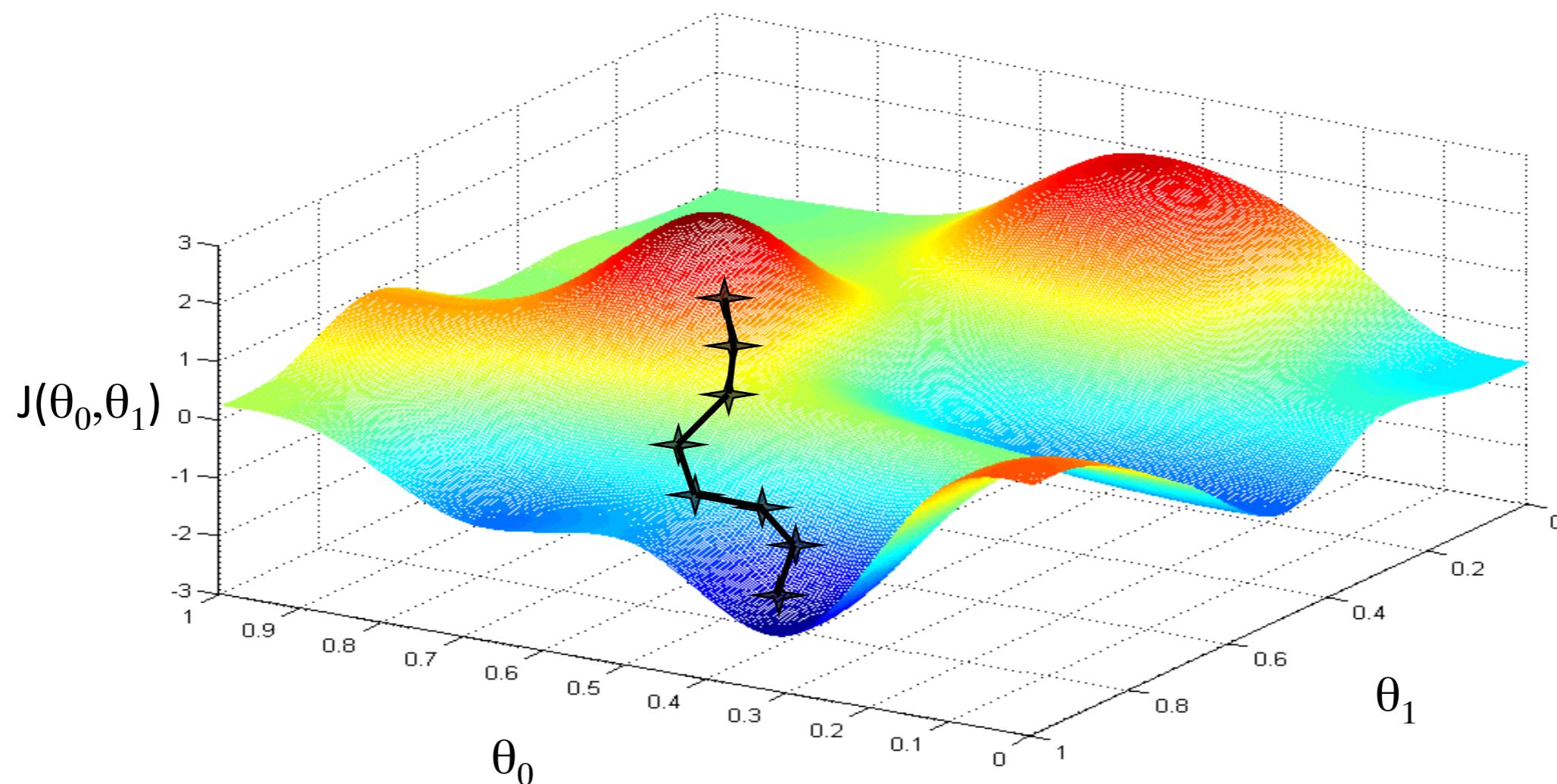
Simplified

$$\theta_1 \coloneqq \theta_1 - \alpha \frac{\partial}{\partial \theta_1} J(\theta_1)$$

learning rate

minimize  $J(\theta_1)$   
 $\theta_1$

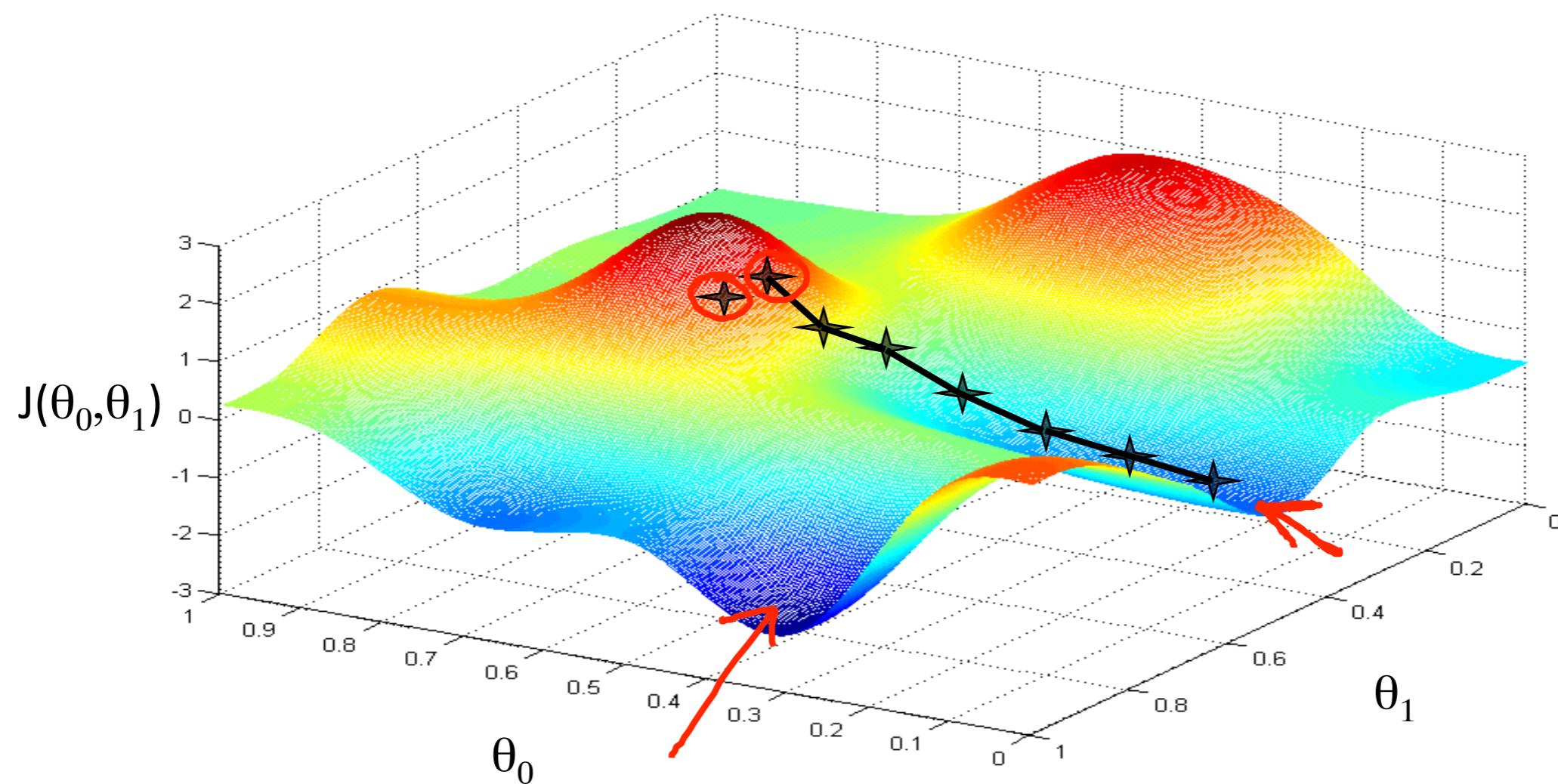
# Gradient Descent



minimize  $J(\theta_0, \theta_1)$   
 $\theta_0, \theta_1$

Andrew Ng

# Gradient Descent



minimize  $J(\theta_0, \theta_1)$   
 $\theta_0, \theta_1$

Andrew Ng

# Gradient Descent

repeat until convergence {

$$\theta_j := \theta_j - \alpha \frac{\partial}{\partial \theta_j} J(\theta_0, \theta_1)$$

**learning rate**

simultaneous update  
for j=0 and j=1

Linear Regression w/ one variable:

# Gradient Descent

$$h_{\theta}(x) = \theta_0 + \theta_1 x$$

## Cost Function



$$J(\theta_0, \theta_1) = \frac{1}{2m} \sum_{i=1}^m (h_{\theta}(x^{(i)}) - y^{(i)})^2$$

$$\frac{\partial}{\partial \theta_0} J(\theta_0, \theta_1) = ?$$

$$\frac{\partial}{\partial \theta_1} J(\theta_0, \theta_1) = ?$$

Linear Regression w/ one variable:

# Gradient Descent

repeat until convergence {

$$\theta_0 \leftarrow \theta_0 - \alpha \frac{1}{m} \sum_{i=1}^m (h_\theta(x^{(i)}) - y^{(i)})$$

