

DOWNDRAG ANALYSIS (FELLENIOUS UNIFIED METHOD)

Project: Sample Project

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1. INPUT PARAMETERS

Parameter	Symbol	Value	Unit
Pile length	L	18.00	m
Pile diameter	D	0.610	m
Pile perimeter	P	1.916	m
Pile cross-sectional area	A_p	0.292247	m ²
Pile Young's modulus	E	200000000	kPa
Pile unit weight	γ_{pile}	24.0	kN/m ³
Dead load at pile head	Q_{dead}	500.0	kN
Fill thickness	H_{fill}	2.00	m
Fill unit weight	γ_{fill}	20.0	kN/m ³
Settlement trigger	$Source$	Fill placement (2.0 m @ 20 kN/m ³)	
Structural capacity	P_r	2000.0	kN
Groundwater depth	GWT	1.00	m

1. SOIL PROFILE

Soil Layer Definition

#	Top (m)	Bottom (m)	Description	Type	γ (kN/m ³)	Strength
1	0.0	5.0	Settling fill / soft clay	Cohesive	17.0	$c_u = 25.0$ kPa, $\alpha = 1.00$
2	5.0	10.0	Stiff clay (not settling)	Cohesive	18.0	$c_u = 60.0$ kPa, $\alpha = 1.00$
3	10.0	20.0	Dense sand bearing layer	Cohesionless	19.5	$\phi = 35.0^\circ$, $\beta = 0.30$

1. NEUTRAL PLANE LOCATION & DRAGLOAD

Force Equilibrium (Neutral Plane)

$$At the neutral plane depth z_{np} : Q_{dead} + W_{pile}(0 \rightarrow z_{np}) + Dragload(0 \rightarrow z_{np}) = R_{toe} + R_{shaft}(z_{np} \rightarrow L)$$

$$Load from top at NP = Resistance from tip at NP \quad Q_{dead} + pileweight + neg. friction = toe + pos. friction$$

$$z_{np} = 18.00 \text{ m}$$

Fellenius (2004), unified neutral plane method

NP at 18.00 m (100% of pile length)

Force Components at the Neutral Plane

Component	Value (kN)	Description
Q_dead	500.0	Applied dead load at pile head
Pile weight to NP	126.3	$\gamma_{pile} \times A_p \times z_{np} = 24.0 \times 0.292247 \times 18.00$
Dragload	1382.8	Negative skin friction above NP
Max pile load	2009.1	Q_dead + pile weight + dragload

Maximum Axial Load at Neutral Plane

$$Q_{np} = Q_{dead} + W_{pile}(0 \rightarrow z_{np}) + Q_{nf}$$

$$Q_{np} = 500.0 + 126.3 + 1382.8$$

$$Q_{np} = 2009.1 \text{ kN}$$

Fellenius (2004); UFC 3-220-20, Eq. 6-80

1. RESISTANCE BELOW NEUTRAL PLANE

Positive Shaft Resistance Below NP

$$R_s = \sum [f_s(z) \times P \times \Delta z] \text{ for } z > z_{np}$$

Sum of positive skin friction from z_{np} to pile tip

$$R_s = 0.0 \text{ kN}$$

Toe Bearing Resistance

$$R_t = N_t \times q_t \times A_{tip}(\text{cohesionless}) \text{ or } N_c \times c_u \times A_{tip}(\text{cohesive})$$

$$R_t = 4895.6 \text{ kN}$$

Fellenius (1991); UFC 3-220-20

Total Resistance Below NP

$$R_{total} = R_s + R_t$$

$$R_{total} = 0.0 + 4895.6$$

$$R_{total} = 4895.6 \text{ kN}$$

1. SETTLEMENT AT THE NEUTRAL PLANE

Elastic Shortening of Pile (above NP)

$$\delta_e = \Sigma [Q_{avg} \times \Delta z / (A_p \times E)] \text{ for } z = 0 \text{ to } z_{np}$$

$$AE = 0.292247 \times 200000000 = 58,449,331 \text{ kN}$$

$$\delta_e = 0.38 \text{ mm}$$

Toe Settlement (bearing stratum compression)

Equivalent footing $B' = D$, influenced depth $= 3 \times D$. 2V : 1H stress distribution below pile tip (UFC Eq 6-51).

$$B' = 0.610 \text{ m}$$

$$\delta_{toe} = 0.00 \text{ mm}$$

UFC 3-220-20, Eqs 6-49 through 6-51

Pile Settlement at Neutral Plane

$$\delta_{pile} = \delta_e + \delta_{toe}$$

$$\delta_{pile} = 0.38 + 0.00$$

$$\delta_{pile} = \mathbf{0.38} \text{ mm}$$

Soil Settlement at Neutral Plane

$$S_{soil}(z_{np}) = \text{cumulative 1-D consolidation settlement from settling layers, accumulated bottom - up.}$$

