

## DOWNDRAg ANALYSIS (FELLENIUS UNIFIED METHOD)

Project: Sample Project      Number: DD-2026-007  
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 Company: Geotech Associates

### 1. INPUT PARAMETERS

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Parameter	Symbol	Value	Unit
Pile length	$L$	18.00	m
Pile diameter	$D$	0.610	m
Pile perimeter	$P$	1.916	m
Pile cross-sectional area	$A_p$	0.292247	$\text{m}^2$
Pile Young's modulus	$E$	200000000	kPa
Pile unit weight	$\gamma_{pile}$	24.0	$\text{kN}/\text{m}^3$
Dead load at pile head	$Q_{dead}$	500.0	kN
Fill thickness	$H_{fill}$	2.00	m
Fill unit weight	$\gamma_{fill}$	20.0	$\text{kN}/\text{m}^3$
Settlement trigger	Source	Fill placement (2.0 m @ 20 $\text{kN}/\text{m}^3$ )	
Structural capacity	$P_r$	2000.0	kN
Groundwater depth	GWT	1.00	m

### 1. SOIL PROFILE

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#### Soil Layer Definition

#	Top (m)	Bottom (m)	Description	Type	$\gamma$ ( $\text{kN}/\text{m}^3$ )	Strength	S
1	0.0	5.0	Settling fill / soft clay	Cohesive	17.0	$c_u = 25.0 \text{ kPa}, \alpha = 1.00$	
2	5.0	10.0	Stiff clay (not settling)	Cohesive	18.0	$c_u = 60.0 \text{ kPa}, \alpha = 1.00$	
3	10.0	20.0	Dense sand bearing layer	Cohesionless	19.5	$\varphi = 35.0^\circ, \beta = 0.30$	

### 1. NEUTRAL PLANE LOCATION & DRAGLOAD

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#### Force Equilibrium (Neutral Plane)

$$At the neutral plane depth z_{np} : Q_{dead} + W_{pile}(0 \rightarrow z_{np}) + Dragload(0 \rightarrow z_{np}) = R_{toe} + R_{shaft}(z_{np} \rightarrow L)$$

$$Load from top at NP = Resistance from tip at NP Q_{dead} + pile weight + neg. friction = toe + pos. friction$$

$z_{np} = \text{18.00 m}$

Fellenius (2004), unified neutral plane method

NP at 18.00 m (100% of pile length)

## Force Components at the Neutral Plane

Component	Value (kN)	Description
Q_dead	500.0	Applied dead load at pile head
Pile weight to NP	126.3	$\gamma_{\text{pile}} \times A_p \times z_{np} = 24.0 \times 0.292247 \times 18.00$
Dragload	1382.8	Negative skin friction above NP
Max pile load	2009.1	$Q_{dead} + \text{pile weight} + \text{dragload}$

## Maximum Axial Load at Neutral Plane

$$Q_{np} = Q_{dead} + W_{pile}(0 \rightarrow z_{np}) + Q_{nf}$$

$$Q_{np} = 500.0 + 126.3 + 1382.8$$

$Q_{np} = \text{2009.1 kN}$

Fellenius (2004); UFC 3-220-20, Eq. 6-80

## 1. RESISTANCE BELOW NEUTRAL PLANE

### Positive Shaft Resistance Below NP

$$R_s = \sum [f_s(z) \times P \times \Delta z] \text{ for } z > z_{np}$$

Sum of positive skin friction from  $z_{np}$  to pile tip

$R_s = \text{0.0 kN}$

### Toe Bearing Resistance

$$R_t = N_t \times q_t \times A_{tip} (\text{cohesionless}) \text{ or } N_c \times c_u \times A_{tip} (\text{cohesive})$$

$$R_t = \mathbf{4895.6} \text{ kN}$$

Fellenius (1991); UFC 3-220-20

### Total Resistance Below NP

$$R_{total} = R_s + R_t$$

$$R_{total} = 0.0 + 4895.6$$

$$R_{total} = \mathbf{4895.6} \text{ kN}$$

## 1. SETTLEMENT AT THE NEUTRAL PLANE

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### Elastic Shortening of Pile (above NP)

$$\delta_e = \Sigma [Q_{avg} \times \Delta z / (A_p \times E)] \text{ for } z = 0 \text{ to } z_{np}$$

$$AE = 0.292247 \times 200000000 = 58,449,331 \text{ kN}$$

$$\delta_e = \mathbf{0.38} \text{ mm}$$

### Toe Settlement (bearing stratum compression)

Equivalent footing  $B' = D$ , influenced depth =  $3 \times D.2V : 1$  H stress distribution below pile tip (UFC Eq 6-51).