simultaneous update  $\theta_0, \theta_1$

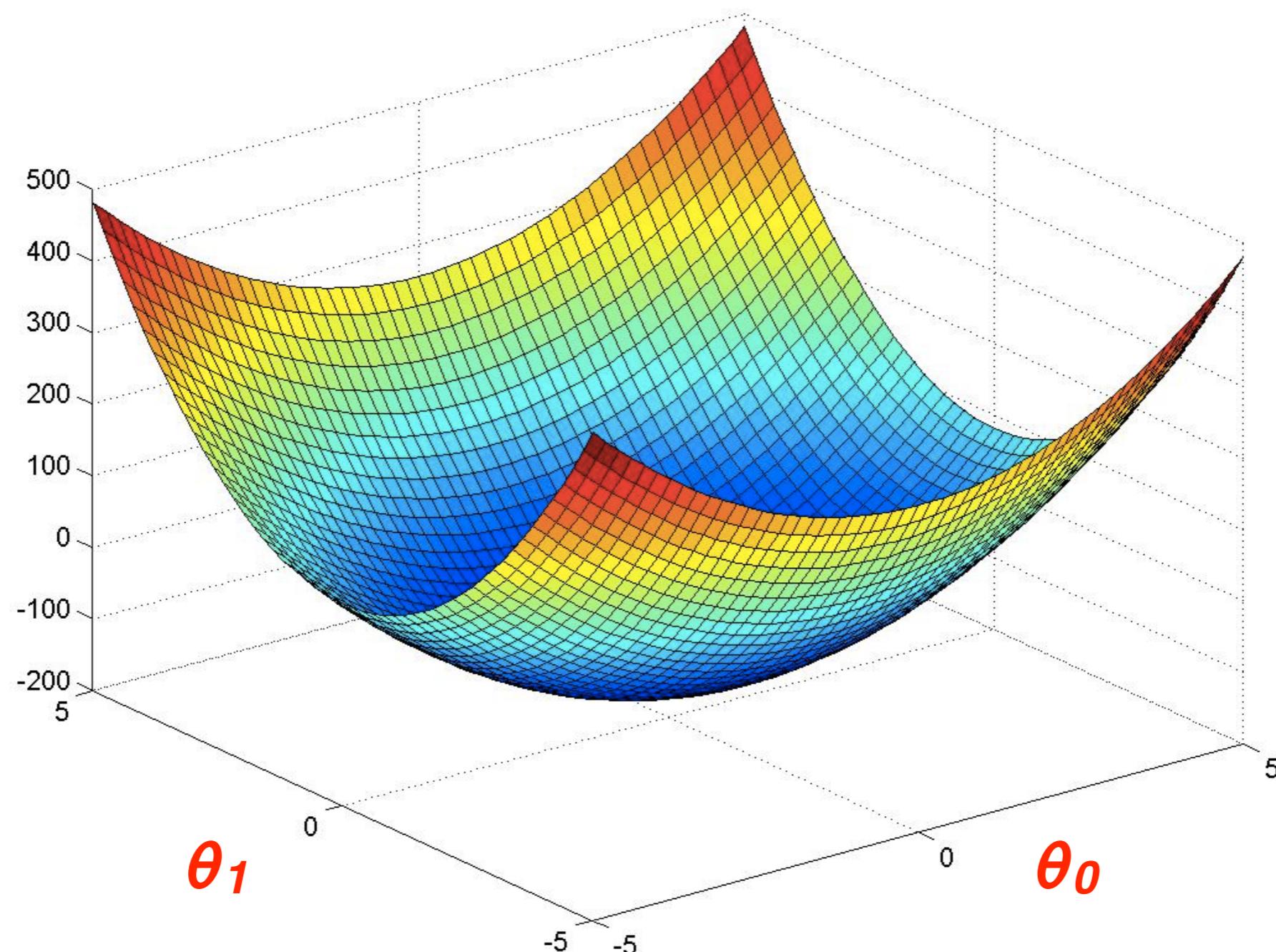
$$\theta_1 \leftarrow \theta_1 - \alpha \frac{1}{m} \sum_{i=1}^m (h_\theta(x^{(i)}) - y^{(i)}) \cdot x^{(i)}$$

}

# Linear Regression

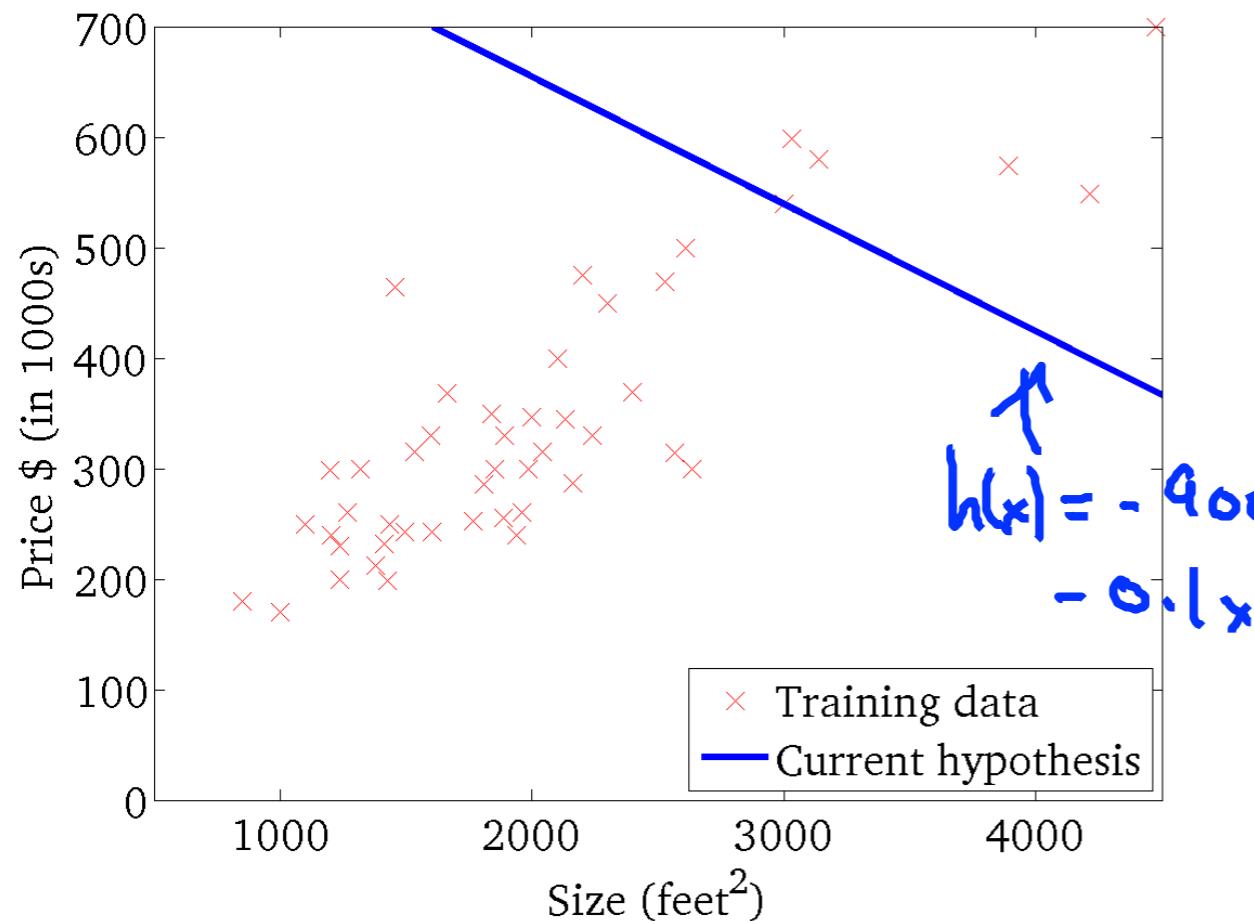
**cost function is convex**

$J(\theta_1, \theta_2)$



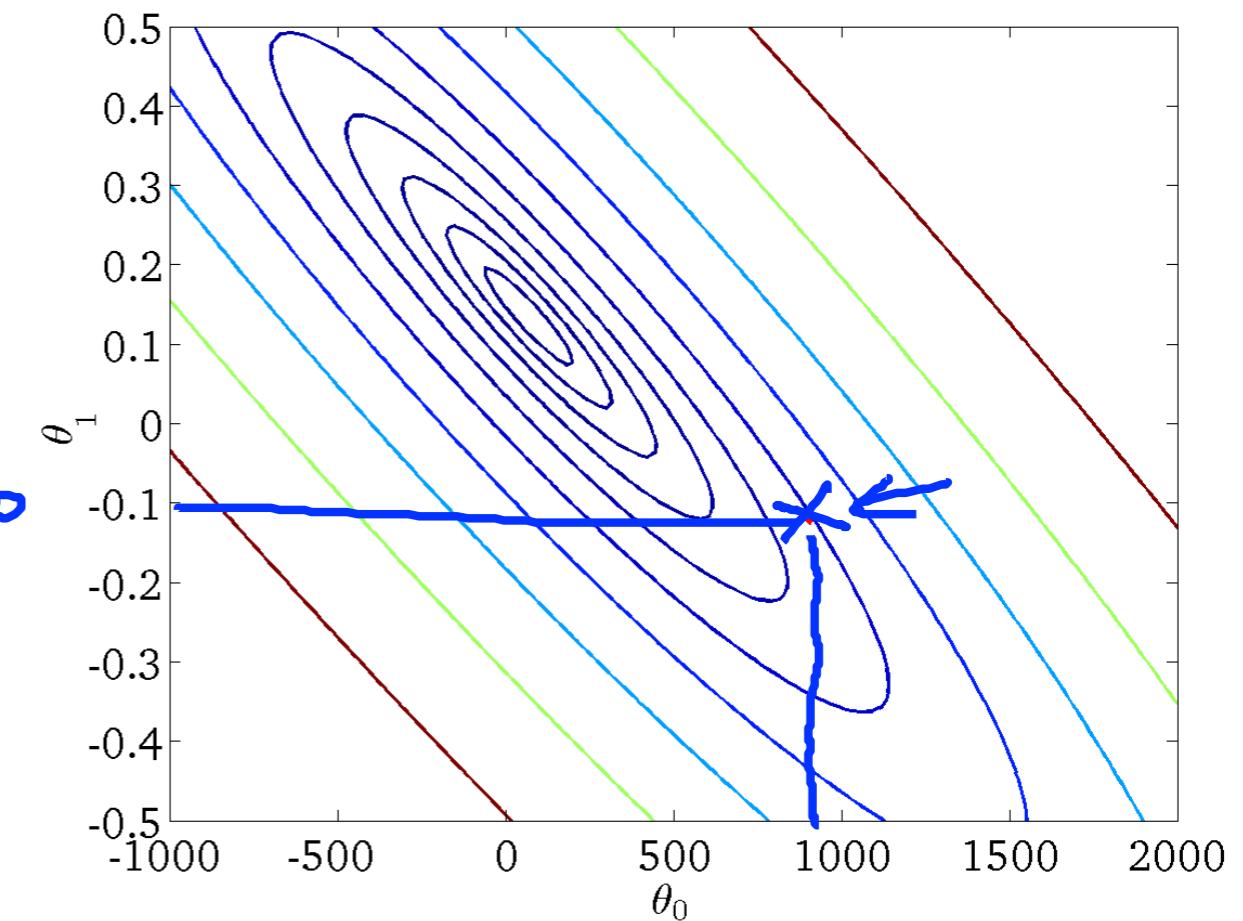
$$h_{\theta}(x)$$

(for fixed  $\theta_0, \theta_1$ , this is a function of  $x$ )