Interpolated from soil settlement profile at z_{np}

$$S_{soil}(z_{np}) = \mathbf{0.00} \text{ mm}$$

UFC 3-220-20, Eq. 6-53 (clay), Eq. 6-54 (sand)

Settlement Summary

Component	Value (mm)	Description
Elastic shortening	0.38	Pile compression above NP
Toe settlement	0.00	Bearing stratum compression below tip
Pile settlement	0.38	$\delta_e + \delta_{toe}$
Soil settlement at NP	0.00	From consolidation of settling layers

Settlement compatibility: pile and soil settlements should be approximately equal at the neutral plane.

1. LIMIT STATE CHECKS

Structural Limit State (UFC Eq 6-80)

$$LRFDDemand = 1.25 \times Q_{dead} + 1.10 \times (Q_{np} - Q_{dead})Demand \leq P_r(\text{factored structural resistance})$$

$$Demand = 1.25 \times 500.0 + 1.10 \times (2009.1 - 500.0)$$

$$Demand = \mathbf{2285.0} \text{ kN}$$

FAIL Structural capacity check (UFC Eq 6-80)

$$LRFDdemand = 2284.9974001863156 \text{ kN} > P_r = 2000.0 \text{ kN} \quad (D/C = 1.14)$$

Geotechnical Limit State

$Q_{dead} \leq R_{total}$ (positive friction + toe) Dragload is NOT included—it cancels at the neutral plane.

$$Q_{dead} = 500.0 \text{ kN} \text{ vs } R_{total} = 4895.6 \text{ kN}$$

$$Q_{dead}/R_{total} = 0.102$$

Fellenius (2004); AASHTO 10.7.3.7

Dragload cancels in geotechnical equilibrium per Fellenius unified method.

PASS Geotechnical capacity check (Q_{dead} vs R_{total})

$$Q_{dead} = 500.0 \text{ kN} \leq R_{total} = 4895.5581781718265 \text{ kN} \quad (D/C = 0.10)$$

1. FIGURES

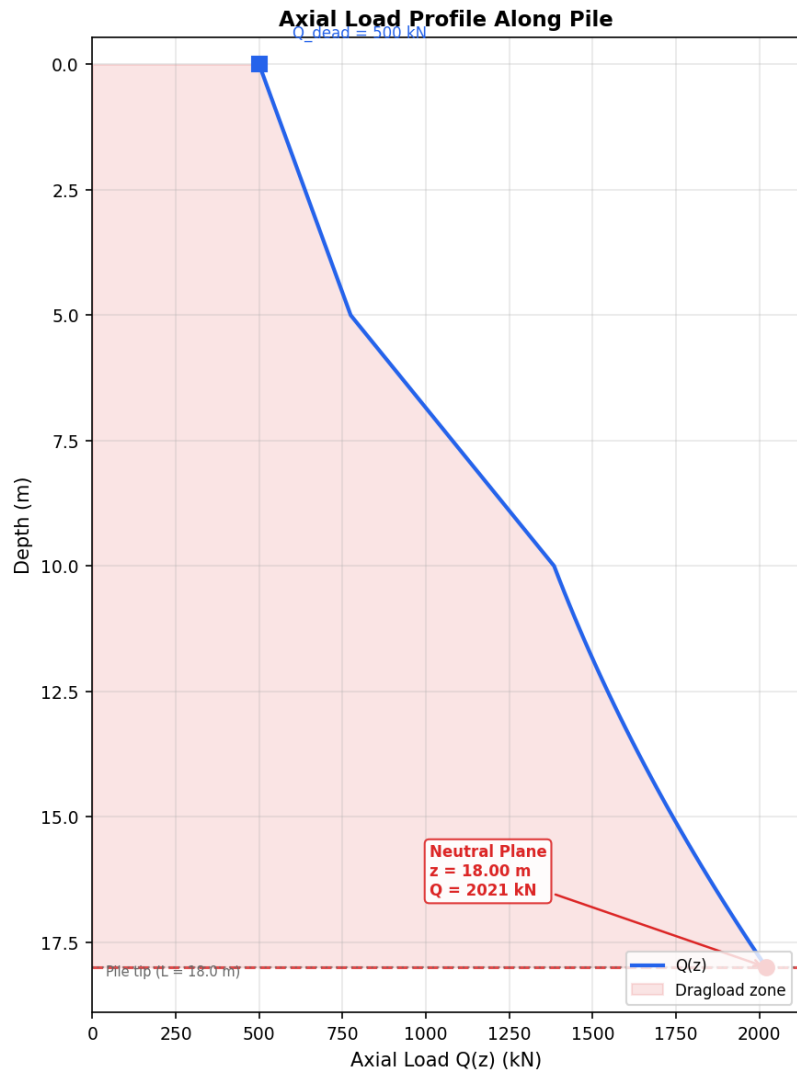
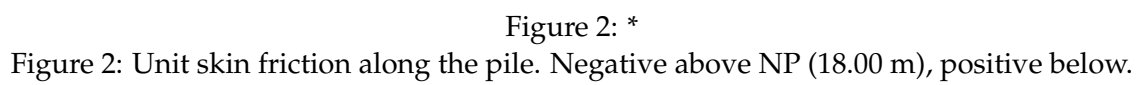


