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## Algorithmen und Wahrscheinlichkeit Programming Exercises 1

## Exercise 1 - Important Stops

You were hired by Swiss Federal Railways to do an important job. Given a map with n cities, denoted by  $\{0,1,\ldots,n-1\}$ , and a map of bi-directional rail segments between them, your task is to decide at which stops should the passengers be checked if they have a valid ticket. Since each city has its corresponding unique stop, we refer to stops and cities interchangeably. The process of ticket control takes time and human resources, thus SBB decided that the passengers should be checked at a stop (city) i only if the stop is very important. A stop  $a \in \{0,\ldots,n-1\}$  is very important if there exist two different cities  $b,c\in\{0,\ldots,n-1\}\setminus\{a\}$  such that the following is satisfied:

- City b is reachable by train from city c (and the other way around).
- For a train to go from city b to city c it must go through city a.

**Input** The first line of the input file contains an integer  $1 \le t \le 20$  denoting the number of test cases that follow. Each of the t test cases is described as follows.

- It starts with a line containing two integers n m, separated by space, denoting the number of stops and the number of rail segments such that  $1 \le n \le 10^4$  and  $1 \le m \le 10^4$ .
- The next m lines describe m different rail segments. Each line consists of two integers **a b**, separated by space, which denote that there is a rail segment between a and b. It is guaranteed that  $0 \le a \ne b \le n-1$ .

**Output** For each test case output one line containing the id's of all the very important stops (cities) separated by space and sorted by the increasing value of the id. In case there are no important stops for a particular test case, output -1.

Sample Input	Sample Output
2	0 5
7 8	-1
3 2	
2 0	
3 0	
1 5	
0 1	
0 4	
4 5	