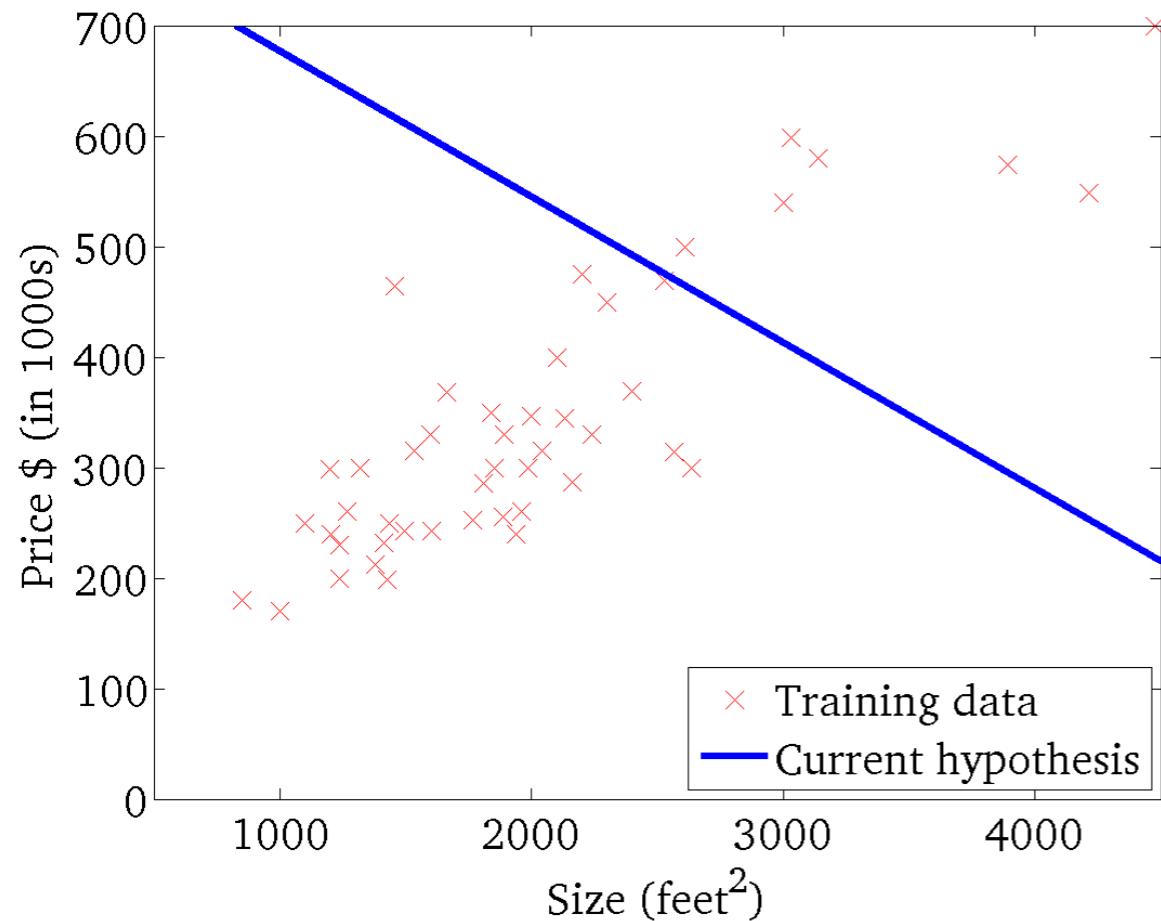
$$J(\theta_0, \theta_1)$$

(function of the parameter  $\theta_0, \theta_1$ )



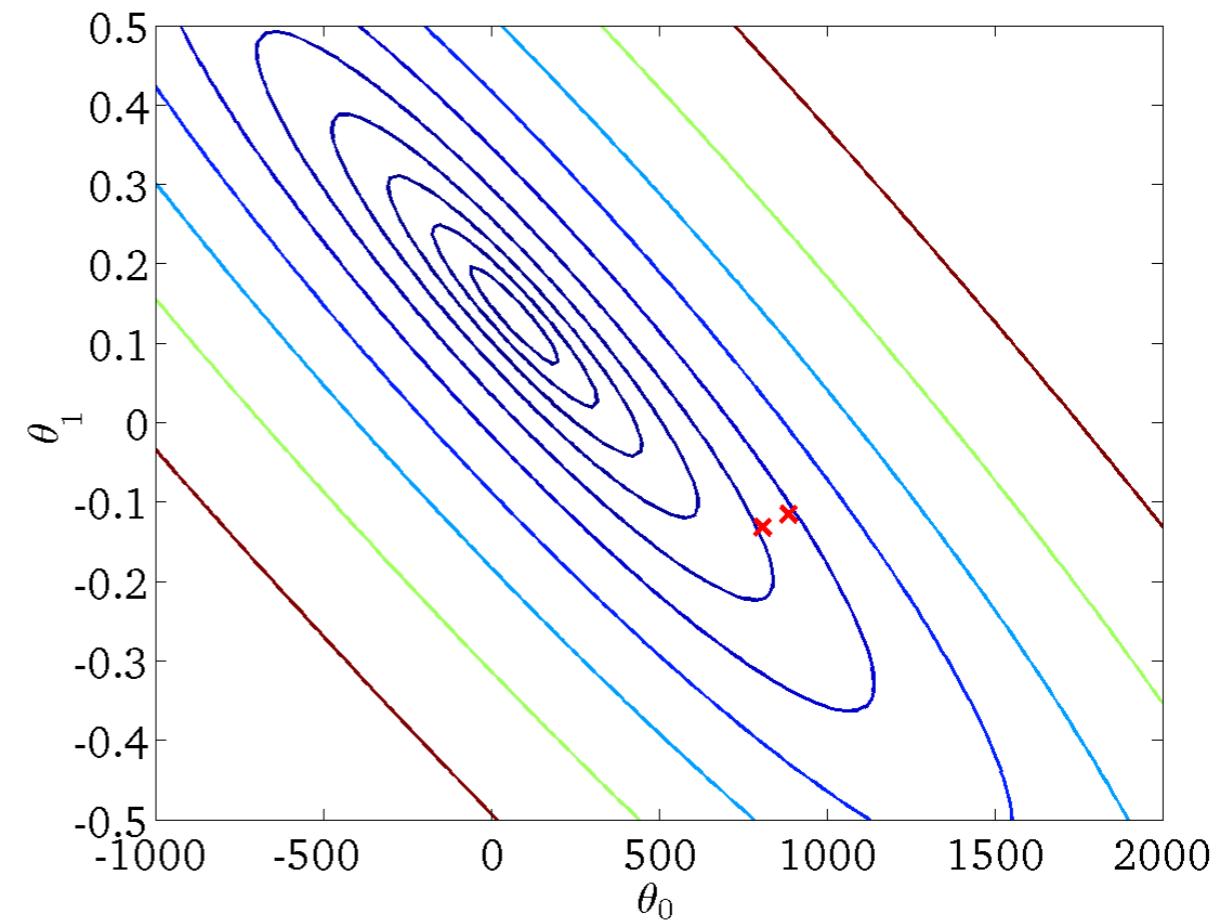
$$h_{\theta}(x)$$

(for fixed  $\theta_0, \theta_1$ , this is a function of  $x$ )



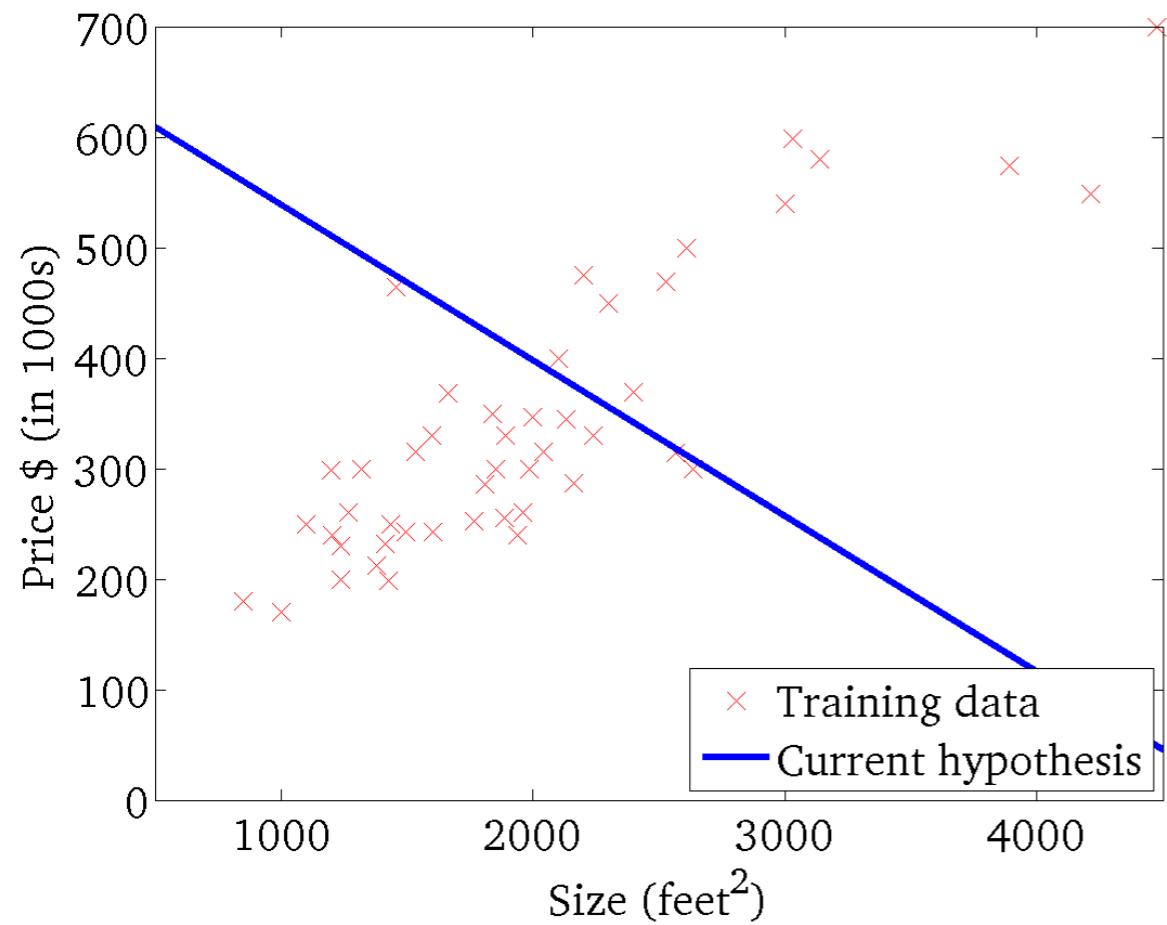
$$J(\theta_0, \theta_1)$$

(function of the parameter  $\theta_0, \theta_1$ )