Figure 1: *

Figure 1: Axial load distribution along the pile. Neutral plane at $z = 18.00 \text{ m}$ ($Q_{max} = 2009.1 \text{ kN}$).



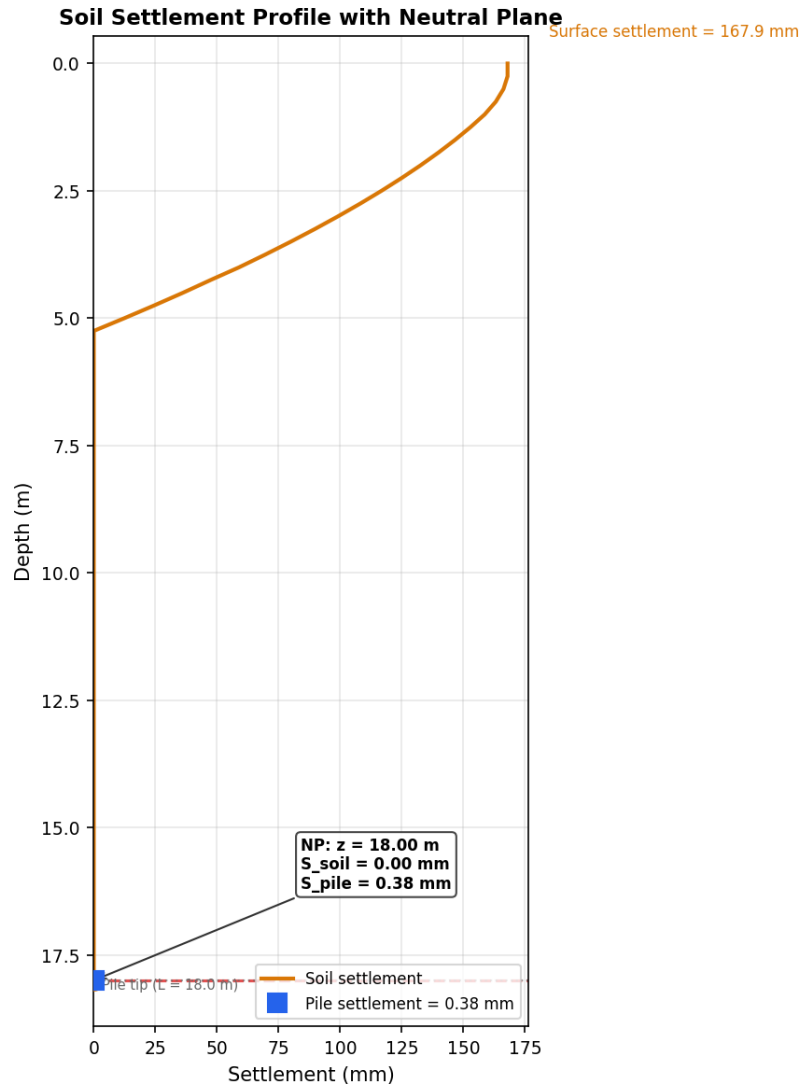


Figure 3: *
Figure 3: Soil settlement profile along the pile depth. Soil settlement at NP = 0.00 mm, pile settlement = 0.38 mm.

1. REFERENCES

1. Fellenius, B.H. (2006). "Results of static loading tests on driven piles." Geotechnical News Magazine.
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3. UFC 3-220-20, 16 Jan 2025. "Geotechnical Engineering." Chapter 6: Deep Foundations.
4. AASHTO LRFD Bridge Design Specifications, 9th Ed. (2020). Section 10.7.3.7: Downdrag.
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