$$B' = 0.610m$$

$$\delta_{toe} = \mathbf{0.00} \text{ mm}$$

UFC 3-220-20, Eqs 6-49 through 6-51

## Pile Settlement at Neutral Plane

$$\delta_{pile} = \delta_e + \delta_{toe}$$

$$\delta_{pile} = 0.38 + 0.00$$

$$\delta_{pile} = \mathbf{0.38} \text{ mm}$$

## Soil Settlement at Neutral Plane

$S_{soil}(z_{np}) = \text{cumulative } 1 - D \text{ consolidation settlement from settling layers, accumulated bottom-up.}$

*Interpolated from soil settlement profile at  $z_{np}$*

$$S_{soil}(z_{np}) = \mathbf{0.00} \text{ mm}$$

UFC 3-220-20, Eq. 6-53 (clay), Eq. 6-54 (sand)

## Settlement Summary

Component	Value (mm)	Description
Elastic shortening	0.38	Pile compression above NP
Toe settlement	0.00	Bearing stratum compression below tip
Pile settlement	0.38	$\delta_e + \delta_{toe}$
Soil settlement at NP	0.00	From consolidation of settling layers

*Settlement compatibility: pile and soil settlements should be approximately equal at the neutral plane.*

## 1. LIMIT STATE CHECKS

### Structural Limit State (UFC Eq 6-80)

$$LRFD \text{ Demand} = 1.25 \times Q_{dead} + 1.10 \times (Q_{np} - Q_{dead}) \text{ Demand} \leq P_r (\text{factored structural resistance})$$

$$\text{Demand} = 1.25 \times 500.0 + 1.10 \times (2009.1 - 500.0)$$

$$\text{Demand} = \mathbf{2285.0} \text{ kN}$$

**FAIL** Structural capacity check (UFC Eq 6-80)

$LRFD_{demand} = 2284.9974001863156 \text{ kN} > P_r = 2000.0 \text{ kN}$  (D/C = 1.14)

**Geotechnical Limit State**

$Q_{dead} \leq R_{total}$  (*positive friction + toe*) Drag load is NOT included—it cancels at the neutral plane.

$$Q_{dead} = 500.0 \text{ kN} vs R_{total} = 4895.6 \text{ kN}$$

$$Q_{dead}/R_{total} = \mathbf{0.102}$$

Fellenius (2004); AASHTO 10.7.3.7

Drag load cancels in geotechnical equilibrium per Fellenius unified method.

**PASS** Geotechnical capacity check ( $Q_{dead}$  vs  $R_{total}$ )

$Q_{dead} = 500.0 \text{ kN} \leq R_{total} = 4895.5581781718265 \text{ kN}$  (D/C = 0.10)

**1. FIGURES**

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Figure 1: \*

Figure 1: Axial load distribution along the pile. Neutral plane at  $z = 18.00 \text{ m}$  ( $Q_{\text{max}} = 2009.1 \text{ kN}$ ).