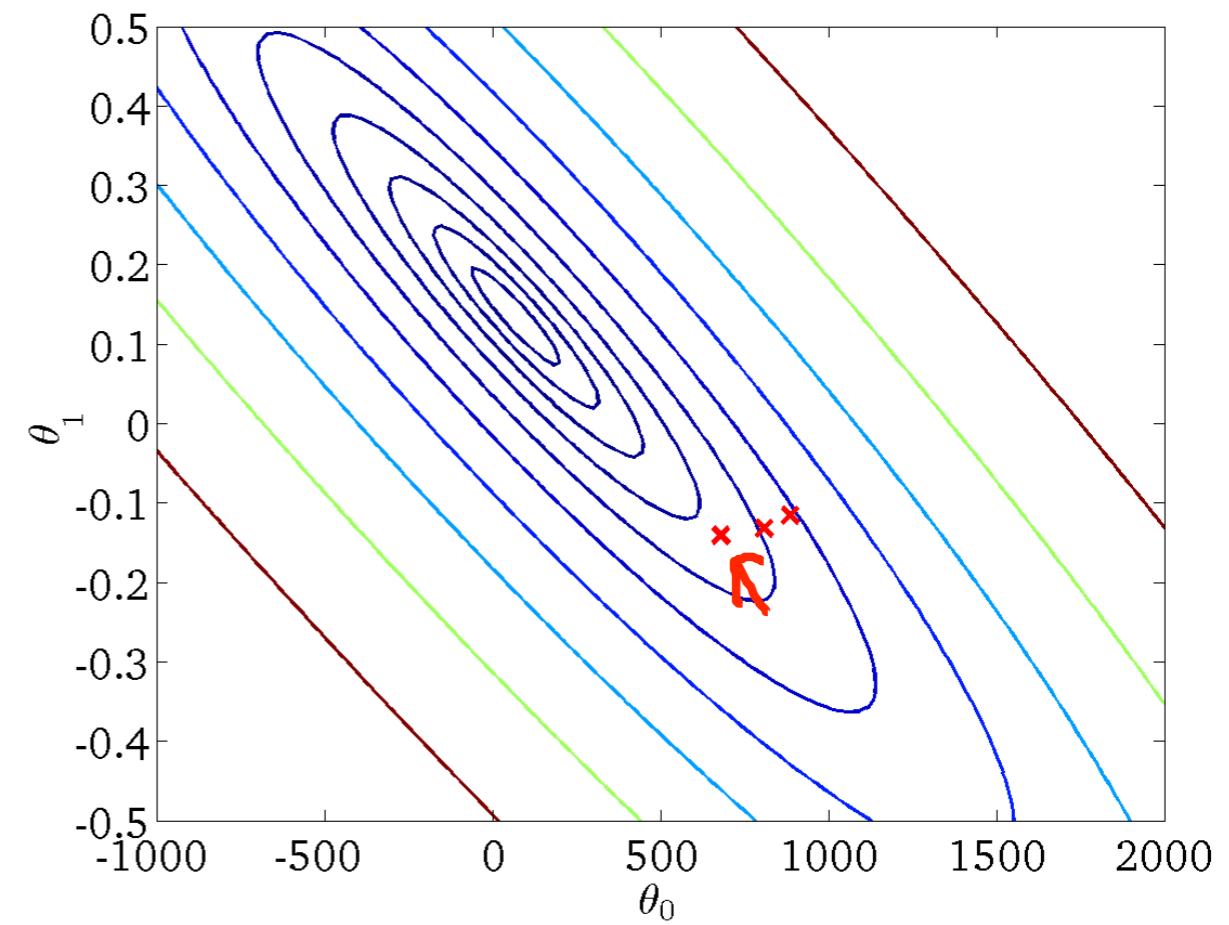
$$h_{\theta}(x)$$

(for fixed  $\theta_0, \theta_1$ , this is a function of  $x$ )



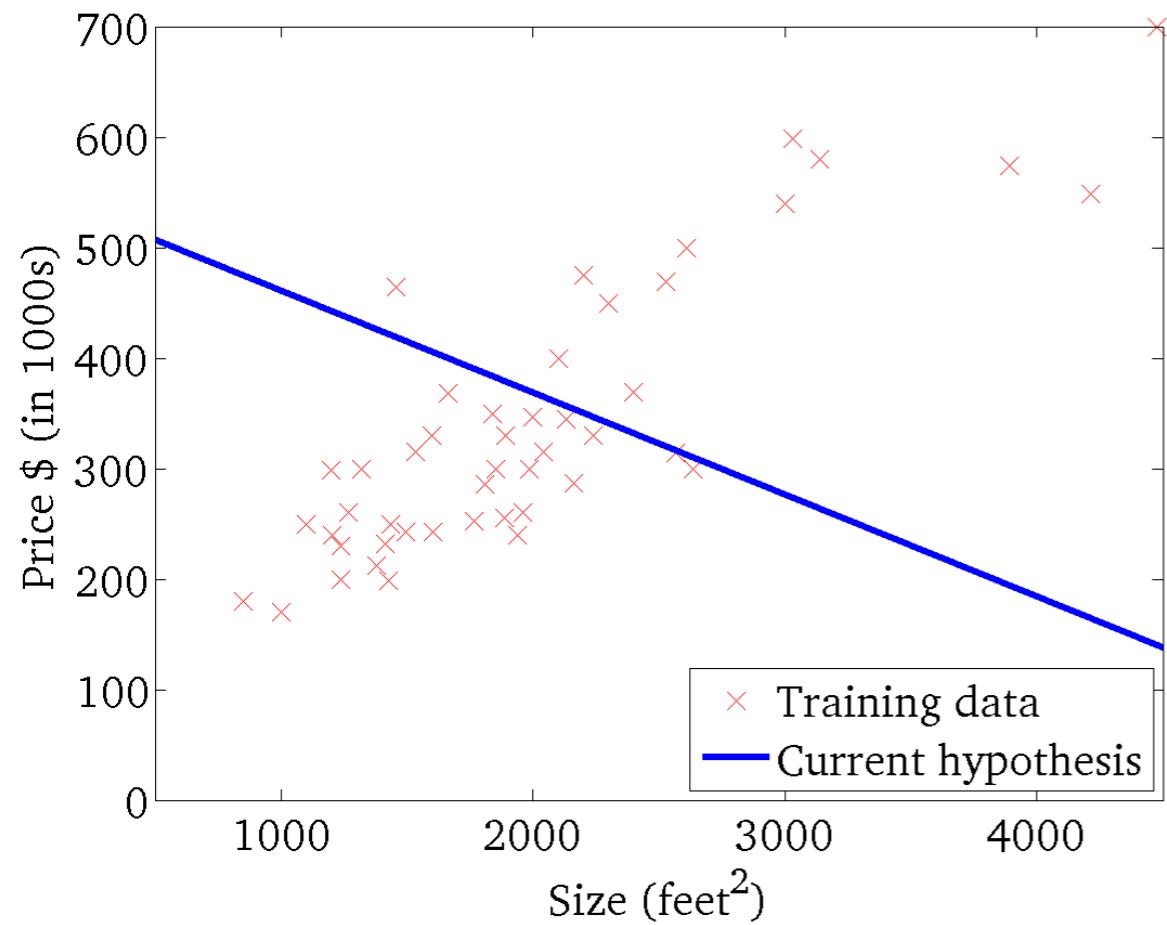
$$J(\theta_0, \theta_1)$$

(function of the parameter  $\theta_0, \theta_1$ )



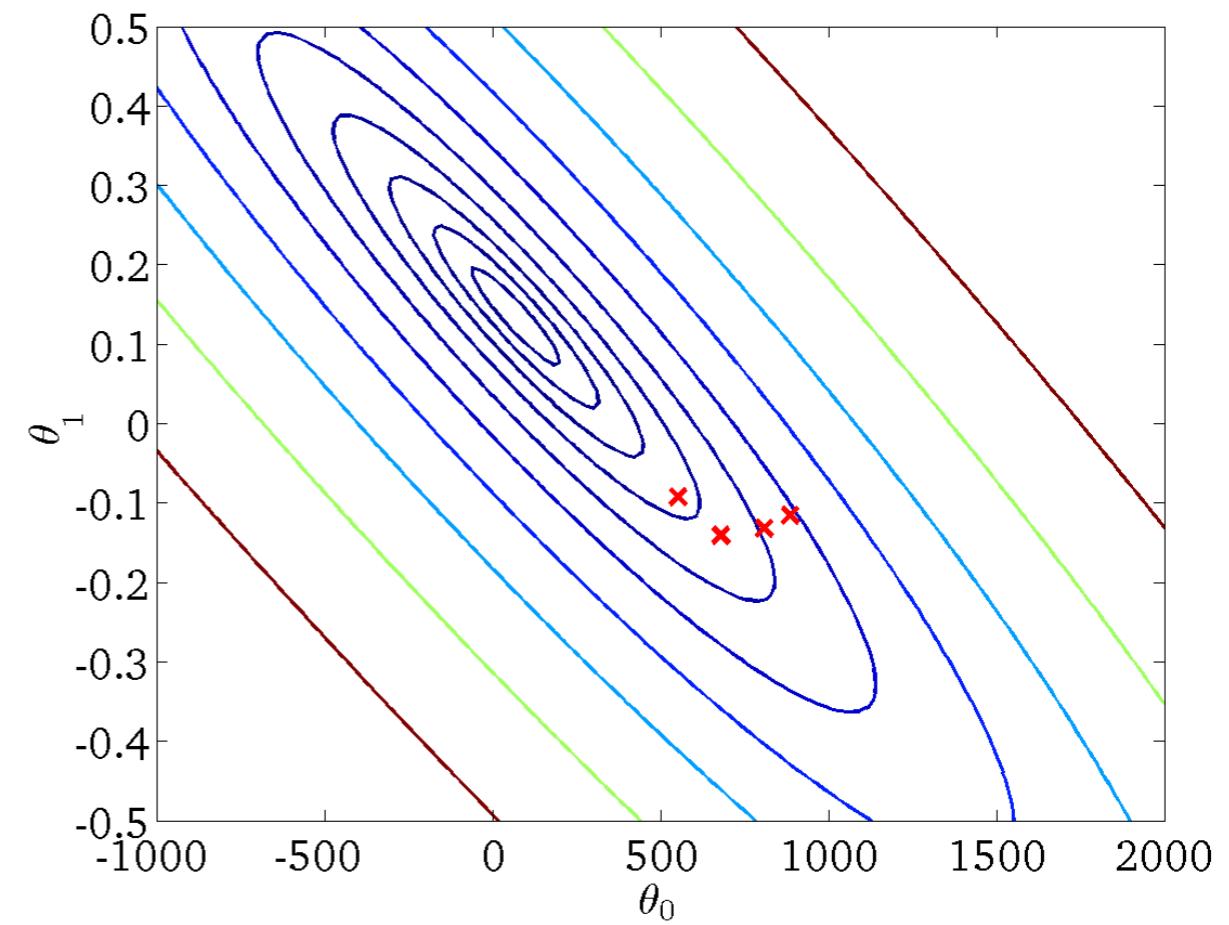
$$h_{\theta}(x)$$

(for fixed  $\theta_0, \theta_1$ , this is a function of  $x$ )



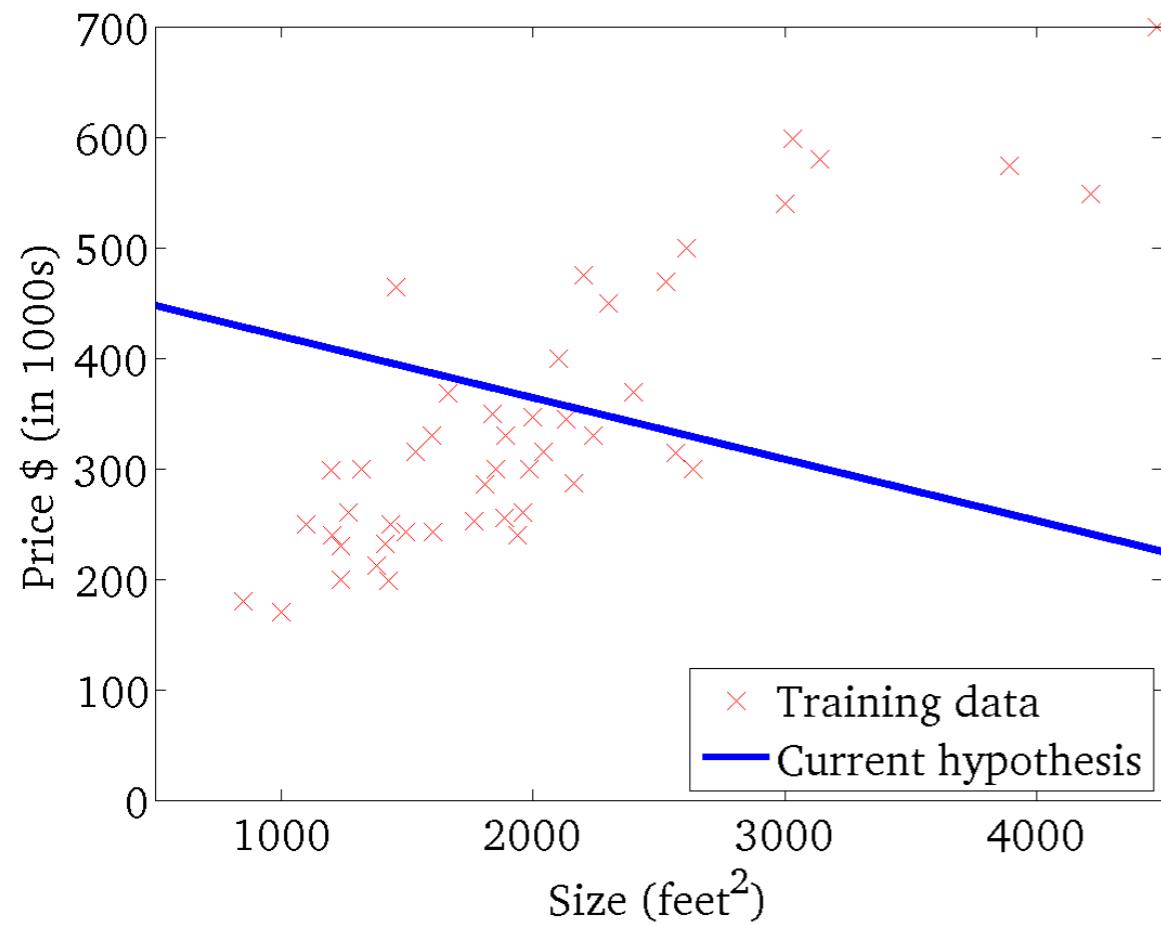
$$J(\theta_0, \theta_1)$$

(function of the parameter  $\theta_0, \theta_1$ )



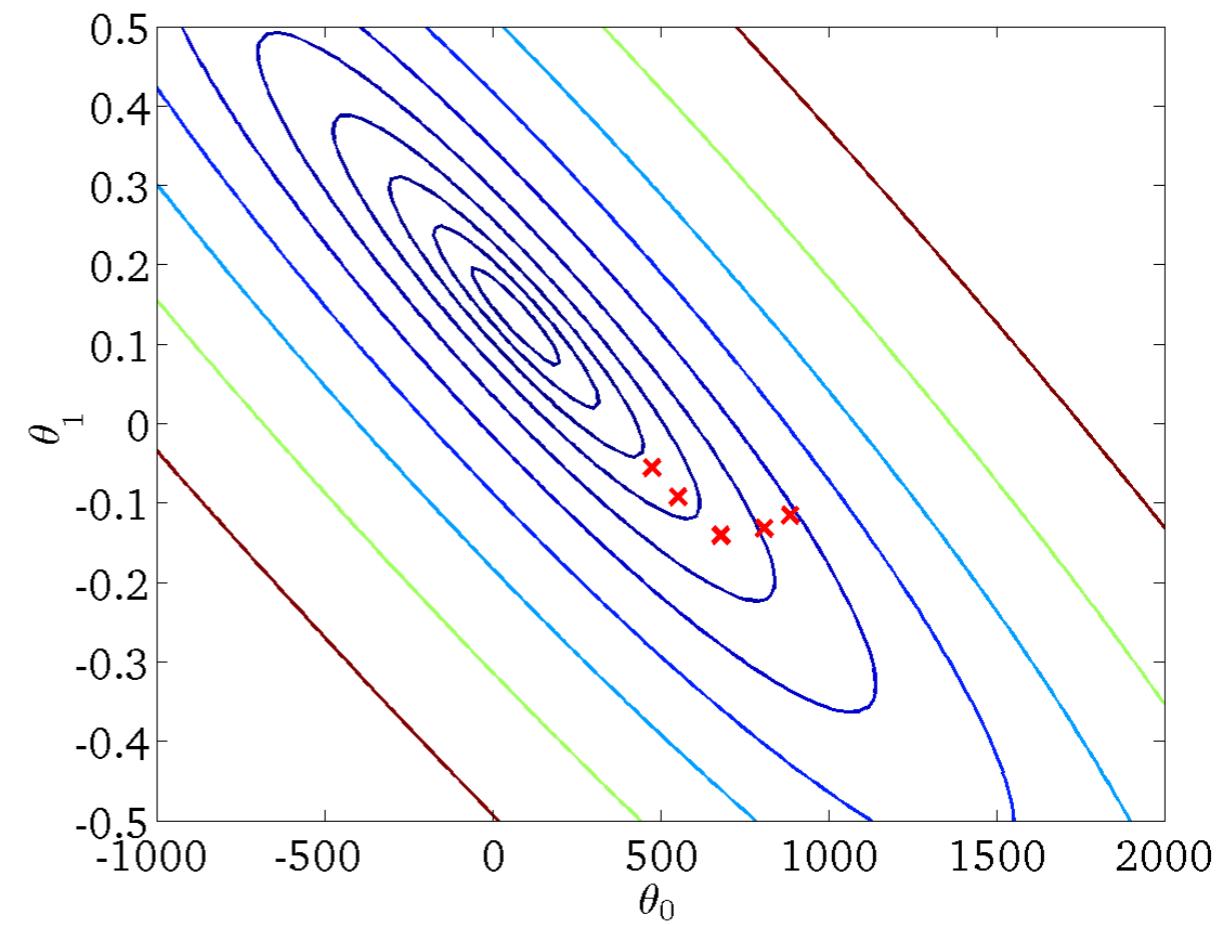
$$h_{\theta}(x)$$

(for fixed  $\theta_0, \theta_1$ , this is a function of  $x$ )



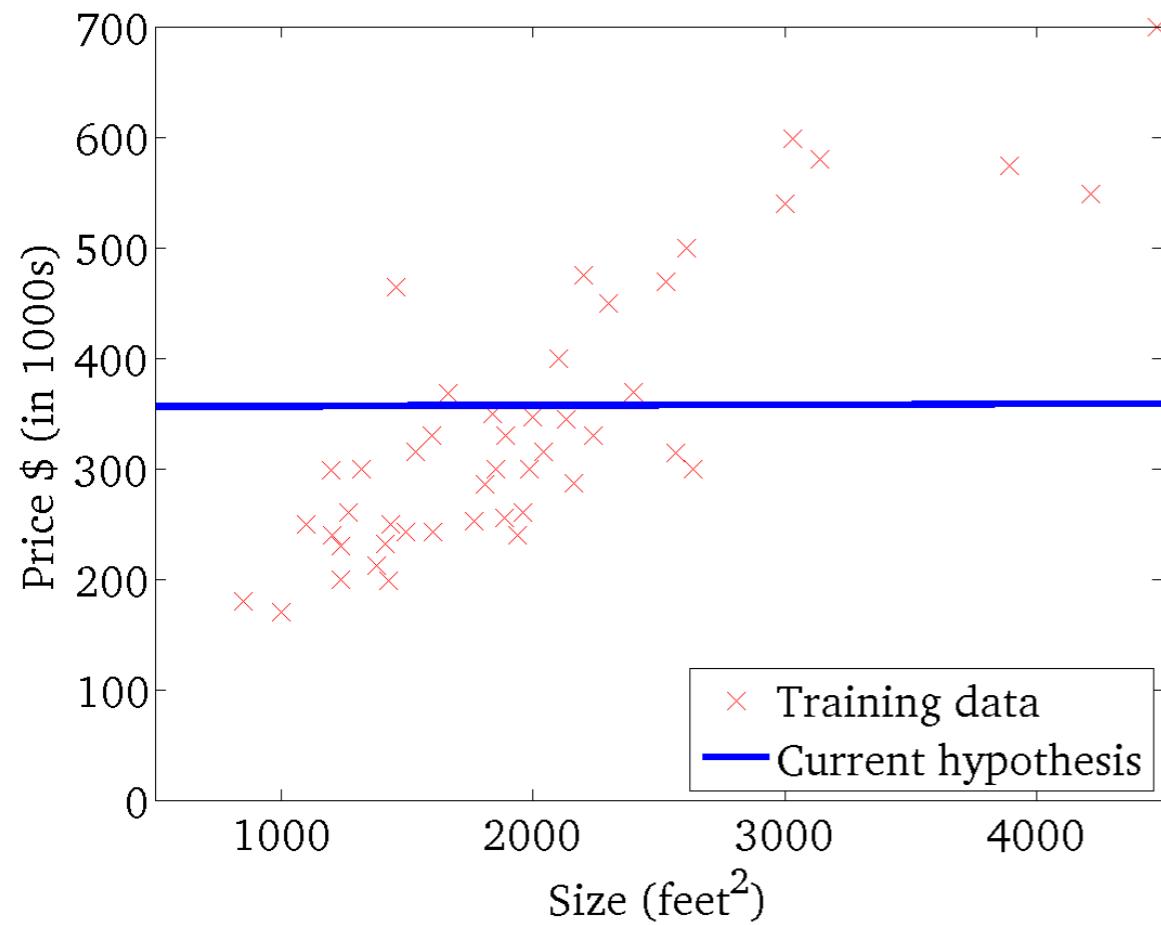
$$J(\theta_0, \theta_1)$$

(function of the parameter  $\theta_0, \theta_1$ )