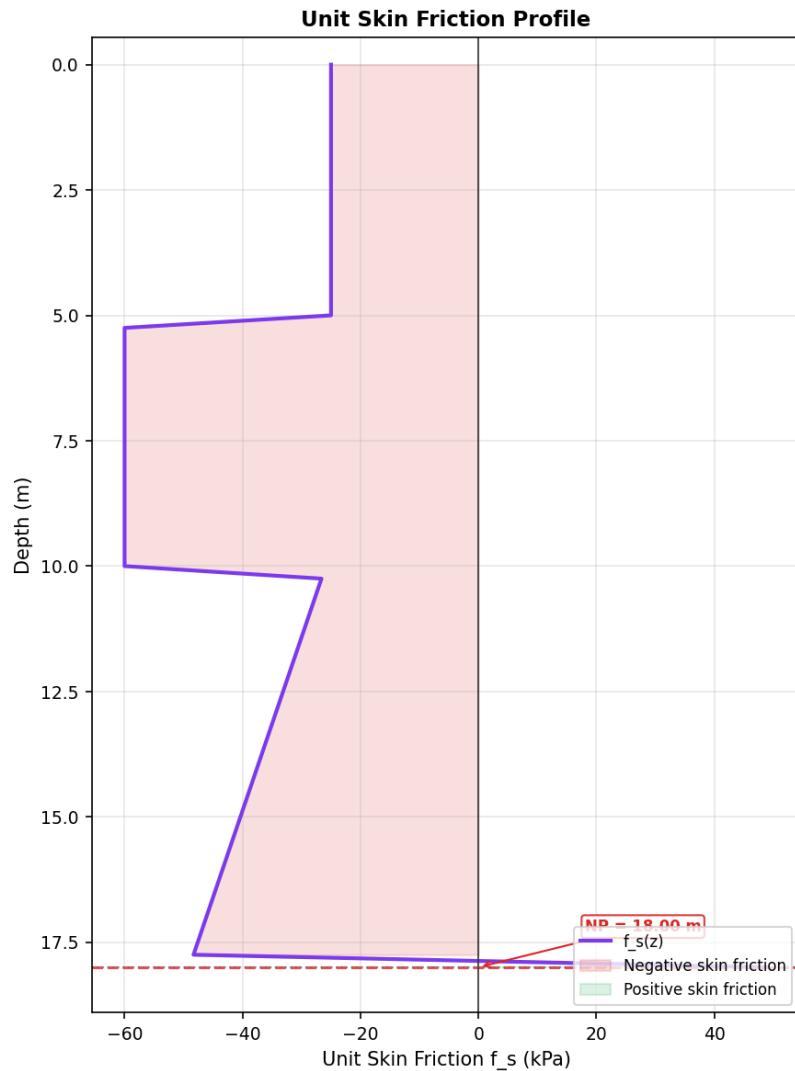


Figure 2: \*

Figure 2: Unit skin friction along the pile. Negative above NP (18.00 m), positive below.

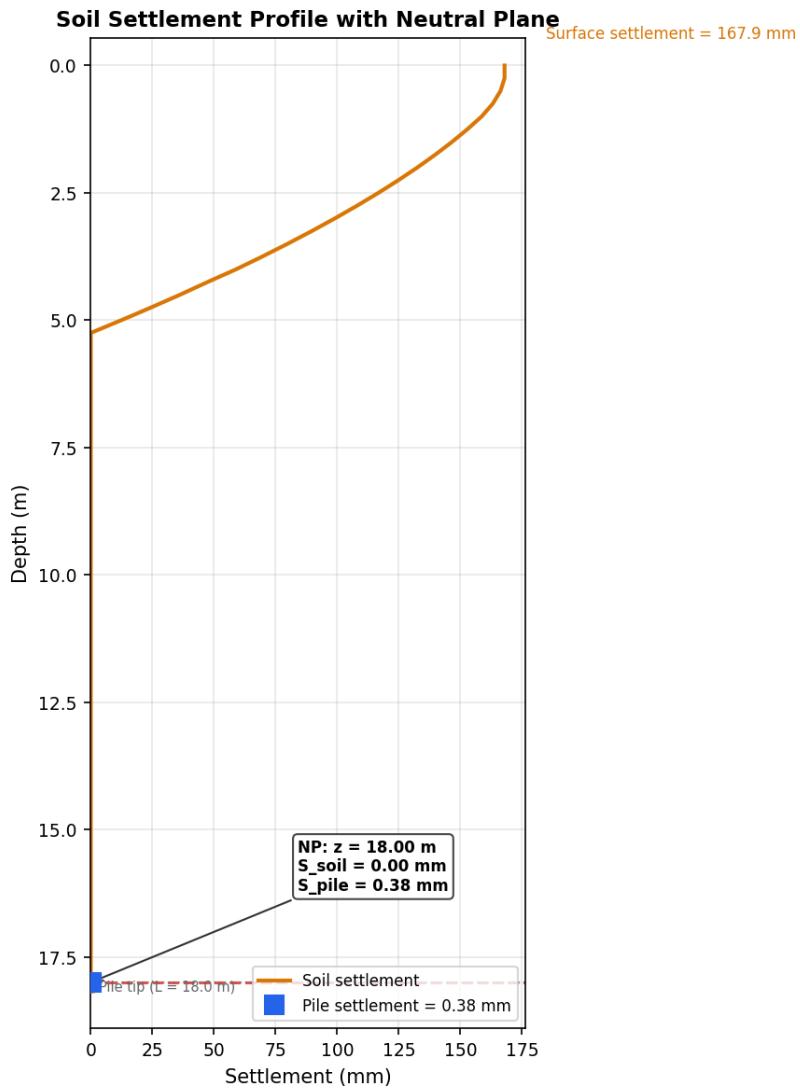


Figure 3: \*

Figure 3: Soil settlement profile along the pile depth. Soil settlement at NP = 0.00 mm, pile settlement = 0.38 mm.

## 1. REFERENCES

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1. Fellenius, B.H. (2006). "Results of static loading tests on driven piles." Geotechnical News Magazine.
  2. Fellenius, B.H. (2004). "Unified design of piled foundations with emphasis on settlement analysis." ASCE GSP 125, pp. 253-275.
  3. UFC 3-220-20, 16 Jan 2025. "Geotechnical Engineering." Chapter 6: Deep Foundations.
  4. AASHTO LRFD Bridge Design Specifications, 9th Ed. (2020). Section 10.7.3.7: Downdrag.
  5. Fellenius, B.H. (1991). "Pile foundations." Chapter 13 in Foundation Engineering Handbook, 2nd Ed. Van Nostrand Reinhold.
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