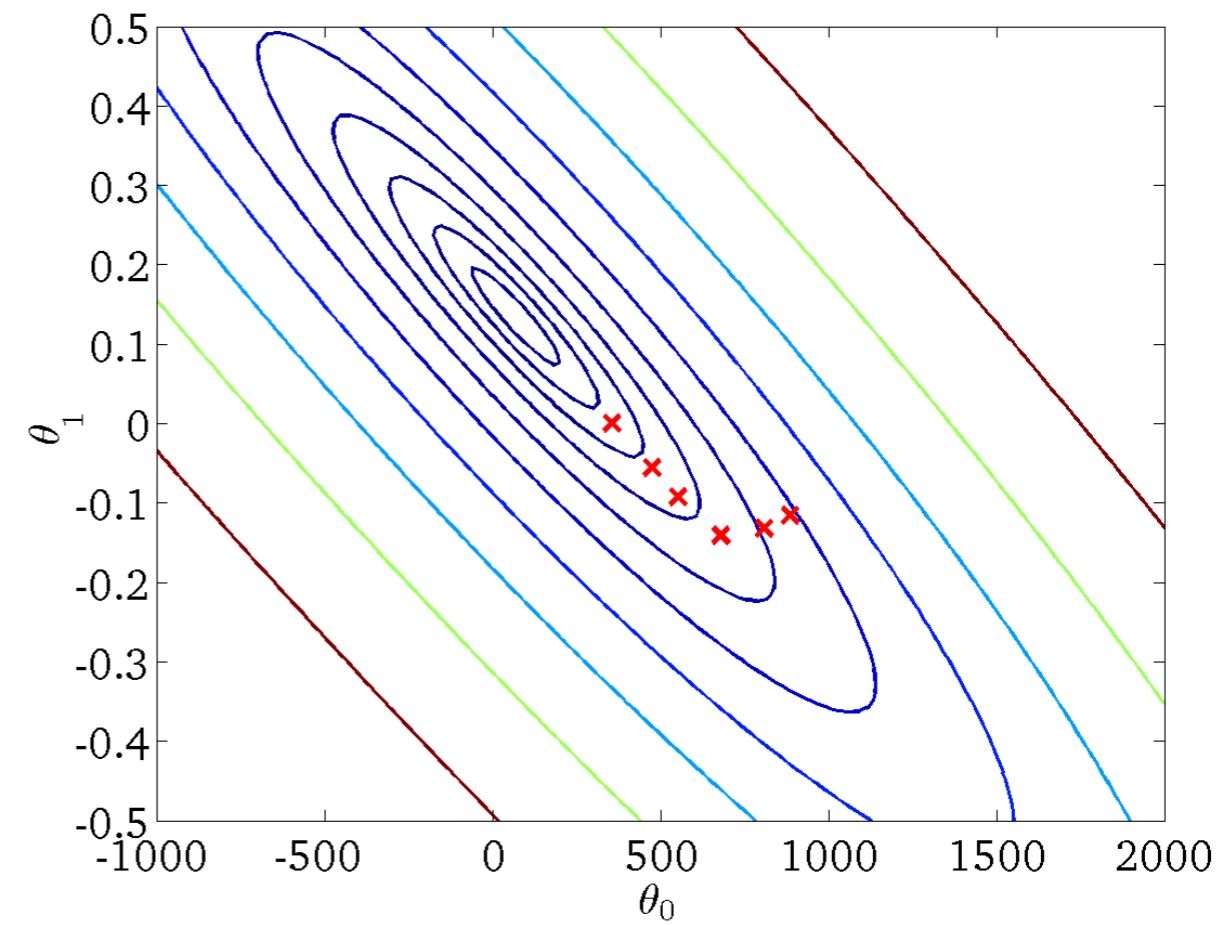
$$h_{\theta}(x)$$

(for fixed  $\theta_0, \theta_1$ , this is a function of  $x$ )



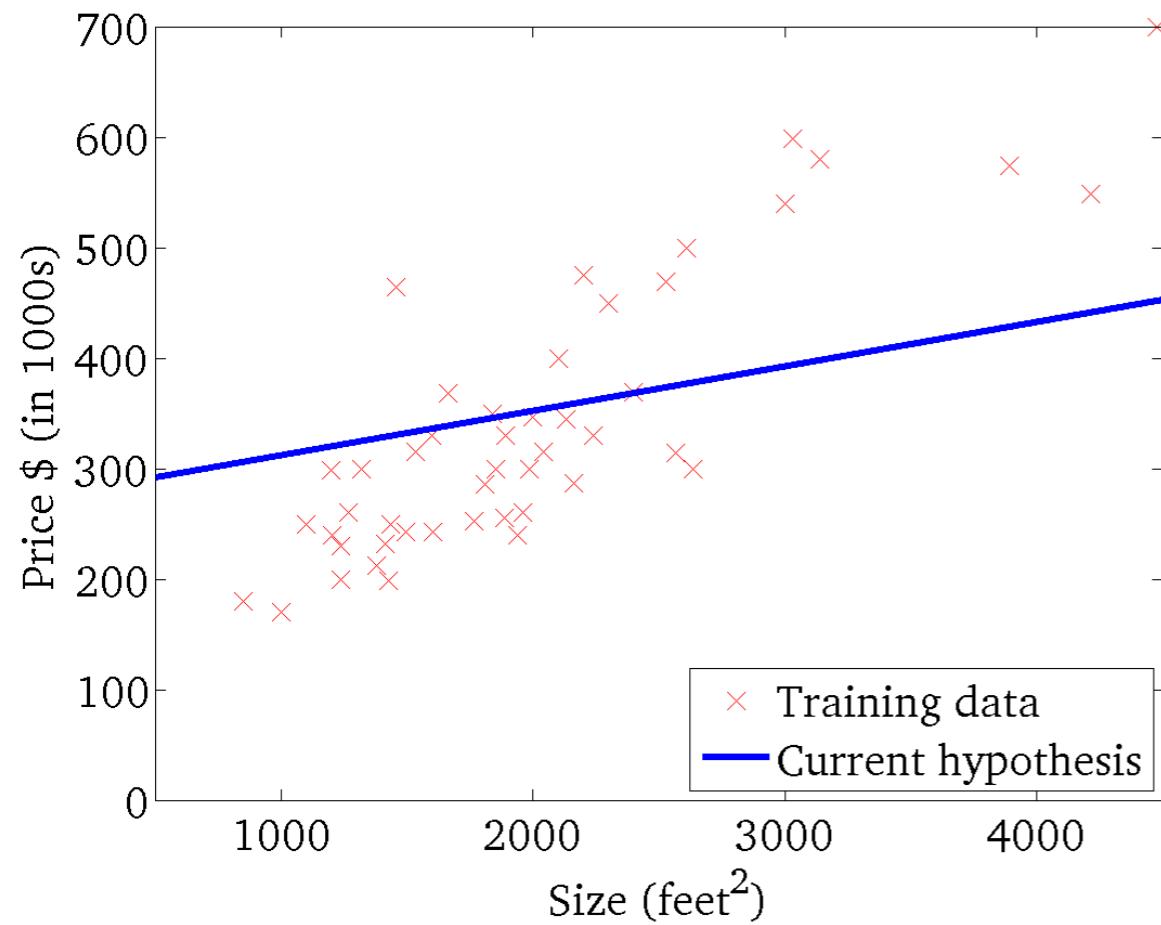
$$J(\theta_0, \theta_1)$$

(function of the parameter  $\theta_0, \theta_1$ )



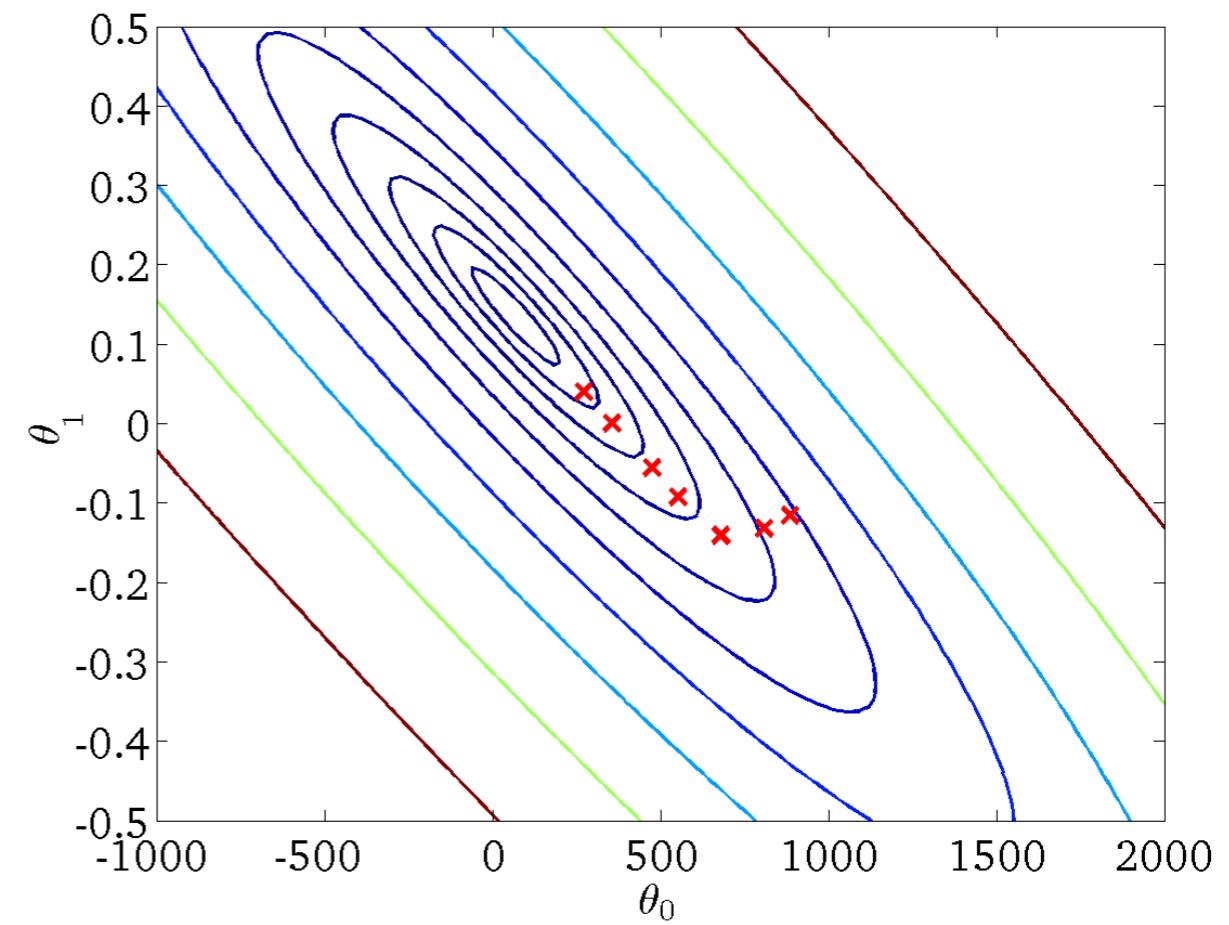
$$h_{\theta}(x)$$

(for fixed  $\theta_0, \theta_1$ , this is a function of  $x$ )



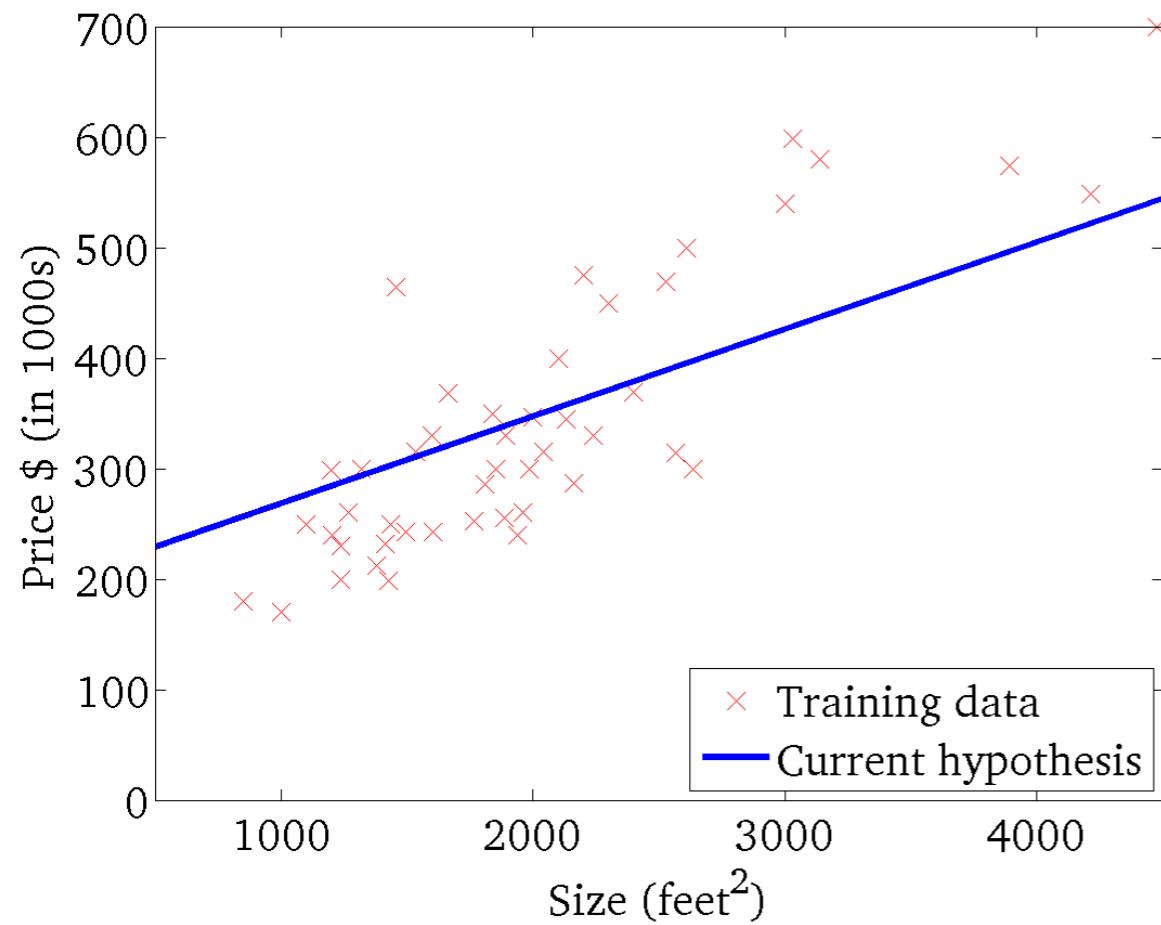
$$J(\theta_0, \theta_1)$$

(function of the parameter  $\theta_0, \theta_1$ )



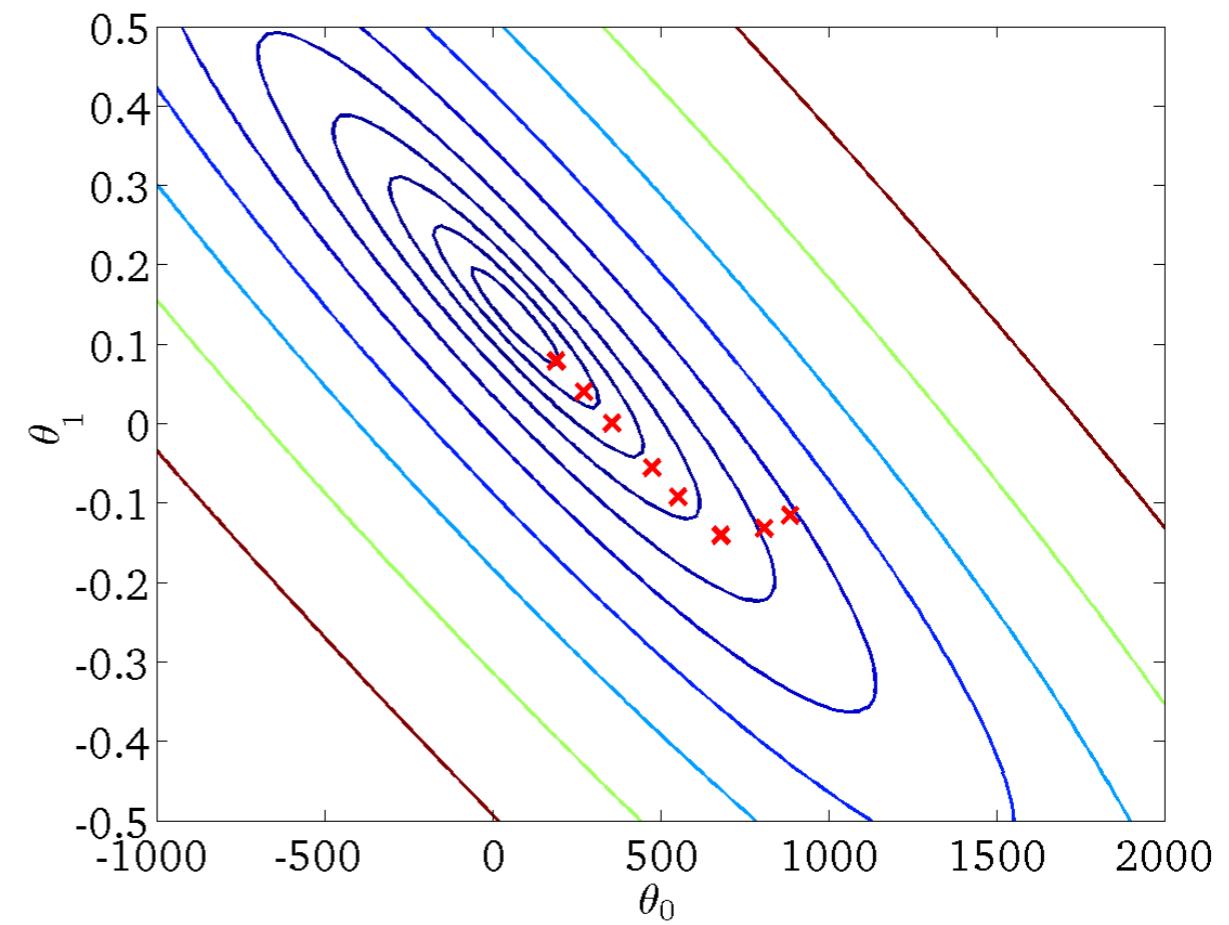
$$h_{\theta}(x)$$

(for fixed  $\theta_0, \theta_1$ , this is a function of  $x$ )



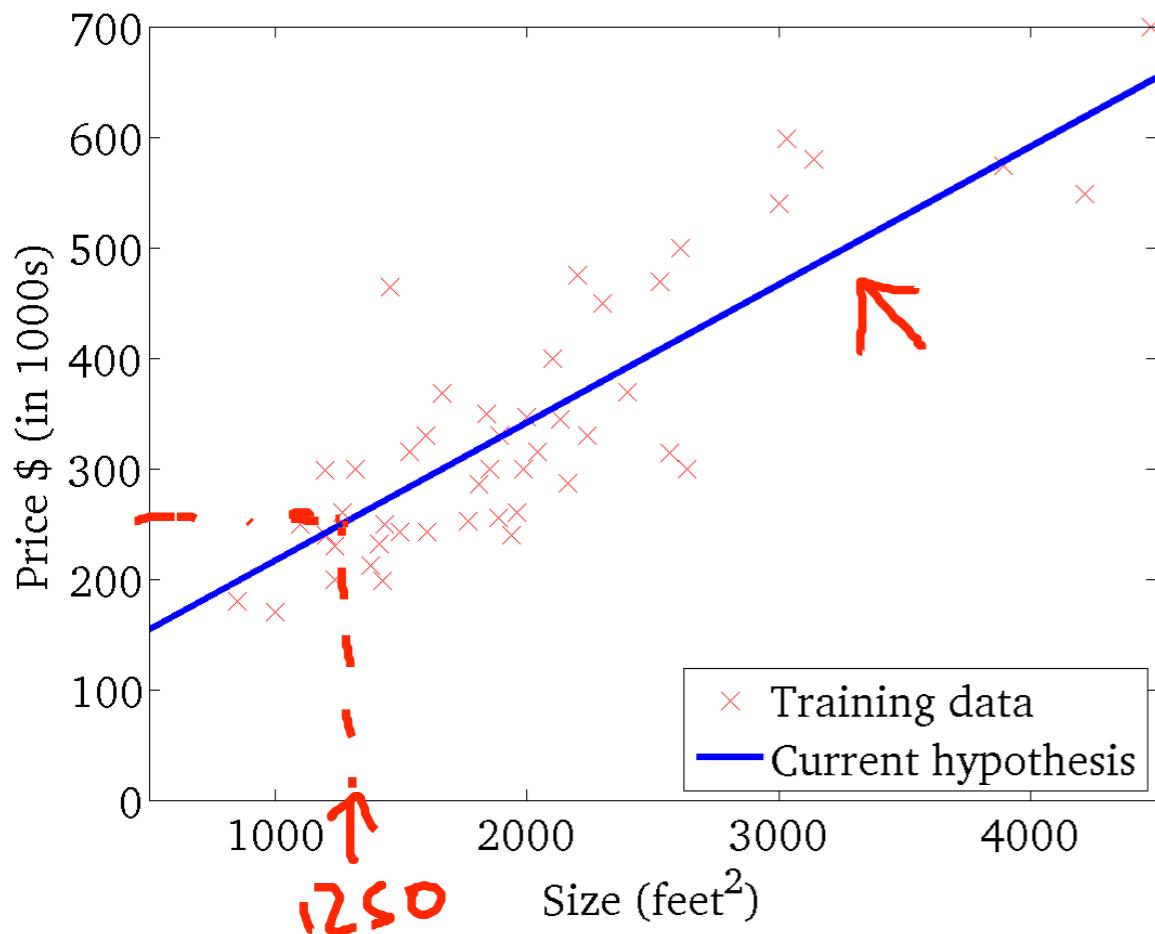
$$J(\theta_0, \theta_1)$$

(function of the parameter  $\theta_0, \theta_1$ )



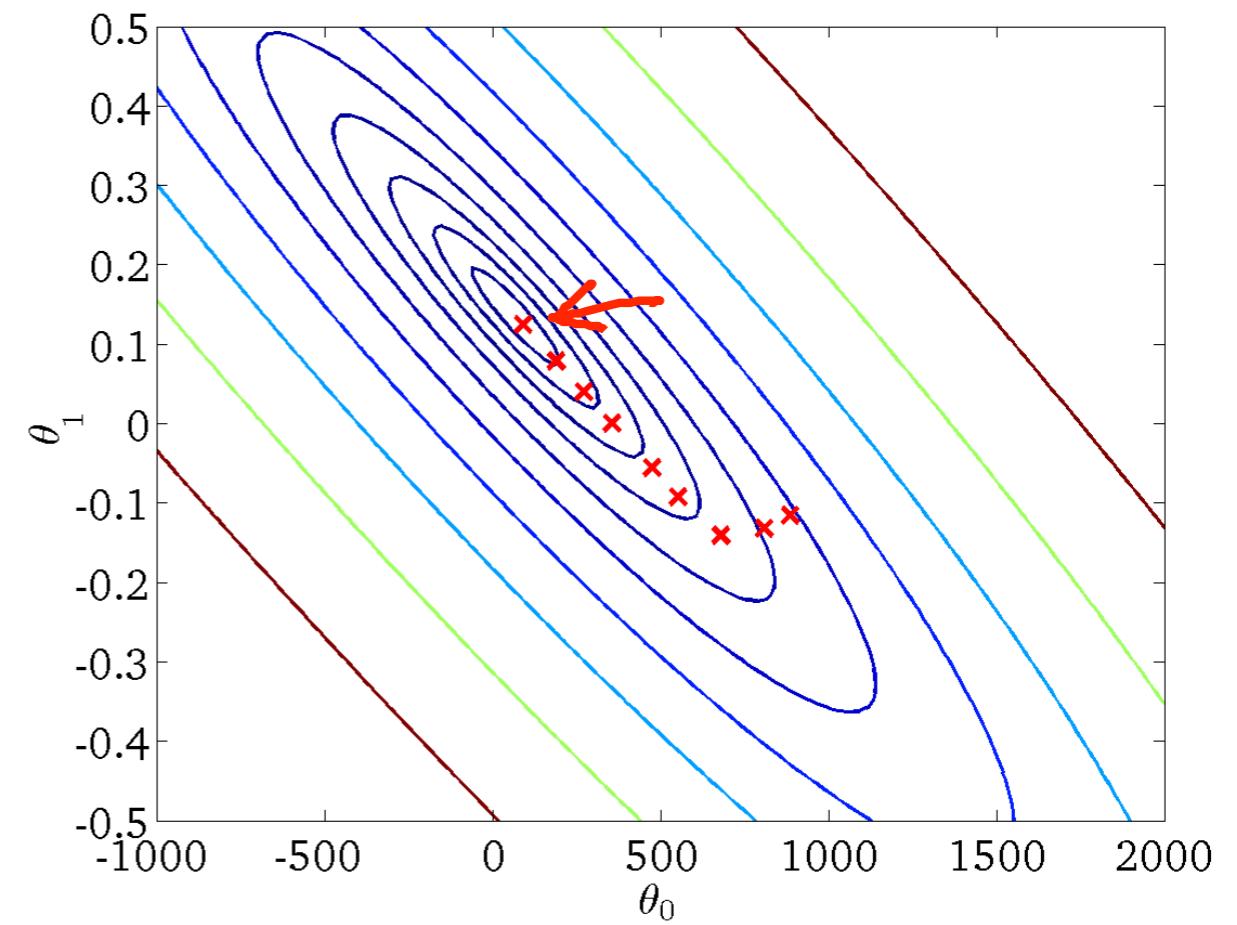
$$h_{\theta}(x)$$

(for fixed  $\theta_0, \theta_1$ , this is a function of  $x$ )



$$J(\theta_0, \theta_1)$$

(function of the parameter  $\theta_0, \theta_1$ )



# Batch Gradient Descent

- Each step of gradient descent uses all the training examples

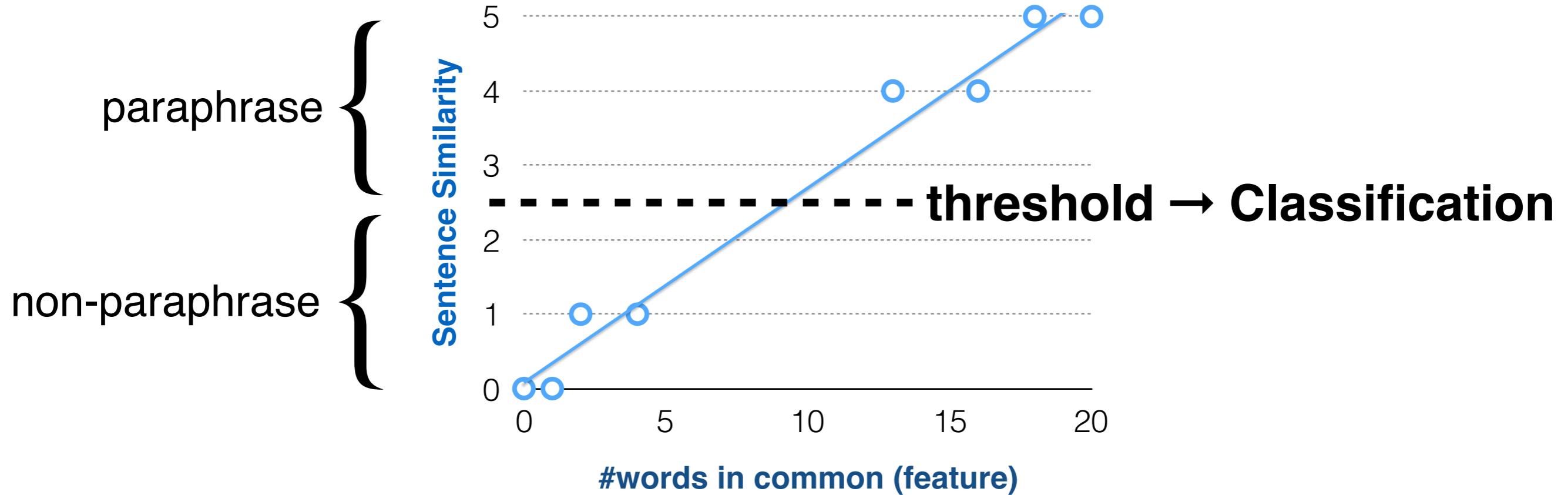
## Cost Function



$$J(\theta_0, \theta_1) = \frac{1}{2m} \sum_{i=1}^m (h_\theta(x^{(i)}) - y^{(i)})^2$$

(Recap)

# Linear Regression



- also supervised learning (learn from annotated data)
- but for **Regression**: predict **real-valued** output  
(Classification: predict discrete-valued output)

(Recap)

# Linear Regression

- **Hypothesis:**

$$h_{\theta}(x) = \theta_0 + \theta_1 x$$

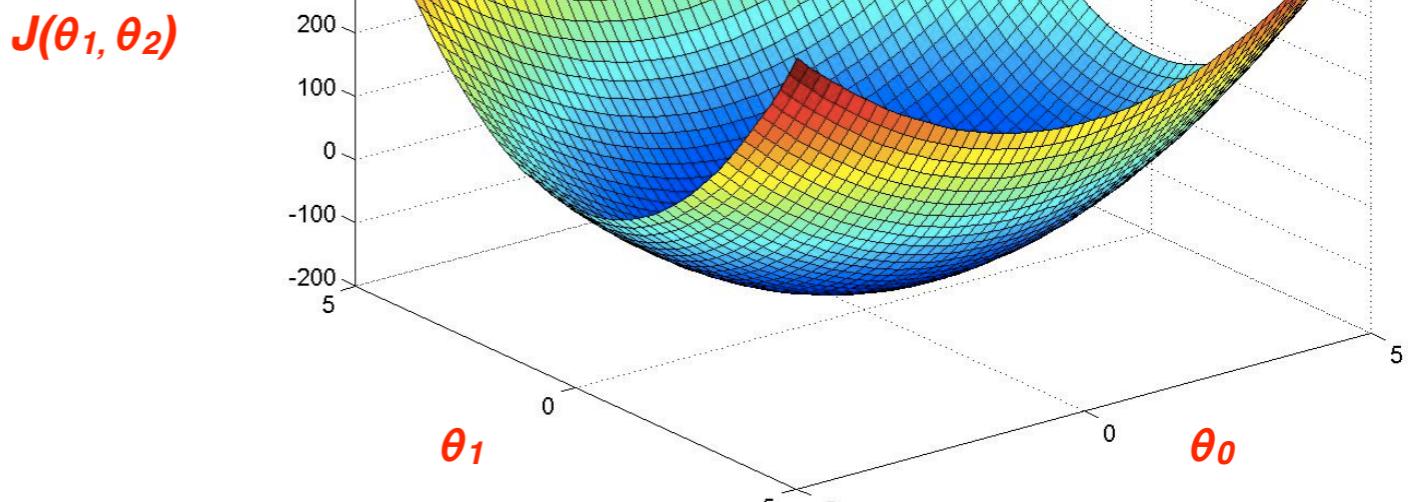
- **Parameters:**

$$\theta_0, \theta_1$$

- **Cost Function:**

$$J(\theta_0, \theta_1) = \frac{1}{2m} \sum_{i=1}^m (h_{\theta}(x^{(i)}) - y^{(i)})^2$$

- **Goal:**  $\underset{\theta_0, \theta_1}{\text{minimize}} J(\theta_0, \theta_1)$



(Recap)

# Gradient Descent

repeat until convergence {

$$\theta_j := \theta_j - \alpha \frac{\partial}{\partial \theta_j} J(\theta_0, \theta_1)$$

**learning rate**

(simultaneous update  
for j=0 and j=1)

# Next Class:

- Logistic Regression

[socialmedia-class.org](http://socialmedia-class.org)